## Photonic crystal horizontally slotted nanobeam cavity for silicon-based nanolasers

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We theoretically propose and investigate a TM-polarized one-dimensional photonic crystal nanocavity with a horizontal SiO $_2$  slot on a suspended silicon nanobeam via the three-dimensional finite-element method. The ultrahigh quality factor and ultrasmall effective mode volume of  $1.5\times10^7$  and 0.176 half-wavelength cubic of the horizontally SiO $_2$ -slotted nanocavity show strong possibilities for realizing an erbium-doped SiO $_2$  nanolaser. This horizontal SiO $_2$  slot structure can be precisely formed via the sputtering process and further transformed into an air slot via selective wet etching for optical index and biomolecule sensing. © 2012 Optical Society of America OCIS codes: 230.5298, 230.5750.

The silicon (Si)-based nanolaser source has long been regarded as the most important core on the blueprint for constructing complementary metal-oxide semiconductor (CMOS) processing compatible on-chip photonic integrated circuits (PICs) for all-optical information processing. To realize Si-based nanolasers, efficient optical emissions from Si-based materials [1] and nanocavity designs with low optical losses are essential. For the former, the erbium (Er)-doped SiO<sub>2</sub> with strong optical emissions near wavelength of 1.54  $\mu m$  via excited electron transition from  ${}^4I_{13/2}$  to  ${}^4I_{15/2}$  states of the Er dopant [2] has been widely used in various active devices in optical communication systems. Although Er-doped SiO<sub>2</sub> microlasers via microtoroid [3] and microdisk [4] with total-internal-reflection (TIR) confinement have been demonstrated recently, the cavity sizes have to be sufficiently large (several tens of micrometers) to ensure adequately high quality (Q) factors for lasing due to the low index  $(n_{SiO_2} \sim 1.45)$  of SiO<sub>2</sub>. Even utilizing photonic crystal (PhC) nanocavity [5,6] can efficiently confine photons in one-wavelength cubic volume, photonic bandgap (PBG) and TIR effects are weak owing to the low index of SiO<sub>2</sub>. And the theoretical Q is limited to only  $2.5 \times 10^4$ [7,8] and insufficient for lasing via the gain medium of Erdoped SiO<sub>2</sub> [4]. In this Letter, we propose and investigate a TM-polarized one-dimensional (1D) PhC SiO<sub>2</sub>-slotted nanocavity with ultrahigh Q factor and extremely small mode volume  $(V_{\text{eff}})$  on a suspended Si nanobeam (NB), which shows the strong possibilities for realizing an Er-doped SiO<sub>2</sub> nanolaser.

Our design starts from a 1D PhC nanocavity on a suspended Si NB shown in Fig.  $\underline{1(a)}$ . The 1D PhCs are composed of air holes on the NB, where the TE/TM PBG effects exist simultaneously [9]. The mirror of the nanocavity is formed by 12-period gradually varied PhCs and a 10-period outer PhC mirror. The lattice constant  $(a_n, n=1-13)$  of the gradually varied PhCs is linearly varied with a 5 nm increment under the fixed air-hole radius  $(r_n)$  over  $a_n$   $(r_n/a_n)$  ratio of 0.32. The refractive index  $(n_{\rm NB})$  and width (w) of the Si NB are set as 3.48 and 340 nm, respectively. Via the three-dimensional (3D) finite-

element method (FEM), we calculate the Q factors of the TM-polarized zeroth-order mode in nanocavities with different NB thickness  $t_{\rm NB}$  from 300 to 1100 nm, as shown in Fig. 1(b). The Q factor increases with the  $t_{\rm NB}$  and shows a saturated value as high as  $9.7 \times 10^6$  when  $t_{\rm NB} = 900$  nm. The simulated mode profile for the  $E_z$  field in the x-y plane is shown in the inset of Fig. 1(b).

