# Fuzzy Macromodel for Dynamic Simulation of Microelectromechanical Systems

Chun-Hsu Ko and Jin-Chern Chiou

Abstract—This paper proposes an efficient approach that consists of an experimental design and a fuzzy-logic model (FLM) to generate macromodels for the simulation of microelectromechanical systems. Firstly, in the present approach, a force macromodel is adapted to perform the coupled simulations. Then, an experimental design is utilized to reduce the number of data needed for macromodel identification, and an FLM is chosen to fit the data. The identification scheme involves cluster estimation to determine the FLM structure and backpropagation method to efficiently obtain the FLM structure parameters that lead to an accurate macromodel. In order to verify the accuracy of the macromodel, the approach has been applied to a magnetic microactuator. The simulation results show that the force macromodel yielded errors of less than 1.5% for a 5- $\mu$ m displacement. Furthermore, the dynamic coupled simulation takes only several minutes. The results demonstrate the efficiency and effectiveness of the current approach.

*Index Terms*—Coupled analysis, experimental design, fuzzy-logic model (FLM), macromodel, microactuator.

# I. INTRODUCTION

**C** OMPUTATIONAL coupled analysis has attracted much attention in the design of microelectromechanical systems (MEMS), which require self-consistent solutions to coupled energy domains via nonlinear partial differential equations [1]. Numerical approaches, such as the finite-element method (FEM), can yield coupled quasi-static solutions [2]. However, the coupled simulations of fully meshed FEM models are usually time consuming, due to the fact that the models are usually with significant degrees of freedom (DOF). Furthermore, the coupled dynamic analysis of the system-level design requires many simulations, which are quite inefficient. Approaches using macromodels with relatively fewer DOFs (also called as reduced-order models) have been proposed to improve the efficiency of coupled dynamic analysis [3]–[6]. These macromodel approaches can accurately model the system by capturing the

Manuscript received April 27, 2004; revised December 9, 2004 and April 11, 2005. This work was supported by the Ministry of Economic Affairs, R.O.C., under Contract 92-EC-17-A-07-S1-0011, by the National Science Council of Taiwan, R.O.C., under Grant NSC 92-2215-E-009-009, and by the Brain Research Center, University System of Taiwan, under Grant 91B-711 and Grant 92B-711. This paper was recommended by Associate Editor T. H. Lee.

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Digital Object Identifier 10.1109/TSMCA.2005.855787

dominant dynamic behaviors and are effective for fast coupled system-level design.

In general, macromodel generation requires first finding the basis functions by using techniques, such as modal analysis [3], [4], singular-value decomposition [5], and neural-network method [6]. The macromodels are then built by adopting the generalized coordinates accompanied with these basis functions. It is possible to determine the macromodels by using analytical models [5], [6]. However, the use of analytic models usually demands assumptions, which may affect model accuracy and effectiveness. An attractive alternative is to build empirical macromodels using identification techniques [3], [4], [7]. The identified macromodel can be obtained via the fitting of a set of sampling data. This approach may demand many basis functions, leading to high input dimensions and also raising the complexity of data generation in running a large number of simulations [3]. Also, these previously proposed methods, such as multivariate polynomials [3] and neural network [4], have some drawbacks. The multivariate-polynomial model has low efficiency, and the neural-network approach cannot provide a meaningful interpretation of the network structure, which poses a difficulty in determining the structure. The macromodels in [3] and [4] are even with the differentiation of the identified energy model. Based on the discussions, it is imperative to achieve an efficient macromodel.

Fuzzy-logic models (FLMs), which can be used as structured numerical estimators, categorize the data obtained in experiments and then create meaningful fuzzy IF-THEN rules to form expert knowledge [8]. These FLMs combine fuzzy sets with fuzzy rules that have the capability to model the complex nonlinear behavior. Furthermore, the structure/parameter of the FLM has been efficiently identified by using the proposed learning approach, including cluster estimation, gradient descent, and the back-propagation method [9], [10]. Previous studies have demonstrated the feasibility of the Sugeno-type FLM in system modeling and control [10]–[13], which motivates us to further explore its possibility in building the MEMS macromodel.

