

Numerical analysis on the effect of electron blocking layer in 365-nm ultraviolet light-emitting diodes

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ABSTRACT

For 365-nm ultraviolet light-emitting diodes (UV LEDs), an electron blocking layer (EBL) is usually utilized to mitigate electron overflow. However, using EBL might obstruct holes from injecting into the active region. Moreover, the large polarization field in conventional EBL might also pull down the effective barrier height for electrons, and thus the electrons could easily overflow to the p-side region. To solve the above drawbacks, in this study, the Al content and *p*-doping concentration of the EBL in typical 365-nm UV LEDs are investigated systematically. Specifically, designs of AlGaInN/GaN superlattice EBL and Al-content-graded EBL are explored in detail.

Keywords: ultraviolet light-emitting diodes, electron blocking layer, polarization

1. INTRODUCTION

The 365-nm ultraviolet light-emitting diodes (UV LEDs) are of special interest for curing light source, biochemistry, sensing, and data storage applications¹. To enhance the device performance, various approaches including crystal quality enhancement², increasing *p*-doping efficiency³, improving light extraction efficiency⁴, decreasing self-heating⁵, carrier confinement improvement⁶, and usage of non-polar or semi-polar substrate⁷ have been reported. Among the numerous suggestions, the weak carrier confinement should be a significant issue due to the shallow well and polarization field in both the active region and electron blocking layer (EBL). The employment of AlGaIn material as an EBL is usually believed to be necessary for blocking the electrons from overflowing to the p-side region. When the Al-content in AlGaIn EBL is increased, the energy bandgap of EBL increases. However, the polarization mismatch and the relevant polarization field, which create serious polarization-induced band-bending and thus lower the electron-blocking capability, increase as well. Moreover, the wide-bandgap EBL also creates a potential barrier in the valence band and thus obstructs the holes from p-side into the active region. The Al-content in EBL therefore needs to be carefully considered/adjusted in order to achieve the superior performance. In addition, the *p*-type doping concentrations in EBL which corresponds to the hole injection efficiency should be another issue to obtain the higher-power UV LEDs. Several suggestions about the design of EBL in UV LEDs have been reported, such as adopting the AlGaInN polarization-matched⁸ or AlGaInN polarization-reversed⁹ EBL, grading Al-content AlGaIn EBL¹⁰, and AlGaInN/GaN-superlattice EBL¹¹. Note that although there are advantages for the use of quaternary AlGaInN EBL, there still exist limitations till now, such as the degradation of crystalline quality or even failure to obtain the AlGaInN crystal film. In this study, with the purpose of effectively reducing the electron leakage and enhancing the hole injection efficiency, the Al-content and Mg-doping concentrations of the EBL in 365-nm UV LED are investigated systematically. Specifically, since there were no comparisons between the employment of grading Al-content AlGaIn EBL and AlGaInN/GaN-superlattice EBL have been made in the literature, designs of superlattice as EBL and Al-content-graded EBL are explored in detail. All the systematical investigations and specific designs for the EBL of 365-nm UV LEDs are

simulated with the APSYS simulation program so as to improve the efficiency of hole injection without losing the blocking capability of electron overflow and consequently optimize the output performance of UV LEDs.

