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Cite this: *RSC Adv.*, 2016, 6, 39542

# Chiral conversion and periodical decay in bridged-azobenzene photoisomerization: an *ab initio* on-the-fly nonadiabatic dynamics simulation†

Wanqing Gao,<sup>a</sup> Le Yu,<sup>\*bc</sup> Xiaolei Zheng,<sup>b</sup> Yibo Lei,<sup>b</sup> Chaoyuan Zhu<sup>c</sup> and Huixian Han<sup>\*a</sup>

With the implementation of global nonadiabatic switching probability algorithm based on the Zhu–Nakamura theory, we performed on-the-fly trajectory surface hopping simulations at the CASSCF level to analyze the *cis* ↔ *trans* photoisomerization mechanism of bridged-azobenzene upon  $S_1$  excitation. The *cis*-to-*trans* isomerization process was initiated by the pedal-like twist of –N=N– moiety and observed hopping to  $S_0$  mainly via the *cis*-form conical intersection region. While, the *trans*-to-*cis* process is induced by the nonsymmetrical torsion motion toward the central eight-membered ring and encountered surface hopping through another conical region lying in the middle of the isomerization pathway. In *cis*-to-*trans* photoisomerization, we also observed a particular chiral conversion pathway with surface hopping occurs at *Ci-trans* conical region. The trajectories followed this pathway possess relative longer excited state lifetimes as the ~40 fs initial stage oscillation in the *cis* Franck–Condon region. Moreover, the periodical population decay pattern of  $S_1$  state in *trans*-to-*cis* process was observed with an interval of ~16 fs.

Received 10th February 2016

Accepted 11th April 2016

DOI: 10.1039/c6ra03788g

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## 1. Introduction

Azobenzene (Ab) derivatives have been widely studied experimentally and theoretically for their peculiar photochromic properties which enable them to act as potential candidates for molecular motors, optical data storage and photobiological devices *etc.*<sup>1–3</sup> The Ab molecule was proposed to photoisomerize via torsion, inversion or the mixed inversion-assisted-torsion pathways,<sup>4–11</sup> while in the Ab derivatives with geometrical hindrance, these isomerization pathways may be strengthened, weakened or even prohibited.<sup>2,12–16</sup>

Many efforts have been devoted to enhance the photo-response and photostability of azobenzene derivatives. The bridged-azobenzene (b-Ab) molecule which has been synthesized for decades<sup>17,18</sup> was recently found to exhibit superior photochromic properties than the parent Ab molecule and therefore it has become a topic of interests.<sup>19–28</sup> In the experimental investigations of Siewertsen *et al.*,<sup>19,20</sup> the well separated

$S_1(n\pi^*)$  absorption bands at  $\lambda = 404$  nm (*cis*) and 490 nm (*trans*) together with large numbers of switching cycles was reported. They have also proposed that with an additional –CH<sub>2</sub>–CH<sub>2</sub>– bridge between the two benzene rings, the thermodynamics stability of *cis* and *trans* conformers has exchanged compare to parent Ab as the *trans*-b-Ab no longer adopts the planar equilibrium structure. Moreover, the severe conformational constraints led to a much accelerated *trans* → *cis* photoisomerization, however, comparing with the parent Ab, the *cis* → *trans* process is hardly affected. Meanwhile, relative higher quantum yields of  $\Phi_{cis \rightarrow trans} = 0.72 \pm 0.04$  and  $\Phi_{trans \rightarrow cis} = 0.50 \pm 0.10$  with corresponding time constants  $\tau_1 = 70$  (<50) and  $\tau_2 = 270$  (320) were derived.<sup>20</sup>

Attracted by the high efficient photo-induced conformation conversion, many nonadiabatic trajectory surface hopping (TSH) molecular dynamics (MD) simulations have been performed to reveal the photoisomerization mechanisms of b-Ab. Böckmann and co-workers<sup>21</sup> investigated the photoisomerization process of *trans*-b-Ab by using *ab initio* MD simulation at DFT level with the Tully's fewest-switches algorithm accounted for the nonadiabatic surface hopping. They have attributed the enhanced isomerization efficiency to favorable out-of-plane conformational preorientation of phenyl rings by the ethylenic bridge via ultrafast pedal motion of N atoms. Later, they have extended the investigation to both *trans* → *cis* and *cis* → *trans* processes with the same methodology.<sup>26</sup> Contrary to the accelerated *trans* → *cis* isomerization, the *cis* → *trans* process was found to be slightly hindered by a significant rearrangement of the bridge in the  $S_1$  state. They proposed that

<sup>a</sup>School of Physics, Northwest University, Xi'an, Shaanxi, 710069, P. R. China. E-mail: hxhan@nwnu.edu.cn

<sup>b</sup>Key Laboratory of Synthetic and Natural Functional Molecule Chemistry of Ministry of Education, College of Chemistry & Materials Science, Shaanxi Key Laboratory of Physico-Inorganic Chemistry, Northwest University, Xi'an, Shaanxi, 710127, P. R. China. E-mail: yule@iccas.ac.cn

<sup>c</sup>Institute of Molecular Science, Department of Applied Chemistry, and Center for Interdisciplinary Molecular Science, National Chiao-Tung University, Hsinchu 300, Taiwan

† Electronic supplementary information (ESI) available. See DOI: 10.1039/c6ra03788g

both of the isomerization processes were proceeded by the NN twist mechanisms with equally or unequally contributing nitrogen sites, respectively, as those observed in parent Ab.<sup>29,30</sup> Furthermore, they have observed a nonreactive chirality switch induced by pseudorotation of the central 8-membered ring system in *cis*-b-Ab. In the dynamics simulation work of Carstensen *et al.*<sup>22</sup> at the AM1 floating-occupation configuration interaction (FOCI-AM1) level, they proposed that the ethylenic bridge does not provide a steric hindrance in the *cis* → *trans* isomerization while the complex interplay of motions towards the central 8-membered ring blocks the forward reaction in the ground state and result in a reduced quantum yields. Based on potential energy surfaces (PESs) constructed at the CASSCF level with active space composed of 14 electrons in 12 orbitals, they have concluded that the *cis* → *trans* and the *trans* → *cis* photoisomerization proceed *via* different conical intersection regions. The two processes exhibit different features: barrierless *versus* ground state barrier and steep *versus* flat potential energy landscape, respectively. Density-functional based semiclassical electron-radiation-ion dynamics (SERID) simulations on the topic reaction system have been performed by Liu *et al.*<sup>23</sup> and Jiang and coworkers.<sup>24,25</sup> The former investigation<sup>23</sup> also provides PESs of S<sub>1</sub> and S<sub>0</sub> states constructed at CASPT2 level based on CASSCF optimized geometries and confirmed that only one conical intersection exists between S<sub>1</sub> and S<sub>0</sub> states. Moreover, they proposed that the internal energy redistribution controls the relaxation process from the S<sub>1</sub> Franck-Condon region to the conical region and therefore determines the lifetime. Jiang and coworkers<sup>24,25</sup> also confirmed that the ethylenic bridge does not hinder the rotation pathway and the S<sub>1</sub> → S<sub>0</sub> internal conversions occur in the same conical region in the *cis* ↔ *trans* processes. Surface hopping dynamics simulations based on the original Zhu-Nakamura theory has been carried on by Gao *et al.*,<sup>27,28</sup> which confirmed that the torsion around -N=N- moiety together with the twisting of phenyl rings in opposite direction is the dominant mechanism. They also reproduced the two types of CI regions and proposed that in the *trans* → *cis* and *cis* → *trans* isomerization, the azo-moiety initially approaches product region and then the two phenyl rings and ethylenic bridge adjust themselves to complete the process.

