行政院國家科學委員會專題研究計畫 期中進度報告

使用 60GHz 之室內十億級位元傳輸率之無線基頻傳收機-子計畫三:針對通訊數位訊號處理器之電子系統層級驗証 與合成環境(2/3)

期中進度報告(完整版)

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處理方式:本計畫可公開查詢

中 華 民 國 99 年 05 月 28 日

針對通訊數位訊號處理器之電子系統層級驗證與合成環境(2/3) An ESL system verification and synthesis environment for communication DSP (2/3)

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一、 中文摘要

快速傅利葉轉換處理器相當廣泛的應用在訊號處理系統及通訊系統中。雖然 現存的文獻提供了許多快速傅利葉轉換處理器的架構,但要能夠在給定的條件下 挑選出最適合的架構仍是一個相當重要的技術問題。一個快速傅利葉轉換處理器 產生器,不但可以增加設計的生產力,同時也可以縮短整個系統設計開發的時 程。在這篇論文中,我們針對管線化的快速傅利葉轉換架構提出了面積與通量折 衷的方法,且能自動地產生對應的硬體設計。實驗結果顯示,我們在通量的限制 之下,可以產生硬體面積較小的架構。

關鍵字

快速傅利葉轉換、管線化、參數化、產生器

英文摘要

The Fast Fourier Transform (FFT) processors are widely used in signal processing systems and communication systems. Many FFT architectures are proposed in literature to meet different applications. While designing an FFT processor, one of the most difficult issues is to choose the best architecture under the design constraints. An FFT generator can not only improve the productivity but also shorten time-to-market. In this thesis, we propose approaches which can make appropriate design trade-off between throughput and area of pipeline FFT architectures, and automatically generate the corresponding hardware design. The experimental results show that the proposed methodology can generate area-efficient architectures under throughput constraints.

Keywords

Fast Fourier Transform, pipeline, parameterization, generator

二、 計畫的緣由與自的

A. Introduction

Fast Fourier Transform (FFT) and Inverse Fast Fourier Transform (IFFT) are widely used algorithms for calculating the Discrete Fourier Transform (DFT) and Inverse Discrete Fourier Transform (IDFT) because of the low computation complexity. FFT processor is an important block in communication system and signal processing system. For example, as shown in Figure 1, Orthogonal Frequency Division Multiplexing (OFDM) system is widely used in many communication applications such as xDSL modem, HDTV, and wide band mobile terminals. In those applications, FFT and IFFT are the most important processing blocks to meet the design constraints.

Figure 1 An example architecture of OFDM system

An automatic FFT generator can not only improve productivity but also shorten time-to-market. To support user customization, the automatic FFT generator provides some parameters to customize for the design constraints, such as the FFT transform sizes, I/O data ordering, data bitwidth, and the various architectures. In this thesis, we mainly focus on the trade-off between throughput and area of the FFT architectures.

Since the FFT algorithm was proposed by Cooley and Turkey in 1965 [\[1\],](#page-13-0) many similar algorithms have been proposed to reduce the computation complexity of FFT. As the technology progress and algorithm improvement, FFT is widely used in Digital Signal Processing (DSP) applications. According to different algorithms, many kinds of FFT architectures have been proposed. Generally, there are two kinds of popular FFT architectures. One is memory-based architecture and the other is pipelined-based architecture. A single processing elements (PE) is used in memory-based architecture. It can be easily extended to other FFT transform sizes, so the memory-based architectures are usually used for low hardware cost and low throughput designs. Pipeline-based architectures have features such as regularity, simplicity, and high throughput rate. In this thesis, we only focus on pipelined-based architectures.

