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## Short Communication

# The optical absorption and hydrogen production by water splitting of (Si,Fe)-codoped anatase TiO<sub>2</sub> photocatalyst

Yanming Lin<sup>a,b</sup>, Zhenyi Jiang<sup>a,\*</sup>, Chaoyuan Zhu<sup>b</sup>, Xiaoyun Hu<sup>c</sup>, Haiyan Zhu<sup>a</sup>, Xiaodong Zhang<sup>a</sup>, Jun Fan<sup>d</sup>, Sheng Hsien Lin<sup>b,e</sup>

<sup>a</sup> Institute of Modern Physics, Northwest University, Xi'an 710069, PR China

<sup>b</sup> Department of Applied Chemistry, Institute of Molecular Science and Center for Interdisciplinary Molecular Science, National Chiao-Tung University, Hsinchu 30050, Taiwan

<sup>c</sup> Department of Physics, Northwest University, Xi'an 710069, PR China

<sup>d</sup> School of Chemical Engineering, Northwest University, Xi'an 710069, PR China

<sup>e</sup> Institute of Atomic and Molecular Sciences, Academia Sinica, Taipei 106, Taiwan

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## ABSTRACT

The electronic and optical properties are studied using the density functional theory in (Si,Fe)-codoped anatase TiO<sub>2</sub>. The calculated results suggest that the synergistic effects of (Si,Fe) codoping can effectively induce the redshift of optical absorption edge, which leads to higher visible-light photocatalytic activity for hydrogen production by water splitting than pure anatase TiO<sub>2</sub>. To verify the reliability of our calculated results, nanocrystalline (Si,Fe)-codoped TiO<sub>2</sub> is synthesized by a sol-gel-solvothermal method, and excellent absorption performance and photocatalytic activity for hydrogen production by water splitting are observed in our experiments.

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Among many candidates of semiconductor photocatalyst, titania (TiO<sub>2</sub>) has become the most investigated one for overall water splitting for hydrogen production, due to its outstanding chemical stability, low cost, and non-toxicity [1,2]. However, the photocatalytic water splitting for hydrogen production of TiO<sub>2</sub> are restricted to ultraviolet (UV)-light ( $\lambda < 385$  nm) due to the wide band gap of anatase TiO<sub>2</sub> ( $\sim 3.2$  eV). Therefore, reducing the band gap of anatase TiO<sub>2</sub> to make it photosensitive to visible-light has become one of the

most important goals in photocatalytic water splitting for hydrogen production. It has been suggested that doping with different cations and anions would result in a reduced band gap for TiO<sub>2</sub> [3–11]. For example, Yang et al. studied systematically the nitrogen concentration influence on N-doped anatase TiO<sub>2</sub> [6]. The results indicate that some localized N 2p states are formed above the valence band in N-doped anatase TiO<sub>2</sub> at lower doping levels, which leads to the reduction of the photon transition energy. And the energy gap has little further

\* Corresponding author. Tel.: +86 29 88303491; fax: +86 29 88302331.

E-mail addresses: [linymnwu@gmail.com](mailto:linymnwu@gmail.com) (Y. Lin), [jiangzy@nwu.edu.cn](mailto:jiangzy@nwu.edu.cn) (Z. Jiang).

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narrowing compared with that at lower doping levels when the doping level rises. A few latest researches indicate that different cations and anions codoping into  $\text{TiO}_2$  can further narrow its band gap and enhance its photocatalytic activity [12–20]. For instance, Jia et al. studied the microscopic mechanism for band gap narrowing and the origin of the enhanced visible-light photocatalytic activity in N/S-codoped anatase  $\text{TiO}_2$  [13]. Li et al. reported that the C/H-codoping produces significant band gap narrowing, which leads to higher visible-light photocatalytic efficiency than the C-doped anatase  $\text{TiO}_2$  [16]. The research of Su et al. suggested that the codoping of  $\text{TiO}_2$  with N and Fe leads to the much narrowing of the band gap and greatly improves the photocatalytic activity under visible irradiation [17]. The results showed that codoping is one of the most effective approaches to extend the absorption edge to the visible-light region in anatase  $\text{TiO}_2$ . However, photocatalytic activity for hydrogen production by water splitting and optical absorption properties of (Si,Fe)-codoped  $\text{TiO}_2$  has no report on the theory and experiment. Therefore, the enhanced visible-light absorption efficiency and photocatalytic activity are expected for (Si,Fe)-codoped  $\text{TiO}_2$ .

