

## Orbital polarization of the unoccupied states in multiferroic $\text{LiCu}_2\text{O}_2$

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Using measurements of polarization-dependent soft-x-ray absorption and band-structure calculations including the on-site Coulomb interaction, we investigated the symmetry of the intrinsic  $3d$  holes in the low-dimensional quantum magnet  $\text{LiCu}_2\text{O}_2$  with edge-sharing spin chains. The Cu  $L$ -edge and O  $K$ -edge measurements with in-plane and out-of-plane  $\mathbf{E}$  vectors of x ray reveal the orbital character of the valence states of Cu on different sites. The unoccupied  $3d$  states of nominal  $\text{Cu}^{2+}$  exhibit predominantly  $xy$  symmetry, whereas  $3d$  holes of  $3z^2-r^2$  symmetry reside on the nominal  $\text{Cu}^+$  sites. Both the experimental observations and theoretical calculations agree on the hybridization of the O  $2p$  and Cu  $3d$  states above the Fermi level. The existence of  $3d$  holes on  $\text{Cu}^+$  enhances the interlayer magnetic coupling.

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### I. INTRODUCTION

Low-dimensional quantum spin systems with geometric frustration have attracted much attention for decades. One-dimensional  $\text{CuO}$  chains with a Cu-O-Cu bond angle of  $180^\circ$  as found in  $\text{Sr}_2\text{CuO}_3$  and  $\text{SrCuO}_3$  are antiferromagnets which exhibit strong quantum spin fluctuations. Similarly, compounds of edge-sharing  $\text{CuO}_2$  chains with the Cu-O-Cu bond angle of about  $90^\circ$  such as  $\text{LiCu}_2\text{O}_2$  are frustrated magnets because of competition between ferromagnetic (FM) and antiferromagnetic (AFM) exchanges and, thus, exhibit rich magnetic phases.  $\text{LiCu}_2\text{O}_2$  is also important for studying interesting spin-lattice interaction, magnetic ordering, quantum spin correlations, and specific heat of a spin- $\frac{1}{2}$  quantum antiferromagnet with spin spirals.<sup>1-6</sup> Its low dimensionality and quantum spin fluctuations lead to profound and intriguing effects on magnetic and electronic properties. For example, Pisarev *et al.*<sup>7</sup> observed an anomalous optical spectral feature which thoroughly disagrees with *ab initio* calculations. Masuda *et al.*,<sup>1</sup> using neutron diffraction, found that the spin structure of  $\text{LiCu}_2\text{O}_2$  is helimagnetic. Local-density-approximation-based calculations of exchange integrals also reveal a large in-chain frustration leading to a spin spiral.<sup>2</sup> Based on data of angle-resolved photoemission and optical measurements, Papagno *et al.*<sup>3</sup> suggested a one-dimensional scenario of strongly correlated antiferromagnetic insulators for  $\text{LiCu}_2\text{O}_2$ ; however, results of soft-x-ray magnetic scattering by Huang *et al.*<sup>4</sup> imply a quasi-two-dimensional magnetic order.

Recently,  $\text{LiCu}_2\text{O}_2$  has been found to be a member of cuprate multiferroics in which magnetism and ferroelectricity coexist and ferroelectric polarization can be reversibly flipped with an applied magnetic field.<sup>5,6,8,9</sup> Of particular interest is how the induced electric polarization by magnetism can survive out of quantum fluctuations. The magnetic structure in the ferroelectric ground state of  $\text{LiCu}_2\text{O}_2$  is still

perplexing.<sup>5,6,10-12</sup> Density-functional calculations of electric polarizations by Xiang and Whangbo<sup>10</sup> show that the observed spin-spiral plane is inconsistent with the observed direction of the electric polarization. In addition, Moskvin and Drechsler<sup>11</sup> concluded that, in the scenario of spin current, the induced polarization due to two consecutive  $\text{CuO}_4$  plaquettes along the chain gets canceled exactly, and the  $c$ -axis coupling of spins are essential for the observed multiferroicity,<sup>12</sup> supported by measurements of soft-x-ray magnetic scattering.<sup>4</sup>

