

# Design of Power Control Mechanisms with PCM Realization for the Uplink of a DS-CDMA Cellular Mobile Radio System

Chung-Ju Chang, *Senior Member, IEEE*, Jeh-Ho Lee, and Fang-Ching Ren, *Student Member, IEEE*

**Abstract**—Power control (PC) is an important issue in a direct sequence-code division multiple access (DS-CDMA) cellular mobile radio system. Higher link performance and greater system capacity cannot be achieved unless an appropriate PC mechanism is employed. In previous research, a delta-modulation (DM) realization of strength-based and SIR-based PC mechanisms for uplink communication has been studied by simulation. In order to obtain higher PC trackability, in this paper we study a pulse-code-modulation (PCM) realization of the above two PC mechanisms for the uplink of a DS-CDMA cellular mobile radio system. The simulation results presented here indicate that PC mechanisms with PCM realization for the uplink can achieve a lower outage probability and thus higher link performance than PC mechanisms with DM realization. We also obtain optimal design parameters such as the stepsize and the control mode for the two PCM PC mechanisms. In addition, we compare the two PCM PC mechanisms in terms of their outage probability and stability and find that the strength-based mechanism has a higher outage probability but greater stability than the SIR-based mechanism.

## I. INTRODUCTION

THE code division multiple access (CDMA) scheme for cellular mobile radio systems was developed mainly for capacity reasons. Many papers [1], [2] have shown that CDMA can achieve a greater capacity than frequency division multiple access (FDMA) or time division multiple access (TDMA). However, several radio link techniques must be used for CDMA to provide greater capacity than these other schemes. One of the most important of these radio link techniques is appropriate control of transmitted power [1]–[3].

In a direct-sequence code division multiple access (DS-CDMA) system, users (mobiles) are distinguished by their respective spreading codes. Since these spreading codes are not completely orthogonal, in the despreading of a user's waveform, nonzero contributions to the user's test statistic may arise from the transmissions of other users in the system. This effect, which is called *self-jamming* [4], does not occur in FDMA or TDMA, which preserve the orthogonality of received signals almost completely.

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The authors are with the Department of Communication Engineering and Center for Telecommunications Research, National Chiao Tung University, Hsinchu, Taiwan 300, Republic of China.

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Because self-jamming may occur in DS-CDMA systems, the transmitted power of users has to be regulated so as to prevent mutual interference and maintain communication quality [1], [2], [4], [5]. Ariyavisitakul and Chang [6]–[9] have studied strength-based and SIR (signal-to-interference ratio)-based power control (PC) mechanisms with a fixed-step, or delta modulation (DM), realization for the reverse link (uplink). In [6] they also mentioned a variable-step approach and stated that variable-step PC may perform slightly better (in terms of system capacity) than the fixed-step approach, but they have not investigated the design of a variable-step mechanism in detail.

In this paper, we study a pulse-code-modulation (PCM) realization of these two PC mechanisms for the uplinks of a DS-CDMA cellular mobile radio system [10]. We have performed an extensive simulation analysis of the performance of the two mechanisms, along with a study of the sensitivity of each mechanism to all the relevant design parameters, including stepsize, control mode, loop delay, and desired power level. As we will see later, the PCM realization of a PC mechanism can achieve a lower outage probability and thus higher link performance than the DM realization of the same PC mechanism. Such a PCM PC mechanism could be applied in a personal access communication system that requires the same communication quality as a wired system. We have also compared strength-based and SIR-based PCM PC mechanisms, in terms of both outage probability and stability. Our findings show that the SIR-based PCM PC mechanism has less outage probability but greater instability than the strength-based PCM PC mechanism.

The remainder of the paper is organized as follows. In Section II, the strength-based and SIR-based PCM PC mechanisms are described. In Section III, the system model is introduced. The framework of the simulation program and the simulation results are presented in Section IV, and our concluding remarks appear in Section V.

## II. POWER CONTROL MECHANISMS WITH PCM REALIZATION

As their names indicate, the strength-based and the SIR-based PCM PC mechanisms are based on different objectives. The strength-based mechanism is based on the original idea of PC—to keep the power of all signals received at the base station as nearly the same as possible so as to mitigate the

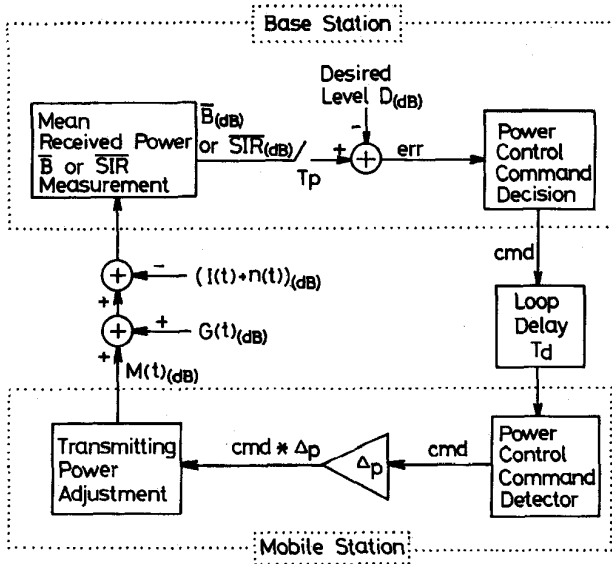


Fig. 1. Block diagram of the uplink power control mechanisms.

near-far effect. The SIR-based mechanism is based on the objective of directly controlling the communication quality or the system performance according to the SIR received at the base station. These two mechanisms force the transmitted power of the mobile to *track* the variation in the channel gain.