This paper proposes an efficient approach to generating macromodels by using an experimental design and FLM. It is organized as follows. Section II introduces the macromodel approach for the MEMS systems. The fuzzy macromodelgeneration method, which includes the experimental design for data sampling, an FLM to represent the data, and an efficient identification scheme for data fitting, is given in Section III. The example involving a magnetic microactuator, along with its corresponding static and dynamic simulations, are performed



Fig. 1. Block diagram of the macromodel approach with FLM.

and reported in Section IV. Finally, the conclusion of the present paper are covered in Section V.

## II. MACROMODEL APPROACH

Fig. 1 shows the procedure for the coupled dynamic analysis of MEMS using the macromodel approach with FLM. First, a fully meshed model of an MEMS is constructed by meshing the continuous distributed domains. Next, the degrees of freedom (DOF) of the system are reduced by selecting the basis functions, and inputs to the model are defined on the generalized coordinates. The identified macromodel is then built by using the FLM. Finally, a coupled dynamic simulation is performed based on the macromodel to yield the system response. From the procedure, to perform the simulation using the macromodel approach, we must first find the coupled dynamic equations of the system.

MEMS typically involve multiple energy domains, and their dynamic equations can be directly obtained from Lagrange's equations [14], which are given as

$$\frac{\mathrm{d}}{\mathrm{d}t} \left( \frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} = 0 \tag{1}$$

where the Lagrangian  $L(q, \dot{q}, t)$  is a function of the generalized coordinate q, their first derivatives  $\dot{q}$ , and time t.  $L(q, \dot{q}, t)$  is defined by

$$L(q, \dot{q}, t) = T(q, \dot{q}, t) - U(q, \dot{q}, t)$$
(2)

where  $T(q, \dot{q}, t)$  is the kinetic energy and  $U(q, \dot{q}, t)$  the potential energy. By selecting the meshed nodal displacements u as the generalized coordinates, and assuming u as small displacements, the dynamic equations described in (1) then become

$$M\ddot{u} + Ku - F_m(u,t) = 0 \tag{3}$$

where M is the mass matrix defined on the mesh, K the stiffness matrix, and  $F_m$  the nodally defined actuation force. Note that the equations of motion of (3) are nonlinear and coupled. The meshed models for realistic calculation usually involve high DOFs, such that the users need to endure an intensive computation to obtain the simulation result. On the other hand, the macromodels have the capability to accurately simulate the system behavior of the modeled dynamic system with a few coupled equations. To build the macromodel, we select the *n*-dimensional generalized coordinates  $q_i$  (i = 1, 2, ..., n), and n is much lower than the meshed model's DOFs, which yields

$$u = \sum_{i=1}^{n} q_i(t)\varphi_i \tag{4}$$

where  $\varphi_i(i = 1, 2, ..., n)$  are the selected basis functions. These basis functions can be conveniently determined by using the natural modes from the modal analysis. The natural modes possess a useful property known as orthogonality. Equation (3) then becomes

$$\ddot{q}_i + \omega_i^2 q_i = \varphi_i^{\mathrm{T}} F_m(q, t) \tag{5}$$

where  $\omega_i (i = 1, 2, ..., n)$  are the natural frequencies and  $q = [q_1 \quad q_2 \quad ... \quad q_n]^{\mathrm{T}}$ . Note that the electromagnetic force  $F_m$  for actuating MEMS can be expressed as

$$F_m(q,t) = I^2(t)f_m(q) \tag{6}$$

where I(t) is the input current that depends on time t in currentcontrolled devices and  $f_m(q)$  is the magnetic force resulting from the unit input current. Substituting (6) into (5), we have

$$\ddot{q}_i + \omega_i^2 q_i = I^2(t) p_i(q) \tag{7}$$

where  $p_i(q) = \varphi_i^{\mathrm{T}} f_{\mathrm{m}}(q)$  is the generalized force, referred to as the force macromodel.

On the other hand, the reduced-order dynamic equations can also be directly derived from (1) using the magnetic coenergy [3]

$$\ddot{q}_i + \omega_i^2 q_i = I^2(t) \frac{\partial u_{\rm m}^*(q)}{\partial q_i} \tag{8}$$

where  $u_{\rm m}^*(q)$  is the magnetic coenergy resulting from the unit input current, referred to as the energy macromodel, and its differentiation  $\partial u_{\rm m}^*(q)/\partial q_i$  represents the generalized force.