Several pipeline-based FFT architectures are proposed, such as the Radix-2 Multi-path Delay Commutator (R2MDC) [\[2\],](#page-14-0) Radix-4 Multi-path Delay Commutator (R4MDC) [\[2\],](#page-14-0) Radix-2 Single-path Delay Feedback (R2SDF) [\[3\],](#page-14-1) Radix-4 Single-path Delay Feedback (R4SDF) [\[4\],](#page-14-2) Radix-2² Single-path Delay Feedback (R2²SDF) [\[5\],](#page-14-3) Radix-2² Multi-path Delay Commutator ($R2²MDC$) [\[6\]](#page-14-4) and Radix-2³ Single-path Delay Feedback ($R2³SDF$) [\[7\].](#page-14-5) In these architectures, the R4SDF requires fewer multipliers than the R2SDF; however the R2SDF architecture is simpler and more regular than the R4SDF. The R2MDC requires fewer multipliers, adders and memory size than the R4MDC; however, the R4MDC can provide higher throughput. The $R2²SDF$ has the same multiplier complex as R4SDF, but retains the butterfly structure of radix-2 algorithm. The R2²MDC uses the same algorithm as the R2²SDF, and the $R2²MDC$ has higher throughput. As a result, in this work, our proposed FFT generator is based on the $R2²MDC$ and the R2MDC architectures.

B. Pipeline-based FFT architectures

Pipeline-based architectures can be further divided into two kinds of architectures depend on the design of register. One is Single-path Delay Feedback (SDF) architecture, and the other one is Multi-path Delay Commutator (MDC) architecture. SDF architecture has higher hardware usage and lower hardware cost; however, MDC architecture has higher throughput than SDF architecture. We introduce these architectures below.

We first introduce the SDF architecture. The Radix-2 SDF (R2SDF) architecture [\[3\]](#page-14-1) is shown in Figure 2. By storing the butterfly output into the shift registers, R2SDF uses the registers efficiently. The butterfly passes the output to the next stage when doing addition operation and storing the output into the shift register when doing subtraction operation. In each cycle, only one output passes through the multiplier.

Figure 2 R2SDF architecture (N=16)

The Radix-4 SDF (R4SDF) architecture [\[4\]](#page-14-2) is shown in Figure 3. Similar to the R2SDF architecture, radix-4 butterfly store three of outputs into shift registers, and only one output passes through the multiplier in each cycle.

Figure 3 R4SDF architecture (N=16)

The Radix-2² SDF (R2²SDF) [\[5\]](#page-14-3) architecture is similar to the R2SDF architecture and reduces the number of multipliers. $R2²SDF$ uses two types of butterflies, one is the same as that in R2SDF architecture and the other contains also some logic to implement the multiplication of twiddle factor of –j, as shown in Figure 4.

Figure 4 R2² SDF architecture (N=16)

The Radix-2 MDC (R2MDC) architecture [\[2\]](#page-14-0) is straightforward. The inputs are separated into two streams by the control of switches, and then go to butterflies in parallel, as shown in Figure 5.

Figure 5 R2MDC architecture (N=16)

The Radix-4 MDC (R4MDC) architecture [\[2\]](#page-14-0) is also similar to R2MDC architecture besides the raidx-4 butterfly and the number of registers, as shown in Figure 6.

Figure 6 R4MDC Architecture (N=16)

The Radix-2² MDC (R2²MDC) architecture [\[6\]](#page-14-4) is the MDC type architecture of Radix-2² algorithm. In the flow graph of the complete decomposition of an N-point FFT computation with radix- 2^2 algorithm, the even-numbered stages multiple twiddle factors not only the subtraction output but the addition output, so the $R2²MDC$ architecture needs two complex multipliers in even-numbered stages, as shown in Figure 7.

Figure 7 R2²MDC architecture (N=16)

A. Motivation

An exhaustive search approach is proposed to find all possible FFT architectures and then generate a set of acceptable FFT architecture according to the design constraints. However, from Table 1, we can find that all the possible solutions have the same number of multipliers, number of adders and number of registers usage under the throughput constraint.

Pease architecture bases on the radix-2 algorithm. Observing the raidx-2 flow graph, each butterfly is followed by a multiplication operation at the output of subtraction operation. Therefore, Pease architecture is a very regular architecture. However, the radix-2 algorithm contains many trivial multiplications which do not need multipliers to calculate. For example, multiplication of –*j* involves only real-imaginary swapping and sign inversion, as shown in Figure 8.