Fig. 1 depicts the block diagram of the uplink PCM PC mechanisms studied in this paper. If the base station measures the mean received signal strength (power) over a power measurement period, denoted by  $\bar{B}$ , and compares  $\bar{B}_{(dB)}$  with a *desired level*  $D_{(dB)}$  maintained at the base station, the PC is called a *strength-based PC mechanism*. Notice that  $\bar{B}$  and  $D$  are defined as ratios to some reference value. In our simulation analysis,  $\bar{B}$  was obtained by

$$\bar{B} = \frac{1}{T_p} \int_{T_p} M(t) \cdot G(t) dt \quad (1)$$

where  $M(t)$  is the transmitted power of the mobile,  $G(t)$  is the channel gain on the uplink, and  $T_p$  is the power measurement period. On the other hand, if the base station measures the mean received SIR on the desired uplink over a power measurement period, denoted by  $\overline{\text{SIR}}$ , and compares  $\overline{\text{SIR}}_{(dB)}$  with a *desired level*  $D_{(dB)}$ , the PC is called an *SIR-based PC mechanism*. In our simulation analysis,  $\overline{\text{SIR}}$  was obtained by

$$\overline{\text{SIR}} = \frac{\int_{T_p} M(t) \cdot G(t) dt}{\int_{T_p} (I(t) + n(t)) dt} \quad (2)$$

where  $I(t)$  is the interference power from all the other mobiles in the system and  $n(t)$  is the background noise.

The difference between  $\bar{B}_{(dB)}$  and  $D_{(dB)}$  in a strength-based mechanism, or the difference between  $\overline{\text{SIR}}_{(dB)}$  and  $D_{(dB)}$  in an SIR-based mechanism, denoted by  $err$ , is then fed into a "Power Control Command Decision" block. This block sends

a PC command, denoted by  $cmd$ , which is the realization of pulse code modulation (PCM) for  $err$ , to the mobile station via the feedback channel of the downlink (forward link) to track the variation in the channel gain. We define the PCM PC mechanism as follows.

*Definition:* A PCM PC mechanism in *control mode-n* is defined as a mechanism whose PC command set, denoted by  $CMD_n$ , is given by

$$CMD_n \triangleq \{-n, -(n-1), \dots, -1, 0, 1, \dots, n-1, n\}$$

where  $n$  is a natural number; and the corresponding decision rule for determining the PC command,  $cmd \in CMD_n$ , is given by

$$cmd = \begin{cases} -n & \text{if } key \in (n-0.5, \infty) \\ -n+1 & \text{if } key \in (n-1.5, n-0.5] \\ \vdots & \vdots \\ -1 & \text{if } key \in (0.5, 1.5] \\ 0 & \text{if } key \in (-0.5, 0.5] \\ 1 & \text{if } key \in (-1.5, -0.5] \\ \vdots & \vdots \\ n-1 & \text{if } key \in (-n+0.5, -n+1.5] \\ n & \text{if } key \in (-\infty, -n+0.5] \end{cases}$$

where  $key \triangleq err/\Delta_p$  and  $\Delta_p$  is the minimum *stepsize* for the power tracking.

Having received the PC command,  $cmd$ , the mobile transmits power  $M(t)$  updated by an amount of  $cmd \cdot \Delta_p_{(dB)}$ . The time period that the mobile takes for one operation of tracking, denoted by  $T_d$ , is called the *loop delay*. The loop delay consists of the following components: the power measurement period  $T_p$ , the uplink and the downlink propagation delays, and the time delay involved in generating, transmitting, and executing a PC command. The loop delay plays an important role in the PC mechanism, which will be explored below.

### III. SIMULATION MODEL

In our simulations, we considered only the uplinks of 19 cells in a DS-CDMA cellular mobile radio system and concentrated on a center cell surrounded by the other 18 cells in a hexagonal-grid configuration [8], [9]. The cells were assumed to be wrapped so as to avoid the edge effect; and the mobiles in these 19 cells were assumed to be randomly located with a uniform density and  $N_u$  mobiles per base station.

The radio signal at time  $t$  in the uplink of the center cell was assumed to be attenuated by a channel gain  $G(t)$  containing long-term fading, denoted by  $L(t)$ , which describes the local mean signal power, and short-term fading, denoted by  $S(t)$ , which accounts for multipath fading [11]. Hence, as shown in Fig. 1, given a mobile's transmitted power  $M(t)$ , the received power in the base station  $B(t)$  can be obtained by

$$B(t) = M(t) \cdot G(t) = M(t) \cdot L(t) \cdot S(t). \quad (3)$$

The long-term fading  $L(t)$  is a random variable modeled as

$$L(t) = \kappa \cdot r^{-\alpha} 10^{\xi/10} \quad (4)$$

where  $\kappa$  is a constant,  $r$  is the distance between the base station and the mobile station,  $\alpha$  is called the path loss exponent, and  $\xi$  is a normal-distributed random variable with zero mean and variance  $\sigma_L^2$  [11]. In our simulations, we let  $\kappa = 1$ ,  $\alpha = 4$ , and  $\sigma_L = 8$ . The short-term fading  $S(t)$  is also a random variable that is assumed to have Nakagami- $m$  statistics [12], [13]. After normalization by  $M(t) \cdot L(t)$ ,  $S(t)$  is gamma distributed with probability density function (pdf)  $g(\cdot)$ , which is given by

$$g(p) = \frac{1}{\Gamma(m)} (m)^m p^{m-1} \exp(-m \cdot p) \quad p > 0 \quad (5)$$

where  $\Gamma(\cdot)$  is the gamma function, the parameter  $m$  equals  $1/\text{AF}$ , and AF denotes the amount of fading, which is defined as the ratio of the variance of the received energy to the square of the mean of the received energy [12].

Two-branch antenna diversity was used at the base station receiver. For each diversity antenna, we assumed that two resolvable paths are captured by the receiver. The two captured signals were assumed to be equal in average strength, but with independent Nakagami-1 (i.e., Rayleigh) fading. After the signals on these two paths are combined, a Nakagami-2 faded signal can be assumed in each diversity antenna. The largest SIR in these two diversity antennae was then selected as the received SIR. On the other hand, each mobile scans signals from all the surrounding base stations and decides to communicate with the base station that has the largest time-averaged signal power. Note that the time-averaged signal power is in fact the long-term fading signal.