2. PHYSICAL MODEL AND PARAMETERS

For the 365-nm UV LED under study, the original GaN-based UV LED structure as a reference, which has peak emission wavelength of approximately 365-nm around 60 mA, was grown on c-plane sapphire substrate by metal organic chemical vapor deposition (MOCVD). This LED structure is composed of a 2.5- μm -thick $n\text{-Al}_{0.039}\text{Ga}_{0.961}\text{N}$ layer (Si -doping: $5 \times 10^{18} \text{ cm}^{-3}$), ten pairs of $\text{In}_{0.04}\text{Ga}_{0.96}\text{N}/\text{Al}_{0.16}\text{Ga}_{0.82}\text{In}_{0.02}\text{N}$ MQWs with 2.5-nm-thick wells and 10-nm-thick barriers, 17-nm-thick $p\text{-Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL (Mg -doping: $1 \times 10^{19} \text{ cm}^{-3}$), 13-nm-thick $p\text{-Al}_{0.1}\text{Ga}_{0.9}\text{N}$ (Mg -doping: $1 \times 10^{19} \text{ cm}^{-3}$), and 55-nm-thick $p\text{-GaN}$ contact layer (Mg -doping: $5 \times 10^{19} \text{ cm}^{-3}$). The mesa size was $1000 \times 1000 \mu\text{m}^2$. In the simulation, the light extraction efficiency and background loss are assumed to be 40% and 20 cm^{-1} . The Shockley-Read-Hall (SRH), radiative recombination, and Auger recombination coefficients are set to $5 \times 10^7 \text{ s}^{-1}$, $2 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$, and $9.5 \times 10^{-31} \text{ cm}^6 \text{ s}^{-1}$, respectively. The polarization-induced surface charges at the interfaces are calculated by the methods developed by Fiorentini *et al.*¹² Considering the screening caused by defects, the surface charge densities are assumed to be 55% of the calculated values so that the output performance of this UV LED obtained from simulation can be best matched to the experiment data. The band-offset ratio is assumed to be 0.65/0.35 for 365-nm UV LEDs. The energy bandgaps of unstrained nitride-based materials are calculated by the formula proposed by Vurgaftman *et al.*¹³ The unstrained bandgap energies of the AlGaInN quaternary alloy can be expressed as

$$E_g(\text{Al}_x\text{Ga}_z\text{In}_y\text{N}) = \frac{x \cdot y \cdot T_{\text{AlInN}}(u) + y \cdot z \cdot T_{\text{InGaN}}(v) + x \cdot z \cdot T_{\text{AlGaN}}(w)}{x \cdot y + y \cdot z + x \cdot z} \quad (1)$$

$$T_{\text{AlInN}}(u) = u \cdot E_{g,\text{InN}} + (1 - u) \cdot E_{g,\text{AlN}} + B_{\text{AlInN}} \cdot u \cdot (1 - u) \quad (2)$$

$$T_{\text{InGaN}}(v) = v \cdot E_{g,\text{GaN}} + (1 - v) \cdot E_{g,\text{InN}} + B_{\text{InGaN}} \cdot v \cdot (1 - v) \quad (3)$$

$$T_{\text{AlGaN}}(w) = w \cdot E_{g,\text{GaN}} + (1 - w) \cdot E_{g,\text{AlN}} + B_{\text{AlGaN}} \cdot w \cdot (1 - w) \quad (4)$$

$$u = \frac{1-x+y}{2}, \quad v = \frac{1-y+z}{2}, \quad w = \frac{1-x+z}{2} \quad (5)$$

Where x , y , and $z = 1-x-y$ represent the compositions of aluminum (Al), indium (In), and gallium (Ga) in the AlGaInN material system. B_{AlInN} , B_{InGaN} , and B_{AlGaN} are the bandgap bowing parameters of AlInN, InGaN, and AlGaN, that are assumed to be 3.6 eV, 2.0 eV, and 0.24 eV, respectively. $E_{g,\text{InN}}$, $E_{g,\text{AlN}}$, and $E_{g,\text{GaN}}$ are the bandgap energies of InN, AlN, and GaN, which have values of 0.641 eV, 5.965 eV, and 3.417 eV at 300K, respectively. The Caughey–Thomas approximation is employed for the low-field mobility as a function of carrier density¹⁴

$$\mu_0(N) = \mu_{\min} + \frac{\mu_{\min} - \mu_{\max}}{1 + (N/N_{\text{ref}})^\alpha} \quad (6)$$

Moreover, the high-field electron mobility is expressed by the formula¹⁵

$$\mu_e(F) = \frac{\mu_{e0}(N) - \mu_{e,\text{sat}}(F\beta_1^{-1}/F_0\beta_1)}{1 + (F/F_0)\beta_1 + \alpha(F/F_0)\beta_2} \quad (7)$$

and the standard Caughey–Thomas formula is used to calculate the high-field hole mobility¹⁴

$$\mu_h(F) = \frac{\mu_{h0}(N)F}{1 + \mu_{h0}(N)F/\mu_{h,\text{sat}}} \quad (8)$$

