# A New Power Collection Architecture for Future Spacecraft

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The generalized tree-like transmission line network system having n layers in total with m-to-1 branch connection at each joint (T-TLNS-n-m) is proposed to replace the traditional series-parallel combined dc networks to automatically accumulate identically distributed power cells into the large amount of useful power for the spacecrafts. The proposed system has the attractive features of simple structure, easy construction and maintenance, and low cost, because two kinds of parts, ac current sources and m-to-1 transmission line (TL) branch connection parts, are used in the whole system. A method of implementing ac current cells having high output impedance is proposed to improve the power collection efficiency of the whole network system. Simulated results show that that low-pass nominal  $\pi$ - or T-circuit with high characteristic impedance, which is used for the voltage source to current source converter in the current cell, improves the efficiency of the voltage inverter, filters out the harmonics, and increases the output impedance of the whole current cell.

Manuscript received February 20, 1996; revised September 24, 1006

IEEE Log No. T-AES/33/4/06849.

Patents have been applied for for the appropriate contents of this manuscript.

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### I. INTRODUCTION

For space navigation, electric power is everything. The energy sources of the spacecraft can be from solar light or a rain of energetic particles from the universe. The common features of these energies are that the amount of energy on the locally small area is little and is not usually stable and therefore useless. The amount of energy over a large area becomes larger and useful if it is collected effectively and stored safely.

Many solar modules have been developed to transfer solar light into electricity [1]. If every identical renewable energy is converted into dc electric energy by highly efficient dc-to-dc or ac-to-dc converters with maximum power point tracking (MPPT) [2–3], high regenerative power supply could be traditionally created by directly connecting these dc sources in parallel, in series, or in series-parallel via dc mains. However, the series and parallel circuit networks have some drawbacks, such as the reduction of power collection efficiency resulting from connecting a large number of nonideal sources, the ratings of sources, and the complexity of network construction increasing with increasing the number of sources, etc. Additionally, the series-parallel combined structure has the potential of optimum power collection efficiency, but there are still some problems that once some unbalanced power supply modules happen, this makes the defect or weak modules inversely get charged. It had been found that adding a great number of blocking diodes and bypass diodes into these traditional network system protects each power source from being charged [4]. However, these diodes contribute to energy loss, which cannot be negligible in the case of large amount of sources.

The presented two-dimensional ac-type power collection network system is simply created by using the shunt connection to connect transmission lines (TLs) (such as the coaxial cables) in parallel like a tree with its branches regularly branching out all around. By utilization of the TL theory and the concept similarly used in the phase-array antenna, the power coming from every cell is automatically accumulated and directed toward the target load along the tree-like network. It is to be emphasized that all the cell units share the same single minimum voltage and current rating of the system while the absolute maximum of voltage and current exist only at the output target load of network; the TL network itself linearly bears the increased voltage and current. The proposed tree-like network system has the attractive features of simple structure, easy construction and maintenance, and low cost, because only two kinds of parts, ac current sources and m-to-1 TL branch connection parts, are used in the whole system.

This work addresses the tree-like two-dimensional TL structure in Section II. Comparing this tree-like

network system with comb-like network systems, which have been proposed in [6–8], the comb-like systems are found to be difficult in construction and maintenance because sources inside the system have different voltage, current, and power ratings and have different power factors. This newly presented tree-like network is a much improved system over the comb-like networks and the conventional series-parallel combined dc networks.

It has been shown that the presented tree-like network system has higher power collection efficiency with growing the equivalent output impedance of current cell. Section III describes one of many possible methods to implement ac current sources having high output impedance, i.e., to cascade the phase-controlled series-resonant voltage inverter having low output impedance, for example, with the voltage source to current source converter and the step-up transformer into the phase-controlled resonant current source cell.

The simulated results in Section IV show that lump-type low-pass  $\pi$ - or T-circuit with high characteristic impedance, which is used for the voltage source to current source converter in the current cell, improve the efficiency of the voltage inverter, filter out harmonics, and increase the output impedance of the whole current cell.

## II. TREE-LIKE TRANSMISSION LINE NETWORK SYSTEMS

## A. Important Properties of a Quarter-Wavelength Transmission Line

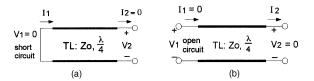
The input impedance of a lossless TL having the characteristic impedance  $Z_O$  and the length l, and terminated by a load  $Z_L$  is

$$Z_{i} = Z_{O} \frac{Z_{L} + jZ_{O} \tan(\beta l)}{Z_{O} + jZ_{L} \tan(\beta l)}$$
 (1)

where  $\beta$  is the phase constant,  $\lambda$  is the wavelength, and  $\beta = 2\pi/\lambda$ . A quarter-wave lossless TL is described by an important relation:

$$Z_i = \frac{Z_O^2}{Z_I}. (2)$$

Fig. 1(a)–(b) shows a quarter-wave lossless TL terminated with two different terminations at port 1: the short-circuit terminal and the open-circuit terminal. A quarter-wave lossless TL converts the load impedance into an input impedance by (2). So, a quarter-wave lossless TL, which is terminated with an open circuit, has a short circuit impedance at the input terminals, and a quarter-wave lossless TL, terminated with a short-circuit, has an open-circuit input impedance. In Fig. 1(a), we have the phasor voltage and current relationships between the input