In this letter, the electronic and optical properties of (Si,Fe)-codoped  $\text{TiO}_2$  are investigated using the density functional theory (DFT) to reveal the synergistic effects of (Si,Fe) codoping on the mechanism of bandgap reducing and the origin of enhanced visible-light photocatalytic activity for hydrogen production by water splitting. Nanocrystalline (Si,Fe)-codoped  $\text{TiO}_2$  was synthesized with sol-gel-solvothermal method. It was found that the (Si,Fe)-codoped  $\text{TiO}_2$  showed excellent photocatalytic activity for hydrogen production, which verified the reliability of our calculated results.

All the spin-polarized calculations were performed using the projector augmented wave pseudopotentials as implemented in the VASP code [21,22]. The exchange correlation function was treated by the generalized gradient approximation (GGA) with the Perdew–Wang parameterization (known as GGA-PW91) [23]. The Brillouin-zone integrations were approximated by using the special  $k$ -point sampling of the Monkhorst–Pack scheme [24]. A cutoff energy of 500 eV and a mesh size of  $9 \times 9 \times 9$  were used for geometry optimization

and electronic property calculations. Using the block Davidson scheme, both the atomic positions and cell parameters were optimized until the residual forces were below  $0.01 \text{ eV/\AA}$ . To obtain the band gap that was consistent with the experimental result, the GGA +  $U$  method [25] was employed. The Coulombic interaction  $U$  and exchange energy  $J$  were set to be 10.0 eV and 1.0 eV, respectively. Accordingly, the calculated band gap of pure anatase  $\text{TiO}_2$  was 2.9 eV, which was in good agreement with the experimental value [26].

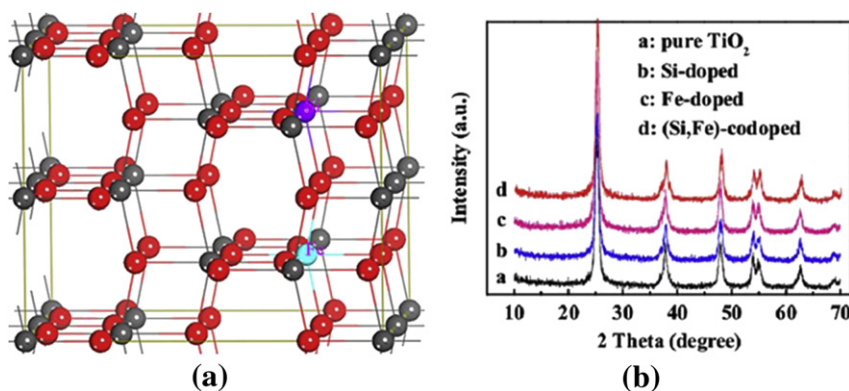
The valence electron configurations considered in this study included Ti ( $3d^24s^2$ ), O ( $2s^22p^4$ ), Si ( $3s^23p^2$ ), and Fe ( $3d^64s^2$ ). All the doped systems were constructed from a relaxed ( $2 \times 2 \times 1$ ) 48-atom anatase  $\text{TiO}_2$  supercell and it is shown in Fig. 1(a). As the position of Fe in the  $\text{TiO}_2$  lattice was unclear, variety of positions of Fe atoms in the lattice were considered, such as substitutional Fe at the Ti site (Fe@Ti) and O site (Fe@O). In the Si-doped  $\text{TiO}_2$ , a Ti atom is substituted by a Si atom (Si@Ti) [27]. Similar substitutions were also considered for codoped systems, as Fe locates at either Ti or O site and Si locates at Ti site, namely, Si@Ti&Fe@Ti and Si@Ti&Fe@O. To study the stabilities of the doped systems, we calculated the defect formation energy ( $E_f$ ) for the doped and codoped systems according to the equations

$$E_{f(X@Y)} = E_{(X@Y)} - E_{(\text{pure})} - (\mu_X - \mu_Y) \quad (1)$$

$$E_{f(\text{Si@Y}\&\text{Fe@Y})} = E_{(\text{Si@Y}\&\text{Fe@Y})} - E_{(\text{pure})} - (\mu_{\text{Si}} + \mu_{\text{Fe}} - \mu_Y - \mu_Y) \quad (2)$$

where  $X = \text{Si, Fe}$ ;  $Y = \text{Ti, O}$ ;  $E$  represents the total energy and  $\mu$  is the chemical potential. The calculated formation energies are listed in Table 1. It shows that Fe impurity is preferred to substitute Ti in lattice because of the smallest formation energy in both Fe-doped and (Si,Fe)-codoped anatase  $\text{TiO}_2$  systems.