Equations (7) and (8) are both reduced-order equations for different forms of magnetic macromodels, leading to different computation procedures. Here, the force macromodel  $p_i(q)$  first requires the evaluation of the magnetic force in displacement (u) space, and is then obtained by projecting the magnetic force onto the generalized q space with the inner product of the magnetic force and the normal modes. The energy macromodel  $u_m^*(q)$ , on the other hand, requires the coenergy function to be established in q's space, and the generalized force is then obtained with the differentiation of the coenergy function.

To increase the efficiency in performing the coupled dynamic-system simulations in (7) and (8), macromodels in analytical form are required. In order to generate macromodels, it is necessary to select the basis functions that are significantly contributed to the system dynamic behavior. The selection process begins with the typical displacement  $u_s$ , which contains information on the amplitude for each basis function [3], [4]. The displacement is calculated from the coupled quasi-static analysis with FEM software, such as ANSYS (ANSYS, Inc., Canonsburg, PA. http://www.ansys.com). Using the  $n_s$  (about 30) modes of the lower natural frequency as the basis functions, the displacement can be expanded with the coefficients  $y_i$  as

$$u_{\rm s} \approx \sum_{i=1}^{n_{\rm s}} y_i \varphi_i. \tag{9}$$

Note that (9) is an overdetermined system requiring a leastsquare solution. The orthogonal-triangular (QR) factorization algorithm is adopted to yield the coefficients  $y_i$  [15]. The displacements of the modes can then be calculated by indicating important modes. Furthermore, the magnitudes of the coefficients  $y_i$  are used to predict the relative ranges of  $q_i$  for the input domain of the macromodel. Once the basis functions and the estimation range are determined, the fuzzy model-identification method can be used to generate the nonlinear macromodel.

#### III. FUZZY MACROMODEL GENERATION

The fuzzy macromodel generation with the identification technique includes data sampling, FLM selection, and FLM identification, which are described below.

## A. Data Sampling

The data for macromodel generation are the generalized coordinates q as the input variables and the generalized force or coenergy as the output. Note that input-data selection is important since it will affect both the reliability of the macromodel and the number of simulation runs. Thus, proper design of the simulation experiments is imperative. The experimental design takes certain values, called levels, for every input variable. The levels are used to adequately span the input range. The number of input data depends on the input variables and levels. Data with more input variables (i.e., more basis functions) and levels lead to more accurate macromodels, but also increase the difficulty in data selection. For example, n input variables and m levels produce a total of  $n^m$  runs for all the combinations, which shows the exponential increase in data number. Hence, an efficient experimental design is needed to obtain accurate results from a minimum number of computer runs.

To achieve this objective, Taguchi's method is proposed [16]. This method provides a predefined set of orthogonal tables that contain fractional orthogonal designs. For example, two-level  $L_4$ ,  $L_{12}$ , and  $L_{16}$  arrays [16] allow 3, 11, and 15 inputs to be evaluated with only 4, 12, and 16 design points, rather than the exponential  $2^3$ ,  $2^{12}$ , and  $2^{16}$ .

#### B. FLM Selection

In Sugeno-type FLM, the *i*th rule is described as follows.

If  $x_1$  is  $F_{i1}$ , and  $x_2$  is  $F_{i2}$ ,  $\cdots$  and  $x_n$  is  $F_{in}$ , then the role output is

$$y_i(x_1, x_2, \dots, x_n) = p_{i0} + p_{i1}x_1 + p_{i2}x_2 + \dots + p_{in}x_n$$

where  $x_j (j = 1, 2, ..., n)$  is the input variable,  $F_{ij}$  the fuzzy set, and output  $y_i$  an internal function with parameters  $P_{i0}, P_{i1}, ..., P_{in}$ . The Gaussian-type membership function  $\mu_{Fij}$  for the input variable  $x_j$  can be expressed as

$$\mu_{Fij}(x_j) = \exp\left[-\frac{1}{2}\left(\frac{x_j - c_{ij}}{\sigma_{ij}}\right)^2\right]$$
(10)

where  $c_{ij}$  and  $\sigma_{ij}$  are, respectively, the location and shape parameters. Then, by using the product operator to represent the and operator in the rules, the weight for each rule's output becomes

$$w_i = \exp\left[-\frac{1}{2}\sum_{j=1}^n \left(\frac{x_j - c_{ij}}{\sigma_{ij}}\right)^2\right].$$
 (11)