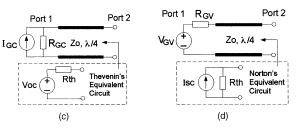


Fig. 1. Equivalent circuits of quarter-wave lossless TL, which is terminated with different loads at port 1. (a) Short circuit. (b) Open circuit. (c) Parallel-connection pair of  $I_{GC}$  and  $R_{GC}$ . (d) Series-connection pair of  $V_{GV}$  and  $R_{GV}$ .

and output ports:

$$V_2 = Z_O I_1 \exp\left(-j\frac{\pi}{2}\right) \tag{3}$$

and  $V_1 = 0$  and  $I_2 = 0$ . Similarly, we determine in Fig. 1(b):

$$I_2 = \frac{V_1}{Z_O} \exp\left(-j\frac{\pi}{2}\right) \tag{4}$$

and  $I_1 = 0$  and  $V_2 = 0$ .

Fig. 1(c) shows that a current source, which has a short-circuit output current  $I_{GC}$  and an internal impedance  $R_{GC}$ , is at the port 1, and based on (2)–(3), the Thevenin's equivalent circuit at port 2, looking backward into TL, is

$$V_{oc} = Z_O I_{GC} \exp\left(-j\frac{\pi}{2}\right)$$
 and  $R_{th} = \frac{Z_O^2}{R_{GC}}$ . (5)

In addition, Fig. 1(d) shows that a quarter-wave TL is terminated by a voltage source, which has the open-circuit output voltage  $V_{GV}$  and an internal impedance  $R_{GV}$  at port 1, and based on (2) and (4), the Norton's equivalent circuit at port 2 has

$$I_{sc} = \frac{V_{GV}}{Z_O} \exp\left(-j\frac{\pi}{2}\right)$$
 and  $R_{th} = \frac{Z_O^2}{R_{GV}}$ . (6)

Equations (5)–(6) facilitate the analysis of the tree-like TL network systems in the next section.

### B. Analysis of Tree-Structure Network

Fig. 2(a) shows a small system of the tree-like TL power collection network which contains successive 5 layers in total with 3-to-1 branch connection at each joint. Each segment of TL has the length of  $\lambda/4$  and characteristic impedance  $Z_O$ . All the distributed power sources are unified and identical ac current

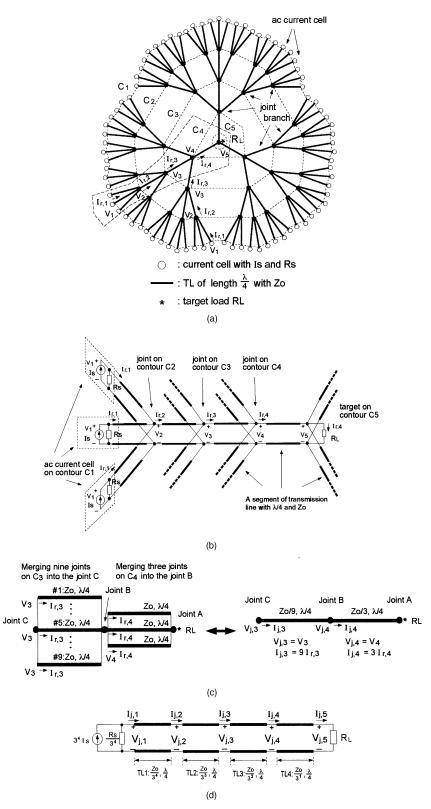


Fig. 2. Graph for tree-like TL network system has 5 layers with 3-to-1 branch connection at each joint (T-TLNS-5-3). (b) Illustration explains practical connection of T-TLNS-5-3. (c) Those TLs between two merging joints can be equivalently lumped into one segment of TL. (d) Equivalent TL circuit derived from applying merger procedure to T-TLNS-5-3.

cells, which has an output current  $I_S$  and an internal impedance  $R_S$ . The system target load is  $R_L$ . The tree-like system has an arrangement of the central-symmetry with respect to  $R_L$ . Fig. 2(b) illustrates

the practical connection of the tree-like network. It has 5 layers, and each layer is indicated by a dotted-line contour  $C_k$ . All current cells are connected to the contour  $C_1$ , contours  $C_2$  to  $C_4$ 