Figure 8 Illustration of –*j* **multiplication**

The radix-2² algorithm considers the multiplication of $-j$ and merges the multiplication of $-j$ into odd-numbered columns. And the architecture of radix- 2^2 algorithm contains two kinds of butterflies, BFI and BFII. From the view of architecture, the radix- $2²$ algorithm is more irregular than the radix-2 algorithm.

The R2²MDC [\[6\]](#page-14-4) is a pipeline architecture that implements the radix-2² algorithm with throughput $\frac{2}{\sqrt{2}}$ *N* , so $R2²MDC$ architecture is more irregular than Pease architecture. In the following subsections, we introduce how we make the trade-off between hardware and throughout based on $R2²$ MDC and R2MDC architecture.

B. R2²MDC Vertical Expansion Architecture

A general form of R2²MDC vertical expansion architecture is shown in Figure 9. Parameter *N* indicates the FFT transform size, where $N = 2^m$, $m = 1, 2, 3...$ *Parameter t* indicates the degree of parallelism, where $t = 1, 2, 4, \ldots, 2^{m-1}$. The number of registers of each original R2²MDC architecture decreases as the degree of parallelism increases, and the number of interconnection permutation matrix also increases. With the interconnection permutation matrix, data dependence would be kept. From Figure, we can derive the number of multipliers is $t(2 \lceil log_4 N \rceil - 2)$, the number of adders is $2t \log_2 N$, the number of registers is $N - 2t$ and the throughput is $\frac{2t}{N}$.

N

Figure 9 General form of R2²MDC vertical expansion architecture

Figure 10 shows the case when $t = 1$, the original R2²MDC architecture, the number of multiplier is 2, the number of adders is 8, the number of registers of datapath is 14, and the throughput is $\frac{1}{2}$ 8 .

Figure 10 Example of R2²MDC vertical expansion architecture for t=1

Figure 11 shows the case when $t = 2$, the number of multipliers is 4, the number of adders is 16, the number of registers of datapath is 12, and the throughput is $\frac{1}{x}$ 4 .

Figure 11 Example of R2²MDC vertical expansion architecture for t=2

Figure 12 shows the case when $t = 4$, the number of multipliers is 8, the number of adders is 32, the number of registers of datapath is 8, and the throughput is $\frac{1}{2}$ 2 .

Figure 12 Example of R2²MDC vertical expansion architecture for t=4

Figure 13 shows the case when $t = 8$, namely, a fully parallelized R2²MDC vertical expansion architecture, the number of multipliers is 16, the number of adders is 64, the number of registers of datapath is 0, and the throughput is $\frac{1}{2}$ 2 .

Figure 13 Example of R2²MDC vertical expansion architecture for t=8

C. Summary

In this project, we proposed two directional trades-off approaches based on $R2²MDC$ architecture and R2MDC architecture. In vertical direction, we provide an expansion approach for $R2²MDC$ architecture to increase the throughput. Under the throughput constraint, our approach can provide only one exact solution. Table 1 lists the hardware and throughput comparison between our approach and previous work, where $R2²EMDC$ indicates the vertically expanded R22MDC architecture. Table 2 gives the normalized hardware and throughput comparison with the same throughput by replacing jk with $t \log_2 N$.

Table 1 Hardware Requirement Comparison

Table 2 Hardware Requirement Comparison with the same throughput

四、 結論與討論

The FFT processor is an important computing block in communication and signal processing systems. To improve productivity and shorten time-to-market, an automatic FFT generator can be used to design a specified FFT processor. In this thesis, we propose a parameterizable FFT generator with two approaches to make good design trade-off between throughput and area under the design constraints. First, the vertical expansion approach parallels the datapath to increase the throughput. Second, the horizontal compression approach folds the datapath to reduce the hardware usage. Besides, only the best FFT architecture is generated under the user-specified throughput constraint to reduce the computation time in our proposed FFT generator. Compared with the Pease architecture, for the length of 256 and 1024 cases, the generated FFT processor saves about 30.8% area under throughput constraints.