$\text{LiCu}_2\text{O}_2$  also represents a useful starting point to obtain basic information relevant to complex behavior displayed by transition-metal compounds. It is a mixed-valence compound with a layered orthorhombic crystal structure of the space group  $Pnma$  ( $Z=4$ ), lattice parameters  $a=5.72$  Å,  $b=2.860$  Å, and  $c=12.399$  Å. This compound has an equal number of nominal  $\text{Cu}^{2+}$  and  $\text{Cu}^+$  oxidation states.  $\text{Cu}^{2+}$  ions are magnetic and located at the center of the square base of a fivefold oxygen pyramid with an apical oxygen. Quasi-one-dimensional chains of magnetic order develop along the  $b$  axis with  $\text{CuO}_4$  plaquettes in which the Cu-O-Cu bonding angle is  $94^\circ$ . Two adjacent  $\text{Cu}^{2+}$  ions in the  $\text{CuO}_4$  plaquette are labeled as Cu(3) and Cu(4), as shown in Fig. 1. Double layers of  $\text{Cu}^{2+}$  stack along the  $c$  direction with intervened layers of nonmagnetic  $\text{Cu}^+$  ions, which are labeled as Cu(1) and Cu(2). This edge-sharing cuprate  $\text{LiCu}_2\text{O}_2$  is a unique and simple model system for testing theories of spin correlations in frustrated quantum magnets.

Revealing the underlying mechanism of physical properties of  $\text{LiCu}_2\text{O}_2$  such as quantum multiferroic features requires a full understanding of the electronic structure involved with magnetic coupling, particularly the orbital polarization and the  $p$ - $d$  hybridization in the unoccupied states. Several experiments and theories indicate that  $\text{LiCu}_2\text{O}_2$  exhibits strong electron-hole correlations of coppers on different sites<sup>7</sup> and that  $\text{Cu}^{2+}$  possesses characteristics of  $p$ - $d$  hybridization in the  $ab$  plane. In contrast, non-

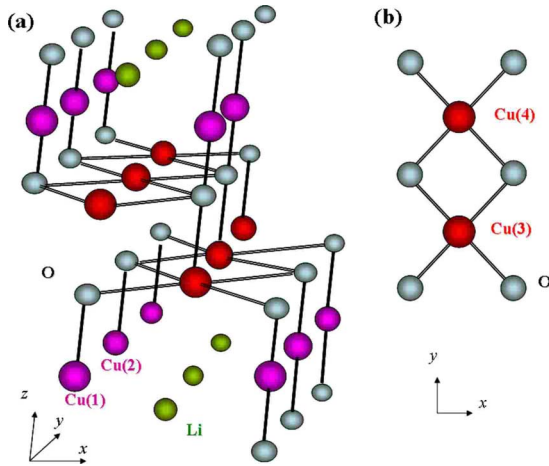


FIG. 1. (Color online) (a) Illustration of the crystal structure of  $\text{LiCu}_2\text{O}_2$ . Cyan balls stand for oxygen. Li ions are denoted by green balls. Purple and red balls represent the monovalent and divalent copper ions, respectively. (b) Two-dimensional (2D) view of the edge-sharing chain along the  $y$  axis, i.e., the  $b$  axis. Adjacent  $\text{Cu}^{2+}$  ions along the chain are labeled Cu(3) and Cu(4);  $\text{Cu}^+$  ions are labeled Cu(1) and Cu(2) which bridge the double layers of  $\text{Cu}^{2+}$ .

magnetic ions  $\text{Cu}^+$  in the linear bonding of O-Cu-O along the  $c$  axis are expected to exhibit fully occupied  $3d$  orbitals.<sup>3,7,13</sup>

X-ray absorption spectroscopy (XAS) provides information on the symmetry of the unoccupied electronic states. The absorption cross section of x ray depends on the direction of the  $\mathbf{E}$  vector with respect to the crystallographic orientations and the orbital orientation of unoccupied electronic states of transition-metal  $3d$  and oxygen  $2p$ . XAS with linearly polarized x ray yields a characterization of the orbital orientation of the unoccupied states.<sup>14,15</sup> Here, we present measurements of polarization-dependent Cu  $L$ -edge and O  $K$ -edge XAS to understand the electronic structure derived from  $\text{Cu}^{2+}$  and  $\text{Cu}^+$ . Band-structure calculations in the scheme of generalized gradient approximation (GGA) (Ref. 16) with the on-site Coulomb interaction  $U$  taken into account,<sup>17</sup> i.e., GGA+ $U$  calculations, are also presented to interpret the XAS results. We discuss the orbital polarization of unoccupied electronic states derived from  $\text{Cu}^{2+}$  and  $\text{Cu}^+$ .

