

# Adaptive Neuro-Wavelet Control for Switching Power Supplies

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**Abstract**—The switching power supplies can convert one level of electrical voltage into another level by switching action. They are very popular because of their high efficiency and small size. This paper proposes an adaptive neuro-wavelet (ANW) control system for the switching power supplies. In the ANW control system, a neural controller is the main controller used to mimic an ideal controller and a compensated controller is designed to recover the residual of the approximation error. In this study, an online adaptive law with a variable optimal learning-rate is derived based on the Lyapunov stability theorem, so that not only the stability of the system can be guaranteed but also the convergence of controller parameters can be speeded up. Then, the proposed ANW control system is applied to control a forward switching power supply. Experimental results show that the proposed ANW controller can achieve favorable regulation performance for the switching power supply even under input voltage and load resistance variations.

**Index Terms**—Adaptive control, Lyapunov stability theorem, optimal learning-rate, switching power supply, wavelet neural network (WNN).

## I. INTRODUCTION

RECENTLY, the neural-network-based control technique has represented an alternative design method for various control systems [1]–[5]. The successful key element is the approximation ability, where the parameterized neural network can approximate an unknown system dynamics through learning. Wavelets have been combined with the neural network to create wavelet neural networks (WNNs). The training algorithms for WNN typically converge in a smaller number of iterations than the conventional neural networks [6]–[8]. Unlike the sigmoid functions used in conventional neural networks, the second layer of WNN is a wavelet form, in which the translation and dilation parameters are included. Thus, WNN has been proved to be better than the other neural networks in that the structure can provide more potential to enrich the mapping relationship between inputs and outputs [8]. There has been considerable interest in exploring the applications of WNN to deal with nonlinearity and uncertainties of real-time servo control systems [9]–[12]. These WNN-based controllers combine the capability of artificial neural networks for learning

ability and the capability of wavelet decomposition for identification ability. Thus, the WNN-based control systems have been adopted widely for the closed-loop control of complex dynamical systems owing to its fast learning property and good generalization capability [9], [10].

Due to the rapid development of power semiconductor devices in personal computers, computer peripherals, and adapters, the switching power supplies are popular in modern industrial applications. To obtain high quality power systems, the popular control technique of the switching power supplies is the pulsewidth modulation (PWM) approach [13], [14]. By varying the duty ratio of the PWM modulator, the switching power supply can convert one level of electrical voltage into the desired level. From the control viewpoint, the controller design of the switching power supply is an intriguing issue, which must cope with wide input voltage and load resistance variations to ensure the stability in any operating condition while providing fast transient response. Over the past decade, there have been many different approaches proposed for PWM switching control design based on PI control [15], optimal control [16], sliding-mode control [17], [18], fuzzy control [17], [19], and adaptive control [20] techniques. However, most of these approaches require the time-consuming trial-and-error tuning procedure to achieve satisfactory performance; some of them can not achieve satisfactory performance under the changes of operating point; and some of them have not given the stability analysis.

The motivation of this paper is to design an adaptive neuro-wavelet (ANW) control system for the switching power supply. The proposed ANW control system is comprised of a neural controller and a compensated controller. The neural controller using a WNN is designed to mimic an ideal controller and a compensated controller is designed to compensate for the approximation error between the ideal controller and the neural controller. The online adaptive laws are derived based on the Lyapunov stability theorem so that the stability of the system can be guaranteed. Finally, the proposed ANW control scheme is applied to control a forward switching power supply. The experimental results demonstrate that the proposed ANW control scheme can achieve favorable control performance, even the switching power supply is subject to the input voltage and load resistance variations.

## II. PROBLEM FORMULATION

The switching power supplies can convert one level of electrical voltage into another level by switching action. Nowadays, they are very popular because of its high efficiency and small size [13]. Among the various switching control methods, PWM which is based on fast switching and duty ratio control is the

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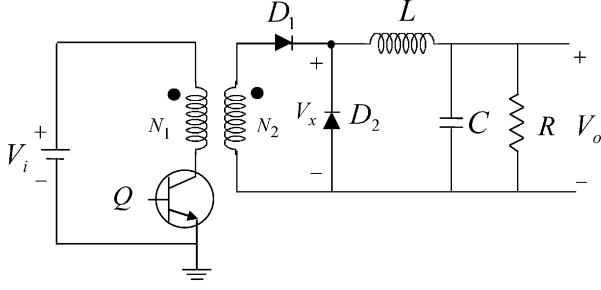


Fig. 1. Forward switching power supply.

most widely considered one. The switching frequency is constant and the duty cycle,  $d(N)$ , varies with the load resistance variations at the  $N$ th sampling time. The output of the designed controller,  $\delta d(N)$ , is the change of duty cycle. Then, the duty cycle is determined by adding the previous duty cycle  $d(N-1)$  to the change of duty cycle  $\delta d(N)$ , i.e.

$$d(N) = d(N-1) + \delta d(N). \quad (1)$$

This duty cycle signal is then sent to a PWM output stage that generates the appropriate switching pattern for the switching power supplies. In this paper, a forward switching power supply is discussed as shown in Fig. 1, where  $V_i$  and  $V_o$  are the input and output voltages of the converter, respectively,  $D_1$  and  $D_2$  are the diodes,  $L$  is the inductor,  $C$  is the output capacitor,  $R$  is the resistor, and  $Q$  is the transistor which control the converter circuit operating in different modes. When the transistor is ON,  $V_i$  appears across the primary and then generates

$$V_x = \frac{N_2}{N_1}(V_i - V_{\text{lost}}) \quad (2)$$

where  $N_1$  is the turns of primary power winding,  $N_2$  is the turns of slave power winding, and  $V_{\text{lost}}$  denotes the voltage drop occurring by transistor and diodes and represents the unmodeled dynamics in practical applications. The diode  $D_1$  on the secondary ensures that only positive voltages are applied to the output circuit while diode  $D_2$  provides a circulating path for inductor current. By the averaging method, the output voltage can be expressed as [13]

$$V_o = \frac{N_2}{N_1}(V_i - V_{\text{lost}})d. \quad (3)$$

Since  $N_1$ ,  $N_2$ , and  $V_i - V_{\text{lost}}$  are considered as constants, differentiating both sides of (3) with respect to time yields