For the electrons of AlGaIn alloys, the values of μ_{\max} , μ_{\min} , N_{ref} , and α are $306 \text{ cm}^2/\text{V}_s$, $132 \text{ cm}^2/\text{V}_s$, $1.0 \times 10^{17} \text{ cm}^{-3}$, and 0.29, respectively. The low-field hole mobility are assumed to be $10 \text{ cm}^2/\text{V}_s$. The parameters, $\mu_{e,\text{sat}}$, $\mu_{h,\text{sat}}$, F_0 , β_1 , and β_2 , for high-field mobility models employed in the AlGaIn alloys are $1.12 \times 10^7 \text{ cm/s}$, $1.0 \times 10^7 \text{ cm/s}$, 370

kV/cm, 5.3, and 1.0, respectively. The doped carrier densities in the simulation represent actual densities of free carriers. Other material parameters used in the simulation can be found in Ref [16].

3. SIMULATION RESULTS

Figure 1 plots the experimental (open dots) and simulated (solid curves) (a) light output power versus current ($L - I$) and (b) current as a function of voltage ($I - V$) characteristics of the original 365-nm UV LED. The output power of this UV LED is 24.1 mW at 60 mA with operation voltage around 4.9 V. According to both $L - I$ and $I - V$ curves, it is observed that the simulation results are in good agreement with experimental data.

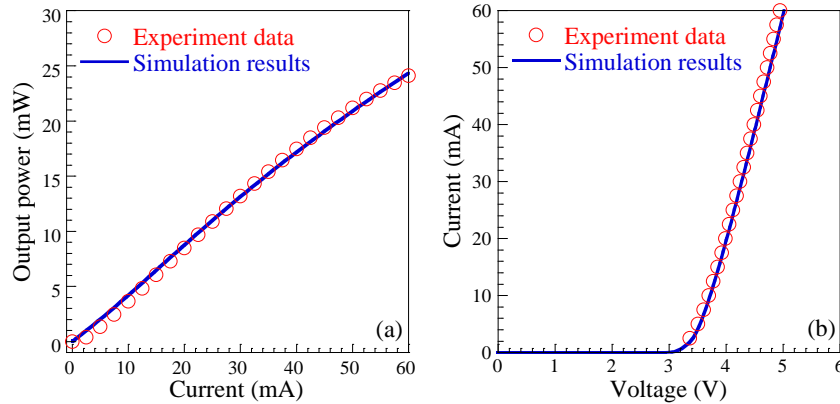


Fig. 1. Experimental (open dots) and simulated (solid curves) (a) $L - I$ and (b) $I - V$ characteristics of the original 365-nm UV LED.

3.1 Al-content in AlGaN EBL

In this section, the optical and electrical performances of 365-nm UV LED with various Al-content in AlGaN EBL are systematically studied. The light output power at 60 mA as a function of Al-content of EBL and the $I - V$ characteristics of the structures with $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$, $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$, and $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBLs are shown in Figs. 2(a) and 2(b), respectively. In Fig. 2(a), it is found that the structure with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL has the best light output power at 60 mA. Besides, the operation voltage of the LED is reduced when the Al-content of EBL is decreased, as shown in Fig. 2(b). Note that there exists an obvious increment between $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ and $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ structures.

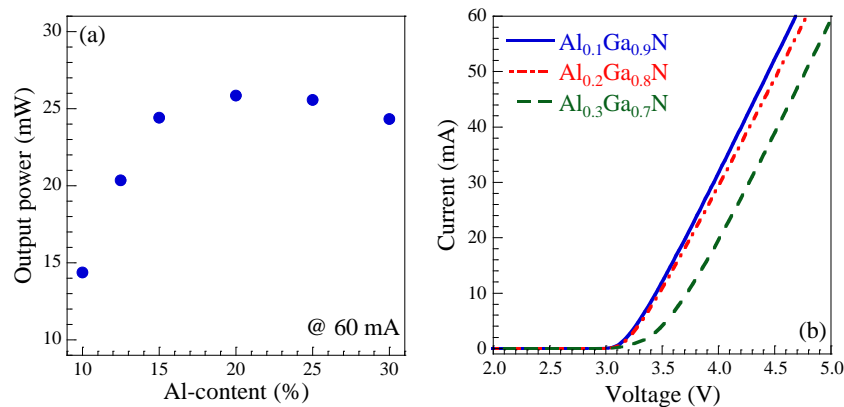


Fig. 2. Simulated (a) light output power at 60 mA as a function of Al-content of EBL and (b) $I - V$ characteristics of the structures with $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$, $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$, and $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBLs. Note that the LED with $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL is the original LED structure.