## II. EXPERIMENTAL

Single crystals of  $\text{LiCu}_2\text{O}_2$  were grown by the floating zone technique in which the oxygen atmosphere was well controlled to stabilize the  $\text{LiCu}_2\text{O}_2$  phase by reducing the Cu loss that occurs typically in the growth by the self-fluxing technique.<sup>1</sup> Characterization of x-ray diffraction indicates that the  $\text{LiCu}_2\text{O}_2$  samples exhibit a good crystalline structure and are free of impurity phases such as  $\text{Li}_2\text{CuO}_2$ ,  $\text{LiCu}_3\text{O}_3$ , and CuO. The x-ray Laue pattern shows that (not shown here) the crystals were discovered to be twinned at  $[110]$  plane with a mixing of the  $a$ - and  $b$ -axis domains as observed previously in the literature.<sup>1,4–6,18</sup>

Polarization-dependent x-ray absorption spectra were recorded at the Dragon (11A1) beamline of the National Synchrotron Radiation Research Center (NSRRC) in Taiwan. To

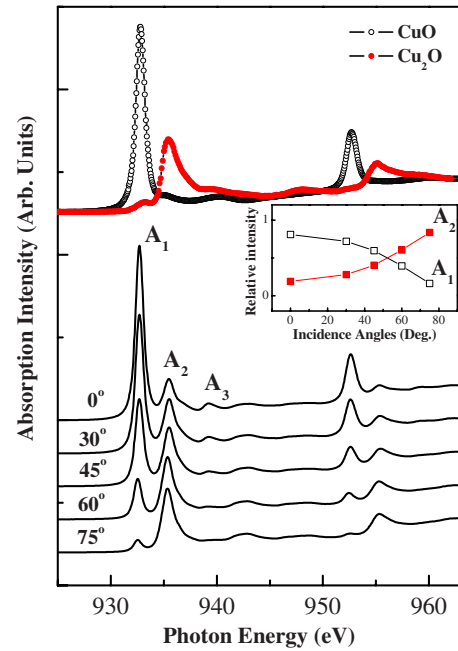


FIG. 2. (Color online) XAS spectra of Cu  $2p_{3/2}$  ( $L_3$ ) and  $2p_{1/2}$  ( $L_2$ ) absorption edges of  $\text{LiCu}_2\text{O}_2$  for different orientations of the  $\mathbf{E}$  x ray.  $\theta$  is the incidence angle between the incident photon beam and the surface normal  $\hat{c}$  of crystal, i.e., the crystallographic  $c$  axis. The origins of XAS features  $A_1$ ,  $A_2$ , and  $A_3$  are discussed in the text. The inset shows the relative intensities of  $A_1$  and  $A_2$  as a function of  $\theta$ .

obtain XAS spectra containing the evolution from  $\mathbf{E} \perp \hat{c}$  to  $\mathbf{E} \parallel \hat{c}$ , we measured XAS of Cu  $L$  and O  $K$  edges with the total electron yield method under various incidence angles  $\theta$  between the incident photon beam and the surface normal  $\hat{c}$  of crystal, i.e., the crystallographic  $c$  axis. The energy resolutions are 0.15 and 0.4 eV in the O  $K$ -edge and Cu  $L$ -edge regions, respectively. All XAS measurements of different crystal orientations are normalized to have an equal XAS intensity at 40 and 70 eV above the Cu  $L$  and O  $K$  edges, respectively. Standard oxide powders of CuO and  $\text{Cu}_2\text{O}$  are used for energy calibration and also for comparing different electronic valence states.