$$\dot{V}_o = \frac{N_2}{N_1}(V_i - V_{\text{lost}})\delta d = gu \quad (4)$$

where  $g \equiv (N_2/N_1)(V_i - V_{\text{lost}})$  is the control gain which is a positive constant and  $u \equiv \delta d$  is the controller output. The control problem of forward switching power supplies is to control the change of duty cycle  $\delta d$  so that the output voltage  $V_o$  can provide a fixed voltage under the occurrence of the uncertainties such as the wide input voltages and load variations. The output error voltage is defined as

$$e = V_{\text{ref}} - V_o \quad (5)$$

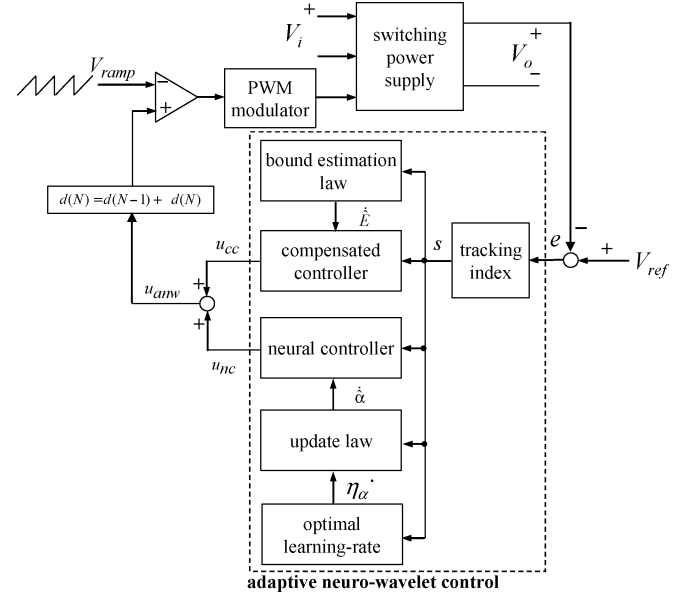


Fig. 2. Block diagram of the ANW control for switching power supply.

where  $V_{\text{ref}}$  is the output reference voltage. The control law of the duty cycle is determined by the error voltage signal to provide fast transient response and small overshoot in the output voltage. If the system parameters are well known, an ideal controller can be designed as

$$u^* = g^{-1}(\dot{V}_{\text{ref}} + ke). \quad (6)$$

If  $k$  is chosen to correspond to the coefficients of a Hurwitz polynomial, that is a polynomial whose roots lie strictly in the open left half of the complex plane, then  $\lim_{t \rightarrow \infty} e = 0$ . Since the system parameters may be unknown or perturbed, the ideal controller  $u^*$  in (6) can not be precisely implemented.

### III. DESIGN OF ADAPTIVE NEURO-WAVELET CONTROL

In order to efficiently control the output voltage of the switching power supplies, an ANW control system shown in Fig. 2 is introduced. The configuration of the ANW control system consists of a neural controller and a compensated controller, i.e.

$$u_{\text{anw}} = u_{\text{nc}} + u_{\text{cc}} \quad (7)$$

where  $u_{\text{nc}}$  is the neural controller and  $u_{\text{cc}}$  is the compensated controller. The neural controller uses a WNN to mimic the ideal controller and the compensated controller is designed to compensate for the difference between the ideal controller and the neural controller. Substituting (7) into (4), we get

$$\dot{V}_o = g(u_{\text{nc}} + u_{\text{cc}}). \quad (8)$$

The error equation governing the system can be obtained by combining (6) and (8), i.e.

$$\dot{e} + ke = g(u^* - u_{\text{nc}} - u_{\text{cc}}). \quad (9)$$

### A. Wavelet Neural Network

A four-layer WNN shown in Fig. 3, which comprises an input layer (the  $i$  layer), a mother wavelet layer (the  $j$  layer), a wavelet layer (the  $k$  layer), and an output layer (the  $o$  layer), is adopted to implement the neural controller. The signal propagation and the basic function in each layer are now introduced. In this subsection, the superscript denotes the number of layer. For every node  $i$  in the input layer, the net input and the net output are represented as follows.

Layer 1: Input Layer:

$$net_i^1 = x_i^1 \quad (10)$$

$$y_i^1 = f_i^1(net_i^1) = net_i^1, \quad i = 1, 2, \dots, n_L. \quad (11)$$

Layer 2: Wavelet Layer:

A family of wavelets is constructed by translations and dilations performed on the mother wavelet. In the mother wavelet layer each node performs a wavelet  $\phi_j$  that is derived from its mother wavelet. For the  $j$ th node

$$net_j^2 = \frac{x_i^2 - m_{ij}}{\sigma_{ij}} \quad (12)$$

$$y_j^2 = f_j^2(net_j^2) = \phi_j(net_j^2), \quad j = 1, 2, \dots, n_M \quad (13)$$

where  $m_{ij}$  and  $\sigma_{ij}$  are, respectively, the translation and dilation in the  $j$ th term of the  $i$ th input  $x_i^2$  to the node of mother wavelet layer and  $n_M$  is the total number of the wavelets with respect to the input nodes.

Layer 3: Inference Layer:

Each node  $k$  in the wavelet layer is denoted by  $\prod$ , which multiplies the input signals and outputs the result of the product, i.e., the product of  $j$  mono-dimensional wavelets with respect to the input node. For the  $k$ th rule node

$$net_k^3 = \prod_j x_j^3 \quad (14)$$

$$y_k^3 = f_k^3(net_k^3) = net_k^3, \quad k = 1, 2, \dots, n_N \quad (15)$$

where  $x_j^3$  represents the  $j$ th input to the node of wavelet layer and  $n_N$  is the number of wavelets.

Layer 4: Output Layer:

The single node  $o$  in the output layer is labelled as  $\Sigma$ , which computes the overall output as the summation of all input signals

$$net_o^4 = \sum_k \alpha_k^4 \cdot x_k^4 \quad (16)$$

$$y_o^4 = f_o^4(net_o^4) = net_o^4 \quad (17)$$

where the connecting weight  $\alpha_k^4$  is the output action strength of the  $k$ th output associated with the  $k$ th wavelet and  $x_k^4$  represents the  $k$ th input to the node of output layer.