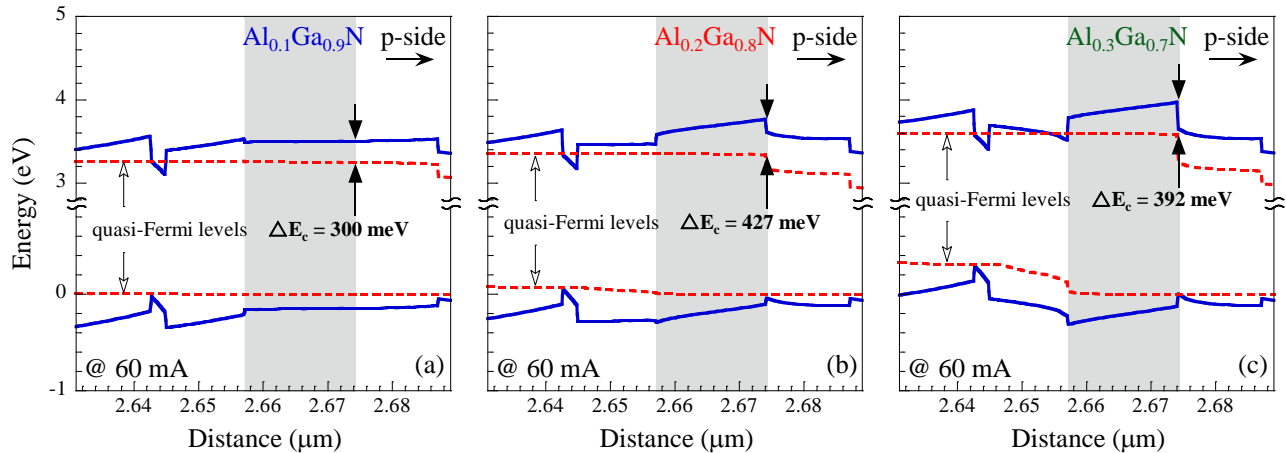


Fig. 3. Energy band diagrams near EBL of the structures with (a) $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$, (b) $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$, and (c) $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL at 60 mA.

Figure 3 shows the energy band diagrams near EBL of the structures with $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$, $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$, and $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL at 60 mA. In this figure, the effective potential height of EBL for electrons (ΔE_c), which is defined as the difference between quasi-Fermi level and the band edge at conduction band maximum of EBL, is calculated to estimate the blocking capability for electron leakage. It is observed that, since the bandgap energy increases with the increase of Al content, ΔE_c of the structure with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL is much higher than that of the structure with $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$ one (427 meV versus 300 meV). However, there exists a trade-off that the polarization mismatch between last barrier and EBL also increases when an EBL with higher Al content is employed. In this case, the polarization fields in last barrier and EBL are higher, and the LED structure thus suffers from more serious band bending and insufficient electron-blocking capability of EBL. In Fig. 3(c), ΔE_c of the structure with $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL is 392 meV, which is even smaller than the $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ structure.

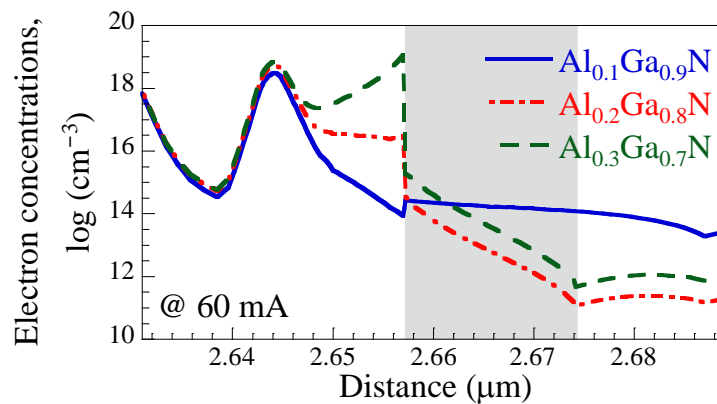


Fig. 4. Distribution of electron concentrations near EBL of the structures with $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$, $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$, and $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL at 60 mA.