Although such a lot dynamics simulations have been put forward on the photoisomerization of b-Ab, the mechanism for chirality conversion in the *cis* → *trans* photoisomerization and the properties of population decay on the excited state are still unclear. The main reasons are the insufficiency of the DFT method in dealing with conical intersections and the limited number of simulated trajectories in previous theoretical investigations. Thus a large scale full dimensional on-the-fly trajectory based nonadiabatic molecular dynamics simulation investigation employing high level *ab initio* calculation is required to resolve the existed problems. In this work, with implementation of recently developed Zhu-Nakamura nonadiabatic switching probability calculation formula which only using adiabatic potential energy surface and its gradients,<sup>5</sup> we have performed an extensive on-the-fly trajectory surface-hopping dynamics simulations at the CASSCF *ab initio*

quantum level to probe both the *cis* → *trans* and the *trans* → *cis* photoisomerization mechanism of the bridged-azobenzene. The quantum yields and lifetimes are estimated by analyzing 400 trajectories for *cis*-to-*trans* and 550 trajectories for *trans*-to-*cis* processes and the roles of the pathways involved in the processes will also be discussed. In the next section, we will give a brief description on the present trajectory surface-hopping method and *ab initio* method incorporated on-the-fly into the nonadiabatic molecular dynamic simulation algorithm. In Section 3, we will provide detailed analyses and explanations on the b-Ab photoisomerization mechanisms upon S<sub>1</sub> excitation.

## 2. Theoretical methods and computational details

Novel trajectory surface hopping method based on the improved Zhu-Nakamura theory (ZN switches) has been successfully applied to investigate nonadiabatic photodynamics of several reaction systems<sup>4,5,31</sup> and the algorithm is briefly described as follows. The on-the-fly trajectory is propagated by numerically integrating the Newtonian equation of motion with the velocity-Verlet method<sup>32</sup> with the potential energy and its' gradients calculated by CASSCF method step by step. Along trajectory propagation, we detect avoided crossing point by computing minimum separation of two adjacent adiabatic potential energy surfaces within three consecutive time steps (this is usually executed in conical intersection region). At this avoided crossing point, we compute global nonadiabatic switching probability according to the improved Landau-Zener formula by Zhu and Nakamura,<sup>33,34</sup>

$$p = \exp \left[ -\frac{\pi}{4\sqrt{a^2}} \sqrt{\frac{2}{b^2 + \sqrt{b^4 \pm 1}}} \right], \quad (1)$$

in which two unitless parameters, namely effective coupling and effective collision energy, are given by

$$a^2 = \frac{\hbar^2}{2\mu} \frac{\sqrt{|F_2 F_1|} |F_2 - F_1|}{(2V_{12})^3} \quad (2)$$

and

$$b^2 = (E_t - E_x) \frac{|F_2 - F_1|}{\sqrt{|F_2 F_1|} (2V_{12})} \quad (3)$$

in which,  $F_1$  and  $F_2$  are forces on two diabatic potential energy surfaces,  $V_{12}$  is diabatic coupling,  $\mu$  is reduced mass of diatomic molecule,  $E_x$  is energy at crossing point and  $E_t$  is potential energy plus kinetic energy component in direction of hopping vector (note + (-) in eqn (1) stands for  $F_2 F_1 > 0$  ( $F_2 F_1 < 0$ )). Diabatic coupling  $V_{12}$  in eqn (2) is directly computed by the energy separation between two adiabatic potential energy surfaces at avoided crossing. At this avoided crossing, we convert mass-scaled multidimensional forces into mass-scaled one-dimensional forces as given in eqn (4) and (5),<sup>5</sup>

$$\frac{|F_2 - F_1|}{\sqrt{\mu}} = \sqrt{\sum_{i=1}^N \frac{1}{m_i} \sum_{\alpha=x,y,z} (F_2^{i\alpha} - F_1^{i\alpha})^2}, \quad (4)$$

and

$$\frac{\sqrt{|F_2 F_1|}}{\sqrt{\mu}} = \sqrt{\left| \sum_{i=1}^N \frac{1}{m_i} \sum_{\alpha=x,y,z} F_2^{i\alpha} F_1^{i\alpha} \right|} \quad (5)$$

where  $N$  is number of nuclei in molecule with the mass  $m_i$  ( $i = 1, 2, \dots, N$ ),  $\alpha$  stands for  $x$ ,  $y$ , and  $z$  component of Cartesian coordinates for the  $i$ -th nucleus, and multidimensional diabatic forces  $F_1^{i\alpha}$  and  $F_2^{i\alpha}$  are generalized from adiabatic forces within three consecutive time steps around detected avoided crossing along the trajectory. Detailed description along with definition of hopping direction and momentum change at an attempted trajectory hopping position is given in the ref. 4.

The simulated trajectories are started from Franck–Condon region of *cis*- or *trans*-b-Ab in  $S_1$  state, and initial velocities are set up by the procedure summarized in ref. 4. The thermal kinetic energy with  $T = 300$  K is added to all sampling trajectories with randomly distributing into initial Wigner velocities. Following the previous investigation in azobenzene,<sup>4,5</sup> the 0.5 fs time-step is selected in the entire simulation on b-Ab. For trajectories starting from both *cis*- and *trans*-b-Ab, the time limit is set up to 200 fs. In total, 400 trajectories for *cis*  $\rightarrow$  *trans* photoisomerization process and 550 trajectories for the *trans*  $\rightarrow$  *cis* case were run to get converged excited state lifetimes and quantum yields.

In the current work, the structures of *cis*- and *trans*-b-Ab in  $S_0$ , *trans*-b-Ab in  $S_1$  and the minimum energy conical intersections (CI) between the  $S_0$  and  $S_1$  states were optimized by using

the two-state averaged CASSCF method (SA2-CASSCF) with active spaces composed of 10 electrons in 8 orbitals (10e, 8o) and 6 electrons in 5 orbitals (6e, 5o), referred as CASSCF(10,8) and CASSCF(6,5), respectively. Based on the consideration of both the accuracy and efficiency, (which will be discussed in detail in next section) the CASSCF(6,5) was selected in the potential energy and energy gradients calculation embedded in molecular dynamics simulation. All the calculations were carried out with the 6-31G basis set. The CIs were optimized by using the MOLPRO 2009.1 package<sup>35–37</sup> and the optimization of other geometries as well as on-the-fly potential energies and their gradients' calculations were performed with the MOLCAS 7.5 program.<sup>38</sup> To account for the dynamical electron correlation, the corrected energy for optimized geometries at complete active space second order perturbation theory (CASPT2) and internally contracted multi-reference configuration interaction (ICMRCI) level were performed by employing the MOLCAS 7.5 and Xi'an CI program of our group,<sup>39</sup> respectively.

### 3. Results and discussions

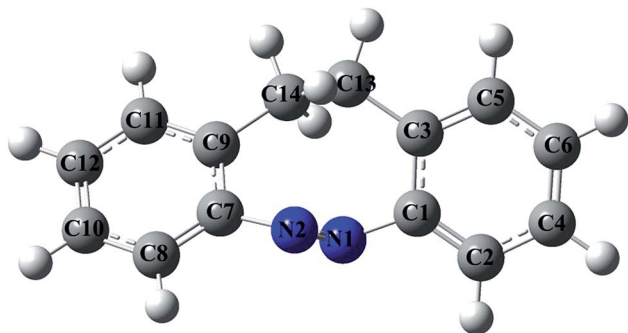
#### 3.1 Stationary structures and possible isomerization pathways

To explore the topology of potential energy surface along the photoisomerization channels starting from both isomers at  $S_1$ , we optimize the ground state minima, transition state and minimum-energy conical intersections between the  $S_1$  and  $S_0$

Table 1 Optimized geometry parameters for the ground state minima and  $S_0/S_1$  conical intersections<sup>a</sup>