There are many kinds of wavelets that can be used in WNN. In this paper, the Gaussian wavelet function  $\phi(x) = \cos(\omega x) \exp(-x^2)$  is selected as a mother wavelet and one can take direct products of such scalar wavelets in the multidimensional case in which  $\omega$  is the frequency. Define the

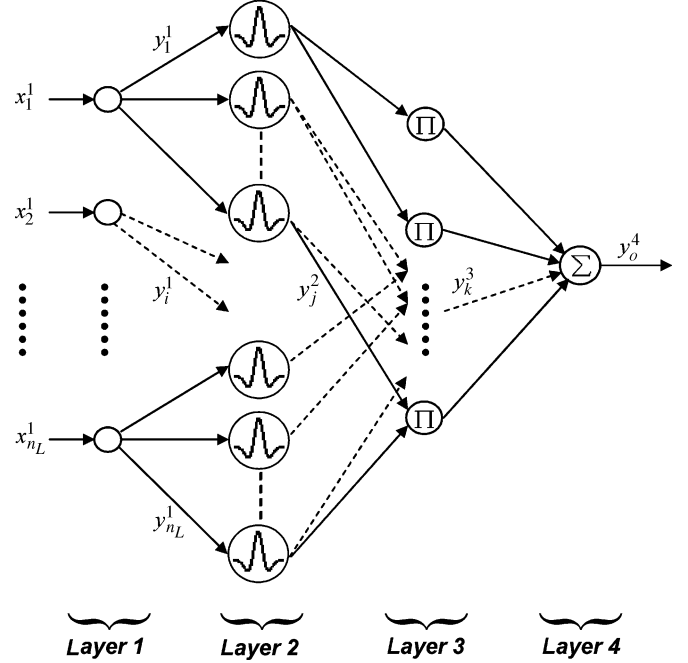


Fig. 3. Structure of wavelet neural network.

vectors  $\sigma$  and  $m$  collecting all parameter of hidden layer in WNN as

$$\sigma = [\sigma_{11} \cdots \sigma_{n_M 1} \sigma_{12} \cdots \sigma_{n_M 2} \cdots \sigma_{1 n_M} \cdots \sigma_{n_M n_M}]^T \quad (18)$$

$$m = [m_{11} \cdots m_{n_M 1} m_{12} \cdots m_{n_M 2} \cdots m_{1 n_M} \cdots m_{n_M n_M}]^T \quad (19)$$

Then the output of the WNN can be represented in a vector form

$$y_o^4(x, \sigma, m, \alpha) = \alpha^T \Theta(x, \sigma, m) \quad (20)$$

where  $x = [x_1^1, x_2^1, \dots, x_{n_L}^1]^T$ ,  $\alpha = [\alpha_1, \alpha_2, \dots, \alpha_{n_N}]^T$ , and  $\Theta = [\Theta_1, \Theta_2, \dots, \Theta_{n_N}]^T = [x_1^4, x_2^4, \dots, x_{n_N}^4]^T$ .

### B. Control System Design

The neural controller is designed to estimate the ideal controller in (6). By the universal approximation theorem [21], there exists an optimal neural controller  $u_{nc}^*$  such that

$$u^* = u_{nc}^* + \varepsilon \equiv \alpha^{*T} \Theta + \varepsilon \quad (21)$$

where  $\varepsilon$  is a minimum approximation error and  $\alpha^*$  is the optimal parameter vector of  $\alpha$ . The approximation error  $\varepsilon$  is assumed to be bounded by a positive constant  $E$  (i.e.,  $|\varepsilon| < E$ ). This approximation error bound  $E$  is generally unobtainable in practical applications, so that it will be estimated in the following derivations. Moreover, the optimal neural controller  $u_{nc}^*$  can not be obtained, so that an online estimation neural controller is defined as

$$u_{nc} = \hat{\alpha}^T \Theta \quad (22)$$

where  $\hat{\alpha}$  is an estimate of the optimal parameter vector  $\alpha^*$ . Define the estimation error  $\tilde{u}$  as

$$\tilde{u} = u^* - u_{nc} = \alpha^{*T} \Theta + \varepsilon - \hat{\alpha}^T \Theta = \tilde{\alpha}^T \Theta + \varepsilon \quad (23)$$

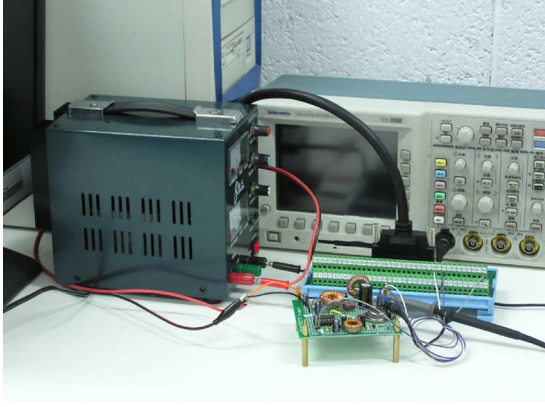


Fig. 4. Snapshot of the experiment setup.

where  $\tilde{\alpha} = \alpha^* - \hat{\alpha}$ . Define a tracking index as

$$s = e + k \int_0^t e d\tau \quad (24)$$

which is the input of the neural network. Then, the error (9) can be rewritten as

$$\dot{s} = g(\tilde{\alpha}^T \Theta + \varepsilon - u_{cc}). \quad (25)$$

To relax the requirement of the uncertain bound  $E$ , a bound estimation mechanism is developed to observe the bound of the approximation error. Define the estimation error of the bound

$$\tilde{E} = E - \hat{E} \quad (26)$$

where  $\hat{E}$  is the estimated error bound. To guarantee the stability of the adaptive neuro-wavelet control approach, a Lyapunov function candidate is defined as

$$V_1(s, \tilde{\alpha}, \tilde{E}) = \frac{1}{2}s^2 + \frac{g}{2\eta_\alpha} \tilde{\alpha}^T \tilde{\alpha} + \frac{g}{2\eta_E} \tilde{E}^2 \quad (27)$$

where  $\eta_E$  is a constant learning-rate, and  $\eta_\alpha$  is a variable learning-rate, which will be discussed in the following subsection to speed up the convergence of controller parameter. Differentiating (27) with respect to time and using (25), we get