## III. RESULTS AND DISCUSSION

Figure 2 shows Cu  $L$ -edge XAS spectra obtained with various incidence angles  $\theta$ . The spectra stem from excitations of a core electron in the  $2p_{1/2}$  or  $2p_{3/2}$  manifold to the unoccupied  $3d$  state, i.e., transitions from a ground state of  $2p^6 3d^n$  to an excited electronic configuration of  $2p^5 3d^{n+1}$  with different multiplet excitations. As a result of spin-orbit coupling in the  $2p$  state, the spectra display two prominent features in the energy ranges of 931–939 and 951–959 eV, respectively, corresponding to the  $L_3$  ( $2p_{3/2} \rightarrow 3d$ ) and  $L_2$  ( $2p_{1/2} \rightarrow 3d$ ) absorptions. Because of the change in the incidence angle, Fig. 2 provides the evolution of XAS with the electric-field vector  $\mathbf{E}$  from being parallel to being perpendicular to the  $c$  axis. Two main anisotropic peaks marked as  $A_1$  and  $A_2$  dominate the features of spectral evolution about

the  $L_3$ -edge absorption. Comparing the divalent and monovalent oxidation states of Cu with different symmetries, one can identify the valence states from the evolution of the absorption spectra. The ground state of the nominal  $\text{Cu}^{2+}$  is a hybridization of  $3d^9$  and  $3d^{10}\bar{L}$ , where  $\bar{L}$  denotes a hole in the O  $2p$  valence band, i.e., the  $2p$  ligand hole. The sharp peak  $A_1$  centered at photon energy 932.7 eV in the  $L_3$ -edge absorption arises from the  $2p^63d^9 \rightarrow 2p^53d^{10}$  transition of  $\text{Cu}^{2+}$ , such as that of  $\text{Cu}^{2+}$  in  $\text{CuO}$ .<sup>19</sup> The effective screening by the core-hole potential in the XAS final state gives rise to the observed sharp resonance of  $A_1$ . On the contrary,  $A_2$  stands out in the XAS geometry close to  $\mathbf{E} \parallel \hat{c}$  at an energy almost identical to that of  $\text{Cu}^+$  in  $\text{Cu}_2\text{O}$  which exhibits a combination of  $3d^{10}$ ,  $3d^94s^1$ , and  $3d^{10}4s^1\bar{L}$  in the ground state.<sup>19–21</sup> Such a broad feature of  $A_2$  originates from a  $d^9$ -like ground state. A weak feature of  $A_3$  also appears at 939.2 eV, as a contribution from the  $3d^{10}\bar{L}$  configuration in the ground state, which has the  $p_{x,y}$  bonding state.<sup>22,23</sup>

Our XAS data show that the ground state of  $\text{Cu}^+$  contains the electronic configuration  $3d^94s^1$ . This observation of  $3d$  hole  $\text{Cu}^+$  does not result from a nonstoichiometric effect. Masuda *et al.*<sup>1</sup> found that a chemical disorder and a Cu deficiency are inherently present in  $\text{LiCu}_2\text{O}_2$ . The excess  $\text{Li}^+$  ions occupy  $\text{Cu}^{2+}$  sites due to a good match of ionic radii. The charge compensation requires that the introduction of  $\text{Li}^+$  ions into the double chains of  $\text{Cu}^{2+}$  is accompanied by a transfer of the holes onto the  $\text{Cu}^+$  interchain sites. However, the energy of the observed XAS feature in  $A_2$  coincides with that of the nominal  $\text{Cu}^+$  in  $\text{Cu}_2\text{O}$  rather than the divalent  $\text{Cu}^{2+}$  in  $\text{CuO}$ . XAS results hence indicate that intrinsic  $3d$  holes do exist on the nominal  $\text{Cu}^+$  sites regardless of nonstoichiometry, in contrast to the intuitive expectation of  $3d^{10}$  configuration.