Figure 4 shows the distribution of electron concentrations near EBL of the structures with $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$, $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$, and $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL at 60 mA. Evidently, the amount of electrons that leak out of the active region is markedly reduced when $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL is employed. The result coincides with the above analyses of energy bandgap and the light output power should be effectively improved when $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL (original EBL) is replaced by $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL.

3.2 Al-content and Mg-doping concentration in AlGaN EBL

In this section, the optical and electrical performances of 365-nm UV LEDs with various Al-content and Mg-doping concentrations in AlGaN EBL are systematically studied. The light output power at 60 mA as a function of Al-content of EBL and the $I - V$ characteristics of the structure with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL when the Mg-doping concentrations are $1 \times 10^{18} \text{ cm}^{-3}$, $5 \times 10^{18} \text{ cm}^{-3}$, and $1 \times 10^{19} \text{ cm}^{-3}$ respectively are shown in Figs. 5(a) and 5(b). It is obvious that the optical and electrical properties are promoted, i.e. higher output power and lower operation voltage, when higher Mg-doping concentration is adopted.

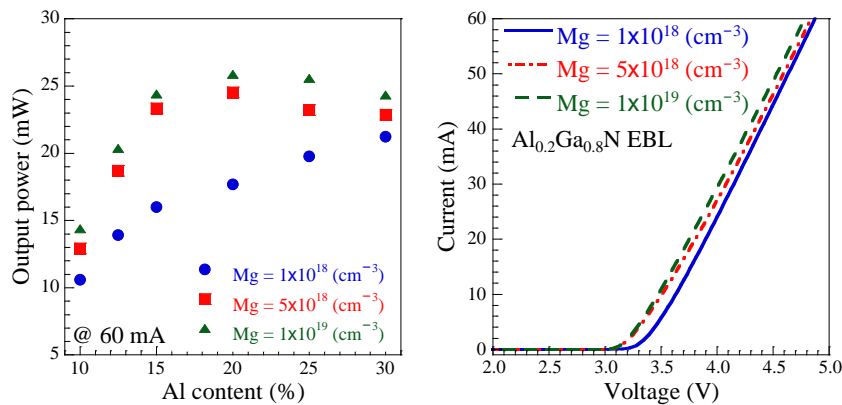


Fig. 5. Simulated (a) light output power at 60 mA as a function of Al-content of EBL and (b) $I - V$ characteristics of the structure with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL when the Mg-doping concentrations are $1 \times 10^{18} \text{ cm}^{-3}$, $5 \times 10^{18} \text{ cm}^{-3}$, and $1 \times 10^{19} \text{ cm}^{-3}$ respectively.

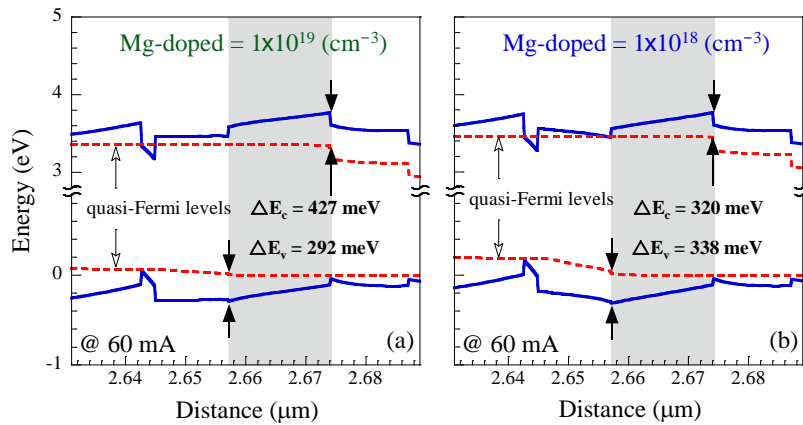


Fig. 6. Energy band diagrams near EBL of the structures with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL and (a) $1 \times 10^{19} \text{ cm}^{-3}$ and (b) $1 \times 10^{18} \text{ cm}^{-3}$ Mg-doping concentration at 60 mA.

