# **Suppression of spatial hole burning in a solidstate laser with the degenerate resonator configuration**

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**Abstract:** Under degenerate resonator configuration and tightly focused pump beam in a linear-cavity solid-state laser, the spatial hole-burning effect can be suppressed. This laser can attain very high intensity in the gain medium due to shrinkage of its beam waist to match the pump beam and therefore most of its gain is depleted even by a standing wave. This was demonstrated by a simulation with spatial dependent rate equations and experiment results of a plano-concave  $Nd:YVO<sub>4</sub>$  laser. The suppression effect was observed up to 20 times the pump threshold.

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#### **1. Introduction**

The single-frequency laser is essential for stable operation of intracavity frequency doubling, precision measurement, high-resolution spectroscopy, and laser trapping or cooling. The most common method of obtaining the single-frequency operation in a homogeneously broadened solid-state laser is to build a traveling wave cavity, usually by means of a ring cavity together with an intracavity optical diode, so as to prevent the spatial hole-burning effect. To acquire single-frequency operation in a linear cavity, other ways are required to diminish the spatial hole-burning effect. For example, a twisted mode technique [1] had been proposed to achieve axially uniform energy density in the laser cavity. In addition, the mechanisms of Auger upconversion and energy diffusion in the laser crystal were also employed to reduce the spatial hole-burning effect [2-4].

Recently, it was shown that a plano-concave cavity with the degenerate resonator configuration could support more or less arbitrary beam distribution. Under tightly focused pump beam, the laser exhibited the shrinkage of beam waist and the lower pump threshold than the neighboring configurations [5, 6]. In this Article, we report a novel way by employing the degenerate resonator configuration to relief the spatial hole-burning effect. Because the laser with a degenerate resonator configuration is capable of self-adjusting the mode distribution to match the small pump beam, very high intensity is able to attain in the gain medium of this laser. Most of the gain, therefore, can be depleted even by a standing wave. The spatial hole-burning effect is then effectively suppressed. This was numerically simulated in terms of a spatial dependent rate equation and experimentally demonstrated by using a Nd:YVO<sub>4</sub> laser. The Nd:YVO<sub>4</sub> laser crystal has high absorption coefficient which is a merit for single-frequency operation in a standing-wave cavity, but the pump power is usually limited to slightly above the threshold [7]. Our method, however, is capable of suppressing the spatial hole-burning effect up to 20 times the pump threshold.

#### **2. Theoretical model and simulation**

In order to investigate the spatial hole-burning effect in a plano-concave  $Nd:YVO<sub>4</sub>$  laser, we employ a spatial dependent rate equation. By taking into account both the Auger upconversion and energy diffusion effects, the rate equation for the density of population inversion  $N(z)$  in an ideal four-level system can be expressed as  $[2, 4, 8]$ 

$$
\tau \frac{\partial}{\partial t} N(z) = \tau R(z) - \left(1 + \frac{I(z)}{I_s}\right) N(z) + \tau D\left(\frac{\partial^2 N(z)}{\partial z^2}\right) - A \tau N^2(z),\tag{1}
$$

where z is the cavity axis with  $z = 0$  at the flat mirror,  $R(z)$  is the pump rate,  $I_s$  is the saturation intensity,  $\tau$  is the spontaneous emission lifetime, *D* is the diffusion constant, and *A* is the Auger upconversion coefficient. Assuming a low roundtrip loss in the plane wave approximation, we can write the intensity  $I(z)$  of standing wave as

$$
I(z) = 4I_0 \sin^2(kz) , \qquad (2)
$$

where  $k$  is the propagation number and  $I_0$  is the average intracavity intensity. Because we do not consider the radial effect in Eq. (1), the pump rate can be written as

$$
R(z) = \frac{P_p}{h\nu \times \pi w_p^2} \times \frac{e^{-\alpha z}}{\alpha},
$$
\n(3)

where  $P_p$  is the incident pump power, *h* is the Planck's constant, *v* is the pump frequency,  $w_p$ is the pump size, and  $\alpha$  is the absorption coefficient at pump wavelength. Under the steadystate condition, we substituted Eqs.  $(2)$  and  $(3)$  into  $(1)$ , and numerically solved the equation by the Newton's method to obtain the spatial profile of *N*(z). The Auger upconversion

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coefficient  $A = 3x10^{-21}$  m<sup>3</sup>/s [4, 8], diffusion constant  $D = 0.7x10^{-11}$  m<sup>2</sup>/s [4], absorption coefficient  $\alpha = 31.4$  cm<sup>-1</sup>, and saturation intensity  $I_s = 1.19 \times 10^7$  J/(m<sup>2</sup>s) are used in our simulation.

