# Microstrip Open-Loop Resonator With Multispurious Suppression

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*Abstract—***A compact open-loop resonator with multispurious suppression is proposed. When excited symmetrically, the resonator shows two tunable transmission zeros. By adjusting the open-end gap capacitance, one of the zeros is placed near the passband and the other is tuned to collocate with the leading two degenerated higher order resonances, so that the circuit has a sharp transition as well as a wide upper stopband. The experimental circuit shows the first spurious peak occurs at four times** the passband frequency  $(4f_o)$ , and the measurement shows good **agreement with the theoretic prediction.**

*Index Terms—***Bandpass filter (BPF), microstrip circuit, spurious suppression, stepped-impedance resonator (SIR), transmission zero.**

### I. INTRODUCTION

**MIATURIZATION** and wide rejection bandwidth are highly desirable for bandpass filters (BPFs) in radio frequency (RF) front ends of wireless communication systems. BPFs with a single resonator are attractive because they are compact and have a low inband insertion loss. Making planar resonators compact, the open-loop square ring [1], [2] and the hairpin [3] structures can be used. In general, single-resonator BPFs may have poor transition bands since its order is low. In addition, a uniform resonator inherently has spurious passbands at higher order resonances which may seriously degrade BPF performance in the upper stopband.

There have been numerous effective approaches for spurious suppression. The slow-wave resonators [1] and the stepped-impedance resonators (SIRs) [3], [4] push the spurious resonances to higher frequencies so as to extend the upper stopband. A low-pass or bandstop circuit can also be incorporated into a BPF for suppressing the unwanted spurious passbands [5]. By incorporating the ground-plane aperture [6] or the photonic bandgap configuration [7] into the design, the upper stopband can also be extended. The tradeoff, however, includes extra inband insertion loss and increased circuit size.

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Fig. 1. (a) Triangular open-loop SIR with input/output (I/O) feeders. (b) Equivalent circuit of the resonator.

In this letter, we introduce a novel SIR for filter design with a sharp transition band and multispurious suppression. The SIR is folded as an open triangular loop so that a capacitance exists between its two ends. When the resonator has symmetric input/output, two transmission zeros can be created in upper stopband. The zero placements can be controlled by adjusting the open-end gap capacitance. One of the zeros is placed near the passband so that the BPF has a sharp transition, and the other is tuned to suppress the two leading spurious responses. A BPF is fabricated and measured for demonstration.

## II. TRIANGULAR OPEN-LOOP SIR

The triangular open-loop resonator shown in Fig. 1(a) is simply a SIR with its two low-impedance sections bent to form an open-end capacitance. Tight coupling is purposely established between the two ends to provide a sufficiently large capacitance and an alternative path for the signal traveling from input to output port. Fig. 1(b) shows the equivalent circuit for analysis. The open-end capacitance  $C_1$  is a part of resonant condition. The dashed lines indicate the two possible signal paths.

Since the resonator is symmetric, the even-odd method [8], [9] can be used for simplifying the analysis. The corresponding resonant frequencies can be derived from the reduced circuits in Fig. 2(a) and Fig. 2(b). By enforcing the input admittance  $Y_{\text{in}}^o$  to zero, the resonant condition for the odd mode can be derived as

$$
Z_a \left( \frac{1}{2\omega C_1} - Z_a \tan \theta_a \right) - Z_b \tan \theta_b \left( Z_a + \frac{\tan \theta_a}{2\omega C_1} \right) = 0. \tag{1}
$$



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Fig. 2. Reduced equivalent circuit for analysis. (a) Odd mode. (b) Even mode.



Fig. 3. Calculations of the  $Y_{in}^o$  and  $Y_{in}^e$  with  $Z_a = Z_b = 54.7 \Omega$ ,  $l_a = 10 \text{ mm}$ ,  $l_b = 16$  mm, and  $C_1 = 0.05$  pF (a feed-in capacitance of 0.1 pF is assumed).

Similarly, the even mode resonant frequencies can be obtained by letting  $Y_{\text{in}}^e = 0$ 

$$
Z_b \tan \theta_a + Z_a \tan \theta_b = 0. \tag{2}
$$

Based on [8], the transmission zeros of the circuit Fig. 1(b) can be calculated by  $Y_{\text{in}}^o = Y_{\text{in}}^e$ 

$$
Z_b \sin 2\theta_b + Z_a \sin 2\theta_a - \frac{\cos^2 \theta_a}{\omega C_1} = 0.
$$
 (3)

Fig. 3 plots  $Y_{\text{in}}^o$  and  $Y_{\text{in}}^e$  versus frequency when  $Z_a = Z_b =$ 54.7  $\Omega$ ,  $l_a = 10$  mm,  $l_b = 16$  mm, and  $C_1 = 0.05$  pF. All resonant frequencies with zero input admittance are marked with dots. It can be seen that the fundamental resonance occurs in the odd mode, and the first higher-order resonance in the even mode, and so forth. As shown in the zoomed window, the intersections of the  $Y_{\text{in}}^o$  and  $Y_{\text{in}}^e$  curves are two transmission zeros,  $f_{z1}$  and  $f_{z2}$ ; both are less than the first spurious  $f_1$ . The creation of the two zeros is explained as follows. At  $f_{z1}$ , the slant section of the open triangular resonator in Fig. 1(a) is a quarter-wave open stub (including the effect of  $C_1$ ) so that the feeding point is virtually short-circuited. The zero  $f_{z2}$  is resulted from the multipath effect in which  $C_1$  is a portion of one of the two paths for the signal traveling from the input to the output port.