$$\begin{aligned} \dot{V}_1(s, \tilde{\alpha}, \tilde{E}) &= s\dot{s} + \frac{g}{\eta_\alpha} \tilde{\alpha}^T \dot{\tilde{\alpha}} - \frac{g}{2\eta_\alpha^2} \tilde{\alpha}^T \dot{\tilde{\alpha}} \eta_\alpha + \frac{g}{\eta_E} \tilde{E} \dot{\tilde{E}} \\ &= sg(\tilde{\alpha}^T \Theta + \varepsilon - u_{cc}) + \frac{g}{\eta_\alpha} \tilde{\alpha}^T \dot{\tilde{\alpha}} \\ &\quad - \frac{g}{2\eta_\alpha^2} \tilde{\alpha}^T \dot{\tilde{\alpha}} \eta_\alpha + \frac{g}{\eta_E} \tilde{E} \dot{\tilde{E}} \\ &= g\tilde{\alpha}^T \left( s\Theta + \frac{\dot{\tilde{\alpha}}}{\eta_\alpha} - \tau \right) + sg(\varepsilon - u_{cc}) \\ &\quad + \frac{g}{\eta_E} \tilde{E} \dot{\tilde{E}} - \frac{g}{2\eta_\alpha^2} \tilde{\alpha}^T \dot{\tilde{\alpha}} \eta_\alpha \end{aligned} \quad (28)$$

where  $\tau = \tilde{\alpha} \dot{\eta}_\alpha / 2\eta_\alpha^2$ . For achieving  $\dot{V}_1 \leq 0$ , the adaptive laws and the compensated controller are chosen as

$$u_{cc} = \hat{E} \text{sgn}(s) \text{sgn}(g) = \hat{E} \text{sgn}(s) \quad (29)$$

$$\dot{\tilde{\alpha}} = -\dot{\hat{\alpha}} = -\eta_\alpha (s\Theta - \tau) \quad (30)$$

$$\dot{\tilde{E}} = -\dot{\hat{E}} = -\eta_E |s| \text{sgn}(g) = -\eta_E |s| \quad (31)$$

where  $\text{sgn}(\cdot)$  is a sign function. Then (28) can be rewritten as

$$\begin{aligned} \dot{V}_1(s, \tilde{\alpha}, \tilde{E}) &= \varepsilon sg - \hat{E} |s| |g| - (E - \hat{E}) |s| |g| \\ &\leq |\varepsilon| |s| |g| - E |s| |g| \\ &= - (E - |\varepsilon|) |s| |g| \leq 0. \end{aligned} \quad (32)$$

Since  $\dot{V}_1(s, \tilde{\alpha}, \tilde{E})$  is negative semidefinite, that is  $V_1(s(t), \tilde{\alpha}(t), \tilde{E}(t)) \leq V_1(s(0), \tilde{\alpha}(0), \tilde{E}(0))$ , it implies that  $s$ ,  $\tilde{\alpha}$ , and  $\tilde{E}$  are bounded. Let function  $\Omega(t) \equiv (E - |\varepsilon|) |s| |g| \leq -\dot{V}_1$ , and integrate  $\Omega(t)$  with respect to time, then it is obtained that

$$\int_0^t \Omega(\tau) d\tau \leq V_1(s(0), \tilde{\alpha}(0), \tilde{E}(0)) - V_1(s(t), \tilde{\alpha}(t), \tilde{E}(t)). \quad (33)$$

Because  $V_1(s(0), \tilde{\alpha}(0), \tilde{E}(0))$  is bounded, and  $V_1(s(t), \tilde{\alpha}(t), \tilde{E}(t))$  is nonincreasing and bounded, the following result can be obtained:

$$\lim_{t \rightarrow \infty} \int_0^t \Omega(\tau) d\tau < \infty. \quad (34)$$

Moreover, since  $\dot{\Omega}(t)$  is bounded, by Barbalat's Lemma [22],  $\lim_{t \rightarrow \infty} \Omega(t) = 0$ . That is,  $s \rightarrow 0$  as  $t \rightarrow \infty$ . As a result, the stability of the proposed adaptive neuro-wavelet system can be guaranteed.

### C. Convergence Analyses

The adaptive law shown in (30) calls for a proper choice of the learning-rate  $\eta_\alpha$ . For a small value of learning-rate, the convergence of controller parameter can be guaranteed but the convergent speed is very slow. On the other hand, if the learning-rate is too large, the parameter convergence may become more unstable. In order to train the WNN efficiently, an optimal learning-rate will be derived to achieve the fast convergence of output tracking error. First, the adaptive law shown in (30) can be rewritten as

$$\dot{\hat{\alpha}}_k = \eta_\alpha s x_k^4. \quad (35)$$

The central part of the training algorithm for a WNN concerns how to obtain recursively a gradient vector in which each element in the training algorithm is defined as the derivative of an energy function with respect to a parameter of the network. This is done by means of the chain rule, and this method is generally referred to as the back-propagation learning rule, because the gradient vector is calculated in the direction opposite to the