Figure 6 shows the energy band diagrams near EBL of the structures with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL and (a) $1 \times 10^{19} \text{ cm}^{-3}$ and (b) $1 \times 10^{18} \text{ cm}^{-3}$ Mg-doping concentration at 60 mA. When the $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL is with higher Mg-doping concentration, ΔE_c increases while the effective potential height for holes of EBL (ΔE_v) decreases simultaneously. Under the circumstances, electrons of the active region are with higher confinement and holes in the p -side can inject into the active region more effectively.

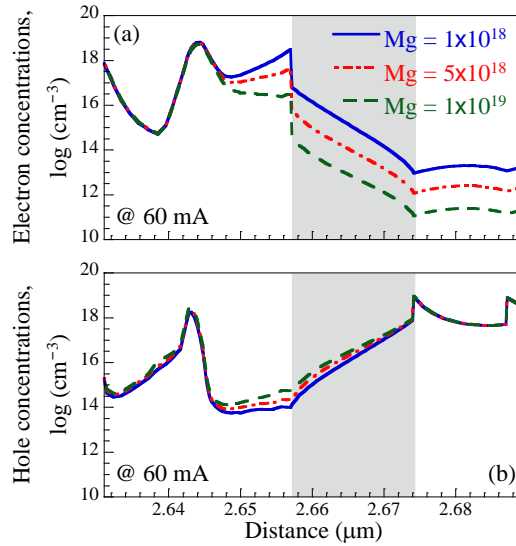


Fig. 7. Distribution of (a) electron concentrations and (b) hole concentrations near EBL of the UV LED structures with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL and $1 \times 10^{18} \text{ cm}^{-3}$, $5 \times 10^{18} \text{ cm}^{-3}$, and $1 \times 10^{19} \text{ cm}^{-3}$ *Mg*-doping concentrations.

The distribution of electron concentrations and hole concentrations near EBL of the UV LED structures with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL and $1 \times 10^{18} \text{ cm}^{-3}$, $5 \times 10^{18} \text{ cm}^{-3}$, and $1 \times 10^{19} \text{ cm}^{-3}$ *Mg*-doping concentrations are shown in Figure 7. It is found the amount of electrons that leak out of the active region is markedly increased and the holes inject into the active region is decreased when the *Mg*-doping concentration of EBL is reduced. The light output power and the electrical performance are therefore improved.

3.3 Comparison of AlGa_n/Ga_n superlattice EBL and Al-content-graded EBL

In this section, the UV LED structures with AlGa_n/Ga_n superlattice EBL and Al-content-graded EBL are compared numerically. The “original EBL” represents the structure with original $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL (17-nm-thick). In the structure with “gradual EBL”, the original EBL is replaced by a 30-nm-thick AlGa_n EBL in which the Al content is linearly graded from 10% to 20%. As for the structure with “SL EBL”, the original EBL is replaced by seven pairs $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}/\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$ (2 nm / 2nm) periodical superlattice layers. Note that, for the latter two structures, the thickness of *p*- $\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$ layer is relevantly reduced in order to keep the total thickness unchanged.

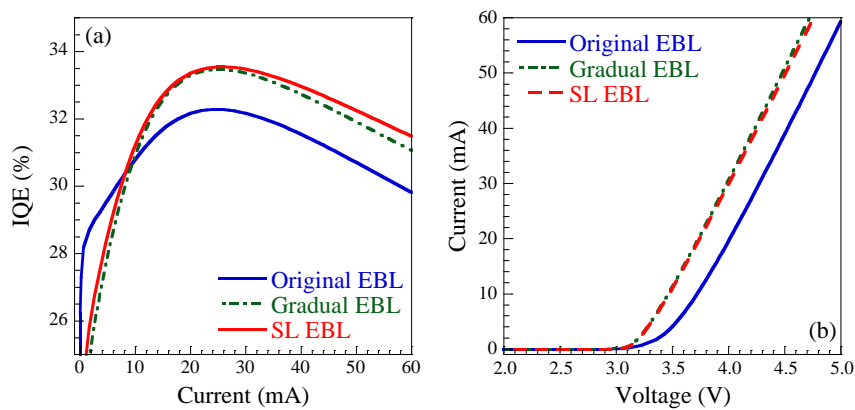


Fig. 8. Simulated (a) IQE curves and (b) $I-V$ characteristics of the 365-nm UV LEDs with original EBL, gradual EBL, and SL EBL.