Method	Geometry	NN	CNN <sup>b</sup>	CNNC <sup>c</sup>	CCCC <sup>d</sup>	CCNN <sup>e</sup>	CCCC <sup>f</sup>
CASSCF (6e,5o)/6-31G <sup>g</sup>	<i>cis</i>	1.26	123.3/122.2	7.1	40.4	69.3/–72.3	34.3/–85.5
	<i>trans</i>	1.27	112.8/113.3	145.4	100.0	–65.3/–63.3	–44.8/–46.0
	CI- <i>cis</i>	1.33	127.3/117.4	94.7	85.9	–3.8/–87.0	–13.7/–76.4
	CI- <i>trans</i>	1.33	130.8/122.0	97.8	111.9	–26.5/–51.1	–48.8/–54.7
CASSCF (10e,8o)/6-31G <sup>g</sup>	<i>cis</i>	1.26	122.6/122.0	7.4	35.7	69.8/–73.1	39.5/–84.1
	<i>trans</i>	1.27	113.0/113.0	145.7	100.7	–64.4/–64.4	–45.9/–45.9
	CI- <i>cis</i>	1.33	127.5/117.8	95.0	86.4	–4.5/–86.4	–14.4/–76.2
	CI- <i>trans</i>	1.30	135.2/123.4	97.2	110.0	–21.8/–56.0	–47.1/–57.7
CASSCF (6e,5o)/6-31G <sup>h</sup>	<i>cis</i>	1.26	122.8/122.1	6.4	37.7	70.1/–71.8	
	<i>trans</i>	1.27	113.3/112.8	145.4	100.0	–63.2/–65.3	
CASSCF (10e,8o)/6-31G <sup>*h</sup>	<i>cis</i>	1.25	121.3/120.9	6.3	30.7	72.7/–75.6	
	<i>trans</i>	1.25	111.1/111.1	148.3	97.1	–66.1/–66.1	
CASSCF (14e,12o)/6-31G <sup>*h</sup>	<i>cis</i>	1.25	121.4/120.9	5.8	31.3	73.1/–74.9	42.5/–82.0
	<i>trans</i>	1.25	111.1/111.1	147.5	96.2	–65.6/–65.6	–43.6/–43.6
	CI- <i>cis</i>	1.28	134.7/121.6	95.3	103.4	–33.9/–95.3	
	CI- <i>trans</i>	1.28	136.2/121.6	99.5	108.8	–34.3/–43.2	
FOCI-AM1 <sup>i</sup>	<i>cis</i>	1.26	121.4/122.6	6.2	8.3	66.3/78.1	
	<i>trans</i>	1.27	114.9/114.9	138.6	20.0	66.7/66.6	
	CI- <i>cis</i>		129.7/111.4	90.6	74.2	5.6/105.3	
	CI- <i>trans</i>		132.1/132.0	95.5	111.9	40.8/39.9	
CASSCF (10e,8o)/6-31G <sup>*j</sup>	<i>cis</i>	1.26	118.6/118.2	5.9	27.2	74.3/–80.4	47.5/–84.5
	<i>trans</i>	1.28	114.1/114.1	145.8	108.4	–64.0/–64.0	–50.3/–50.3
DFT/6-31G <sup>*k</sup>	<i>cis</i>	1.26	121.7/121.6	6.6	35.3	72/113.4	
	<i>trans</i>	1.27	112.0/112.1	146.3	98.6	125/127	
Expt <sup>l</sup>	<i>cis</i>	1.24	122.6/122.2	6.5	37.3	71.3/–72.0	37.5/–83.4
	<i>trans</i>	1.25	112.4/112.4	146.8	96.5	–64.3/–64.5	–42.9/–43.1

<sup>a</sup> Bond length is given in angstroms (Å), and bond angles and dihedral angles are given in degrees. <sup>b</sup> C7N2N1/C1N1N2. <sup>c</sup> C7N2N1C1. <sup>d</sup> C9C14C13C3. <sup>e</sup> C3C1N1N2/C9C7N2N1. <sup>f</sup> C7C9C14C13/C1C3C13C14. <sup>g</sup> This work. <sup>h</sup> Ref. 27. <sup>i</sup> Ref. 22. <sup>j</sup> Ref. 23. <sup>k</sup> Ref. 26. <sup>l</sup> Ref. 19.



Scheme 1 Atomic numbering (geometry of *trans*-b-Ab).

states at the SA2-CASSCF(10,8) and SA2-CASSCF(6,5), respectively. The optimized geometries at CASSCF level with different active spaces are listed in Table 1 and the relative energies with respect to  $S_0$  *cis* and vertical excitation energies for these geometries are given in Table S1.† The atomic numbering is displayed in Scheme 1. Moreover, the optimized Cartesian coordinates for minima and CIs with different chirality at the CASSCF(10,8) and CASSCF(6,5) level are listed in Table S2.†

As shown in Table 1, the internal coordinates of ground state *cis* and *trans* conformers optimized at CASSCF(6,5) are in very good agreement with those obtained by CASSCF(10,8) and also reproduces the experimental values<sup>19</sup> very well. These results indicate that the dynamics simulation with CASSCF(6,5) could reasonably describe the geometrical changes in the isomerization process. The accuracy of energies calculated by CASSCF(6,5) was further verified by comparing with the relative energies to the  $S_0$  *cis* isomer calculated by the CASPT2 and ICMRCI based on the CASSCF optimized geometry. Comparing with the experimental value of 70.8 and 58.4 kcal mol<sup>-1</sup>,<sup>19</sup> respectively, the calculated vertical excitation energies for  $S_0$  *cis* and *trans* are overestimated with CASSCF(6,5), even with the ICMRCI correction (84.7 and 77.4 kcal mol<sup>-1</sup>). It can be seen from Table 1, the calculations with (10e, 8o) active space gives better vertical excitation energies. However, the relative energies computed by CASSCF, CASPT2 and ICMRCI methods with (10e, 8o) and (6e, 5o) active spaces at the optimized geometries are on the whole quite close. With consideration of the computation cost and accuracy, the CASSCF(6,5) was used in the following dynamics simulations to obtain the potential energies and their gradients along the trajectories.

With default conical intersection optimization procedure, we could only reproduce the four conical structures reported by Gao *et al.*<sup>27</sup> at CASSCF(10,8). (CI-*trans* type) By loosening convergence threshold in MOLPRO program,<sup>37</sup> we could also obtain similar conical geometries with CASSCF(6,5). Moreover, another type of conical regions, namely CI-*cis*, was roughly located by the dynamics simulation on the *cis* → *trans* isomerization with CASSCF(6,5), and then optimized by CASSCF(10,8) with default procedure and CASSCF(6,5) by loosening convergence threshold in MOLPRO.<sup>37</sup> This observations agree with previous reported CoIn-Z geometry by Carstensen *et al.*<sup>22</sup> and CI<sub>3</sub>/CI<sub>4</sub> by Gao *et al.*,<sup>27,28</sup> which were both optimized

at the CASSCF level with larger active space involving 14 electrons in 12 orbitals. The four CI-*trans* type conical intersections are enantiomers mirroring to the perpendicular and parallel molecular plane, and can be distinguished by the signs of dihedral angles C7N2N1C1, C3C1N1N2 and C9C7N2N1. In which, the C7N2N1C1 angle is close to ~95°, slightly smaller than CI-*trans* type CIs, but the other dihedral angles and bond angles relating to the central eight-membered ring are much different. In the process of approaching the CI-*trans* type conical regions, large amplitude benzene rings' open-close twist with respect to the central azo- and ethyl-bridge moiety and small amplitude N=N torsion are needed. While for the CI-*cis* case, the relative positions of the two benzene rings and ethyl-bridge stay close to *cis*-b-Ab, and the evident changes on C7N2N1C1 are mainly induced by the pedal-like twist motion of azo-bridge and related molecules. The two distinct types of conical regions would induce different photoisomerization mechanisms, and through which one the internal conversion occurs will be discussed in the next section in detail.