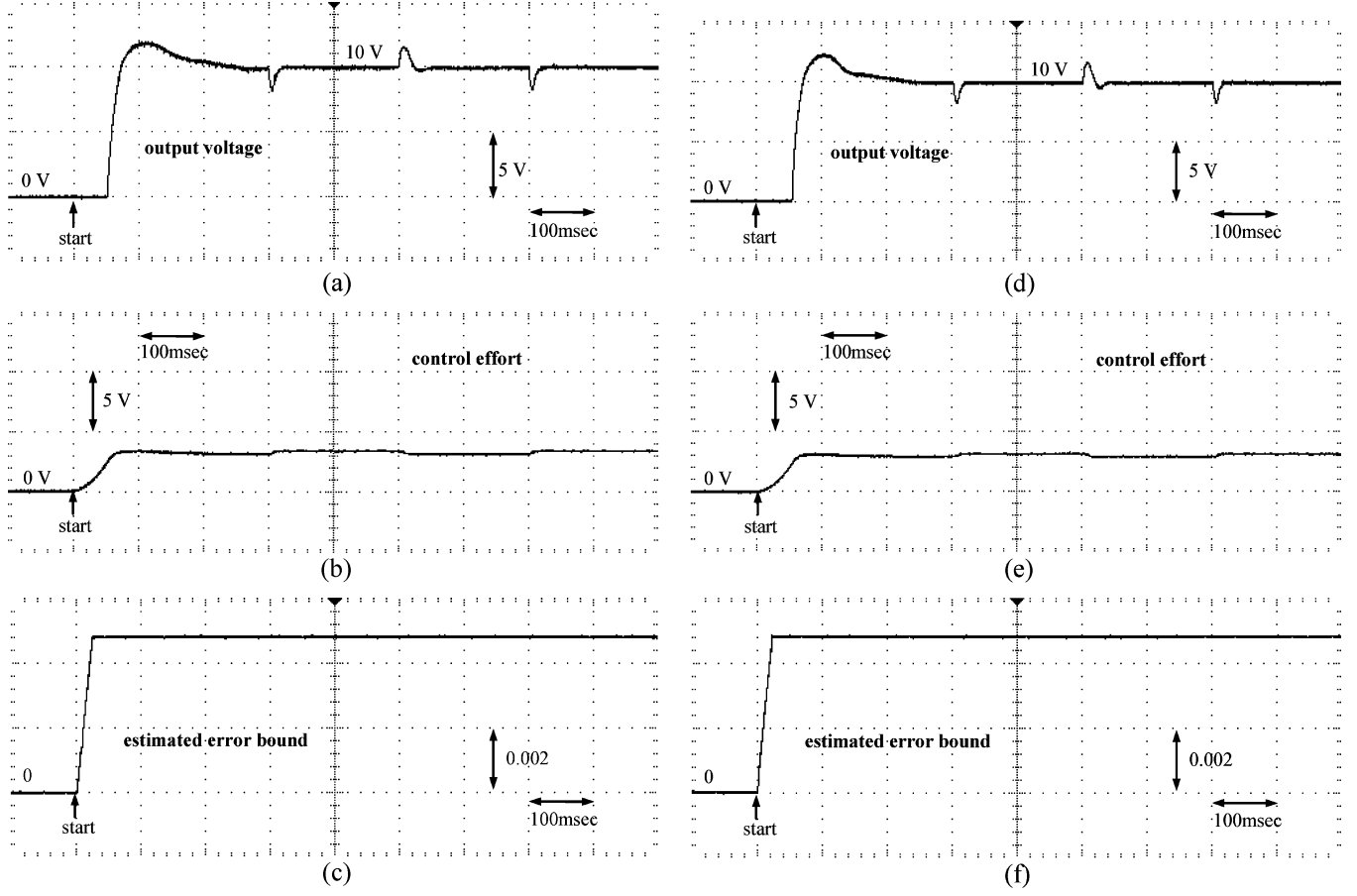


Fig. 5. Experimental results of ANW control with  $\eta_\alpha = 0.0005$ .

flow of the output of each node. In order to describe the online training algorithm of the WNN, a cost function is defined as

$$C = \frac{1}{2}e^2. \quad (36)$$

According to the gradient descent method, the adaptive law of the weight also can be represented as

$$\begin{aligned} \dot{\hat{\alpha}}_k &= -\eta_\alpha \frac{\partial C}{\partial \hat{\alpha}_k} \\ &= -\eta_\alpha \frac{\partial C}{\partial y_o^4} \frac{\partial y_o^4}{\partial net_o^4} \frac{\partial net_o^4}{\partial \hat{\alpha}_k} \\ &= -\eta_\alpha \frac{\partial C}{\partial y_o^4} x_k^4. \end{aligned} \quad (37)$$

Comparing (35) with (37), yields  $(\partial C / \partial y_o^4) = -s$ . Then, the convergence analysis in the following theorem is to derive specific learning-rate to assure convergence of the output tracking error.

*Theorem 1:* Let  $\eta_\alpha$  be the learning-rate of the WNN output weights, and let  $P_{\alpha \max}$  be defined as  $P_{\alpha \max} \equiv \max_{n_N} \|P_\alpha(N)\|$ , where  $P_\alpha(N) = (\partial y_o^4 / \partial \alpha_k^4)$  and  $\|\cdot\|$  is the Euclidean norm in  $\mathfrak{R}^n$ . Then, the convergence of the output tracking error is guaranteed if  $\eta_\alpha$  is chosen as

$$0 < \eta_\alpha < \frac{2}{(P_{\alpha \max})^2 \left[ \frac{s}{e(N)} \right]^2}. \quad (38)$$

Moreover, the optimal learning-rate which achieves the fast convergence can be obtained as

$$\eta_\alpha^* = \frac{1}{(P_{\alpha \max})^2 \left[ \frac{s}{e(N)} \right]^2}. \quad (39)$$

*Proof:* Since

$$P_\alpha(N) = \frac{\partial y_o^4}{\partial \alpha_k^4} = \frac{\partial \left( \sum_{k=1}^{n_N} \alpha_k^4 x_k^4 \right)}{\partial \alpha_k^4} = x_k^4. \quad (40)$$

Then, a discrete-type Lyapunov function is selected as

$$V_2(N) = \frac{1}{2}e(N)^2. \quad (41)$$

The change in the Lyapunov function can be expressed as

$$\Delta V_2 = V_2(N+1) - V_2(N) = \frac{1}{2} [e(N+1)^2 - e(N)^2]. \quad (42)$$

Moreover, the error difference can be represented by

$$\begin{aligned} e(N+1) &= e(N) + \Delta e(N) \\ &= e(N) + \left[ \frac{\partial e(N)}{\partial \alpha_k^4} \right]^T \Delta \alpha_k^4 \end{aligned} \quad (43)$$