Usually the laser is expected to operate at the single longitudinal mode when the pump power is just above the threshold. From the Ref. 7, we estimate that the second longitudinal mode would begin to oscillate at  $\gamma = 1.78$  where  $\gamma$  is the ratio of pump power to laser threshold, therefore, we will discuss the numerical results using the pump power around  $\gamma = 1.78$ . Because the thickness of the laser crystal is less than the Rayleigh parameter of the pump beam, we assume that the pump size  $w_p$  is constant throughout the crystal. When a laser operates in the vicinity of  $g_1g_2 = 1/4$  with a curve mirror of 8-cm curvature, the radius of the fundamental transverse mode is about 108µm. It corresponds to Rayleigh parameter of about 34 mm which is much longer than the length of gain medium of 1 mm. In addition, the plane wave assumption is adequate for a beam with or close to Gaussian profile. Note that the laser beam spot in vicinity of flat mirror (gain medium) is almost equal to the pumping size of  $w_p$  = 20 µm and similar to Gaussian profile [5] when it is operated with the degenerate resonator configuration under tightly-focused pumping. The plane wave assumption in Eq. (2) is still valid even with the high-order Laguerre-Gaussian mode up to  $LG_{12,0}$ , whereas, the shrinkage of beam spot can be observed at the degeneracy with only a superposition of  $LG_{00}$  and the lowest degenerate mode, e.g.,  $LG_{3,0}$  for  $g_1g_2=1/4$  [13].

Figure 1(a) is the spatial profile of N(z) for a laser operated at cavity length  $L = 6.06$ -cm which is a typical example of population inversion in a standing wave resonator. It only burns a small hole of  $N(z)$  at anti-node of standing wave and leaves a lot of gain for the second longitudinal mode. The horizontal dash line in this figure stands for the threshold population inversion which is equal to the pump power of 33 mW, the solid and dash curves respectively show *N*(z) for the laser operating at  $\gamma_c = 1.5$  and  $\gamma_c = 2.4$  where the subscript c denotes the conventional cavity. To allow the second mode to oscillate ( $\gamma_c$  > 1.78), the residual population inversion should higher than that for the laser operating at  $\gamma_c = 1.5$  as shown in Fig. 1(a).



Fig. 1 Numerical spatial distribution of steady-state upper level density to show influence of spatial hole-burning effect. The normalized pumping  $\gamma$  (to the threshold) for both of the conventional laser operated at  $\bar{L}$ =6.06cm (a) and bottle beam laser at  $g_1g_2=1/4$  (b).

If we operate the laser at the degenerate resonator configuration where  $g_1g_2 = 1/4$  (L = 6.0) cm), good overlapping between the pumping and the laser beam will result in a lower laser threshold which equals to  $15mW$ . The beam radius will be about 20  $\mu$ m which approximates to the size of pump. The intracavity intensity at the beam waist  $(z = 0)$  is about 29 times higher than that of the laser with the conventional cavity ( $L = 6.06$ -cm). Because of the very high intracavity intensity, there leaves only a little residual population inversion above the threshold which is located around the node of the standing wave, as shown in Fig. 1(b). The horizontal dash line again stands for the threshold population inversion. In addition, other

(C) 2005 OSA 7 March 2005 / Vol. 13, No. 5 / OPTICS EXPRESS 1681 #6502 - \$15.00 US Received 31 January 2005; revised 25 February 2005; accepted 25 February 2005 longitudinal modes could have significant access to the residual inversion only if they had at least  $\pi/2$  phase shift relative to the first mode [7]. Two lasing frequencies, which is in-phase at beginning, will possess  $\pi/2$  phase difference after propagating a dephasing length. Usually the first lasing mode in a homogeneously broadened gain medium is located near the center of gain profile, and the shortest dephasing length is provided by the maximum frequency difference. So we used half of bandwidth to estimate the shortest dephasing length to be 700µm. This implies that the other longitudinal mode needs more than 2.3 times absorption depth of Nd:YVO<sub>4</sub>, which is reciprocal of absorption coefficient  $\alpha$ , to extract enough residual gain to oscillate. From Fig. 1(b), we see that the residual population inversion for  $\gamma_d = 1.5$ , where the subscript d denotes the degenerate cavity, is too small to allow the oscillation of the second mode. Nevertheless, for  $\gamma_d = 2.4$  or even higher pump power, because higher residual population inversion occurs at node of the standing wave the second mode still can not obtain the sufficient gain. In addition, it is worth to mention that by neglecting the energy diffusion and Auger upconversion effects, the last two terms of the right-hand side of Eq. (1), we still obtained the similar numerical results of Fig. 1(b). This means that the effects of Auger upconversion and the energy diffusion are negligible and can be ruled out in our case. Therefore, we conclude that the laser with the degenerate resonator configuration is capable of suppressing the spatial hole-burning effect by means of gain saturation through the very high intensity in the gain medium.