We then designed an Er-doped  $\mathrm{SiO}_2$  layer with thickness of  $t_{\mathrm{SiO}_2}$  in the  $\mathrm{Si}$  NB to form a horizontal  $\mathrm{SiO}_2$  slot structure. The Er-doped  $\mathrm{SiO}_2$  layer was embedded through the entire  $\mathrm{Si}$  NB and served as the gain medium. And the PhCs (air holes) penetrate through this  $\mathrm{SiO}_2$ -slotted  $\mathrm{Si}$  NB vertically, as shown in Fig. 2(a). For the  $E_z$  field of the TM-polarized zeroth-order mode, the  $\mathrm{SiO}_2$  slot shows an index discontinuity in the z direction. Because the electric flux density has to satisfy the Maxwell equations, the  $E_z$  field will obey the relationship of  $\varepsilon_{\mathrm{Si}}E_{z\mathrm{Si}}=\varepsilon_{\mathrm{SiO}_2}E_{z\mathrm{SiO}_2}$  [10], where  $\varepsilon_{\mathrm{Si}}$ ,  $\varepsilon_{\mathrm{SiO}_2}$ ,  $\varepsilon_{\mathrm{ZSi}}$ , and  $\varepsilon_{\mathrm{SiO}_2}$  represent the dielectric constants and the  $E_z$ -field distributions of  $\mathrm{Si}$  and  $\mathrm{SiO}_2$ . Thus, the  $E_z$  field in the  $\mathrm{SiO}_2$  slot will show  $\varepsilon_{\mathrm{Si}}/\varepsilon_{\mathrm{SiO}_2}$  times enhancement to that in  $\mathrm{Si}$  and  $V_{\mathrm{eff}}$  of the TM-polarized zeroth-order mode will also be greatly reduced.

With a fixed  $t_{\rm NB}$  of 900 nm, the simulated Q factors and  $V_{\rm eff}$  of the TM-polarized zeroth-order modes in 1D PhC

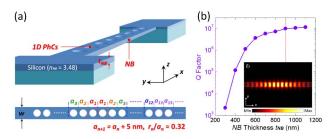


Fig. 1. (Color online) (a) Scheme and design of a 1D PhC nanocavity on a suspended Si NB. (b) Simulated Q factors of the TM-polarized zeroth-order modes in the 1D PhC NB nanocavities with different  $t_{\rm NB}$  from 300 to 1100 nm. Inset, simulated mode profile for the  $E_z$  field in the  $x\!-\!y$  plane of the nanocavity with  $t_{\rm NB}=900$  nm.

 $SiO_2$ -slotted NB nanocavities with different  $t_{SiO_2}$  are shown in Fig. 2(b). The Q factor increases to  $1.5 \times 10^7$ when  $t_{SiO_2} = 20 \text{ nm}$ , which is even higher than that of the nanocavity without the  $SiO_2$  slot. This enhanced Qfactor when  $t_{SiO_2}$  increases from 0 to 20 nm comes from the reduced effective index mismatching by the presence of the low-index SiO<sub>2</sub> slot with fine index tuning. However, once the  $t_{\rm SiO_2}$  becomes larger than 20 nm, the effective index mismatching will increase, which significantly degrades the Q factor. The simulated mode profiles for the  $E_z$  field in the x-y, y-z, and x-z planes when  $t_{SiO_2}$  = 20 nm are shown in Fig. 2(c), where the  $E_z$  field is strongly enhanced inside  $\overline{\text{the}}\ \text{SiO}_2$  slot. Furthermore, the  $V_{\mathrm{eff}}$  monotonically decreases with decreasing  $t_{\mathrm{SiO_2}}$ , which can be understood by the  $|E_z|^2$  distributions along the z axis of the nanocavities with different  $t_{\mathrm{SiO}_{2}}$  shown in Fig. 2(d). When  $t_{\rm SiO_2}=10$  nm, the  $V_{\rm eff}$  and  $Q/V_{\rm eff}$  are  $0.176(\lambda/2n_{\rm SiO_2})^3$  and  $5.9\times10^7(\lambda/2n_{\rm SiO_2})^{-3}$ . The ultrahigh  $Q/V_{\rm eff}$  is not only beneficial for realizing nanolasers, but it is also useful to the researches of quantumelectrodynamics (QED) and applications requiring strong light-matter interactions. In addition to the Erdoped  $SiO_2$ , we simulate the Er-doped  $SiN_x$  slot with the higher index of 2.0 as the gain material in our design. The simulated Q factors and  $V_{\rm eff}$  of  ${\rm SiN}_x$ -slotted nanocavities with different  $\mathrm{SiN}_x$  thicknesses  $t_{\mathrm{SiN}_x}$  and fixed  $t_{\mathrm{NB}}$  of 900 nm are shown in Fig. 2(b). The Q factor shows an optimized value of  $1.84 \times \overline{10^7}$  when  $t_{SiN_x} = 80$  nm and the  $Q/V_{\rm eff}$  reaches as high as  $1.16 \times 10^7 (\lambda/2n_{\rm SiN_x})^{-3}$  when  $t_{\text{SiN}_{a}} = 10 \text{ nm}$ . These values are both better than those of the reported 1D and 2D  $SiN_x$  PhC nanocavities [11,12].