The polarization-dependent XAS measurements reveal that, when the absorption geometry evolves from  $\mathbf{E} \perp \hat{c}$  toward  $\mathbf{E} \parallel \hat{c}$ , the intensity of  $A_1$  decreases, whereas the XAS feature of  $A_2$  is enhanced strongly, as further illustrated in the inset of Fig. 2. The intensity of  $A_3$  also gradually decreases as the absorption geometry changes accordingly. These XAS data thus show that the unoccupied  $3d$  state on  $\text{Cu}^{2+}$  has an in-plane orbital polarization. In other words, the evolution of  $A_1$  unravels the in-plane character of the unoccupied  $3d_{xy}$  orbital of  $\text{Cu}^{2+}$  in the  $\text{CuO}_4$  plaquettes running along the  $b$  axis. The feature of  $A_2$ , on the other hand, is dominated by the  $z$  character from the  $d^9$ -like ground state of  $\text{Cu}^+$  as confirmed by the O  $K$ -edge spectra that will be discussed later. In addition, the XAS feature of  $A_2$  remains finite even with  $\mathbf{E} \perp \hat{c}$ , such as that of  $\text{Cu}_2\text{O}$  in which the XAS final state is mainly of  $2p^53d^{10}4s^1$ . These spectra therefore indicate that the observed peak  $A_2$  consists of two transitions which reach the XAS final state of  $\text{Cu}^+$ . First, there occurs a transition of  $2p^63d^94s^1 \rightarrow 2p^53d^{10}4s^1$  involved with a  $3d_{3z^2-r^2}$  hole in the ground state. The other is the  $2p^63d^{10} \rightarrow 2p^53d^{10}4s^1$  transition in which the XAS intensity is independent of the orientation of  $\mathbf{E}$  because of the isotropic nature of the  $4s$  state.

To further understand the orbital symmetry of  $3d$  states in  $\text{LiCu}_2\text{O}_2$ , we performed GGA+ $U$  (Ref. 17) electronic structure calculations. Coulomb energy  $U=4.5$  eV and exchange parameter  $J=0.9$  eV for all Cu atoms were adopted. We

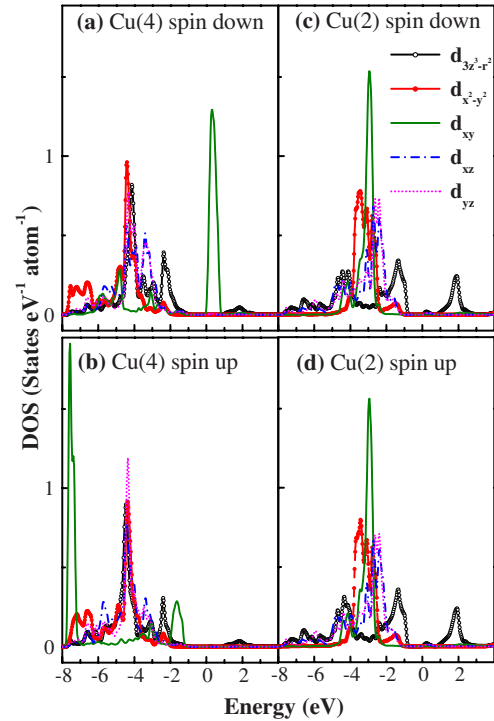


FIG. 3. (Color online) Density of states of  $\text{LiCu}_2\text{O}_2$  in the antiferromagnetic state obtained from GGA+ $U$  band-structure calculation. (a)–(d) are plots of the  $d$ -decomposed DOS of Cu on different sites. The  $E_F$  is located at the energy equal to zero in all the spectra.

used the highly accurate all-electron full-potential linearized augmented plane-wave (FLAPW) method, as implemented in WIEN2K package.<sup>24</sup> The experimental structural parameters with lattice constants  $a=5.7260$  Å,  $b=2.8587$  Å, and  $c=12.4137$  Å (Ref. 25) were used. We considered the simple collinear AFM structure with the  $1 \times 2 \times 1$  supercell and found that the AFM  $\text{LiCu}_2\text{O}_2$  is a semiconductor with a band gap of 0.94 eV. As expected,  $\text{Cu}^+$  ions [Cu(1) and Cu(2)] have a negligible spin magnetic moment ( $<0.001\mu_B/\text{atom}$ ). Nevertheless,  $\text{Cu}^{2+}$  ions [Cu(3) and Cu(4)] have a spin magnetic moment of  $\sim 0.65\mu_B/\text{atom}$  (not  $\sim 1.0\mu_B/\text{atom}$ ), in agreement with previous LSDA+ $U$  calculations.<sup>13</sup>