Finally, the output of the FLM is inferred by taking the weighted average of the rule's outputs. For an FLM with r rules, the output can be expressed as

$$y = \sum_{i=1}^{r} v_i y_i, \quad \text{with } v_i = \frac{w_i}{\sum_{i=1}^{r} w_i}.$$
 (12)

With the energy macromodel described in (8), the generalized force can be obtained by differentiating the fitted coenergy function. The differentiation of the FLM output can be analytically derived as

$$\frac{\partial y}{\partial x_j} = \sum_{i=1}^r v_i \left( \frac{-(x_j - c_{ij})}{\sigma_{ij}^2} + \sum_{k=1}^r \frac{v_k(x_j - c_{ij})}{\sigma_{kj}^2} + p_{ij} \right).$$
(13)

The total number of membership functions and internal function parameters in the FLM to be determined is  $r \times (3 \times n+1)$ . Minimization of the squaring errors between the sampling data and the calculated FLM outputs, in turn, determines these parameters.

#### C. FLM Identification

For a set of sampling data  $(x_{1k}, x_{2k}, \ldots, x_{nk}, y_k)$ , the accuracy of the FLM is given by the multiple correlation coefficient  $R^2$  [10], which is defined as

$$R^{2} = 1 - \frac{\sum_{k=1}^{m} (\hat{y}_{k} - y_{k})^{2}}{\sum_{k=1}^{m} (\hat{y}_{k} - \overline{y})^{2}}$$
(14)

where  $\hat{y}_k$  is the output of the macromodel,  $\overline{y}$  the mean of the output of the sampling data, and m the total number of data sets. When  $R^2 = 1$ , it means that the model fits every sampling data point perfectly. The primary goal of FLM identification is to maximize  $R^2$  to 1, and, thus, the resulting FLM makes accurate predictions of the input domain.

There are two major tasks in identifying an FLM for a system: structure and parameter identification [17]–[19], each of which consists of a premise and a consequence part. To identify the FLM parameters with an optimal structure accurately, we partition the available data into training and testing data. An efficient identification approach involving cluster estimation, gradient-descent, and backpropagation method is then utilized to identify intermediate FLMs with various structures using the training data. The decision rule seeks maximal multiple correlation coefficients among the intermediate FLMs and the testing data to achieve an optimal structure. Thus, the resulting macromodel not only fits the training data well, but also makes accurate predictions.

The cluster-estimation method [9], [10] is used here for the coarse tuning process of the FLM identification algorithm. Data-point potential measure is used to locate the cluster centers, defined as

$$V_{i} = \sum_{k=1}^{m} \exp\left(-\frac{4}{r_{a}^{2}} \|x_{i} - x_{k}\|^{2}\right)$$
(15)

where  $\|.\|$  denotes the Euclidean distance and  $r_a$  a positive constant used to define the effective radius of a neighborhood. The data points with higher potentials are chosen as cluster centers. Each cluster center is, in essence, a prototypical data point that exemplifies a characteristic behavior of the system [9]. Hence, each cluster center can be used as the basis of a rule-describing system behavior, and the number of fuzzy rules will be equal to that of the cluster centers.

When the fuzzy structure is determined, parametric identification of a fuzzy model based on the gradient-descent and backpropagation methods is then conducted. The output of the FLM is calculated and internal parameters are updated by the instantaneous error between the FLM output  $\hat{y}_k$  and the current training data output  $y_k$ . Here, we minimize the square of the instantaneous error with respect to the unknown parameters  $p_{i0}$ ,  $p_{ij}$ ,  $c_{ij}$ , and  $\sigma_{ij}$  of the internal functions and membership functions, i.e.,

$$E_k = \frac{1}{2}(\hat{y}_k - y_k)^2 = \frac{1}{2}e_k^2.$$
 (16)

By applying the chain rule on (16), we can obtain the equations for updating the estimates of the unknown parameters  $p_{i0}$ ,  $p_{ij}$ ,  $c_{ij}$ , and  $\sigma_{ij}$  as

$$p_{i0}(k+1) = p_{i0}(k) - \alpha_0 v_i(k) e_k \tag{17}$$

$$p_{ij}(k+1) = p_{ij}(k) - \alpha_1 v_i(k) e_k x_j$$
(18)

$$c_{ij}(k+1) = c_{ij}(k) - \alpha_2 v_i(k) e_k$$

$$\times \left[y_i(k) - y_k\right] \frac{x_j - c_{ij}(k)}{\sigma_{ij}^2(k)} \tag{19}$$

$$\sigma_{ij}(k+1) = \sigma_{ij}(k) - \alpha_3 v_i(k) e_k$$

$$\times [y_i(k) - y_k] \frac{[x_j - c_{ij}(k)]^2}{\sigma_{ij}^3(k)}.$$
 (20)