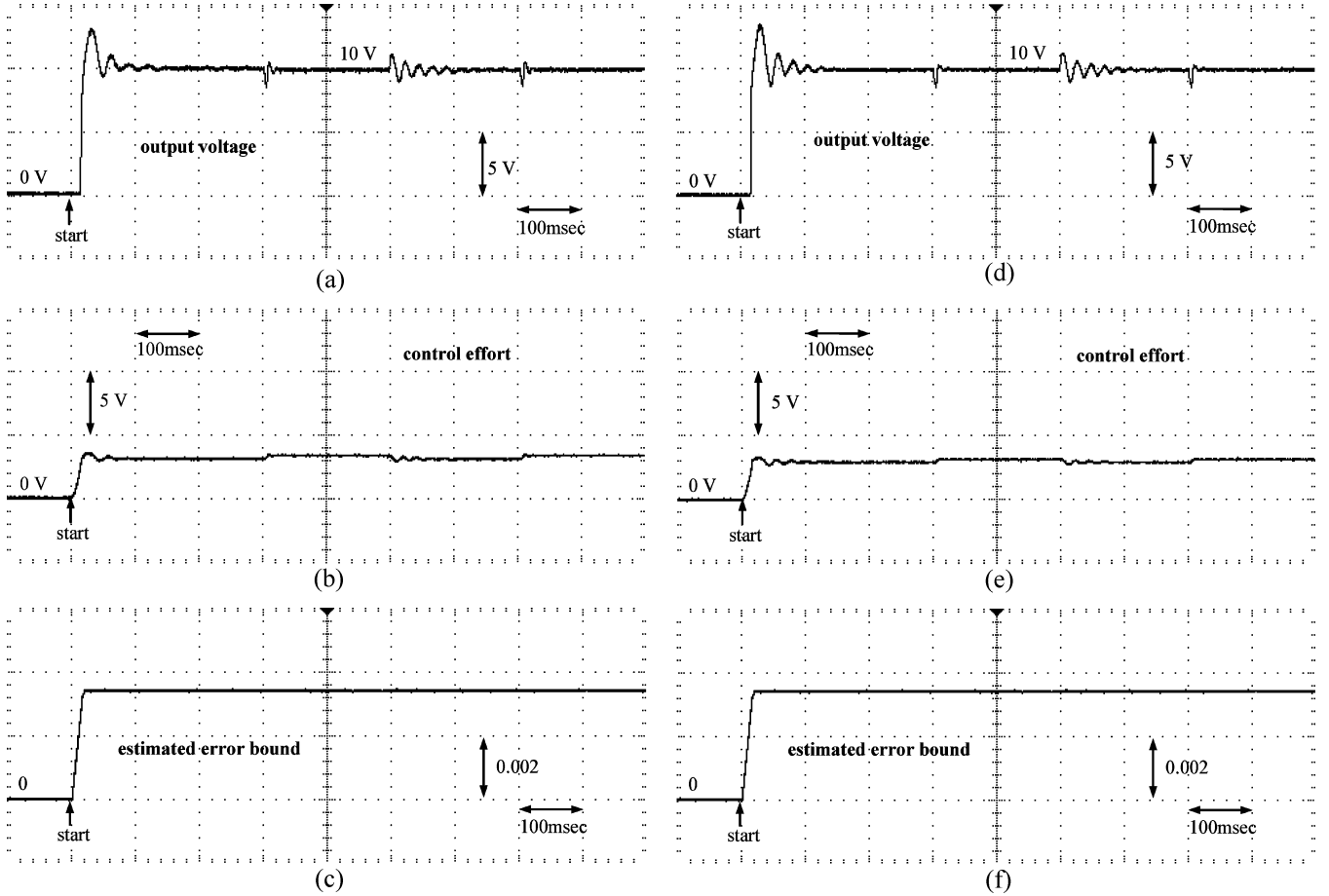


Fig. 6. Experimental results of ANW control with  $\eta_\alpha = 0.007$ .

where  $\Delta e$  is the output error change and  $\Delta\alpha_k^4$  represents the change of weight vector. Using (35) and (40), we get

$$\frac{\partial e(N)}{\partial \alpha_k^4} = \frac{\partial e(N)}{\partial C} \frac{\partial C}{\partial y_o^4} \frac{\partial y_o^4}{\partial \text{net}_o^4} \frac{\partial \text{net}_o^4}{\partial \alpha_k^4} = -\frac{s}{e(N)} P_\alpha(N). \quad (44)$$

Then (43) becomes

$$e(N+1) = e(N) - \left[ \frac{s}{e(N)} P_\alpha(N) \right]^T \eta_\alpha s P_\alpha(N). \quad (45)$$

Thus

$$\begin{aligned} & \|e(N+1)\| \\ &= \left\| e(N) \left[ 1 - \eta_\alpha \left( \frac{s}{e(N)} \right)^2 P_\alpha(N)^T P_\alpha(N) \right] \right\| \\ &\leq \|e(N)\| \left\| 1 - \eta_\alpha \left( \frac{s}{e(N)} \right)^2 P_\alpha(N)^T P_\alpha(N) \right\|. \end{aligned} \quad (46)$$

From (42) and (46),  $\Delta V_2$  can be rewritten as

$$\begin{aligned} \Delta V_2 &= \frac{1}{2} \eta_\alpha s^2 P_\alpha(N)^T P_\alpha(N) \\ &\quad \times \left\{ \eta_\alpha \left[ \frac{s}{e(N)} \right]^2 P_\alpha(N)^T P_\alpha(N) - 2 \right\} \\ &\leq \frac{1}{2} \eta_\alpha s^2 (P_{\alpha \max})^2 \\ &\quad \times \left\{ \eta_\alpha \left[ \frac{s}{e(N)} \right]^2 (P_{\alpha \max})^2 - 2 \right\}. \end{aligned} \quad (47)$$

If  $\eta_\alpha$  is chosen as  $0 < \eta_\alpha < (2 / ((P_{\alpha \max})^2 [s/e(N)]^2))$ , then the Lyapunov stability of  $V_2 > 0$  and  $\Delta V_2 < 0$  is guaranteed so that the output tracking error will converge to zero as  $t \rightarrow \infty$ . Moreover, the optimal learning-rate which achieves the fast convergence is corresponding to  $2\eta_\alpha^* [s/e(N)]^2 (P_{\alpha \max})^2 - 2 = 0$ , i.e.

$$\eta_\alpha^* = \frac{1}{(P_{\alpha \max})^2 \left[ \frac{s}{e(N)} \right]^2} \quad (48)$$

which comes from the derivative of (47) with respect to  $\eta_\alpha$  and equals to zero. This shows an interesting result for the variable optimal learning-rate which can be online tuned at each instant.

In summary, the online learning algorithm of the ANW controller is based on the adaptation law (30) for the weight adjustment with the optimal learning-rate in (39). The effectiveness of the adaptive neuro-wavelet control switching power supply can be verified by the following experimental results.