There are several unique features and advantages in the presented horizontally slotted nanocavity design. First, for a 1D PhC nanocavity based on effective index matching, the horizontal slot formed on the entire NB can plays the role of index tuner to further optimize the Q

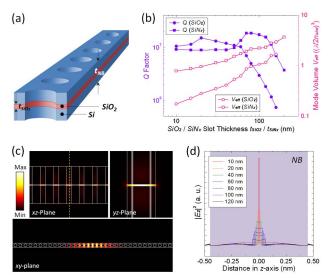


Fig. 2. (Color online) (a) Scheme of 1D PhC nanocavity on a horizontally SiO<sub>2</sub>-slotted Si NB. (b) Simulated Q factors and  $V_{\rm eff}$  of the TM-polarized zeroth-order modes in 1D PhC SiO<sub>2</sub>/SiN $_x$ -slotted nanocavities with  $t_{\rm SiO_2}/t_{\rm SiN}_x=10$  – 160/200 nm. (c) Simulated mode profiles for the  $E_z$  field in the x–z, y–z, and x–y planes when  $t_{\rm SiO_2}=20$  nm. (d) Simulated  $|E_z|^2$  distributions along the z axis [the dotted line in (c)] of the nanocavities with different  $t_{\rm SiO_2}$ .

factor, which means the  $V_{\rm eff}$  can be greatly minimized while the Q factor remains high. Second, the most important advantage, the horizontal slot can be easily made via the sputtering process or chemical vapor deposition (CVD) with nanometer-scale precision, while the optimized electron beam lithography and dry etching processes in PhC vertically slotted nanocavities are not needed. In addition, compared with the traditional vertical slot formed by etching process, excellent uniformity and minimized surface roughness of the horizontal slot formed by sputtering process also greatly improve the losses at the interfaces of the slot and the Si. Third, the optical gain medium, the Er dopant, can be placed in the horizontal slot by cosputtering or the ion-implantation process during or after slot formation, which cannot be achieved in most reported PhC nanocavities with vertical slots. Moreover, via the slot, the radiative photon lifetime of the gain medium can be significantly extended [13]. Thus, with the enhanced mode properties and ease of insertion of the optical gain medium, utilizing our proposed horizontally slotted nanocavity to realize the Sibased nanolasers is possible. Furthermore, the presented nanocavity is also suitable for PhC quantum cascade lasers with TM polarization that lack a high Q cavity design before [14,15].

To evaluate the required minimum  $Q\left(Q_{\text{lasing}}\right)$  of the horizontally slotted nanocavities with different  $t_{\text{SiO}_2}/t_{\text{SiN}_x}$  for lasing, the gain condition of the Er dopant and the optical loss of the nanocavity are considered via the following equation [4]:

$$Q_{\text{lasing}} > \frac{2\pi}{\lambda} n_{\text{slot}} \frac{1}{\Gamma \sigma_c N_{\text{Fr}}}.$$
 (1)

The terms  $\sigma_{\varepsilon}$  and  $N_{\rm Er}$  represent the emission cross section and concentration of the Er, which are set as  $4\times 10^{-21}~{\rm cm^2}$  and  $1\times 10^{22}~{\rm ions/cm^3}$ . The value of  $N_{\rm Er}$  is chosen as the upper limit before clustering of the Er [4]. The mode overlap  $\Gamma$  factor with the Er-doped  ${\rm SiO_2/SiN_x}$  slot is defined as the ratio of the  $|E|^2$  field of the mode concentrating inside the slot. The simulated  $Q_{\rm lasing}$  factors under different  $t_{{\rm SiO_2}}/t_{{\rm SiN_x}}$  are shown in Fig. 3(a), which strongly depend on the  $\Gamma$  factors also shown in Fig. 3(a). For  $t_{{\rm SiO_2}}$  and  $t_{{\rm SiN_x}}$  equal to 10 nm, the  $\Gamma$  factors are 0.193 and 0.077, respectively, while the  $Q_{\rm lasing}$  factors reach their highest values of  $7.6\times 10^3$  and  $2.64\times 10^4$ . Compared