To investigate the electronic properties of Si and/or Fe (co) doping anatase  $\text{TiO}_2$ , the total density of states (TDOS) and partial density of states (PDOS) were plotted in Fig. 2. It indicates that the valence band (VB) is dominated by O  $2p$  states while the conduction band (CB) consists mainly of Ti  $3d$  states for pure anatase  $\text{TiO}_2$ . In Si-doped  $\text{TiO}_2$  (Si@Ti), the VB broadens with the mixing of O  $2p$  and Si  $3p$  states, and the CB bottom has a decline of about 0.15 eV, which can lead to a



**Fig. 1 – (A) 48-atom supercell model for defective anatase  $\text{TiO}_2$  shows the location of the dopants. The atom doping sites are marked with Si and Fe. The gray spheres and red spheres represent the Ti and O atoms, respectively. The purple sphere and cyan sphere represent Si and Fe atom, respectively. (b) XRD patterns for the pure and doped  $\text{TiO}_2$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)**

**Table 1 – Defect formation energies  $E_f$  for different doped anatase  $\text{TiO}_2$  systems.**

Doped models	Doped			Codoped	
	Si@Ti	Fe@Ti	Fe@O	Si@Ti and Fe@Ti	Si@Ti and Fe@O
$E_f$ (eV)	-8.7293	-1.5953	12.7225	-11.2535	1.7695

band gap narrowing. For Fe-doped  $\text{TiO}_2$  (Fe@Ti), it is shown that the band gap decreases by about 0.6 eV and most Fe 3d states are located in the band gap compared with the pure anatase  $\text{TiO}_2$ , which may be due to stronger interactions between the Fe 3d and Ti 3d orbitals. For (Si,Fe)-codoped  $\text{TiO}_2$  system (Si@Ti&Fe@Ti), some impurity states (Si 3p and Fe 3d) are mixed with the VB and CB edge. The top of the VB has an obvious upward shift while the CB bottom has an obvious downward shift, which results in a band gap narrowing of about 1.0 eV compared with the pure anatase  $\text{TiO}_2$ . Therefore, synergistic effect of (Si,Fe)-codoped can lead to a decrease of the photon excitation energy and redshift the optical absorption edge to the visible-light range.

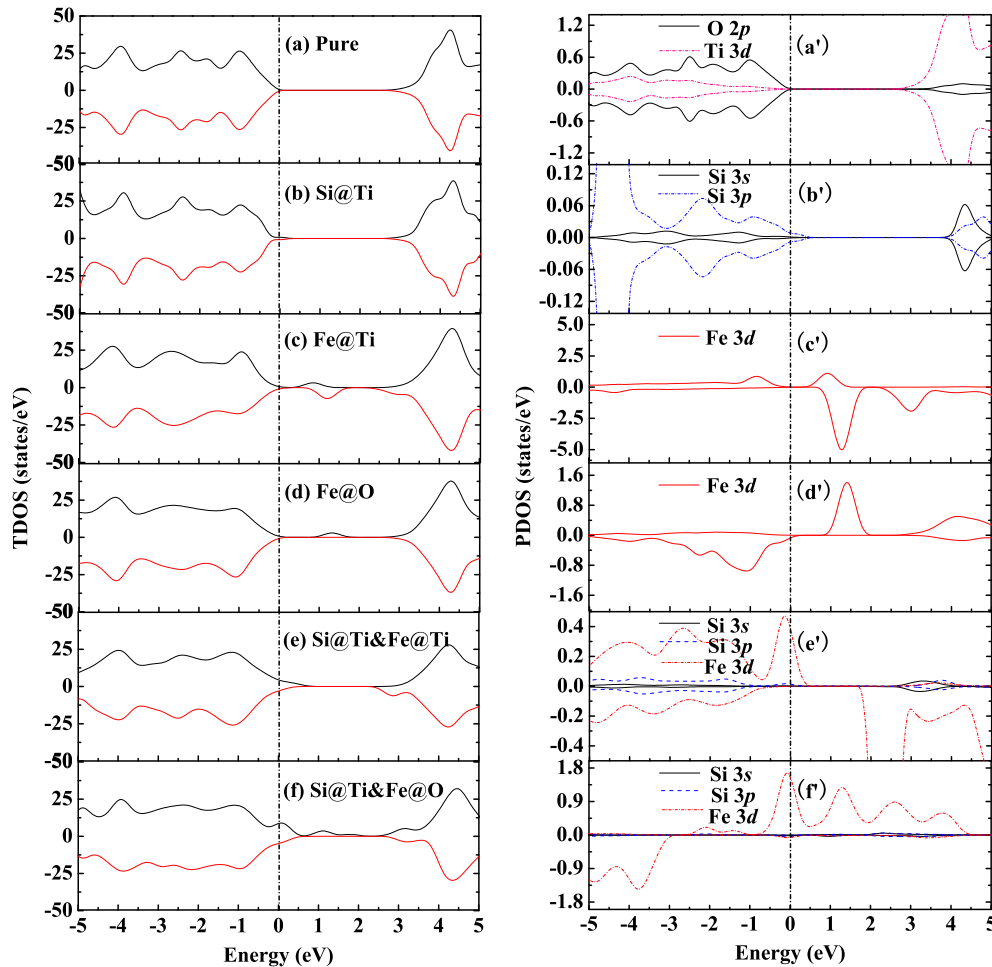
According to the obtained electronic structures, we calculated the complex dielectric function  $\xi = \xi_1 + i\xi_2$ . The