The gradient-descent method is used to minimize the instantaneous error. Since this method is basically a kind of hillclimbing technique, it runs the risk of being trapped in a local minimum, where every small change in synaptic parameters  $p_{i0}$ ,  $p_{ij}$ ,  $c_{ij}$ , and  $\sigma_{ij}$  would increase the squareerror function  $E_k$ . Therefore, initial parameter estimation is crucial when this method is used. Here, the initial parameter estimations  $c_{ij}$  and  $p_{i0}$  are the coordinates of the *i*th cluster center  $(x_{1i}^*, x_{2i}^*, \ldots, x_{ni}^*, y_i^*)$ , and the parameter  $\sigma_{ij}$  is defined as the distance with the constant  $r_a$ , i.e.,  $\sigma_{ij} = l \times r_a$ . By using the results obtained in [10], parameter l is set to  $3/(4\sqrt{2})$ , and  $p_{ij}$  to zero. The method is used repeatedly to update the model parameters until  $R^2 \ge R_{\min}^2$ . Note that the criterion  $R^2 \ge R_{\min}^2$  is to ensure the accuracy of the FLM.

Finally, intermediate FLMs with various structures are built from the training data by using the identification method described above. A multiple correlation coefficient  $R_{\rm search}^2$ (e.g., 0.99) is specified for fast establishing the intermediate FLMs. The testing data are used to evaluate the accuracy of the intermediate FLMs by employing the multiple correlation coefficients recorded as  $R_{\rm test}^2$ . The FLM structure with the highest  $R_{\rm test}^2$  is then chosen as the optimal structure. We further use the training and testing data with a larger multiple correlation coefficient  $R_{\rm goal}^2$  (e.g., 0.9999) than  $R_{\rm search}^2$  to identify the accurate FLM with the optimal structure.

Based on the discussion above, the FLM identification algorithm is developed and stated as follows.

## **FLM Identification Algorithm:**

- Step 1) Specify the input variables  $x_1, x_2, \ldots, x_n$ , and the output variable y.
- Step 2) Provide training and testing data.
- Step 3) Give the maximum number of rules  $r_{\text{max}}$  to establish the intermediate FLMs, and the multiple correlation coefficients  $R_{\text{search}}^2$  and  $R_{\text{goal}}^2$ .
- Step 4) Begin the search algorithm and set the fuzzy rule number r = 1.
- Step 5) Use the cluster-estimation method to search for the constant  $r_a$  for building the FLM structure with r rules and the initial parameters  $p_{i0}$ ,  $p_{ij}$ ,  $c_{ij}$ , and  $\sigma_{ij}$ .



Fig. 2. Quasi-static displacement of asymmetric suspended plate with 36-mA actuation.

 TABLE I

 Mode Contributions to the Displacement of the Plate Center

Mode Number	Contribution (µm)
1	-5.2941
3	0.1789
2	0.0569
6	0.0142
8	0.0044
10	0.0031
7	0.0021
12	0.0021
5	0.0014
9	-0.0013

- Step 6) Calculate the FLM output  $y_k$  with the training data, and the instantaneous error  $e_k$ . Perform back-propagation to refine the parameters  $p_{i0}$ ,  $p_{ij}$ ,  $c_{ij}$ , and  $\sigma_{ij}$  with the gradient-descent method.
- Step 7) Calculate the training correlation coefficient  $R^2$ . If  $R^2$  is less than  $R^2_{\text{search}}$ , go to Step 6) for the next iteration; otherwise, test the FLM using the testing data and record the testing correlation coefficient as  $R^2_{\text{test}}(r)$ .
- Step 8) Set r = r + 1, if r is less than or equal to  $r_{\text{max}}$ , go to Step 5); otherwise, select the rule number r that corresponds to the maximum test correlation coefficient  $R_{\text{test}}^2(r)$  as the optimal rule number  $r_{\text{opt}}$ .
- Step 9) Set-up all available data in Step 2) as new training data and  $R_{\text{goal}}^2$  as the convergence correlation coefficient. Identify the optimal FLM with  $r_{\text{opt}}$  rules and output its parameters.