The *trans*-b-Ab molecule attracts more and more interests to researchers for its higher quantum yields and shorter excited state lifetimes than the parent *trans*-Ab. Here, we present the following explanations for its enhanced photoresponsibilities. Firstly, comparing with parent Ab, the  $S_1$  state PES appears in the steeper slope from Franck–Condon region to CI-*trans* for the *trans*-b-Ab molecule (the energy difference is 6.9 kcal mol<sup>-1</sup> for *trans*-Ab<sup>4</sup> and 39.2 kcal mol<sup>-1</sup> for *trans*-b-Ab). Thus, the *trans*-b-Ab molecule could obtain larger excited state driving force to arrive at the conical region faster on the excited state. Secondly, the *trans*-b-Ab no longer keeps flat, and thus do not need the long time vibrational redistribution to give enough kinetic energy into the out-of-plane motion as those in *trans*-Ab (~350 fs in *trans*-Ab photoisomerization<sup>5</sup>). The third reason is that the CNNC angle in *trans*-b-Ab (145.4) is smaller than that in b-Ab (180.0),<sup>4</sup> while, in corresponding CI involved in the isomerization of these two *trans* form molecules are quite similar (97.8 and 97.4,<sup>4</sup> respectively). Evidently, in *trans*-b-Ab, the isomerization pathway from *trans* side is shorter than the one in *trans*-Ab. With the above mentioned reasons, it is clear that the  $S_1$

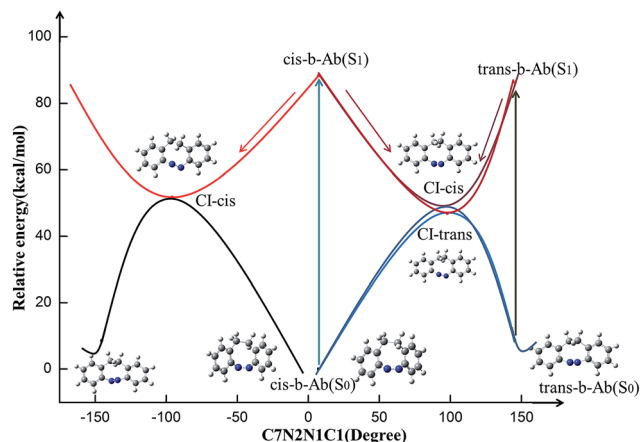


Fig. 1 Potential energy profiles for the *cis* ↔ *trans* photoisomerization of bridged-azobenzene.



state lifetime for *trans*-b-Ab would be rather short and in the same time scales as the *cis* form conformer, which follow a steep downhill in both *cis*-b-Ab and parent *cis*-Ab. Moreover, the quantum yields of *trans*-b-Ab would also be enhanced by the larger driven force along isomerization path in  $S_1$  state.

### 3.2 Photoisomerization reaction dynamics

To verify the reaction mechanism and explore the statistical properties for b-Ab photoisomerization upon  $S_1$  excitation, we have performed ZN switches surface hopping dynamics simulations with 400 trajectories starting from *cis* and 550 trajectories starting from *trans* form. Based on the static electronic

structure computations and dynamics simulations, we propose the following scenario for the photoisomerization processes of b-Ab as depicted in Fig. 1. Upon photoexcitation, the *cis* or *trans* conformers move along the respective isomerization pathways to visit conical regions and after surface hopping, the molecule may continue follow the isomerization path to product region or back to initial geometry. The *trans*  $\rightarrow$  *cis* isomerization encounters surface hopping through CI-*trans* type conical regions, which are in agreement with previous investigations.<sup>22</sup> While the *cis*  $\rightarrow$  *trans* isomerization is more complicated, we have observed two competing processes corresponding to clockwise and counterclockwise torsion toward the N=N

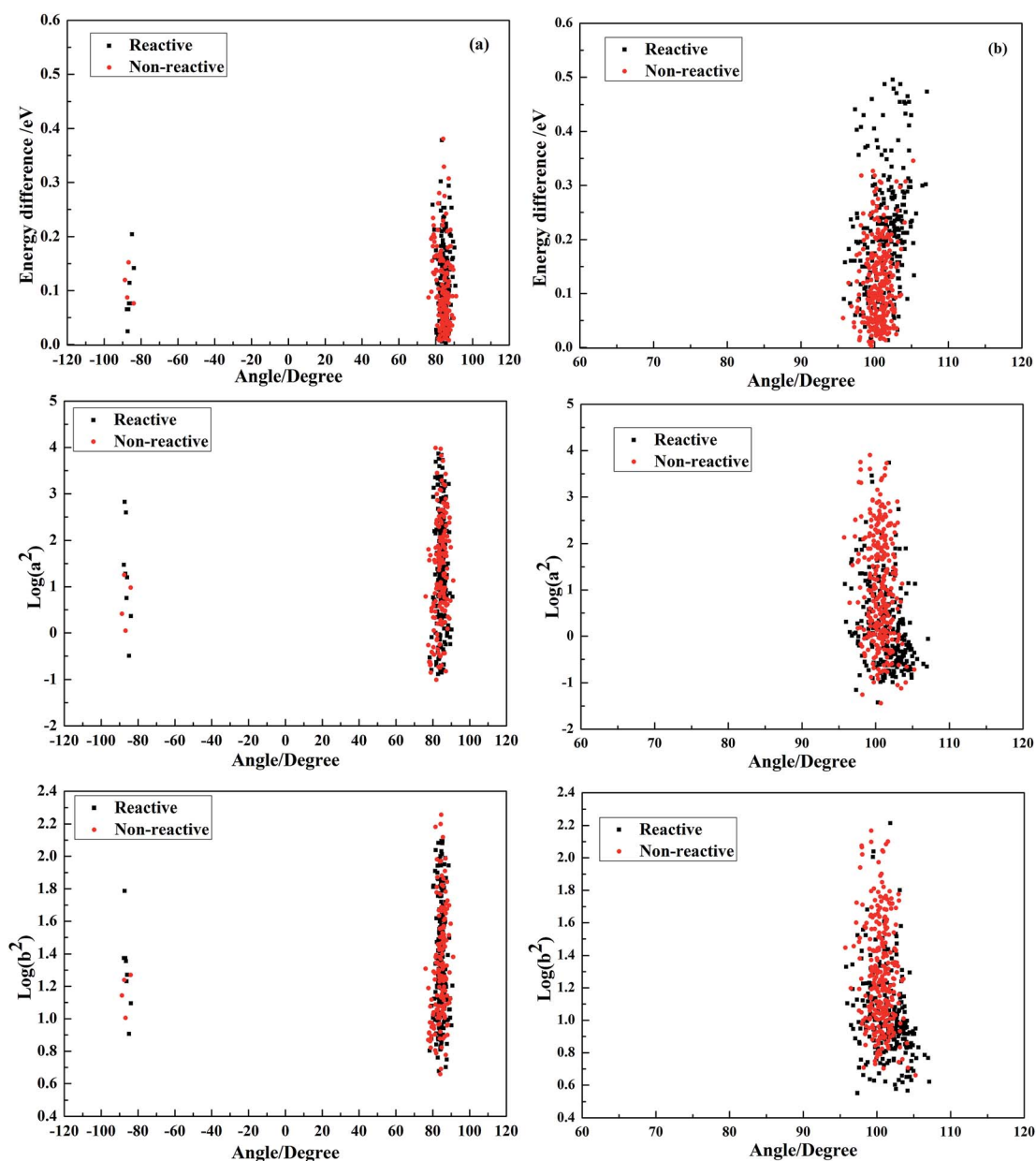


Fig. 2 The distribution of successful hopping points in terms of the CNNC dihedral angle. (a) The first panel is for energy gaps, the second panel is for effective coupling parameters, and the third panel is for effective collision energy in the case of *cis*-to-*trans*. (b) The same as (a) but in the case of *trans*-to-*cis*.

bridge. Moreover, the minority trajectories which experience helicity conversion ( $N=N$  clockwise motion) visit *CI-trans* type conical region, while the majority trajectories that keep helicity unchanged ( $N=N$  counterclockwise motion) hop to the  $S_0$  state through *CI-cis* type conical region. The helicity conversion towards the CNNC dihedral angle in *cis*  $\rightarrow$  *trans* photoisomerization has been reported for parent azobenzene<sup>6–8</sup> and also was proposed to be possible in the bridged-azobenzene.<sup>26</sup> In the current work, this chiral conversion pathway has been confirmed for the first time with implementation of the ZN switches surface hopping dynamics simulations.