corresponding absorption spectrum was estimated by the following equation

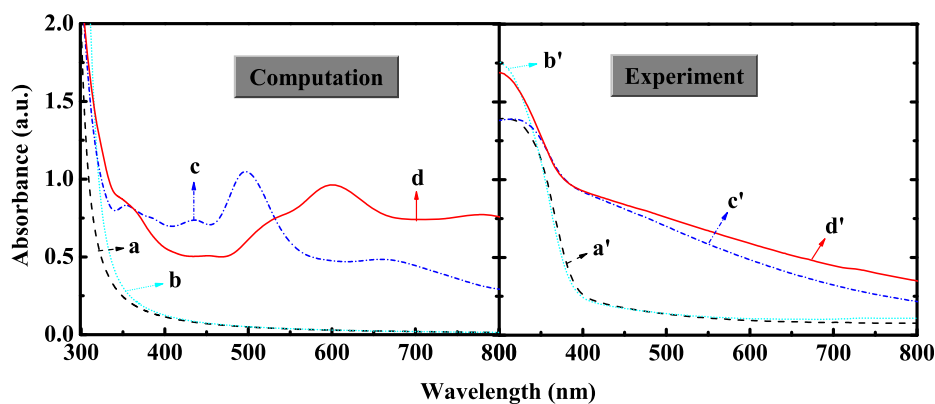
$$I(\omega) = 2\omega \left( \frac{(\xi_1^2(\omega) + \xi_2^2(\omega))^{1/2} - \xi_1(\omega)}{2} \right)^{1/2} \quad (3)$$

where  $I$  is the optical absorption coefficient,  $\omega$  is the angular frequency ( $E = \hbar\omega$ ).

The absorption spectra of the pure and doped anatase  $\text{TiO}_2$  systems are calculated and shown in Fig. 3. It is found that pure anatase  $\text{TiO}_2$  can only respond to the UV-light and shows no absorption activity in the visible-light region. For Si-doped system, it is clear that the narrowed band gap can result in the reduction of the photon transition energy from the VB to the CB, which induces the increasing optical absorption in the UV-light region. For Fe-doped system, there are a series of impurity states (Fe 3d orbital) appearing in the forbidden gap and the band gap has an obvious narrowing compared with the pure anatase  $\text{TiO}_2$ . These results indicate that the electrons are excited easily from the VB to the CB through the Fe 3d states under the visible-light irradiation, which can lead to a good optical absorption for Fe-doped  $\text{TiO}_2$  in the visible-light region. For (Si,Fe)-codoped  $\text{TiO}_2$  system, synergistic effect of (Si,Fe) codoping induces a band gap narrowing and appearing Fe 3d states in the forbidden gap, which lead to a decrease of



**Fig. 2 – Calculated TDOS and PDOS of different doped  $\text{TiO}_2$ . The top of the valence band of pure anatase  $\text{TiO}_2$  is taken as the reference level. Curves above and below the horizontal axis refer to the up-spin and down-spin DOS, respectively.**