#### **IV. SIMULATIONS AND RESULTS**

In order to demonstrate the efficiency of the proposed approach, the macromodeling process was applied to a magnetic microactuator containing a magnetic core and a deformable structure [20]–[22]. The structure of the microactuator was shown in Fig. 2. The magnetic microactuator had an asymmetric  $625 \times 625 \times 5 \ \mu m$  plate suspended from four beams  $50-\mu m$  wide by  $5-\mu m$  thick, the shortest of which was  $150-\mu m$ 









Mode 8

Mode 10

Fig. 3. Mode shapes used as the basis functions.

TABLE II MODE PARAMETERS

Mode Number	Frequency (kHz)
1	16.3
3	53.5
2	34.4
6	192.5
8	266.3
10	363.1

high, the tallest  $300-\mu m$  high, and the others 200- and  $250-\mu m$  high. A  $500 \times 500 \times 5 \ \mu m$  permalloy panel was attached under the plate at the corner near the shortest support beam, and an electromagnet consisting of a 32-turn coil and an enclosed core was placed underneath, separated from the permalloy plate by a  $16-\mu m$  gap. Due to the unequal beam length and the off-center magnetic force, this structure displaced, bent, and tilted upon application of electrical current.

In the simulation, we used the ANSYS software to construct a three-dimensional (3-D) model by meshing a magnetic microactuator to create structural and magnetic FEM models. The structural finite-element mesh, which had its thickness magnified by four times for clarity, comprised 411 solid elements with a total of 799 nodes, and the magnetic FEM model contained 17 408 eight-node brick elements for a total of 19 602 nodes. An equilibrium displacement was obtained via the quasi-static magnetostructural simulation, with the resulting deformation depicted in Fig. 2.

The first thirty mode shapes of the structural FEM model are determined using modal analysis. We projected the quasistatic solution onto the mode shapes using QR factorization. Table I lists the ten most significant modes contributing to this

TABLE III  $L_{25}(5^6)$  Orthogonal Array

Setting	А	В	С	D	Е	F
1	1	1	1	1	1	1
2	1	2	2	2	2	2
3	1	3	3	3	3	3
4	1	4	4	4	4	4
5	1	5	5	5	5	5
6	2	1	2	3	4	5
7	2	2	3	4	5	1
8	2	3	4	5	1	2
9	2	4	5	1	2	3
10	2	5	1	2	3	4
11	3	1	3	5	2	4
12	3	2	4	1	3	5
13	3	3	5	2	4	1
14	3	4	1	3	5	2
15	3	5	2	4	1	3
16	4	1	4	2	5	3
17	4	2	5	3	1	4
18	4	3	1	4	2	5
19	4	4	2	5	3	1
20	4	5	3	1	4	2
21	5	1	5	4	3	2
22	5	2	1	5	4	3
23	5	3	2	1	5	4
24	5	4	3	2	1	5
	_	_			-	

TABLE IV  $L_{16}(4^5)$  Orthogonal Array

Setting	А	В	С	D	E, F
1	1	1	1	1	1
2	1	2	2	2	2
3	1	3	3	3	3
4	1	4	4	4	4
5	2	1	2	3	4
6	2	2	1	4	3
7	2	3	4	1	2
8	2	4	3	2	1
9	3	1	3	4	2
10	3	2	4	3	1
11	3	3	1	2	4
12	3	4	2	1	3
13	4	1	4	2	3
14	4	2	3	1	4
15	4	3	2	4	1
16	4	4	1	3	2

deformation and their contributions to the displacement of the plate center. To obtain a reduced-order model, the six dominant modes, shown in Fig. 3, were selected as the basis functions for computing system response. Table II lists the frequencies for each of the selected modes.