To further reveal the origin of discrepancy between *cis*  $\rightarrow$  *trans* and *trans*  $\rightarrow$  *cis* isomerization mechanism, we have

depicted the distribution of successful hopping points' in terms of CNNC dihedral angle *versus* energy gap, effective nonadiabatic coupling factors and effective collision energy in Fig. 2 and in terms of the other important internal coordinates in Fig. 3. As in Fig. 2a and b, the CNNC dihedral angle is distributed in the range  $[-80^\circ, -90^\circ]$  and  $[75^\circ, 95^\circ]$  for *cis*  $\rightarrow$  *trans* and  $[95^\circ, 110^\circ]$  for *trans*  $\rightarrow$  *cis*. It is clear that the surface hopping takes place in the range of absolute value of CNNC smaller (larger) than 97.8 and 94.7 at the conical intersection for *cis*  $\rightarrow$  *trans* (*trans*  $\rightarrow$  *cis*). This also agrees with the parent azobenzene<sup>5</sup> and reflects the different motion direction when the reactant approaches the conical regions. In the *cis*-to-*trans* and *trans*-to-*cis* cases, the potential energy differences at hopping spots are distributed in

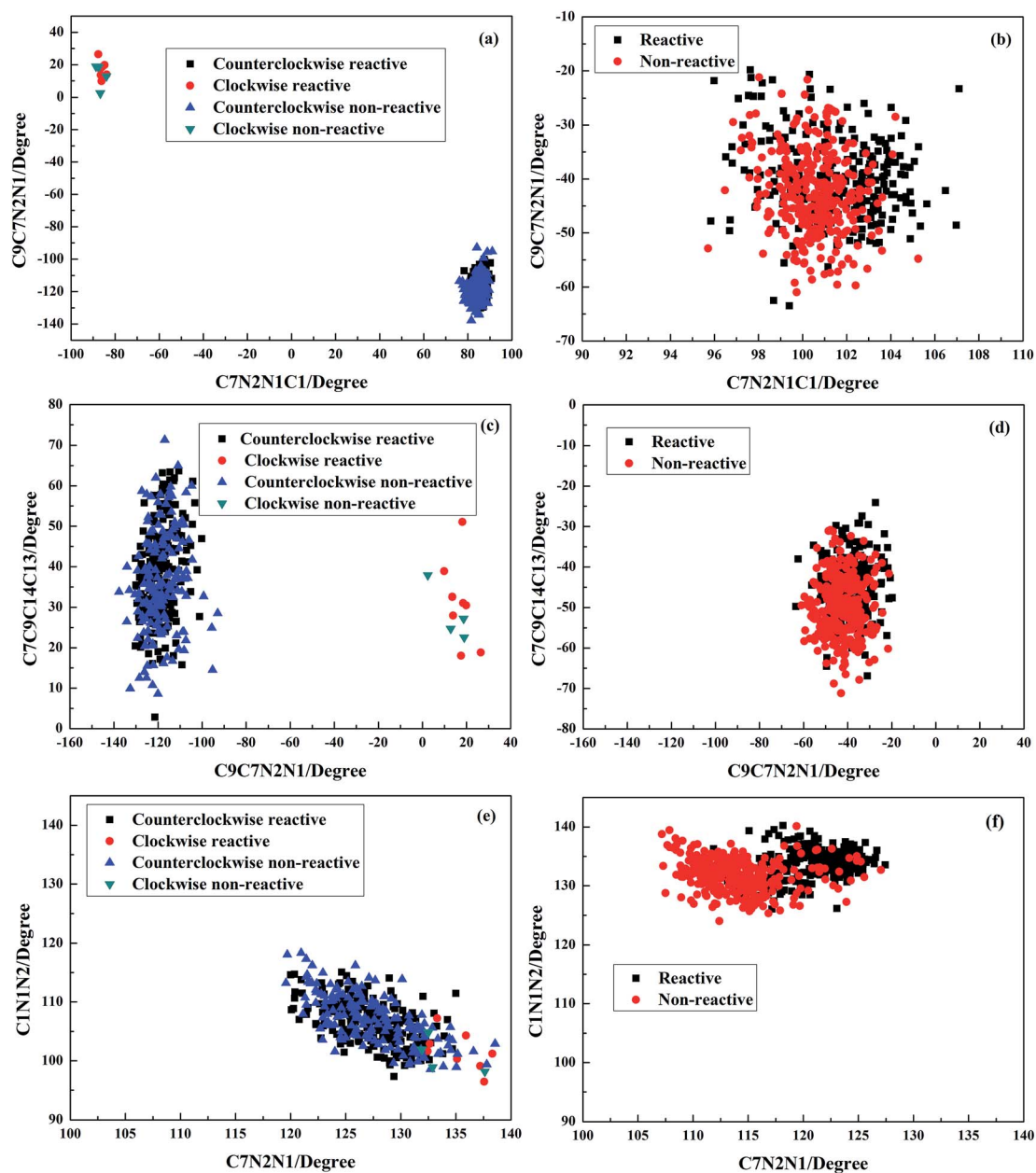


Fig. 3 Geometrical parameter distribution for dihedral angles  $C7N2N1C1$  versus  $C9C7N2N1$  (upper panel), dihedral angles  $C7C9C14C13$  versus  $C9C7N2N1$  (middle panel), bond angles  $C1N1N2$  versus  $C7N2N1$  (bottom panel) at the surface hopping points involve in *cis*-to-*trans* (a, c and e) and *trans*-to-*cis* (b, d and f) processes respectively.

0.00 to 0.40 eV and 0.00 to 0.50 eV regions, respectively (Fig. 2 upper panel). However, the distribution of the effective coupling parameter  $a^2$  and the effective collision energy  $b^2$  are all in the region of  $a^2 \sim [0.1, 10^4]$  (Fig. 2 middle panel) and  $b^2 \sim [2200]$  (Fig. 2 bottom panel) for both *cis*-to-*trans* and *trans*-to-*cis* cases. According to the ZN-switches algorithm, the dimensionless parameters  $a^2$  and  $b^2$  determine the switching probabilities at the conical zones and the similar distribution of these parameters in both isomerization processes demonstrate the reliability of the current simulation. Moreover, for *trans*-to-*cis* isomerization, more reactive surface hopping points distributed in the region with larger energy gap, and consequently result in preference on smaller  $a^2$  and  $b^2$  values. For *cis*-to-*trans* isomerization, the hopping points for reactive and nonreactive trajectories cover similar regions. With only CNNC related distributions shown in Fig. 2, we could not distinguish how the CI-*trans* and CI-*cis* type conical regions contribute to the photoisomerization and therefore we display distributions of the other important internal coordinates at hopping spots in Fig. 3. Fig. 3a and b show the distribution of C9C7N2N1 versus C7N2N1C1 at surface hopping points for the *cis*-to-*trans* and *trans*-to-*cis* processes respectively. It can be seen that the counterclockwise channel in *cis*  $\rightarrow$  *trans* process visits the CI-*cis* type conical region with C9C7N2N1 distributed in the range  $[-90^\circ, -140^\circ]$ , while the clockwise channel in *cis*  $\rightarrow$  *trans* process and all the trajectories of *trans*  $\rightarrow$  *cis* visit chiral symmetric CI-*trans* type conical regions with C9C7N2N1 distributed in the range  $[0^\circ, 30^\circ]$  and  $[-20^\circ, -65^\circ]$ , respectively. The variation of C7C9C14C13 and C9C7N2N1 dihedral angles indicates the twist motion of the central eight-membered ring in b-Ab. As shown in Fig. 3c and d, counterclockwise channel in *cis*  $\rightarrow$  *trans* undergo surface hopping in the region which has inverse C7C9C14C13 value of  $[0^\circ, 60^\circ]$  and much smaller C9C7N2N1 value around  $-120^\circ$  compared with the *trans*  $\rightarrow$  *cis* pathway. The CNN angles reflect the inversion motion toward the azo-bridge, as shown in Fig. 3e, with C1N1N2 distributed in the range of  $[95^\circ, 112^\circ]$ . The clockwise ones possess larger C7N2N1 angle, which may be related to the flip of the azo-bridge. In Fig. 3f, more reactive surface hopping points were found in the region where C7N2N1 is larger than  $117^\circ$  in *trans*

$\rightarrow$  *cis* process, indicating that the enhanced torsion motion would assist the reactive pathway.