Figure 3 plots the decomposed partial density of states (DOS) of  $\text{Cu}^{2+}$  and  $\text{Cu}^+$  on different Cu sites from GGA+ $U$  calculations. Figures 3(a) and 3(b) show the calculated spin-down and spin-up DOSs of Cu(4) for divalent  $\text{Cu}^{2+}$ , respectively; Figs. 3(c) and 3(d) show the spin-down and spin-up DOSs for monovalent  $\text{Cu}^+$ , respectively. Note that the spin-up DOS of Cu(4) and spin down of Cu(3) are identical because of the antiferromagnetic order set in the calculations. The calculations indicate that  $\text{Cu}^{2+}$  on the Cu(4) sites has a spin-down  $3d_{xy}$  state at 0.32 eV above the Fermi level ( $E_F$ ). In addition,  $\text{Cu}^{2+}$  on both Cu(3) and Cu(4) sites have a weak nonmagnetic  $3d_{3z^2-r^2}$  state at 1.87 eV. There also exist  $3d$  holes of  $d_{3z^2-r^2}$  symmetry on  $\text{Cu}^+$  at 1.90 eV on both Cu(1) and Cu(2) sites, as shown in Figs. 3(c) and 3(d). The above observations of Cu  $L$ -edge XAS and GGA+ $U$  calculations lead us to conclude that there exist unoccupied  $3d$  states on the nominal  $\text{Cu}^+$  sites in  $\text{LiCu}_2\text{O}_2$  to mediate the magnetic coupling between successive double-layered  $\text{CuO}_4$

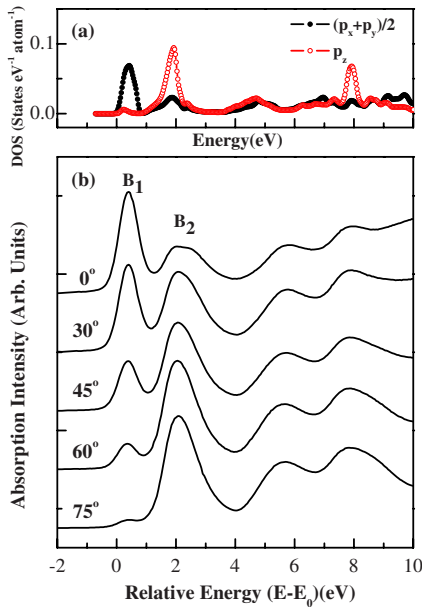


FIG. 4. (Color online) (a)  $p$ -decomposed density of states of  $\text{LiCu}_2\text{O}_2$  from GGA+ $U$  band-structure calculations. (b) O  $K$ -edge XAS of  $\text{LiCu}_2\text{O}_2$  for the electronic field vector  $\mathbf{E}$  from being parallel to perpendicular to the surface normal (exact angle value depending on  $\theta$ ). The relative energy denoted in (b) is aligned with the absorption energy of O  $K$  edge in such a way that the first peak of the DOS in (a) coincides with peak  $B_1$ . The relative zero energy in (b) corresponds to the photon energy of 529.3 eV in the O  $K$ -edge XAS.

plaquettes. Such a weakly magnetic coupling along the  $c$  axis is through the  $3d_{3z^2-r^2}$  orbitals of  $\text{Cu}^+$ . Furthermore, as will be discussed later, the energies of O  $2p$  unoccupied states above the Fermi level shown in Fig. 4(a) coincide with those of Cu, evidencing the  $p$ - $d$  hybridization.

Figure 4(a) displays the O  $2p$  DOS projected onto the directions perpendicular and parallel to the  $c$  axis. The scale of relative energy denoted in Fig. 4(a) is aligned with the O  $K$ -edge data in such a way that the first peak of the DOS coincides with the  $B_1$  peak of Fig. 4(b). The prediction of the  $p$ - $d$  hybridization from GGA+ $U$  calculations is also corroborated by the measurements of O  $K$ -edge absorption, a dipole-allowed transition from O  $1s$ - to  $2p$ -derived unoccupied states. The threshold structures observed near the O  $K$ -edge XAS are determined by the electronic structure of Cu  $3d$  because of the ground-state hybridization between Cu  $3d$  and O  $2p$ . Hence O  $K$ -edge absorption can be interpreted in a similar way as the one-electron addition of Cu  $3d$ , such as the bremsstrahlung isochromat spectroscopy. The near-edge structure of O  $1s \rightarrow 2p$  absorption provides a measure of the partial density of states projected onto the O  $2p$  states. Figure 4(b) shows the polarization-dependent O  $K$ -edge XAS of  $\text{LiCu}_2\text{O}_2$  with various incidence angles. These XAS spectra display several prominent features of the oxygen  $2p$  bands. As the XAS geometry changes from the in-plane to out-of-plane  $\mathbf{E}$  vectors, the intensity of the lowest-energy absorption marked as  $B_1$  decreases and the XAS of 2 eV above marked  $B_2$  is enhanced, such as the evolution of the Cu  $L$ -edge XAS. The features of  $B_1$  and  $B_2$