Figure 8 shows the IQE curves and $I - V$ characteristics of the 365-nm UV LEDs with original EBL, gradual EBL, and SL EBL. In Fig. 8(a), it is found that the IQEs of the structures with gradual EBL and SL EBL are better than that of the original structure with $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL. Furthermore, the turn-on voltages of the two new-proposed structures are markedly reduced as well, as shown in Fig. 8(b).

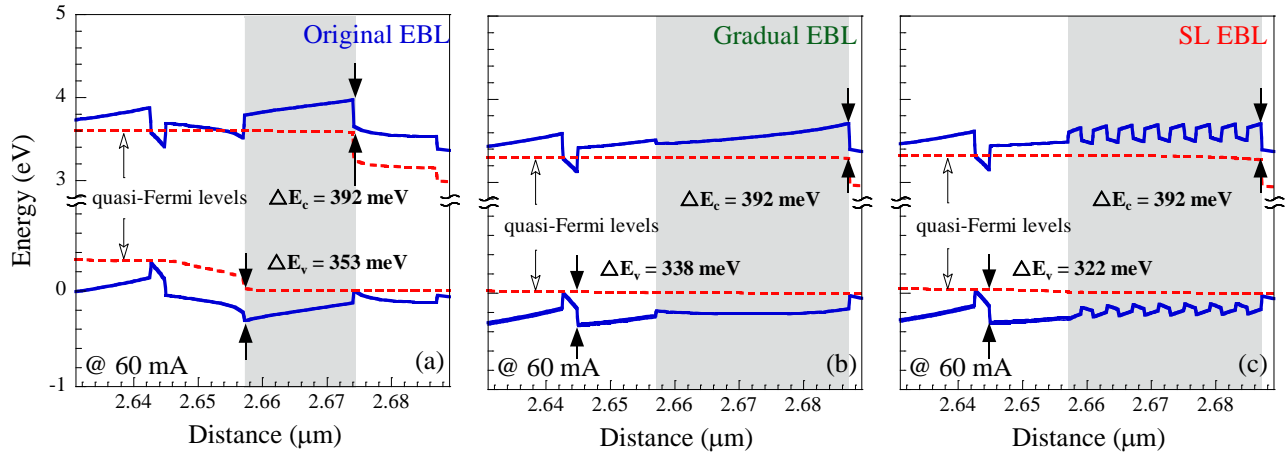


Fig. 9. Energy band diagrams near EBL of the structures with (a) original EBL, (b) gradual EBL, and (c) SL EBL at 60 mA.

Figure 9 shows the energy band diagrams near EBL of the structures with original EBL, gradual EBL, and SL EBL at 60 mA. It is interesting that ΔE_c of all the three structures are identical ($=392$ meV), indicating that the capabilities for electron blocking are similar. While for holes, ΔE_v of the structures with original EBL, gradual EBL, and SL EBL at 60 mA are 353 meV, 338 meV, and 322 meV, respectively. The efficiency of hole injection thus plays an important role for the various optical and electrical characteristics of these structures. The simulation results suggest that, among the structures, the one with SL EBL has optimal performance at 60 mA due to its lowest effective potential barrier height for holes.

4. CONCLUSION

In this paper, optimizations of 365-nm UV LEDs with various Al-content and Mg -doping concentrations of EBL are systematically studied. In addition, specific designs on band structure of EBL in 365-nm UV LEDs, including conventional AlGa N EBL, Al-content-graded EBL and AlGa N /Ga N superlattice EBL are investigated numerically. According to the simulation results, the $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL with high Mg -doping concentration had optimal performance at 60 mA due to the enhanced hole injection efficiency and suppressed electron overflow. Moreover, the structure with $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}/\text{Al}_{0.1}\text{Ga}_{0.9}\text{N}$ superlattice EBL has better IQE and electrical performance at 60 mA than the structures with $\text{Al}_{0.3}\text{Ga}_{0.7}\text{N}$ EBL and Al-content-graded EBL due to the enhanced hole injection efficiency.

5. ACKNOWLEDGMENTS

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