Within the 400 trajectories started at  $S_1$  *cis*, 12 trajectories follow the clockwise pathway (8 isomerize to *trans* conformer and 4 back to *cis* form) and 388 trajectories follow counterclockwise pathway (217 isomerize to *trans* conformer and 171 back to *cis* form). While, for 550 trajectories started at  $S_1$  *trans*, 244 isomerize to *cis* conformer and 306 back to *cis* form. As the C9C7N2N1 is the most important dihedral angle involving in the motion of photoisomerization, time evolutions of C9C7N2N1 dihedral angle for the simulated trajectories started at *cis* and *trans* are depicted in Fig. 4a and b, respectively. The trajectories follow clockwise and counterclockwise channels are clearly demonstrated in Fig. 4a, and the clockwise ones need more time to arrive the conical region with C9C7N2N1 around  $95^\circ$  as the flip of molecular plane.

The quantum yields and the excited state lifetimes are estimated by the following procedure based on the simulated data. The quantum yield equal to the ratio of reactive ones in all trajectories with a standard error  $\sigma = \sqrt{N - N_r} / (NN_r)$ . The isomerization lifetime is obtained by fitting the time-dependent decay curve of  $S_1$  state population to the exponential function  $f(t) = e^{-(t-t_d)/\tau}$ , where  $t_d$  is the onset time of the  $S_1$  population loss, and  $\tau$  is the time constant for the exponential decay. The lifetime is estimated as the value of  $\tau + t_d$ .

Simulated quantum yield and the lifetime for *cis*-to-*trans* (*trans*-to-*cis*) converge to 0.57 and 64 fs (0.44 and 35.5 fs) with 400 (550) sampling trajectories as summarized in Table 2. In current work, the estimated quantum yields for both the *cis*-to-*trans* and *trans*-to-*cis* processes show decrease trend with more trajectories taken into account. The simulated results are in good agreement with experimental values<sup>19,20</sup> and the other previous simulations based on relatively limited number of trajectories to some extent.<sup>21–28</sup>

Fig. 5 shows the distribution of the  $S_1 \rightarrow S_0$  hopping times and time-dependent decay curves of  $S_0$  and  $S_1$  population for the *cis*-to-*trans* and *trans*-to-*cis* processes. Periodical decay pattern in *cis*  $\rightarrow$  *trans* isomerization of azobenzene has been presented in a recent letter,<sup>6</sup> while in b-Ab photoisomerization, we observe similar feature in the *trans*  $\rightarrow$  *cis* process. As

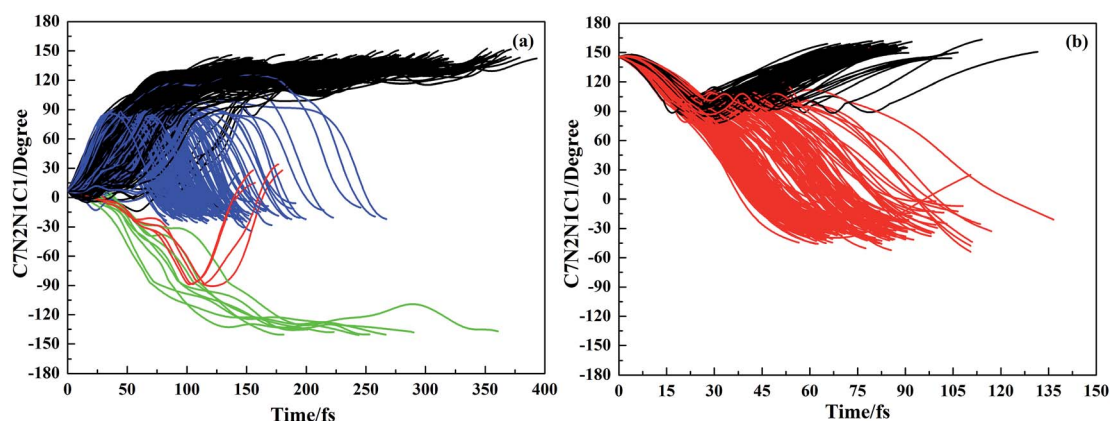


Fig. 4 Time evolution of the C7N2N1C1 dihedral angle along simulated trajectories starting from (a) *cis*-b-Ab and (b) *trans*-b-Ab.

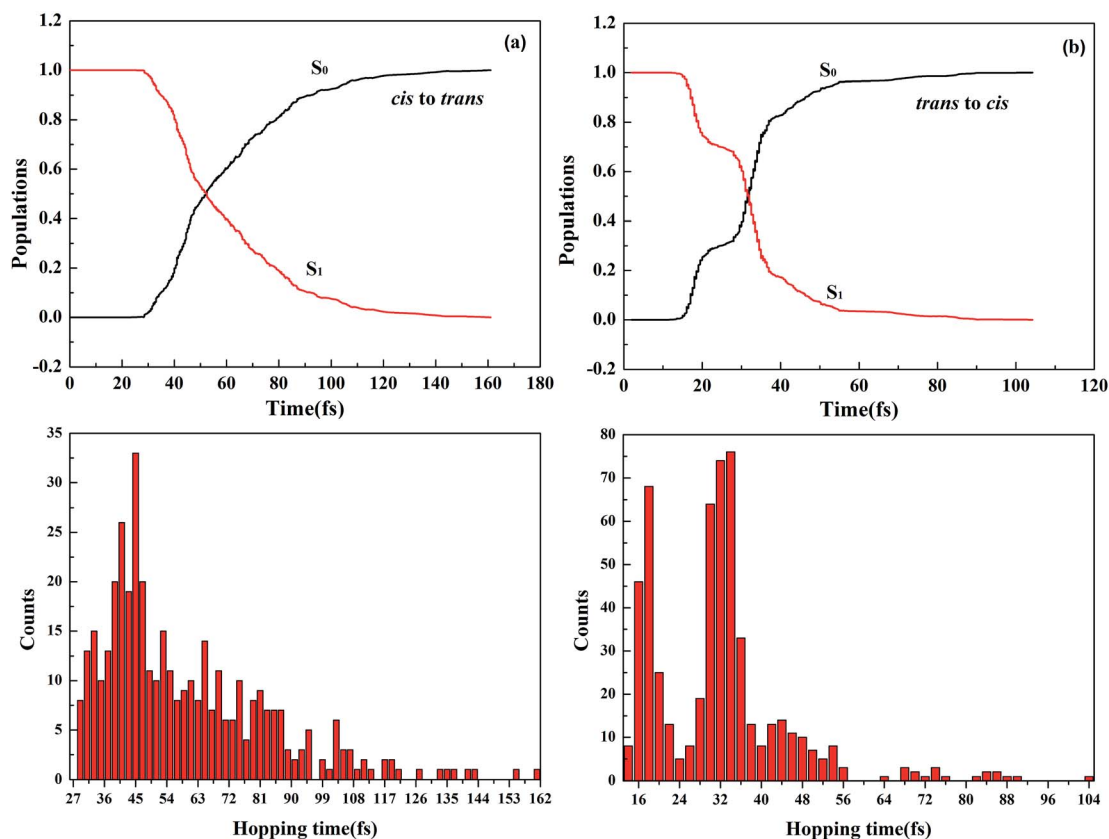
**Table 2** Convergence of simulated quantum yields and lifetimes for the b-Ab photoisomerization in the  $S_1$  state with respect to the number of trajectories in comparison with selected simulations and experimental results