#### IV. EXPERIMENTAL RESULTS

The block diagram of the computer control system for the converter is depicted in Fig. 4. A servo control card is installed in the control computer, which includes multi-channels of D/A, A/D, PIO, and encoder interface circuits. The proposed ANW control system is realized in the Pentium using the "Visual C" language, and its control interval is set at 40 ms. The amplitude of the dc-link voltage is controlled by the forward switching

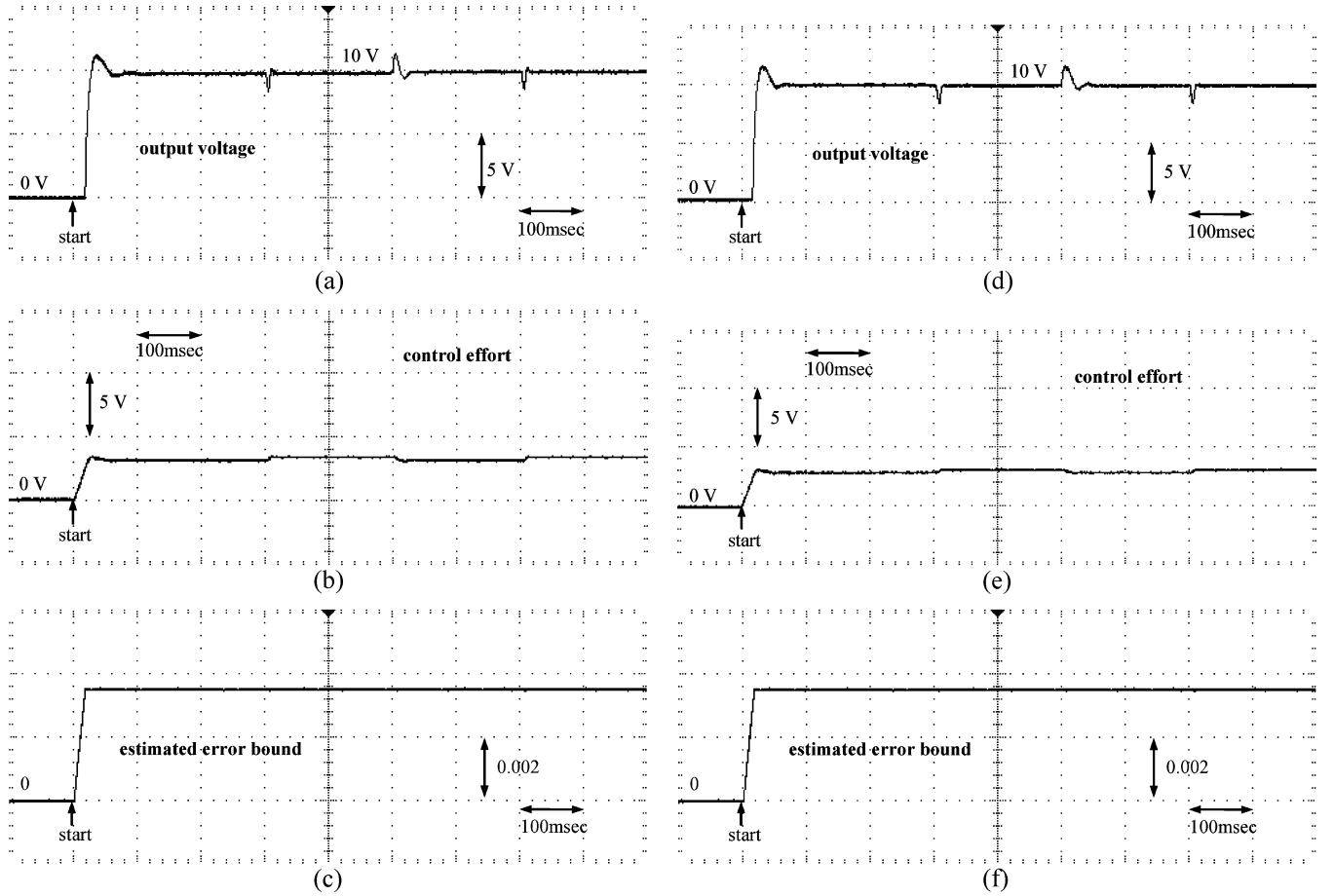


Fig. 7. Experimental results of ANW control with variable optimal learning-rate.

power supply according to the output of the proposed ANN control system. Two experimental cases are addressed as follows: 1) nominal case (the input voltage is set as  $V_i = 20$  V) and 2) input variation case (the input voltage is changed to  $V_i = 25$  V). In both cases, some load resistance variations with step changes are tested: 1) from  $20 \Omega$  to  $4 \Omega$  at 300 ms, 2) from  $4 \Omega$  to  $20 \Omega$  at 500 ms, and 3) from  $20 \Omega$  to  $4 \Omega$  at 700 ms. The circuit parameter values of the forward dc-dc converter are chosen as  $N_1 : N_2 = 4 : 3$ ,  $R = 20 \Omega$ ,  $L = 500 \mu\text{H}$  and  $C = 2200 \mu\text{F}$ . The converter runs at a switching frequency of 20 KHz and the controller runs at a sampling frequency of 1 KHz. The duty cycle is generated by a PWM IC UC1825; the generated duty cycle is directly proportional to the analog output of the controller. The experiment of the proposed adaptive neuro-wavelet control system is implemented based on the scheme shown in Fig. 2. The input of the wavelet neural network is the tracking index  $s$ . The wavelet neural network used in the study can be characterized with the number of elements in layers  $n_L = 2$ ,  $n_M = 5$  and  $n_N = 25$ . In (30), for computing  $\tau$ ,  $\alpha^*$  is set as zero at the first experiment. After  $\hat{\alpha}$  converges, this convergent value is then used as  $\alpha^*$  in the following experiments.

#### A. ANW Control With Constant Learning-Rates

To illustrate the influence of different learning-rates, first  $\eta_\alpha$  is chosen as a small value. The experimental results of the ANW control with  $\eta_\alpha = 0.0005$  for the two cases are shown in Fig. 5.

The converter responses are shown in Fig. 5(a) and (d); the associated control efforts are shown in Fig. 5(b) and (e); and the estimated bound  $\hat{E}$  are shown in Fig. 5(c) and (f), respectively. To speed up the tracking performance, the experimental results of the ANW control with  $\eta_\alpha = 0.007$  for these two cases are shown in Fig. 6. From the experimental results, it can be seen that when a large learning-rate is chosen for achieving fast transient time, the overshoot is relatively large. From the observation, there exists a trade-off between the rise time and the overshoot for the choice of learning-rate. The design of the control parameters must undergo the trial-and-error procedure and the dependency on the expertise experience is unavoidable.

#### B. ANW Control With Variable Optimal Learning-Rate

The variable optimal learning-rate is used for the ANW control. The experimental results are shown in Fig. 7. Since the learning-rate is automatically tuned, tracking performance is better than that of constant learning-rates. However, since the controller parameters are initialized from zero, the ANW control has the drawback of large overshoot at the initial learning phase. After training, the trained ANW control is applied to control the forward switching power supply again. The experimental results of the trained ANW control system for these two cases are shown in Fig. 8. From the experimental results, it is seen that the regulation performance of the trained ANW control is further improved when the initial values are trained, and they can achieve favorable robust characteristics for the load variations.