Moreover, over an observation period of loop delay, each mobile was assumed to move continuously within a small geographical area, so the radio uplink has uniform path loss and shadowing. Therefore, the long-term fading on each uplink, including the desired and the undesired fading, can be considered to be a constant during the observation period. The maximum Doppler frequency normalized by the power measurement sampling rate for each mobile, denoted by  $f_D T_p$ , can be considered to be a random variable, which is given by

$$\begin{aligned} f_D T_p &= \frac{V}{\lambda} T_p \\ &= \frac{F_0 V}{C} T_p \end{aligned} \quad (6)$$

where  $V$  is the speed of the mobile,  $\lambda$  is the wavelength,  $F_0$  is the central frequency of the signal, and  $C$  is the speed of light ( $= 3 \cdot 10^8$  m/s). For example, given that  $F_0 = 900$  MHz,  $V$  ranges from 6 km/h to 60 km/h, and  $T_p = 2$  ms,  $f_D T_p$  will range from 0.01 to 0.1. In our simulations, we assumed that  $f_D T_p$  was uniformly distributed over  $[0.01, 0.1]$ . The background noise and the minimum transmitted power were assumed to be  $10^{-10} M_{\max}$  and  $10^{-5} M_{\max}$ , respectively, where  $M_{\max}$  denotes the maximum transmitted power of a mobile. The maximum path loss due to distance was assumed to be on the order of 40 dB. The antenna used by the base station or the mobile was considered to be omnidirectional. Voice activity and soft handoffs were not considered in the simulations.

We here use the *outage probability* as our performance criterion [6], [14], [15]. The outage probability for a given

communication link  $i$ , denoted by  $P_0^{(i)}$ , is defined as

$$P_0^{(i)} \triangleq \Pr\{\overline{\text{SIR}}_i < \text{SIR}_0\} \quad (7)$$

where  $\overline{\text{SIR}}_i$  is the average SIR of the uplink  $i$  and  $\text{SIR}_0$  is the minimum SIR required to achieve a desired bit error rate [6]. The outage probability for the system, denoted by  $P_0$ , is defined as the average outage probability over all the in-cell links located in different positions of the center cell [14];  $P_0$  is given by

$$\begin{aligned} P_0 &\triangleq \frac{1}{|L_k|} \sum_{i \in L_k} P_0^{(i)} \\ &= \frac{1}{|L_k|} \sum_{i \in L_k} \Pr\{\overline{\text{SIR}}_i < \text{SIR}_0\} \end{aligned} \quad (8)$$

where  $L_k$  is the set of the in-cell links of the center cell and  $|L_k|$  is the size of the set  $L_k$ . If  $\overline{\text{SIR}}_i$  is averaged over a short-term period of a power measurement  $T_p$ , we call the outage probability the short-term outage probability [14], [15]; if  $\overline{\text{SIR}}_i$  is averaged over Rayleigh fading and is a local mean  $\overline{\text{SIR}}_i$ , we call the outage probability the long-term outage probability [6]. The short-term outage probability reflects the percentage of signal outages in which the measured short-term  $\overline{\text{SIR}}_i$  statistics falls below  $\text{SIR}_0$ . The long-term outage probability indicates the percentage of system outages in which a base station's coverage area has a local-mean  $\overline{\text{SIR}}_i$  of less than  $\text{SIR}_0$ . The short-term outage probability inherently is more variable (larger standard deviation) than the long-term outage probability. In the following simulation analysis, we will use the short-term outage probability to evaluate the gain in link performance and use the long-term outage probability to assess the gain in system capacity, for the two PCM PC mechanisms under study.

From [1], [6], [16], SIR can be expressed in terms of  $E_b/I_0$  as

$$\text{SIR} = \frac{E_b}{I_0} \cdot \left(\frac{W}{R}\right)^{-1} \quad (9)$$

where  $E_b$  is the energy per information bit,  $I_0$  is the interference power per hertz,  $R$  is the information bit rate, and  $W$  is the channel bandwidth. In our simulations, we assumed that the required performance in terms of the bit error rate is less than  $10^{-3}$ , and thus  $E_b/I_0$  should be larger than 5 (or 7<sub>(dB)</sub>) [2]; if we consider the spread spectrum processing gain  $W/R = 128$ , then we have the minimum required  $\text{SIR}_{0(\text{dB})} \triangleq -14_{(\text{dB})}$ .

## IV. SIMULATION RESULTS

### A. Framework of the Simulation Program

The framework of the simulation program was as follows:

#### Step 0: [Set Up System Parameters]

- Set up system parameters such as  $m$  (Nakagami- $m$ ),  $\kappa$ ,  $\alpha$ ,  $\sigma_L$ ,  $N_u$ ,  $F_0$ , and  $V$  for the DS-CDMA cellular mobile radio system.
- Set up system parameters such as  $T_p$ ,  $T_d$ , control mode  $n$ ,  $D_p$ , and  $D$  for the PC mechanism.

**Step 1: [Initialization]**

- Randomly assign the positions of the mobiles with uniform distribution.
- For each mobile, set up log-normally distributed long-term fading on its corresponding uplinks and then assign it a home base station.
- Set an initial power for each mobile.
- Set  $t = 0$ .

**Step 2: [Simulation over an Observation Period of Loop Delay ( $t, t + T_d$ )]**

- Simulate the short-term fading on each uplink, including desired and undesired fading.
- Measure the following items over a power measurement period  $T_p$  at each diversity antenna of each base station: the mean received power from each in-cell uplink and the total mean received power from all out-cell uplinks.
- Combine the signal on the diversity antenna for each desired uplink.
- According to the above measurements and the strength-based or SIR-based PCM PC mechanism, generate PC command for each mobile.
- After a delay time of  $(T_d - T_p)$ , the mobile receives the PC command and adjusts its transmitted power.
- Collect the received SIR data to calculate the local-mean SIR and the short-term and long-term outage probabilities.

**Step 3: [Repeat the Simulation]**

- Let  $t = t + T_d$  and go to **Step 2** unless  $t$  is greater than a preset threshold.