**Fig. 3** – The optical absorption curves of (a, a') pure, (b, b') Si-doped, (c, c') Fe-doped, and (d, d') (Si,Fe)-codoped  $\text{TiO}_2$ . The left and right figures represent the absorption spectra obtained by computations and experiments, respectively.

the photon excitation energy in the view of electronic structure. Therefore, the absorption of visible- and UV-light is greatly enhanced in (Si,Fe)-codoped anatase  $\text{TiO}_2$  compared with the pure, Si- and Fe-doped anatase  $\text{TiO}_2$ , which may be responsible for the redshift of optical absorption edge and the outstanding activity for hydrogen generation by photocatalytic water splitting in (Si,Fe)-codoped anatase  $\text{TiO}_2$ .

To confirm the better photocatalytic activity for hydrogen production by water splitting of the (Si,Fe)-codoped  $\text{TiO}_2$  compared to that of pure  $\text{TiO}_2$ , we further observed the UV–vis absorption spectrum by experiments.

Nanocrystalline pure, Si-, Fe-, and (Si,Fe)-codoped  $\text{TiO}_2$  were prepared by a sol-gel-solvothermal method. Firstly, a desired amount (0.3367 g) of  $\text{Fe}(\text{NO}_3)_3 \cdot 9\text{H}_2\text{O}$  was dissolved in 39.66 mL of  $\text{CH}_3\text{COOH}$  solution under stirring. Then, 5.58 mL of  $(\text{C}_2\text{H}_5\text{O})_4\text{Si}$  was dropwise added into the solution with stirring for 1 h. Secondly, 28.36 mL of  $[\text{CH}_3(\text{CH}_2)_3\text{O}]_4\text{Ti}$  was also dropwise added into the solution with continuous stirring for 2 h, and the solution was heated in an oven and kept at  $140^\circ\text{C}$  for 14 h. Finally, the precipitate obtained was dried in a vacuum oven at  $70^\circ\text{C}$  for 48 h. To evaluate the photocatalytic activity of samples, hydrogen generation by photocatalytic water splitting was performed in a cylindrical quartz photo-reactor with a 1000 mL capacity. A flow of dry  $\text{N}_2$  gas was used to purge dissolved  $\text{O}_2$  in the reactor for 30 min prior to illumination. A 500 W long-arc xenon lamp surrounded with a water cooling system was fixed in the center of the reaction cell. Photocatalyst (0.4 g) was suspended in 60 mL ethanol and 540 mL distilled water under stirring magnetically.  $\text{H}_2$  was analyzed by gas chromatograph (GC) using a Fuli GC-9790II (Zhejiang, China), equipped with a thermal conductivity detector (TCD) and a stainless steel column (2 m) packed with molecular sieves (5 A) at 323 K.

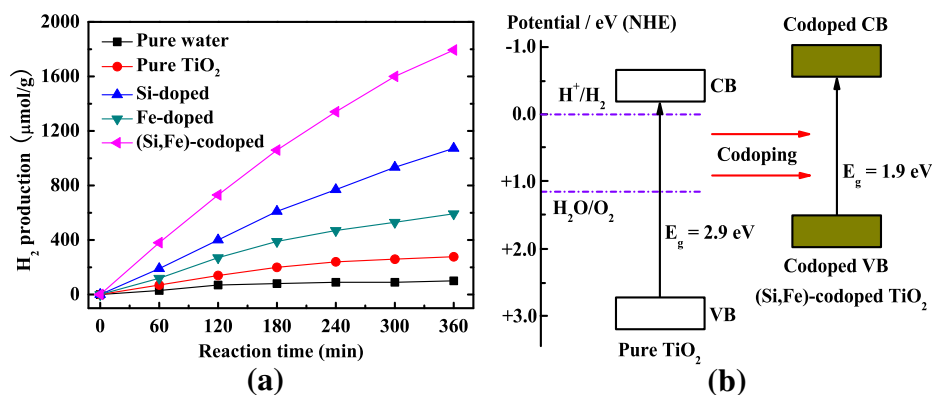
The crystalline phase was identified by X-ray diffraction (XRD) (Rigaku D/MAX-2400). The Brunauer–Emmett–Teller (BET) surface area of the samples was measured through nitrogen adsorption at 77 K (Nova 2000e). The UV–vis absorption spectra were obtained on an UV–vis spectrophotometer (UV-3600) and using  $\text{BaSO}_4$  as the reference sample.