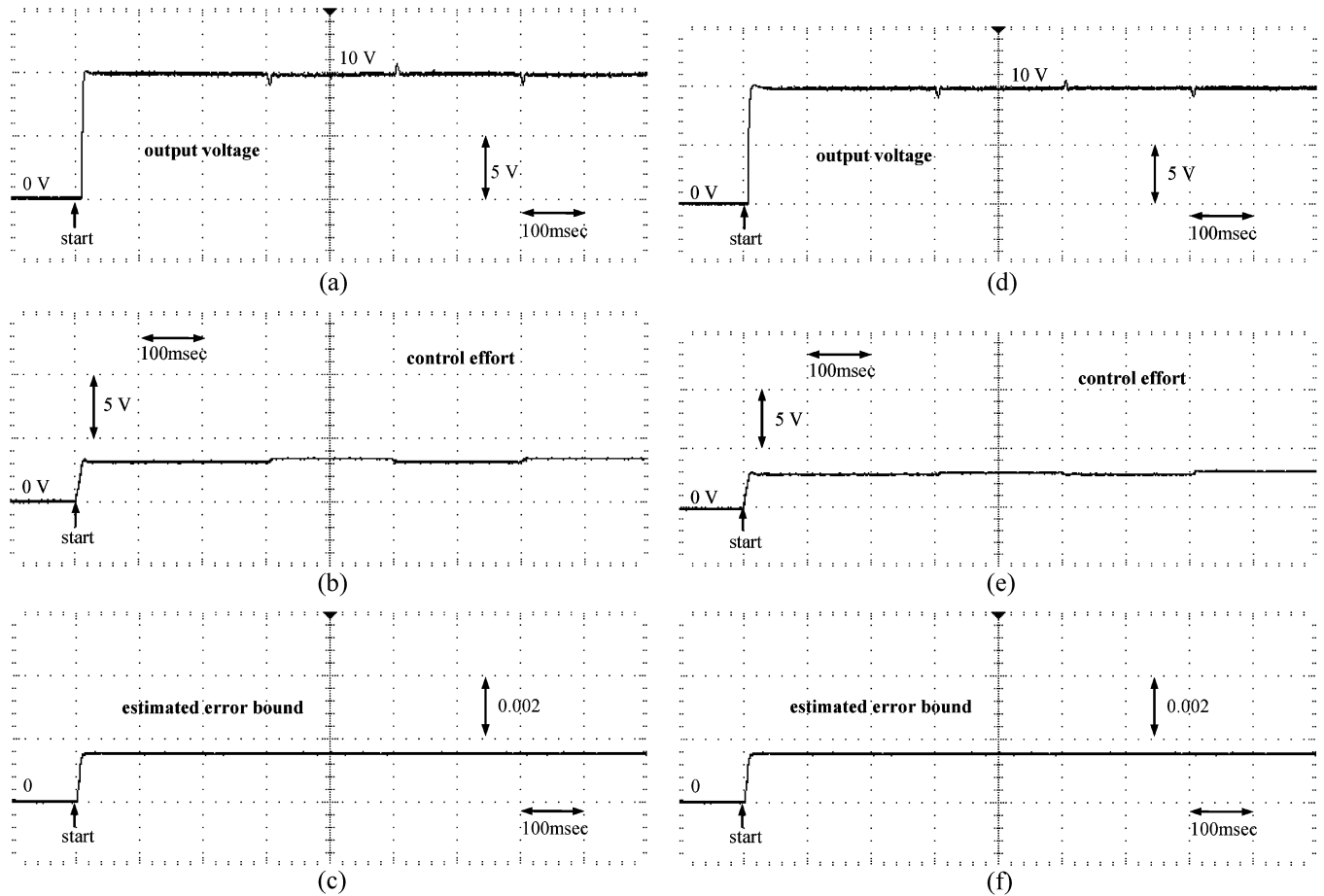


Fig. 8. Experimental results of trained ANW control with variable optimal learning-rate.

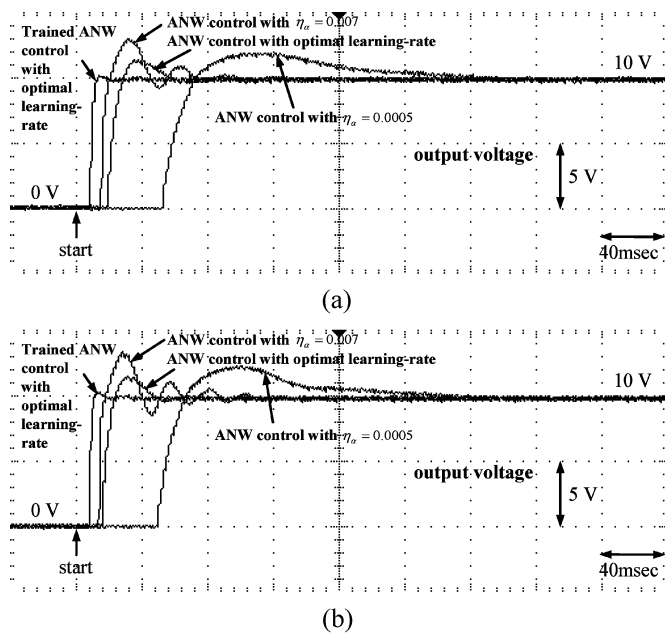


Fig. 9. Transient response comparison.

A transient response comparison among these experiments is shown in Fig. 9. After the ANW control has been sufficiently trained by the developed learning algorithm, the trained ANW

control demonstrates a remarkable performance in voltage stabilization, all in rise time, settling time, overshoot and load variation regulations. In conclusion, the trained ANW control can achieve better performance than the other ones.

## V. CONCLUSION

This paper has successfully implemented an ANW control for a forward switching power supply. The effectiveness of the proposed ANW control is verified by various experimental results. From the experimental results, the output voltage of the forward switching power supply can be maintained to follow the desired output voltage with favorable transient response and regulation performance. The major contributions of this paper are: 1) the successful development of an ANW control system in which the Lyapunov stability theorem is used to online tune the parameters, 2) the successful development of an online training methodology with variable optimal learning-rate for the ANW control system, 3) a computer-based experiment setup has been created, and 4) the successful application of the ANW to control the forward switching power supply.

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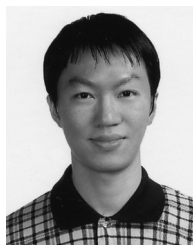


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