**Step 4: [Restart Another Simulation Cycle]**

- Go to **Step 1** to restart a new, independent simulation cycle unless the number of simulation cycles executed exceeds a preset threshold.

A total of 2000 simulation cycles were executed in our study. For each simulation cycle, the system conditions, including the mobile location and the long-term and short-term fading processes, were independently constructed; the initial transmitted power of the mobile was set to be inversely proportional to the long-term fading on its uplink. The total number of observation periods in each simulation cycle was 600, where the latter 400 periods were the average period over Rayleigh fading. We checked the first-order statistics, the CDF (cumulative distribution function) curve, of the simulated Nakagami- $m$  short-term fading for  $m \in \{1, \dots, 8\}$ , and the second-order statistics, i.e., the lcr (level crossing rate) curve, for  $m = 1$  [16]. These data showed that our short-term fading simulator was accurate [17].

**B. The Strength-Based PCM PC Mechanism**

$D$  is irrelevant in the strength-based PC mechanism, because an increment (decrement) in the desired level  $D$  would result in the same amount of increment (decrement) in the desired

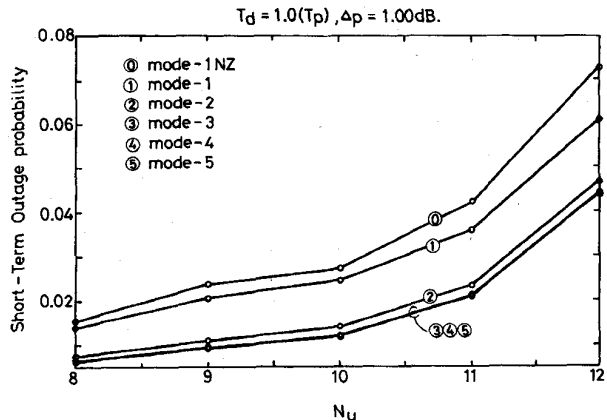


Fig. 2. Outage probability of the strength-based PCM PC mechanism versus  $N_u$  for control mode  $n \in \{1NZ, 1, 2, 3, 4, 5\}$ , given that  $\Delta_p = 1.00_{(dB)}$ ,  $T_d = 1.0T_p$ .

signal power and the interference power. Fig. 2 shows the short-term outage probability of the strength-based PCM PC mechanism versus  $N_u$  for various control mode- $n$ ,  $n \in \{1NZ, 1, 2, 3, 4, 5\}$ , given  $\Delta_p = 1_{(dB)}$ ,  $T_d = 1.0T_p$ . Mode-1NZ is defined as  $CMD_{1NZ} \triangleq \{-1, +1\}$ , where the PC command is determined by

$$cmd = \begin{cases} -1, & \text{if key} \geq 0 \\ 1, & \text{if key} < 0. \end{cases}$$

Mode-1NZ is in fact the DM PC mechanism previously studied in [6]–[9]. In Fig. 2, we find that the PCM PC performs better than the DM PC for the strength-based mechanism and the high-order mode in the PCM PC performs better than the low-order mode regardless of the system load  $N_u$ . This is because compared with a low-order mode, a high-order mode in the PCM PC mechanism has a wider dynamic range of adjustment power, which enables it to track the variation in the channel gain more accurately. However, the improvement provided by the high-order mode becomes insignificant when the control mode is greater than three. This is because the dynamic range of adjustment power in the PCM PC mechanism does not need to be too large for a given variation in short-term fading.

Fig. 3 shows the short-term outage probability of the strength-based PCM PC mechanism with mode- $n$ ,  $n \in \{1NZ, 1, 2, 3, 4, 5\}$ , versus  $\Delta_p$ , given that  $T_d = 1.0T_p$  and  $N_u = 9$ . We again find that a high-order mode performs better than a low-order mode regardless of the stepsize  $\Delta_p$ . We further observe that, for a given mode, if  $\Delta_p$  is either too small or too large, the outage probability increases. There exists an optimal  $\Delta_p^*$ , for the following reason. The transmitted power signal  $M(t)$  does not always track the variation in short-term fading exactly. The *err* signal between the mean received power signal  $\bar{B}$  and the desired level  $D$  in the base station can be classified into two types: quantization noise and slope overload noise [18]. Slope overload noise occurs when the stepsize  $\Delta_p$  is too small for the mobile to follow quick changes in short-term fading; quantization noise occurs for any step size but is small for a small stepsize. Therefore, there

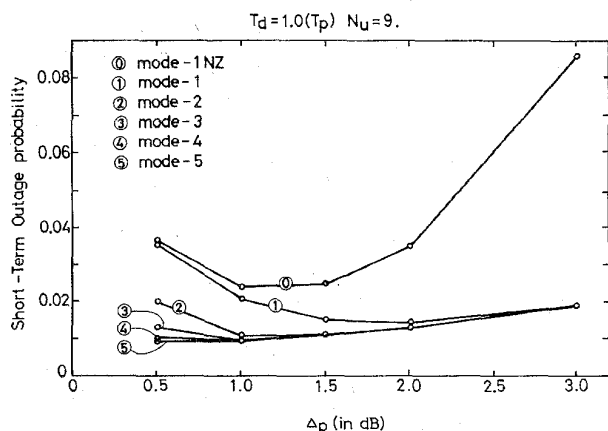


Fig. 3. Outage probability of the strength-based PCM PC mechanism versus  $\Delta_p$  for control mode  $n \in \{1NZ, 1, 2, 3, 4, 5\}$ , given that  $T_d = 1.0T_p$  and  $N_u = 9$ .

should clearly be an optimal value for the stepsize, since if the stepsize is increased, the quantization noise will increase but the slope overload noise will decrease. The higher the order of mode  $n$  is, the smaller  $\Delta_p^*$  will be. As  $n$  tends to infinity,  $\Delta_p^*$  tends to 0, which is the case of continuous-level PC [19].