Fig. 1(b) shows the XRD patterns of the samples of pure, Si-, Fe-, and (Si,Fe)-codoped  $\text{TiO}_2$ . It is found that all of the diffraction peaks are contributed by the anatase  $\text{TiO}_2$  phase

and no other visible impurity peak can be distinguished in the pattern of pure or doped sample. The BET surface areas for pure, Si-, Fe-, and (Si,Fe)-codoped  $\text{TiO}_2$  are 84.21, 252.42, 226.72 and  $308.31\text{ m}^2/\text{g}$ , respectively. It is shown that the surface area of  $\text{TiO}_2$  powders is increased to  $308.31\text{ m}^2/\text{g}$  with the coexistence of Si and Fe in  $\text{TiO}_2$ , about four times of that of pure  $\text{TiO}_2$  powders.

The optical absorption spectra of the pure and doped systems are measured by experiments, and shown in Fig. 3. Compared with the pure  $\text{TiO}_2$ , it is clear that the incorporation of Si into  $\text{TiO}_2$  lattice induces the enhanced optical absorption in the UV-light region. For Fe-doped system, it exhibits an excellent absorption activity in the visible-light region. For (Si,Fe)-codoped  $\text{TiO}_2$ , it is obvious that the optical absorption in the UV–visible region is stronger than that of pure  $\text{TiO}_2$ , especially in the visible-light region. The enhancement of absorption in the visible-light region can promote the utilization of the solar light for the doping  $\text{TiO}_2$ , which enhances the visible-light photocatalytic activity of  $\text{TiO}_2$  for hydrogen production by water splitting. However, there are small misalignments between the experimental and theoretical results, which may be due to neglect of the anisotropy of the absorption coefficient and the well-known limitation of DFT. But, from the perspective of qualitative analysis, the experimental results are consistent with the calculations.

The photocatalytic activity of the pure and doped  $\text{TiO}_2$  samples was evaluated by hydrogen production from water splitting, as shown in Fig. 4(a). Pure water produces very low amount of hydrogen under the visible-light irradiation without photocatalyst, indicating that the photolysis can be ignored. It is obvious that Si, Fe, and (Si,Fe) (co)doping can improve the photocatalytic activity of hydrogen production in  $\text{TiO}_2$  material. Among them, (Si,Fe)-codoped  $\text{TiO}_2$  sample exhibits the best photocatalytic activity of hydrogen production compared with the pure  $\text{TiO}_2$ , which may be due to a stronger absorption of solar light in (Si,Fe)-codoped  $\text{TiO}_2$ . In addition, Fig. 4(b) shows the VB and CB edge potentials of pure and (Si,Fe)-codoped  $\text{TiO}_2$  vs. normal hydrogen electrode (NHE). The CBM potential of (Si,Fe)-codoped  $\text{TiO}_2$  is  $-0.6\text{ eV}$ , more negative than  $\text{H}^+/\text{H}_2$  (0 eV). The results show that it has the ability to reduce  $\text{H}^+$  to produce  $\text{H}_2$ , and the reductive ability is stronger than pure  $\text{TiO}_2$ . Therefore,  $\text{TiO}_2$  exhibits outstanding



**Fig. 4 – (A) Hydrogen production by water splitting as a function of reaction time over the pure and doped TiO<sub>2</sub> samples, and (b) a schematic diagram of band level arrangements for photocatalytic water splitting in pure and codoped TiO<sub>2</sub> systems.**

photocatalytic activity for hydrogen production by water splitting through Si and Fe codoping.

In conclusion, we have investigated the electronic and optical properties of (Si,Fe)-codoped TiO<sub>2</sub> based on DFT calculations. The synergistic effects of (Si,Fe) codoping may further reduce the electrons excited energy from VB to CB compared with the pure TiO<sub>2</sub> under the solar light irradiation, which enhances the photocatalytic activity for hydrogen production by water splitting and induces the redshift of absorption edge. The photocatalytic splitting water and absorption spectra obtained by experiments indicate that (Si,Fe)-codoped TiO<sub>2</sub> sample has a much stronger absorption of the solar light and photocatalytic activity for hydrogen production by water splitting than the pure TiO<sub>2</sub>, which verifies the reliability of the calculation results.

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