	Number of trajectories	From <i>cis</i> -bridged-azobenzene		From <i>trans</i> -bridged-azobenzene	
		Quantum yield	Lifetime (fs)	Quantum yield	Lifetime (fs)
SA2-CAS(6,5)	35	$0.77 \pm 0.092$	55.5	$0.54 \pm 0.150$	34.5
	100	$0.63 \pm 0.077$	62.0	$0.52 \pm 0.096$	34.0
	150	$0.57 \pm 0.071$	62.5	$0.50 \pm 0.082$	34.0
	200	$0.58 \pm 0.061$	63.5	$0.50 \pm 0.071$	35.0
	250	$0.56 \pm 0.056$	64.5	$0.44 \pm 0.071$	35.5
	300	$0.56 \pm 0.051$	64.0	$0.44 \pm 0.065$	35.5
	350	$0.55 \pm 0.048$	63.5	$0.44 \pm 0.061$	35.0
	400	$0.57 \pm 0.044$	64.0	$0.45 \pm 0.056$	35.0
	450			$0.44 \pm 0.053$	35.5
	500			$0.44 \pm 0.051$	35.5
550			$0.44 \pm 0.048$	35.5	
FOCI-AM <sup>a</sup>	250	$0.23 \pm 0.030$		$0.58 \pm 0.030$	
DFTB <sup>b</sup>	15	0.53 (0.73)		~0.50	
DFTB <sup>c</sup>	65	0.49	~200.0	0.45	
DFT <sup>d</sup>	30	$0.32 \pm 0.050$		$0.47 \pm 0.100$	
CASSCF <sup>e</sup>	35	$0.66 \pm 0.060$	40.4	$0.54 \pm 0.080$	51.3
Expt <sup>f</sup>		$0.72 \pm 0.040$		$0.50 \pm 0.100$	

<sup>a</sup> Ref. 22. <sup>b</sup> Ref. 23. The quantum yield in parenthesis is obtained by exclude the resonance trajectories. <sup>c</sup> Ref. 25. <sup>d</sup> Ref. 26. <sup>e</sup> Ref. 28. <sup>f</sup> Ref. 20.

illustrated in Fig. 5a, in *cis*-to-*trans* isomerization, most of the  $S_1 \rightarrow S_0$  hops happen in the region of 30–100 fs with maximum at 45 fs and therefore give birth to a smooth exponential  $S_1$

population decay curve. In *trans*-to-*cis* isomerization, most of the  $S_1 \rightarrow S_0$  hops occur between 15 and 55 fs with maxima at 18 and 34 fs, respectively. The double peak feature in hopping time



**Fig. 5** Time dependent  $S_1$  and  $S_0$  states' populations (top panel) and distributions of the  $S_1/S_0$  hopping time (bottom panel) for (a) *cis*-to-*trans* and (b) *trans*-to-*cis* isomerization.



distribution result in zigzag  $S_1$  population decay curve, in which the slope decreases in the 20–30 fs region. The periodic interval of  $S_1 \rightarrow S_0$  hopping in *trans-to-cis* process is estimated to be about  $\sim 16$  fs. In each period, the trajectories visit conical region on the  $S_1$  PES and hop to  $S_0$  or remain in the excited state until re-enter the conical region in next period to encounter surface hopping. As seen in Fig. 5b, more hops take place during the second interval, indicates the reverse direction motion (from *cis* side to *trans* side) toward C7N2N1C1 moiety is preferred in photoisomerization started from *trans* b-Ab. Based on the surface hopping algorithm, the motion direction of a trajectory keeps unchanged before and after hop event, and consequently the quantum yields are largely determined by the trajectories'

motion direction toward reactive coordinates at surface hopping points. In *trans-to-cis* process, more trajectories hop to  $S_0$  in the second interval, when the molecule motion direction is the same as that of the first period in *cis-to-trans* process. Considering the higher quantum yields in the *cis-to-trans* isomerization, the *trans-to-cis* isomerization would yield more *trans* products and consequently result in relative lower quantum yields. The maximum of hopping time distribution in *cis-to-trans* process (45 fs) is about 20 fs larger than in the *trans-to-cis* process, (26 fs, average of two peak at 18 and 34 fs) which agrees with the experimental lifetime difference ( $\sim 70$  fs for *cis-to-trans* and  $< 50$  fs for *trans-to-cis*) of Siewertsen *et al.*<sup>20</sup>

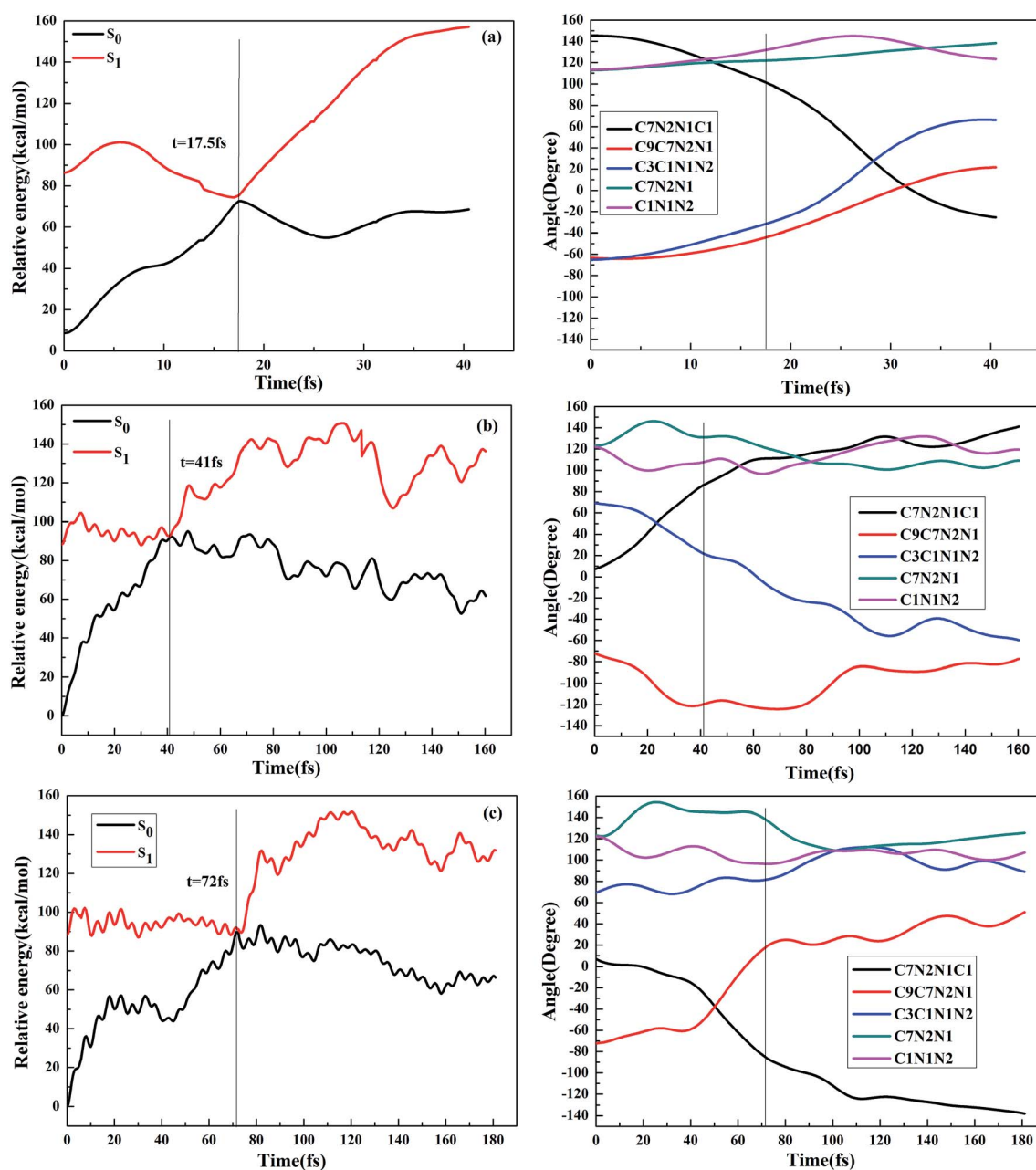


Fig. 6 Time evolution of potential energies of the  $S_1$  and  $S_0$  states and important angles involve in the photoisomerization for (a) *trans* to *cis*, (b) *cis* to *trans* (counterclockwise reactive), (c) *cis* to *trans* (clockwise reactive).