Loop delay  $T_d$  is also an influential factor in determining the short-term outage probability of the system. Fig. 4 depicts the influence of  $T_d$  on the short-term outage probability of the strength-based PCM PC mechanism for various modes, given  $N_u = 9$  and  $\Delta_p = 1.0$  dB. As  $T_d$  increases from  $1.0T_p$ , the short-term outage probability also increases for all modes. This is because if the loop delay is too large, the PC command received by the mobile will already be obsolete and the mobile will be unable to track the variation in the channel fading accurately. As a result, the effectiveness of the PC mechanism deteriorates. We also observe that as  $T_d$  increases the short-term outage probability of the higher mode increases more rapidly than that of the lower mode. Finally, at a certain  $T_d$  there is a crossover between the performance curves of the higher mode and the lower mode. After the crossover, the low-order mode performs better than the high-order mode. This seems to indicate that when  $T_d$  is larger, the wide dynamic range of the high-order mode is not advantageous but leaves larger room for error. Notice that all modes in Fig. 4 operate with  $\Delta_p = 1.0$  dB, which is not the optimal stepsize at  $T_d \geq 1.4T_p$ . However, if the control mode  $n$  in Fig. 4 operates with its optimal value  $\Delta_p^*$  corresponding to  $T_d$ , the higher-order mode will always outperform the lower-order mode and the crossover should not occur. As for the curves of the long-term outage probability, they have the same trends as those for the short-term outage probability shown in above figures, but they are less variable.

### C. The SIR-Based PCM PC Mechanism

In the SIR-based PCM PC mechanism, the desired level  $D$  is an essential system parameter that must be considered. Fig. 5 shows the short-term outage probability of the SIR-

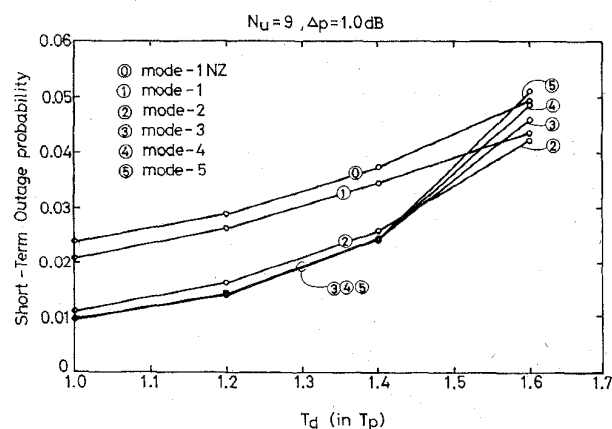


Fig. 4. Outage probability of the strength-based PCM PC mechanism versus  $T_d$  for control mode  $n \in \{1NZ, 1, 2, 3, 4, 5\}$ , given that  $N_u = 9$  and  $\Delta_p = 1.00$  dB.

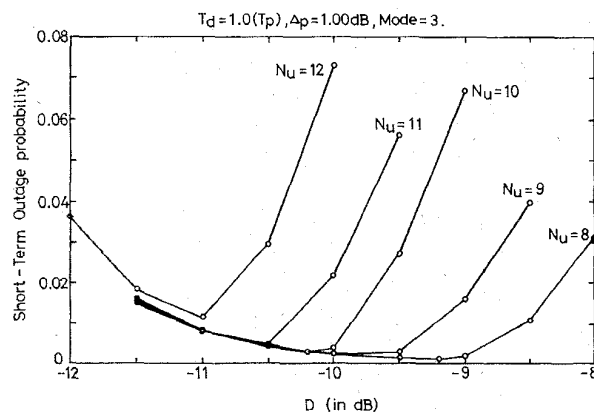


Fig. 5. Outage probability of the SIR-based PCM PC mechanism versus the desired level  $D$  for various system loads  $N_u \in \{8, 9, 10, 11, 12\}$ , given that  $T_d = 1.0T_p$ ,  $\Delta_p = 1.00$  dB, and control mode  $n = 3$ .

based PCM PC mechanism versus the desired level  $D$  (dB) for  $N_u \in \{8, 9, 10, 11, 12\}$ , given control mode  $n = 3$  and  $\Delta_p = 1.0$  dB. We find that for a given  $N_u$ , a relatively higher  $D$  and a relatively lower  $D$  cause a higher outage probability. There exists an optimal  $D$ , denoted by  $D^*$ , that provides the best link performance, for the following reason. According to our SIR-based PCM PC mechanism, the received  $\overline{\text{SIR}}$  should be concentrated at the desired level  $D$ . Hence, the pdf curve of the received  $\overline{\text{SIR}}$  has a peak at the desired level  $D$ . When the desired level  $D$  is low, most mobiles will be able to control their transmitted power so that their received  $\overline{\text{SIR}}$  is concentrated at the desired level  $D$ . As a result, the lower the desired level  $D$  (closer to  $\overline{\text{SIR}}_0$ ), the larger the short-term outage probability will be. When the desired level  $D$  is high, on the other hand, most mobiles will be commanded to increase their transmitted power, and as a mobile's transmitted power increases, its interference also increases, because of the increment in the other mobiles' transmitted power. Consequently, for most mobiles, the received  $\overline{\text{SIR}}$  will still not reach the desired level, and the mobiles will continue to increase their transmitted power until

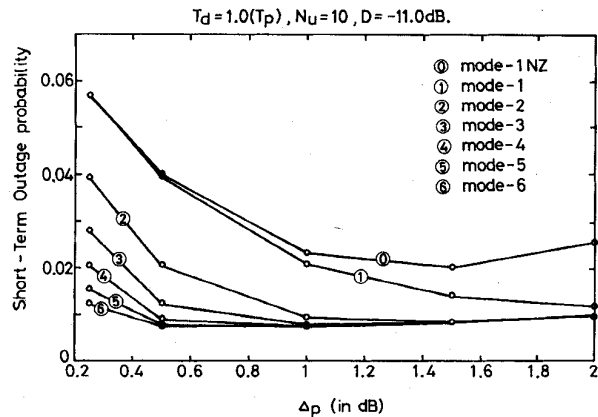


Fig. 6. Outage probability of the SIR-based PCM PC mechanism versus the stepsize  $\Delta_p$  for control mode  $n \in \{1\text{NZ}, 1, 2, 3, 4, 5, 6\}$ , given that  $T_d = 1.0T_p$ ,  $N_u = 10$ , and  $D = -11(\text{dB})$ .