result from the transitions of  $1s$  to  $2p$  states hybridized with  $3d$  of  $\text{Cu}^{2+}$  and  $\text{Cu}^+$ , respectively.<sup>19,20</sup> Peak  $B_1$  is from the contribution of the unoccupied O  $2p$  hybridized with  $3d$  states of  $xy$  symmetry on  $\text{Cu}^{2+}$  which form the upper Hubbard band (UHB).<sup>26</sup> In contrast,  $B_2$  is from those hybridized with  $3d$  of  $\text{Cu}^+$  in which the ground state is a combination of  $3d^{10}$  and  $3d^9 4s^1$ . Consequently, the  $2p$  bands exhibit both  $z$  and  $xy$  characters that exist, consistent with GGA+ $U$  calculations; even a small splitting of  $B_2$  measured with the in-plane geometry can be explained by the calculations. Note that we performed GGA+ $U$  calculations with several different values of Coulomb interaction energy, i.e.,  $U=0.0, 3.0, 4.5, 6.0,$  and  $7.0$  eV. However, we found that good agreement between the O  $K$ -edge XAS and O  $2p$ -orbital-decomposed DOS (Fig. 4) is obtained only when  $U=4.5$  eV.

One can link our results to the mechanism of the magnetoelectric coupling in  $\text{LiCu}_2\text{O}_2$ . At first sight, arising of the induced polarization  $\mathbf{P}$  in  $\text{LiCu}_2\text{O}_2$  seems to be best understood in terms of the spin-current model<sup>27</sup> or the inverse Dzyaloshinskii-Moriya interaction,<sup>28</sup> where  $\mathbf{P}$  is induced by two neighboring spins  $\mathbf{S}_i$  and  $\mathbf{S}_j$  on the chain and is determined by  $\mathbf{S}_i \times \mathbf{S}_j$ . Although neutron results indicated that the spin-chain structure of  $\text{LiCu}_2\text{O}_2$  is spiral,<sup>1</sup> experimentally, conflicting results were reported regarding the magnetic structure and its relation to the observed  $\mathbf{P}$  in  $\text{LiCu}_2\text{O}_2$ .<sup>1,5,6</sup> Whether the spiral spins lie on the  $ab$  or  $bc$  plane remains controversial,<sup>1,6</sup> while the spin-current model requires spiral spins lying on the  $bc$  plane to generate the observed ferroelectricity along the  $c$  axis. Although the true mechanism of the observed multiferroic features is not fully understood yet, the  $c$ -axis coupling of spins might be essential for the observed multiferrocity.<sup>4,12</sup> The existence of  $3d$  holes on the  $\text{Cu}^+$  site enhances the interlayer magnetic coupling along the  $c$  axis and seems to support such a scenario. In other words, the interlayer magnetic coupling via the  $3d$  holes of  $\text{Cu}^+$  could play a role in the induction of electric polarization.

In summary, our results reveal the symmetry of the  $3d$  holes in the low-dimensional quantum magnet  $\text{LiCu}_2\text{O}_2$  with edge-sharing spin chains. XAS measurements show that  $3d$  holes exist not only on the  $\text{Cu}^{2+}$  sites with  $3d^9$  electronic configuration but also on the  $\text{Cu}^+$  sites which bridge layers of  $\text{CuO}_4$  plaquettes. The nominal  $\text{Cu}^{2+}$  exhibits predominantly  $3d_{xy}$  symmetry in the unoccupied states. We also found that there exist  $3d_{3z^2-r^2}$  holes residing on the  $\text{Cu}^+$  site and the hybridization between O  $2p$  and Cu  $3d$  states above the Fermi level. These findings indicate that the  $3d$  holes of  $\text{Cu}^+$  enhances the magnetic coupling between double layers of  $\text{Cu}^{2+}$  along the  $c$  axis.

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