## **3. Experimental setup and results**

The experiment is performed in a  $Nd:YVO<sub>4</sub>$  laser with a plano-concave cavity. The detail setup is similar to that described in Ref. 5. A 1-mm thick  $1\%$  Nd:YVO<sub>4</sub> crystal is used as the gain medium. The crystal facet faced toward the pumping beam has a dichroic coating of high transmission 808 nm pump wavelength as well as high reflection at 1064 nm laser wavelength and is served as the flat mirror. The other facet is antireflection coated at 1064 nm to avoid the effect of intracavity etalons. A curve mirror with radius of curvature  $R_c = 8$ cm and 10% transmission at 1064 nm is employed as the output coupler. It is mounted on a translational stage so that we can adjust the cavity length L and equivalently change the resonator configuration. The pump source is a cw Ti-sapphire laser operated with a nearly  $TEM_{00}$  mode. We place a lens with different focal lengths in front of the crystal to adjust the pumping spot size. A photodetector (rise time < 0.3 ns) together with a RF spectrum analyzer (HP8560E, bandwidth 2.9 GHz) was used for measuring the mode beating and the relaxation oscillation. The optical spectrum was measured by using a Fabry-Perot interferometer (FPI, Burleigh) having finesse > 150 corresponding to a spectral resolution of 100 MHz for a 15 GHz free spectral range (FSR). In addition, the pump size determined by the standard knifeedge method is 20  $\mu$ m, which is less than one-fifth of the waist radius (108  $\mu$ m) of the cold cavity mode. The cavity length corresponding to the degenerate resonator configuration is determined by minimum pump threshold [6]. In this experiment, we operated the laser around the  $1/3$ -degeneracy ( $L = 6$  cm) where corresponds to the longitudinal mode spacing of about 2.4 GHz.

Figure 2 shows a typical single-frequency optical spectrum measured by FPI when the laser is operated at  $\gamma$  < 1.8 (~ 1.78) in the conventional cavity configuration (L = 6.06 cm). The second longitudinal mode appears when the  $\gamma_c = 1.8 > 1.78$  (threshold is 33 mW). The experiment observation agrees well with the theoretical estimation according to the Ref. 7. Figure 3 (a) and (b) respectively show the FPI and the RF spectra for  $\gamma_c = 2.7$  (pumping power  $P_p = 90$  mW). We can clearly see the second longitudinal mode and the beating from these two longitudinal modes. As the pump power increases to over 133 mW ( $\gamma_c = 4$ ), we found that an extra lasing mode appears at 1.1 GHz away from the main features of the FPI spectrum but no corresponding mode beating can be detected by the RF spectrum analyzer. Therefore, we suspected that the spectral spacing of these two lasing modes is larger than the bandwidth of the RF spectrum analyzer (2.9 GHz). Indeed, when the FPI with larger FSR (150 GHz or even 300 GHz) is used, the measured mode spacing becomes 40 GHz.

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Fig. 2 Single frequency optical spectrum of the Fabry-Perot interferometer with FSR = 15 GHz when the pumping is set below 1.8 times threshold.



Fig. 3 Typical multiple optical frequency and corresponding RF spectrum for the common laser at L=6.06cm. (a) The Fabry-Perot interferometer shows two longitudinal lasing modes with spacing of about 2.42 GHz and (b) the beat frequency of two longitudinal modes measured by the RF analyzer.