the maximum transmitted power  $M_{\max}$  is reached. This will also cause the short-term outage probability to increase. We also find that the optimal desired level  $D^*$  increases as  $N_u$  decreases. If the SIR-based mechanism is required to provide optimal performance at any load, the optimal desired level  $D^*$  at each base station could be dynamically changed according to the system load  $N_u$ . However, it is difficult to obtain  $N_u$  and adjust  $D^*$  correctly. Here we suggest choosing a nearly optimal  $D$  so that the SIR-based mechanism will operate effectively for a wide range of traffic load. In the case shown in Fig. 5, we can choose  $D = -11(\text{dB})$  when  $N_u \leq 12$  so that the short-term outage probability remains around 0.01. Note that the choice of  $D$  also depends on other factors, such as the loop delay  $T_d$ , the control mode number  $n$ , and the stepsize  $\Delta_p$  [17].

Fig. 6 depicts the short-term outage probability of the SIR-based PCM PC mechanism versus the stepsize  $\Delta_p$  for control mode  $n \in \{1\text{NZ}, 1, 2, 3, 4, 5, 6\}$ , given  $T_d = 1.0T_p$ ,  $N_u = 10$ , and  $D = -11(\text{dB})$ . It is obvious that the high-order modes improve the link performance more than the low-order modes. This implies that the link performance can be enhanced by increasing the control mode number, as in the strength-based PCM PC mechanism. However, the performance improvement will become saturated if the mode number is large enough, regardless of the stepsize  $\Delta_p$ . The upper limit on the improvement in link performance would be offered by continuous-level PC (i.e.,  $n$  tending to infinity and  $\Delta_p$  tending to zero) [19]. The improvement is almost the same for control mode  $n \geq 3$ , given that  $\Delta_p$  is around  $1(\text{dB})$ . Note that in practice  $\Delta_p = 1(\text{dB})$  is a reasonable choice. The claim that the high-order modes perform better than the low-order modes still holds, regardless of  $N_u$  and  $D$  [17]. Since a higher-order mode wastes more system capacity in the feedback channel, we suggest adopting control mode  $n = 3$ .

Fig. 7 depicts the effect of the loop delay  $T_d$  on the short-term outage probability of the SIR-based PCM PC mechanism for various control modes, given  $\Delta_p = 1(\text{dB})$ ,  $D = -11(\text{dB})$ , and  $N_u = 10$ . The short-term outage probability of every control mode increases as  $T_d$  increases, and the superiority of the high mode holds unless  $T_d$  exceeds a certain threshold

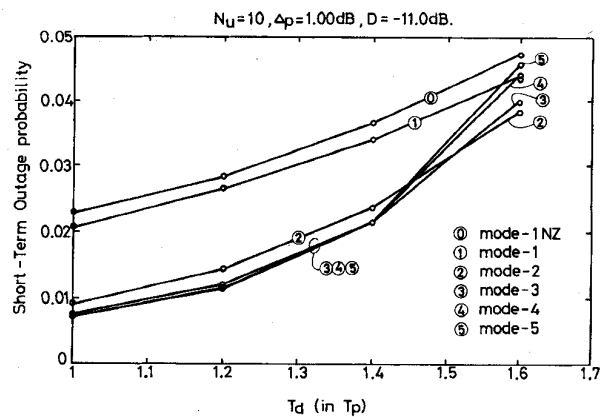


Fig. 7. Outage probability of the SIR-based PCM PC mechanism versus  $T_d$  for control mode  $n \in \{1\text{NZ}, 1, 2, 3, 4, 5\}$ , given that  $N_u = 10$ ,  $\Delta_p = 1.00(\text{dB})$ ,  $D = -11.0(\text{dB})$ .

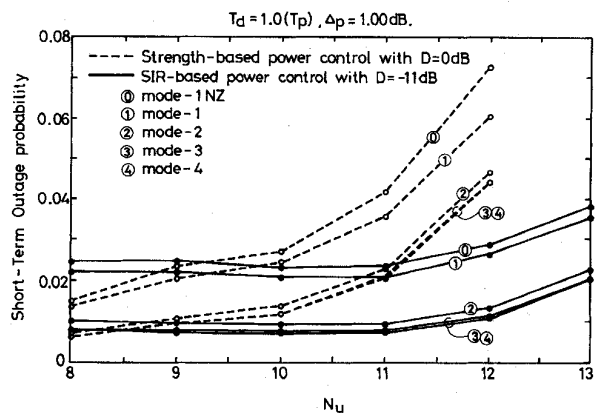


Fig. 8. Outage probability of the strength-based and the SIR-based PCM PC mechanisms versus  $N_u$  for control mode  $n \in \{1\text{NZ}, 1, 2, 3, 4\}$ , given that  $T_d = 1.0T_p$  and  $\Delta_p = 1.00(\text{dB})$ .

(around  $1.4 T_p$ ). Once  $T_d$  is larger than the threshold, the order of superiority of the various control modes is gradually reversed. The crossover phenomenon is the same as that in the strength-based PCM PC mechanism, but it is less dramatic. This could be because  $\overline{\text{SIR}}$  measurement reflects the signal quality more accurately than signal strength  $\overline{B}$  measurement does.

#### D. Comparison of the Two PCM PC Mechanisms

In this subsection, we compare the two PCM PC mechanisms in terms of the outage probability and stability. Fig. 8 illustrates the short-term outage probabilities of the two mechanisms versus  $N_u$ , given  $\Delta_p = 1(\text{dB})$  and  $T_d = 1.0T_p$ . From Fig. 8, we can claim that the system performance achievable by the SIR-based PC mechanism is superior to that achievable by the strength-based PC mechanism at most system loads. We also observe in the simulation that the superiority of the SIR-based PC mechanism always holds, regardless of the loop delay [17]. This is because  $\overline{\text{SIR}}$  reflects the quality of communication more accurately than  $\overline{B}$  does.