In the current nonadiabatic dynamics simulation, we observe trajectories for the *cis*-to-*trans* isomerization *via* clockwise and counterclockwise route and *trans*-to-*cis* process. Time evolution of potential energies of the  $S_1$  and  $S_0$  states and five important angles involve in the photoisomerization, two NNC bond angles, two CCNN and CNNC dihedral angles, for reactive trajectories are displayed in Fig. 6, while the corresponding nonreactive ones are given in Fig. S1.† Fig. 6a shows a typical reactive trajectory for *trans* → *cis* process, and the most evident conformation change is in C7N2N1C1 dihedral angle. Within the process, the energy of  $S_1$  state increases in the first 5 fs and then decreases to meet the increasing  $S_0$  energy at 17.5 fs and then the surface hopping takes place. Simultaneously, the C7N2N1C1 dihedral angle decrease from  $145^\circ$  to  $\sim 100^\circ$  along with the other internal coordinates increase moderately. After surface hopping, the five angles continue to evolve as prior to hop, therefore, this isomerization process can be attributed to nonsymmetrical torsion toward central eight-membered ring moiety.

The potential energy profile in Fig. 6b for the counterclockwise *cis* → *trans* isomerization is similar to *trans* → *cis* process, where the  $S_1$ - $S_0$  potential energy gap decreases quickly to populate the  $S_1$  →  $S_0$  hop at 41 fs. In the stage prior to surface hopping, the C7N2N1C1 and C3C1N1N2 dihedral angles quickly increase and decrease respectively, while, the C9C7N2N1 decreases to  $-120^\circ$  and oscillates around it. The features of these motions demonstrate the *cis* → *trans* isomerization initiated by pedal-like motion towards the -N=N- bridge and then the other parts that linked to the central eight-membered ring start to transform to *trans* form or back to *cis* form. Moreover, the values of the two NNC angles separated, with one increasing to  $\sim 135^\circ$  and the other one decreasing to  $\sim 115^\circ$ , indicating the participation of NNC inversion in the photoisomerization. Our studies reveal that the counterclockwise *cis* → *trans* isomerization passes through the CI-*cis* conical regions, and therefore confirms the two CI model presented in previous investigations.

Fig. 6c shows a typical trajectory for clockwise *cis* → *trans* isomerization. Within the first 20 fs, the  $S_1$ - $S_0$  potential energy gap decreases fast and then oscillates around  $40 \text{ kcal mol}^{-1}$  until 40 fs. The reason for the peculiar potential energy gap variation is that in the initial stage, the C7N2N1C1 dihedral angle oscillates in the region of  $[-20^\circ, 10^\circ]$  for about 40 fs to achieve the CNNC flip, and then the isomerization procedure starts with C7N2N1C1 quickly decreases to  $-100^\circ$  and C9C7N2N1 increases to  $\sim 20^\circ$ . During this period of  $\sim 30$  fs, the  $S_1$ - $S_0$  potential energy gap decreases quickly again and surface hopping occurs at where the absolute value of those dihedral angles are similar to the ones of *trans* → *cis* isomerization shown in Fig. 6a. The reverse direction CNN change was also observed, which means the assistance of CNN inversion is also required in clockwise *cis* → *trans* isomerization. With the  $\sim 40$  fs trap in the semi-*cis* form, the clockwise *cis* → *trans* channel should possess a rather longer lifetime than the trajectories follow the other two isomerization pathway. Generally, the clockwise *cis* → *trans* isomerization process is also dominated by the nonsymmetrical torsion motion with respect to the azo and ethylenic bridges, while the additional CNN inversion is a promotion.

## 4. Concluding remarks

By employing the recently developed analytical switching probabilities calculation algorithm based on the Zhu-Nakamura theory, we have run trajectory-based nonadiabatic on-the-fly molecular dynamics simulations on the bridged-azobenzene photoisomerization for both *cis*-to-*trans* (400 sampling trajectories) and *trans*-to-*cis* (550 sampling trajectories) at the SA2-CASSCF(6,5)/6-31G quantum chemistry level. With all the simulated trajectories incorporated, the estimated quantum yields and lifetimes converge to 0.57 (0.44) and 64 (35.5) fs for the *cis*-to-*trans* (*trans*-to-*cis*) photoisomerization, respectively, which agree with transient absorption experiment observations and previous dynamics simulation investigations. The enhanced photoresponsibilities of *trans*-b-Ab, such as the higher quantum yields and shorter excited state lifetimes than the parent azobenzene are originated from the steeper PES in the  $S_1$  state, shorter isomerization pathway and favorable non-planar initial structure. Furthermore, the most attractive feature in the azobenzene derivatives is the unusual quantum yields drop upon the  $\pi\pi^*$  excitation,<sup>40–42</sup> which will be the topic of our future investigations.

The *cis* ↔ *trans* photoisomerization of b-Ab was proposed to encounter surface hopping through one or two CI regions *via* twist motion toward central 8-membered ring. The current studies indicated that the *cis*-to-*trans* and *trans*-to-*cis* isomerization proceed *via* different conical regions with respective motion modes toward central N=N related moiety. Which agree with the previous investigations of Carstensen *et al.*<sup>22</sup> and Gao *et al.*,<sup>27,28</sup> by using the CASSCF method. However, it is the main difference between the previous studies<sup>21,23–26</sup> and ours. The other simulation investigations which employing the DFT based methods prefer the model that the *cis*-to-*trans* and *trans*-to-*cis* isomerization are induced by the same conical region<sup>21,23–26</sup> with similar relaxation process in  $S_1$  state as those for two CI model. In the current work, the two types of optimized CIs between  $S_0$  and  $S_1$  states are in *cis*-like and *trans*-like form, which possess rather different twisting angles within the central 8-membered rings except for the CNNC dihedral angles. Most of the trajectories starting from *cis*-b-Ab hop to  $S_0$  *via* the CI-*cis* region, and this isomerization process was initiated by the pedal-like twist of -N=N- moiety and followed by the re-orientation of the other neighboring dihedral angles. While, the *trans*-to-*cis* process is induced by the nonsymmetrical torsion motion toward the central eight-membered ring and encountered surface hopping through CI-*trans* region. We also observed the switch between these two isomerization pathways, which is accompanied with the chirality conversion starting from *cis*-b-Ab. This pathway confirms the existence of chirality change toward CNNC dihedral angle in photoisomerization of *cis*-b-Ab as those reported in parent *cis*-Ab.<sup>6</sup> The trajectory follows this pathway stay in the Franck-Condon region for  $\sim 40$  fs to populate the CNNC flip and then converts to the torsion channel directing to the CI-*trans* region with minus CNNC value. Obviously, the lifetime in excited state for this isomerization channel would be prolonged. In the current simulation,

the ratio of the chirality conversion channel is much smaller than that for the parent azobenzene (0.10–0.22).<sup>6,8</sup> One possible reason is that all trajectories in the current simulation start at the same geometry with different initial velocities. We will perform investigation with better initial condition which considering the influence of zero-point vibration energy in the near future. Moreover, in *trans*-to-*cis* process, the periodic S<sub>1</sub> population decay character was observed with an interval of ~16 fs. The second period, in which the molecule moves along *cis*-to-*trans* direction, occupies more hopping events and therefore results in reduced quantum yields.

## Acknowledgements

H. H. thanks support from the National Science Foundation of China under grant no. 21103136. Y. L. thanks support from the National Science Foundation of China under grant no. 21473134. C. Z. thanks support from the Ministry of Science and Technology of the Republic of China under grant no. 103-2113-M-009-007-MY3 and MOE-ATU project of the National Chiao Tung University. L. Y. thanks support from the Postdoctoral Fellowship by the Ministry of Science Technology of the Republic of China under grant no. 103-2811-M-009-048 and Scientific Foundation of Northwest University under grant no. 338050097.

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