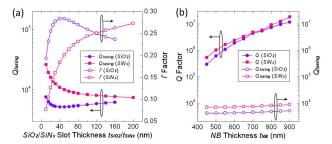


Fig. 3. (Color online) (a)  $Q_{\rm lasing}$  and  $\Gamma$  factors of 1D PhC  ${\rm SiO_2/SiN_x}$ -slotted NB nanocavities with different  $t_{{\rm SiO_2}}$  and  $t_{{\rm SiN_x}}$ . (b) Simulated Q and  $Q_{\rm lasing}$  factors of 1D PhC  ${\rm SiO_2/SiN_x}$ -slotted NB nanocavities with different  $t_{\rm NB}$ , while the  $t_{{\rm SiO_2}}$  and  $t_{{\rm SiN_x}}$  are fixed at 40 and 80 nm, respectively.

with the simulated results in Fig. 2(b), the Q factors of the nanocavities with present  $t_{SiO_2}/t_{SiN_x}$  ranges are much higher (more than 2 orders at least) than the  $Q_{\text{lasing}}$  factors and show they are sufficient for lasing. Even taking the losses arisen from fabrication imperfections in a real situation [5,16] into consideration, the huge excess of the Q factors ensure the lasing capabilities of our design. In contrast, for the TE-polarized modes, the presented horizontally slotted nanocavity does not show a discontinuity in the index for their electric fields ( $E_x$  and  $E_y$ ). Therefore, the electric fields will not tend to concentrate inside the  $SiO_2/SiN_x$  slots, which lead to very low  $\Gamma$  factors and over 1 order higher  $Q_{\text{lasing}}$  factors than those of the TM-polarized modes. Furthermore, to minimize the NB volume and simplify the sputtering process in fabrication, we also calculate the Q and  $Q_{\text{lasing}}$  factors of the nanocavities with different  $t_{\rm NB}$  from 450 to 900 nm, as shown in Fig. 3(b). According to the  $\Gamma$  and Q factors,  $t_{\rm SiO_2}$  and  $t_{\rm SiN_x}$  are fixed at 40 and 80 nm, respectively. In Fig. 3(b), the Q factors decrease rapidly with the decreas- $\overline{Q}_{
m NB}$  and are still 2 orders higher than the  $\overline{Q}_{
m lasing}$  factors when  $t_{\rm NB} > 450$  nm for  ${\rm SiO_2/SiN_x}$ -slotted nanocavities. These results show the lasing from the Er-doped  $SiO_2/SiN_r$ -slotted nanocavity can still be achieved under reasonable  $t_{\rm NB}$ .

Based on our presented design, the air slots widely utilized in optical sensing  $[\underline{17}-\underline{19}]$  in recent years can be easily formed with different thicknesses  $t_{\rm slot}$  by removing the SiO<sub>2</sub>/SiN<sub>x</sub> via proper selective chemical vapor wet etching [5]. To find the sensing capabilities, the environmental index is varied from 1.342 to 1.414. For the nanocavity with the horizontal air slot thickness  $t_{\rm slot}$  of 80 nm, a high index sensitivity [defined as wavelength shift (nm) per refractive index unit (RIU) variation] of 280 nm/RIU and a small minimum detectable index variation at the level of 10<sup>-6</sup> are obtained. In addition, owing to the enhanced electric field inside the air slot, the horizontally air-slotted nanocavity would also be very suitable for sensing biomolecules and can be applied for medical or biological label-free sensing applications via proper functionalization.

In summary, we propose a TM-polarized 1D PhC nanocavity with a low-index (SiO $_2$ /SiN $_x$ ) horizontal slot on a suspended Si NB, where the slot can be easily prefabricated by sputtering or the CVD process with ultrafine control of thickness, uniformity, and surface roughness. Via 3D FEM simulations, the SiO $_2$  slot can greatly minimize the mode volume [ $\sim 0.176 (\lambda/2 n_{\rm SiO}_2)^3$  when  $t_{\rm SiO}_2 = 10$  nm] and keep the Q very high ( $\sim 1.5 \times 10^7$  when  $t_{\rm SiO}_2 = 20$  nm) simultaneously, which are very beneficial for studying QED phenomenon and applications requir-

ing strong light–matter interactions. Moreover, the ease of placing the gain medium (Er-doped  $\mathrm{SiO}_2/\mathrm{SiN}_x$ ) inside the slot provides strong possibilities for realizing Er-doped  $\mathrm{SiO}_2/\mathrm{SiN}_x$  nanolasers for CMOS-processing-compatible PICs. By considering the gain conditions of the Er dopant in the  $\mathrm{SiO}_2/\mathrm{SiN}_x$  slots, the Q factors of nanocavities with presented slot thickness ranges are sufficient for lasing.

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