On the other hand, as the cavity is adjusted to the degenerate resonator configuration ( $L =$ 6 cm), the single frequency operation is observed, as shown in Fig. 2, for the pump power as high as 30 mW. By raising the pump power to above 30 mW ( $\gamma_d$  = 2), we found that the second mode appear in the FPI spectrum which is located 58.6 GHz away from the first mode rather than ~2.4 GHz. The next nearest neighboring longitudinal mode is not observed even the pumping power increases as high as we can. The FPI and the corresponding RF spectrum at P<sub>p</sub> = 310 mW or  $\gamma_d \sim 20$  are shown in the Fig. 4(a) and (b) respectively. The inset of Fig. 4(b) shows that there is neither longitudinal nor transverse mode beating within the bandwidth of the RF spectrum analyzer, the arrow in this figure shows only one relaxation oscillation peak (2.4 MHz) existing in the RF spectrum. Someone may doubt whether the mode spacing of 58.6 GHz comes from the intracavity etalon effect. However, the etalon mode spacing is 72 GHz in this experiment; and there is an antireflection coating at  $1064$  nm on the Nd:YVO<sub>4</sub> facet to avoid the effect of intracavity etalons.

As the simulated results discussed above, the laser with the degenerate resonator configuration is able to deplete most of the population inversion in a homogeneous broadened gain medium. We therefore expect that the second mode 58.6 GHz away from the first mode may have different origin of emission or arise from different manifold of transition (sub-peak of inhomogeneous gain profile). Similarly, the sub-peak of the gain profile will also result in the occurrence of the second mode in the conventional cavity at higher pump power, which is 40 GHz away from the first mode. In the  $Nd:YVO<sub>4</sub>$  crystal, the crystal field interaction gives rise to the Stark splitting at the satellite of  ${}^{4}F_{3/2}$ ,  ${}^{4}I_{9/2}$ , and  ${}^{4}I_{11/2}$  [9]. Under high-resolution absorption and luminescence studies, it was found that the satellite energy of  ${}^{4}F_{3/2} \rightarrow {}^{4}I_{9/2}$ transition depended on the  $Nd^{3+}$  concentration [10]. The lasing transition around 1064 nm is attributed to <sup>4</sup>F<sub>3/2</sub>  $\rightarrow$  <sup>4</sup>I<sub>11/2</sub>. It contains two closely transitions R<sub>1</sub>  $\rightarrow$  Y<sub>1</sub> and R<sub>2</sub>  $\rightarrow$  Y<sub>2</sub> with frequency difference of 90 GHz under 2%  $Nd^{3+}$  doping and 21 GHz under 0.56%  $Nd^{3+}$  doping [11, 12]. The doping concentration used in our experiment is 1%, it is quite reasonable to obtain the frequency difference of  $\sim$ 42 GHz by simple interpolation. The frequency

(C) 2005 OSA 7 March 2005 / Vol. 13, No. 5 / OPTICS EXPRESS 1683 #6502 - \$15.00 US Received 31 January 2005; revised 25 February 2005; accepted 25 February 2005 difference which is estimated by interpolation is in good agreement with our observation in the conventional laser cavity. Note that because the second mode has a frequency more than 40 GHz away from the first mode, it would be easily filtered out, for example, by a grating with 1800 grooves. In principle, it is possible to design a cavity that delivers the same tight beam size in a fundamental  $TEM_{00}$  mode and achieve the same effect. However, such a cavity is usually operating close to the edge of stability and needs to accurately adjust the cavity length according to the spot size of the pump beam. Our scheme, in contrast, is operated within the stability region away from the edge of stability. Without knowing the pump beam size in advance, the laser with a degenerate resonator configuration can self-adjust the mode distribution to match the small pump beam and as a result the spatial hole-burning effect is suppressed.



Fig. 4 Multiple optical frequency and corresponding RF spectrum under 310mW pumping at  $g_1g_2=1/4$ . (a) The FPI spectrum shows mode spacing of about 58.6GHz but without longitudinal beating of 2.42 GHz or transverse mode beating in the RF spectrum in (b). An arrow points out the peak due to relaxation oscillation.

### **4. Conclusion**

We have theoretically shown and experimentally demonstrated that the spatial hole-burning effect can be suppressed by using a plano-concave cavity with degenerate resonator configuration under a tightly focusing pump beam. It not only has the merits of the lowest threshold and stable output but also is independent of the gain medium. The same resonator configuration has been employed to generate the multiple beam waists and the optical bottle beam [13, 14], it has potential applications for trapping atoms in the dark field if the proper gain medium is chosen to generate blue-detuned single frequency laser beam.

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