Since both zeros depend on the end-coupled capacitance, Fig. 4 investigates the variations of  $f_{z1}$  and  $f_{z2}$  versus  $C_1$  up to 0.1 pF. One can observe that  $f_{z1} < f_{z2}$  when  $C_1 > 0$  and  $f_{z1} = f_{z2}$  when  $C_1$  is zero. Also,  $f_{z1}$  has a larger variation when  $C_1$  is changed. Thus it can be used for generating a sharp transition band by controlling the value of  $C_1$  to allocate  $f_{z1}$ near the passband frequency  $f<sub>o</sub>$ .



Fig. 4. Transmission zeros versus end-coupled capacitance.  $Z_a = Z_b$ 54.7  $\Omega$ ,  $l_a = 10$  mm, and  $l_b = 16$  mm.



Fig. 5. Changes of normalized resonant frequencies and transmission zeros with respect to  $W_a$  for the triangular open-loop BPF.  $W_b = 1$  mm,  $g = 0.2$  mm,  $S = 0.2$  mm,  $l_a = 13.58$  mm,  $l_b = 19.4$  mm,  $\varepsilon_r = 10.2$ , and  $h = 1.27$  mm.

#### III. MULTISPURIOUS SUPPRESSION

To establish enough coupling between the resonator and the feeders, the line-to-loop coupling structure [10], [11] is adopted. Since one of our objects is to design a BPF with a stopband as wide as possible, the tuning of the resonances and the zeros is of paramount concern. As indicated in  $(1)$ – $(3)$ , the resonant frequencies and two zeros can be simultaneously tuned by adjusting  $W_a$  (or  $Z_a$ ) since both  $\theta_a$  and  $C_1$  depend much on it. Fig. 5 plots the zeros and the resonant frequencies for the fundamental mode and the leading three higher order modes against  $W_a$ . The software package IE3D is used for circuit simulation. All these frequencies are normalized with respect to the fundamental frequency of a straight half-wave resonator, i.e.,  $W_a = W_b$ . In Fig. 5, when  $W_a$  is increased, the two leading even mode frequencies,  $f_1$  and  $f_3$ , and the second zero  $f_{z2}$  increase faster than the odd mode resonances,  $f_0$  and  $f_2$ . This can be explained as follows. When  $W_a$  is increased, effective electric length  $\theta_a$  becomes shorter since the leg length  $l_a$  is tapered from the outside edge to the inside edge, and this results in a higher resonant frequency. Also, the odd mode currents concentrate at the center base of the triangle, so that the resonant frequencies are just slightly altered by the increase of  $W_a$ . On the other hand, the currents of the even mode and the second zero highly concentrate on the legs of the triangle. Consequently, the



Fig. 6. (a) Simulated and measured responses of the fabricated BPF. (b) Photograph of the fabricated circuit.  $f_o = 1.5$  GHz.  $W_a = 3.19$ ,  $W_b = 1$ ,  $g = 0.2$ ,  $S = 0.15$ ,  $l_a = 13.58$ , and  $l_b = 19.4$  (all in mm).

frequencies of  $f_1$ ,  $f_3$ , and  $f_{z2}$  increase more rapidly as  $W_a$  is increased. As shown in Fig. 5, frequency of  $f_{z2}$  is close to those of  $f_1$  and  $f_2$  when  $W_a = 3.2$  mm. If  $f_{z2}$  can effectively cancel the undesired peaks by  $f_1$  and  $f_2$ , the single resonator circuit will have a wide stopband up to  $4f_o$ . The collocation of the two spurious modes and zero is a general result for the particular open-loop SIR. When  $W_a$  is changed,  $C_1$ ,  $Z_a$  and  $\theta_a$  change at the same time and  $(1)$ – $(3)$  can be satisfied at the same frequency simultaneously.

## IV. EXPERIMENTAL RESULTS

A single open-loop resonator BPF with  $f<sub>o</sub> = 1.5$  GHz is designed and fabricated on a substrate with  $\varepsilon_r = 10.2$  (RT/duroid 6010) and thickness  $h = 1.27$  mm. Fig. 6(a) plots the simulated and measured responses. It can be observed that both responses have good agreement. The rejection level in the upper stopband is better than 25 dB before the spurious passband at  $4 f<sub>o</sub>$ . Detailed data show that the inband insertion loss is no larger than 0.5 dB and return loss better than 20 dB. The 3-dB bandwidth is 5%. Note that the first spurious response is at 6 GHz  $(4f<sub>o</sub>)$ . The simulated  $|S_{21}|$  response of a triangular open-loop resonator filter with  $W_a = W_b$  is also plotted for comparison. Fig. 6(b) shows the photograph of the circuit. The total circuit area is approximately 97.4  $mm<sup>2</sup>$ .

## V. CONCLUSION

A single-triangular open-loop resonator for bandpass filter application is presented. The circuit possesses a sharp passband skirt and a wide upper stopband up to four times the passband frequency. The former is achieved by placing a transmission zero near the passband and the latter is by collocating the second zero and the two leading higher order resonances through adjusting the geometric parameter of the resonator. Since only a single resonator is used, the filter has a compact size and exhibits a very good inband insertion loss.

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