The proposed macromodel-generation approach was used to build the nonlinear magnetic macromodel. The first six modes were taken as the shape functions along with their contributions as the input ranges of the macromodel. By setting five levels for each factor and using the orthogonal table  $L_{25}(5^6)$  from Taguchi's method, shown in Table III, we obtained training

 TABLE
 V

 COMPUTATION TIMES FOR MACROMODEL GENERATION

Macromodel		
	Force Macromodel	Energy Macromodel
Generation Procedure		
Quasi-Static Analysis (s)	4320	4320
Modal Analysis (s)	10	10
Modes Selection (s)	30	30
Data Sampling (s)	10660	10824
FLM Identification (s)	148	16
Total Time (h)	4.21	4.22



Fig. 4. Comparison of the solutions of the plate-center displacement by using force macromodel, energy macromodel, and quasi-static coupled FEM.

data through performing 25 simulations of magnetic force and coenergy. Meanwhile, the orthogonal table  $L_{16}(4^5)$  containing 16 simulations was used for obtaining the testing data, as shown in Table IV. The testing-data levels were determined by taking the four middle points of the five levels in the training data. Note that table  $L_{16}(4^5)$  was for an experimental design of five factors. To permit experimenting on six factors with a table of five factors, we combined minor factors (the fifth and sixth factors) into a compound factor. Finally, the FLM identification algorithm was used to obtain the identified macromodels.

Table V shows the macromodeling computation times for force and energy macromodels run on a Pentium-III 850-MHz microprocessor. The total computation time was almost the same for both macromodeling approaches, approximately within 4.5 h for the complex example. We found that the datasampling procedure took most of the macromodel-generation time. Note that the total run time would have been longer in the absence of the experimental design. Hence, the experimental design was effective in reducing the total required run time. Meanwhile, FLM identification took only a few minutes, demonstrating the efficiency of the proposed identification approach.

To check the accuracy of the fitted macromodel, the quasistatic case was firstly performed by setting the time derivatives

 TABLE VI

 Macromodel Accuracy in Coupled Quasi-Static Simulations

Current	FEM Coupled	Force		Energy		
(mA)	Quasi-Static	Macromodel		Macromodel		
	Solution (µm)	Solution (µm)	Error (%)	Solution (µm)	Error (%)	
5	-0.057	-0.057	-0.20	-0.055	-3.27	
10	-0.231	-0.231	-0.23	-0.224	-3.15	
15	-0.536	-0.534	-0.28	-0.520	-3.02	
20	-0.996	-0.993	-0.31	-0.967	-2.98	
25	-1.664	-1.660	-0.27	-1.606	-3.37	
30	-2.661	-2.657	-0.16	-2.519	-5.33	
35	-4.416	-4.395	-0.47	-3.821	-13.48	
36	-5.034	-4.961	-1.43	-4.142	-17.72	



Fig. 5. Response to a 25-mA square wave with a 125- $\mu s$  hold and a 500- $\mu s$  period.

to zero in the dynamic equations of motion. The solution was obtained by solving a set of coupled algebraic equations, and it agrees well with the solution of the coupled quasi-static FEM simulation. Fig. 4 shows the comparison of the solutions of plate-center displacement, and Table VI presents the accuracy of the macromodels. We found that the force macromodel yields an error of less than 1.5% for a 5- $\mu$ m displace-



Fig. 6. Response to a 25-mA sawtooth wave with a  $50-\mu s$  rise and a  $500-\mu s$  period.

ment, demonstrating that the proposed force-macromodeling approach was very effective. But the solution from the energy macromodel shows a much larger error generated by using the differentiation of the fitted-energy macromodel.

Figs. 5 and 6 show the dynamic responses of the forcemacromodel coupled simulations. In Fig. 5, each mode response containing the ripple has the same timing as the applied square wave. In Fig. 6, mode 1 dominated the main response, while the rest reflected the general shape of the applied sawtooth wave. Each simulation took about 2 min. The results demonstrate that the generated macromodels achieved efficient modeling of the nonlinear coupling effects.

#### V. CONCLUSION

In this paper, we have proposed a macromodeling process for simulating a magnetic microactuator based on a FLM. Approaches, such as force and energy macromodels, have been utilized and discussed. Accordingly, macromodels have been efficiently established by using cluster estimation, gradient descent, and backpropagation. The required data for fitting the macromodel have been also effectively reduced by using the proposed experimental design. Compared with quasi-static coupled simulations, the simulation of the force macromodel using the proposed FLM identification yields an error of less than 1.5% for a 5- $\mu$ m displacement, demonstrating the effectiveness of the proposed scheme.

## ACKNOWLEDGMENT

The authors would like to thank the anonymous reviewers for their valuable suggestions.

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