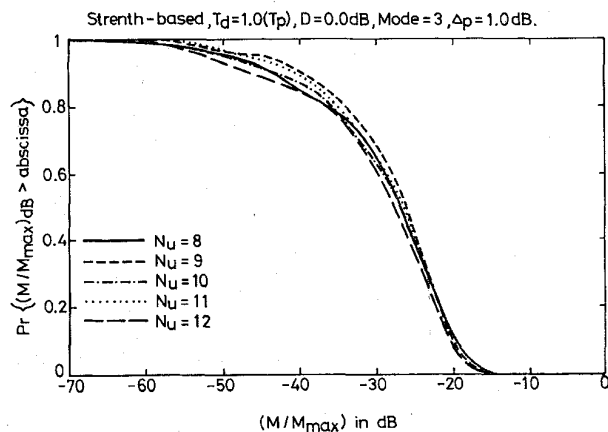


Fig. 9. Complementary CDF of the mobile's transmitted power in strength-based PCM PC mechanism for various  $N_u$ , given that  $T_d = 1.0T_p$ ,  $D = 0.0(\text{dB})$ , control mode  $n = 3$ , and  $\Delta_p = 1.0(\text{dB})$ .

Fig. 9 shows the complementary CDF of the transmitted power of a mobile with the strength-based PCM PC mechanism versus  $N_u$ , given control mode  $n = 3$ ,  $\Delta_p = 1(\text{dB})$ ,  $T_d = 1.0T_p$ , and  $D = 0(\text{dB})$ . As can be seen from the figure, the distribution of the mobile's transmitted power is similar for various  $N_u$ . This is because the power control processes for all desired uplinks are essentially mutually independent in the strength-based mechanism, and thus the mobile's transmitted power can be stably controlled. On the other hand, Fig. 10 depicts the complementary CDF of the transmitted power of a mobile with the SIR-based PCM PC mechanism versus  $N_u$ , given  $T_d = 1.0T_p$ ,  $D = -11.0(\text{dB})$ , control mode  $n = 3$ , and  $\Delta_p = 1(\text{dB})$ , in Fig. 10(a), and versus  $D$ , given  $T_d = 1.0T_p$ ,  $N_u = 10$ , control mode  $n = 3$ , and  $\Delta_p = 1(\text{dB})$ , in Fig. 10(b). From Fig. 10, we find that the distribution of a mobile's transmitted power in the SIR-based mechanism varies greatly as  $N_u$  or  $D$  varies. This is because of the interaction between the power control processes on each desired link in the SIR-based mechanism. We can explain this phenomenon as follows.

When  $N_u$  or  $D$  is relatively small, the interference power is usually small and the received SIR is usually higher than the desired  $D$ . Most mobiles will be commanded to decrease their transmitted power, and thus the mutual interference will also be reduced. The overall effect after one control period is that the received SIRs of most mobiles will still be higher than  $D$ , so the transmitted power of the mobile will be reduced repeatedly until the background noise comes to limit the received SIR. In contrast, when  $N_u$  or  $D$  is relatively high, the received SIR for most mobiles is smaller than the desired  $D$ . Most mobiles will thus be requested to increase their transmitted power in order to increase the received SIR. This will also result in an increase in the interference power. Consequently, the received SIR will still be smaller than the desired  $D$ , and the mobiles must increase their transmitted power repeatedly until they reach their maximum transmitted power. Therefore, a system with the SIR-based PC mechanism is unstable, because in general most mobiles must adjust their transmitted power toward its maximum limitation.

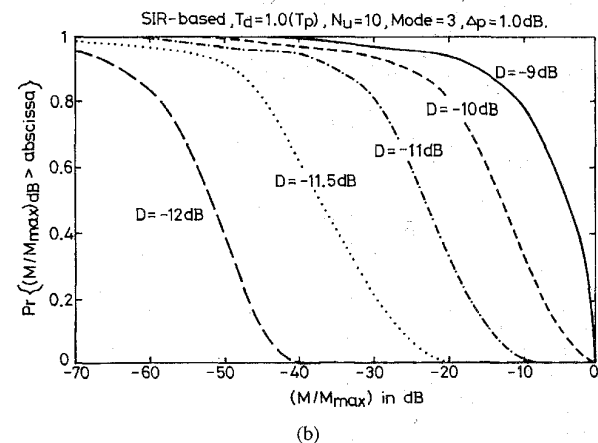
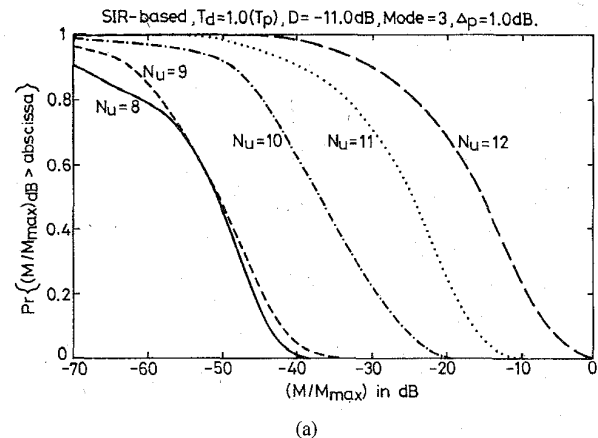


Fig. 10. Complementary CDF of the mobile's transmitted power in SIR-based PCM PC mechanism for various system loads  $N_u$  in (a) and for various  $D$  in (b).