Various FFT architectures are proposed in literature. It can be implemented into our proposed FFT generator. In the future, more FFT algorithms such as the $R2³MDC$ FFT algorithm, mixed-radix FFT [\[17\]](#page-15-0) algorithm will be considered to enlarge the search space. Besides, the bitwidth optimization techniques proposed in [\[18\]](#page-15-1) will also be considered.

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六、 計畫成果自評

This year, we have developed:

- 1) An expandable multipath delay commutator based FFT architecture
- 2) An FFT generator to produce a synthesizable FFT core under a given throughput constraint

在計畫的研究成果豐碩,我們共發表一篇待審之長篇期刊,一篇待審之國際研討會論 文,一篇國際研討會論文,並申請了中國民國與美國專利。未來將能技術移轉運用於產業 界,提升研究的實用價值。雖然,期刊論文的發表進度稍有落後,但是,嚴謹的審查過程, 更能確保發表論文的品質。另外,本計書亦培育多位人才,共有一位博士班研究生、二位 碩士班研究生,目前均有很好的發展。

Submitted journal articles

- [1] Bu-Ching Lin, Juinn-Dar Huang, and Jing-Yang Jou "Bitwidth-Aware Multiple Constant Multiplication (MCM) Synthesis for FIR Filters," submitted to IEICE Transactions Fundamentals.
- [2] Bu-Ching Lin, Jhih-Hong Lu, Juinn-Dar Huang, and Jing-Yang Jou "Delay Optimal Compressor Tree Synthesis for LUT-Based FPGAs," submitted to ACM Transactions on Reconfigurable Technology and Systems.

International conference proceedings

- [1] Bu-Ching Lin, Yu-Hsiang Wang, Juinn-Dar Huang, and Jing-Yang Jou "Delay Optimal Compressor Tree Synthesis for LUT-Based FPGAs," submitted to IEEE International SOC Conference.
- [2] Yu-Hsiang Kao and Juinn-Dar Huang, "High-Performance NAND Flash Controller Exploiting Parallel Out-of-Order Command Execution," *Proc. of IEEE International Symposium on VLSI Design, Automation, and Test*, pp.160-163, Apr. 2010.

Patent

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- [2] 黃俊達、王毓翔、林步青、周景揚, "可參數化管線式快速傳利葉轉換硬體產生器," 中 華民國專利申請案號 099100407, 99 年 1 月 8 日
- [3] Juinn-Dar Huang, Jhih-Hong Lu, Bu-Ching Lin, and Jing-Yang Jou, "Delay optimal compressor tree synthesis for LUT-based FPGAs," US12/717,520, May 4, 2010

表一簡列近年本研究群的相關研究成果。95年發表會議論文3篇,期刊論文4篇,並 有4篇論文於 IEEE 期刊發表。96年發表會議論文3篇,期刊論文3篇,並有3篇論於 IEEE 期刊會議論文發表。97年發表會議論文 1 篇,期刊論文 3 篇,並有 3 篇論於 IEEE 期刊會 議論文發表,98年發表會議論文 1 篇,期刊論文 2 篇,並有 2 篇論於 IEEE 期刊會議論文 發表,99年發表會議論文 2 篇,期刊論文 3 篇,並有 2 篇論於 IEEE 期刊會議論文發表。

		Number of Papers				
Year	Domestic		International		SCI	
	Conference	Journal	Conference	Journal		
2006	0	\mathcal{O}	3	4	4	
				(IEEE: 2)		
2007	1	∩	$\overline{2}$	3	3	
				(IEEE: 2)		
2008	∩	∩	1	3	3	
				(IEEE: 3)		
2009	0	0	$\overline{2}$	\mathfrak{D}	$\mathcal{D}_{\mathcal{L}}$	
				(IEEE: 2)		
2010	1		1	3	$\overline{2}$	
				(IEEE: 1)		

表一、本研究群近年相關研究成果

可供推廣之研發成果資料表 一

※ **2.**本項研發成果若尚未申請專利,請勿揭露可申請專利之主要內容。

※ 3.本表若不敷使用,請自行影印使用。