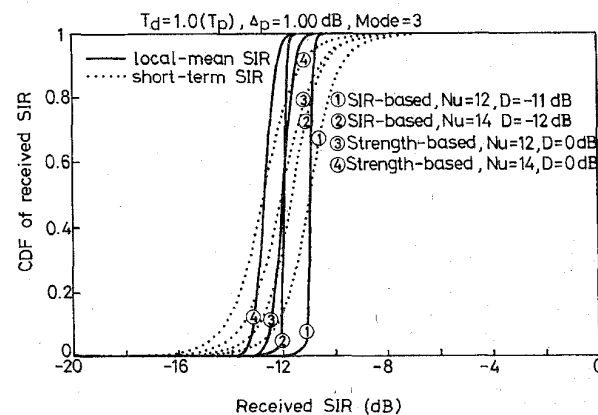


Fig. 11. CDF of the received SIR versus the number of users  $N_u$ .

We further plot the CDF's of the local-mean and the short-term received SIR in Fig. 11. The curve of the local-mean received SIR rises more steeply than that of the short-term received SIR, indicating that the local-mean received SIR is less variable, as we stated in the previous section. Fig. 12

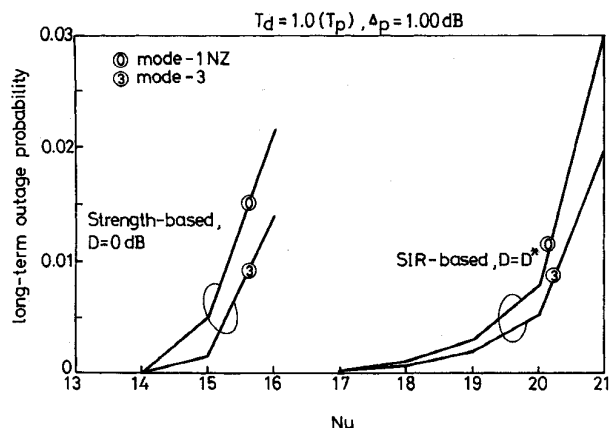


Fig. 12. Long-term outage probability versus the number of users  $N_u$ .

shows the long-term outage probability versus the number of users  $N_u$ . For a given number of users, the system reliability [6], expressed in percent, increases by one when the power control mode is changed from mode-1NZ to mode 3. Notice that the required percentile of system reliability is around 99%. For a 99th percentile of system reliability, the system capacity increases by 3% to 5% when the power control mode is changed from mode-1NZ to mode 3.

## V. CONCLUDING REMARKS

In this paper, we have studied uplink PC mechanisms with PCM realization for a DS-CDMA cellular mobile radio system. We have considered the strength-based and the SIR-based mechanisms and investigated system design parameters such as the PCM control mode, stepsize, and the desired power level. Our main findings are the following.

- 1) In both PCM PC mechanisms, there is an appropriate PCM control mode for a given stepsize. An excessively high PCM mode is not necessary.
- 2) There exists an optimal stepsize  $\Delta_p^*$  for a given variability in short-term fading; the magnitude of  $\Delta_p^*$  is inversely proportional to the PCM control mode.
- 3) When the SIR-based mechanism is used, it is important that the desired level  $D$  be selected carefully, but this is not necessary when the strength-based mechanism is used. Setting the desired level too high or too low in the SIR-based mechanism will significantly degrade the system performance. In particular, if the desired level is too high, most mobiles will be forced to transmit at maximum power.
- 4) The outage probability of the strength-based mechanism is generally higher than that of the SIR-based mechanism, whereas the mean transmitted power of the mobiles is more stable when the strength-based mechanism is used than when the SIR-based mechanism is used. Note that the system load and the desired level are also influential factors.
- 5) The loop delay has an important effect on the system performance. If the loop delay is small, a high PCM control mode yields better performance than a low

control mode. If the loop delay is large, on the other hand, the opposite is true.

The PCM PC can respond more flexibly to channel variations than the DM PC and yields significantly better link performance and a slightly larger system capacity. However, the PCM PC wastes more system capacity on the feedback channel (downlink), which negates some of the gain in the system capacity. The PCM PC should have a niche application in small-sized microcell PCS (personal communication service) systems which intend to obtain the same signal quality as wired systems. Also the PCM PC is more prone to PC command errors if the feedback channel is noisy. According to our observations, when the error rate in the downlink is less than  $10^{-1}$ , the superiority of high-order modes and the curve trends discussed here should hold.

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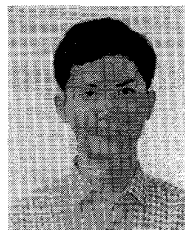
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**Chung-Ju Chang** (S'81-M'85-SM'94) received the B.E. and the M.E. degrees in electronics engineering from National Chiao Tung University, Hsinchu, Taiwan, in 1972, respectively, and the Ph.D. degree in electrical engineering from National Taiwan University in 1985.

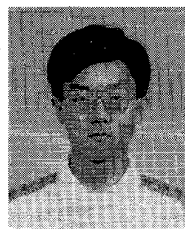
From 1976 to 1988, he was with Telecommunication Laboratories, Directorate General of Telecommunications, Ministry of Communications, Republic of China, as a Design Engineer, Supervisor, Project Manager, and then Division Director. There, he was involved in designing digital switching system, ISDN user-network interface, and ISDN service and technology trials. In the meantime, he also acted as a Science and Technical Advisor for Minister of the Ministry of Communications from 1987 to 1989. In August 1988, he joined the faculty of the Department of Communication Engineering and Center for Telecommunications Research, College of Electrical Engineering and Computer Science, National Chiao Tung University, where he is currently Professor. His research interests include performance evaluation, ATM (asynchronous transfer mode) networks, and mobile radio networks.

Dr. Chang is a member of the Chinese Institute of Engineers (CIE).



**Jeh-Ho Lee** was born in Taiwan, ROC, on Nov. 24, 1969. He received the B.E. and M.E. degrees in Telecommunication Engineering from National Chiao Tung University, Hsinchu, Taiwan, in 1991 and 1993, respectively.

He is now employed as an Engineer in a communication equipment company.



**Fang-Ching Ren** (S'94) received the B.E. and M.E. degrees in telecommunication engineering from National Chiao Tung University, Hsinchu, Taiwan, in 1992 and 1994, respectively. Currently, he is working toward the Ph.D. degree.

His research interests include performance analysis, protocol design, and mobile radio network.