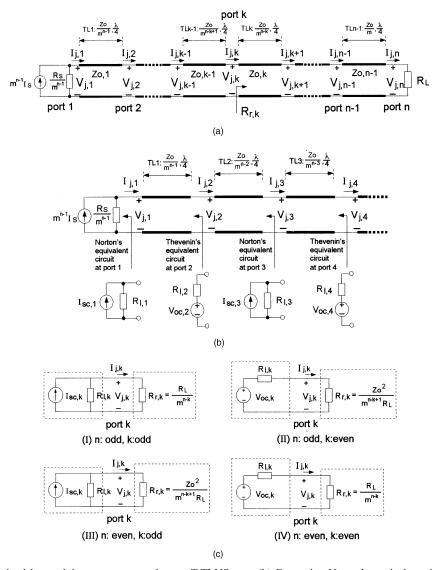


Fig. 3. TL circuit obtained by applying merger procedure to T-TLNS-n-m. (b) Determine Norton's equivalent circuit for odd port k and Thevenin's equivalent circuit for even port k. (c) Equivalent circuit at kth port has four possible circuits which are dependent on pair of integers n and k being odd or even.

contain joints only, and the contour  $C_5$  contains one joint and the target  $R_L$ . We have derived a generalized tree-like TL network system, which has n layers in total with m-to-1 branch connection at each joint, and is abbreviated by **T-TLNS-**n-m. The tree network system shown in Fig. 2(a) has 5 layers with 3-to-1 branch connection at each joint. It is therefore represented by T-TLNS-5-3.

All current cells are synchronized with one another, and it makes every joint on the same contour  $C_k$  have the same phasor voltage, denoted by  $V_k$ , and the same phasor current toward the target, denoted by  $I_{r,k}$ . Merging together those joints on the same contour does not affect the stability of the system. Fig. 2(c) illustrates that three joints on  $C_4$  are merged into joint B, and it makes three TLs become the parallel arrangement between joint A and B. These

three lines can be represented by one segment of TL whose characteristic impedance is  $Z_O/3$ , and the merging TL has the relations of  $V_{j,4} = V_4$  and  $I_{j,4} = 3I_{r,4}$ . When merging nine joints on  $C_3$  into joint C, the parallel connection of nine TLs between joint B and C is equivalent to one segment of TL whose characteristic impedance is  $Z_O/9$ , and this merging line has the equations of  $V_{j,3} = V_3$  and  $I_{j,3} = 3^2I_{r,3}$ . The same merger procedure applies to the other contours of T-TLNS-5-3. Especially, merging  $3^4$  current cells is equivalent to one current source whose output current and internal impedance are  $3^4I_S$  and  $R_S/3^4$ , respectively. The equivalent TL circuit is shown in Fig. 2(d).

Similarly, the TL circuit, as shown in Fig. 3(a), is derived from the application of the merger procedure described previously to T-TLNS-n-m. The characteristic impedances of n-1 segments of

quarter-wavelength TL become a power series:

$$Z_{O,1} = \frac{Z_O}{m^{n-1}}, \qquad Z_{O,2} = \frac{Z_O}{m^{n-2}},$$

$$Z_{O,3} = \frac{Z_O}{m^{n-3}}, \dots, Z_{O,n-1} = \frac{Z_O}{m^1}$$
(7)

where  $Z_{O,k}$  is the characteristic impedance of the kth segment of TL,  $TL_k$ . In Fig 3(a), the  $V_{j,k}$  and  $I_{j,k}$  have relationships with  $V_k$  and  $I_{r,k}$  of T-TLNS-n-m as follows:

$$V_{ik} = V_k \tag{8}$$

$$I_{j,k}$$
 = (Number of branch TLs between  $C_k$  and  $C_{k+1}$ )  $\cdot I_{r,k}$   
=  $m^{n-k} \cdot I_{r,k}$  (9)

where k is from 1 to n.

Fig. 3(b) illustrates that the equivalent circuit at port k, looking in the direction of source, could be the Norton's equivalent circuit for the odd port k, which has

$$\begin{cases} I_{sc,k} = m^{n-(k+1)/2} I_S \exp\left(-j\frac{(k-1)\pi}{2}\right) \\ R_{l,k} = \frac{R_S}{m^{n-k}} & \text{for an odd integer } k \end{cases}$$
 (10)

and the Thevenin's equivalent circuit for the even port k, which has

$$\begin{cases} V_{oc,k} = m^{(k-2)/2} I_S Z_O \exp\left(-j\frac{(k-1)\pi}{2}\right) \\ R_{l,k} = \frac{1}{m^{n-k+1}} \cdot \frac{Z_O^2}{R_S} & \text{for an even integer } k \end{cases}$$
(11)

as based on (2) and (5)–(6). In addition, the definition of  $R_{r,k}$  is the equivalent input impedance at port k, obtained by looking toward the target  $R_L$ , and it is written as

$$R_{r,k} = \begin{cases} \frac{1}{m^{n-k}} \cdot R_L & \text{for an even integer } (n-k) \\ \frac{1}{m^{n-k+1}} \cdot \frac{Z_O^2}{R_L} & \text{for an odd integer } (n-k) \end{cases}$$

By combining (10)–(11) with (12), the equivalent circuit at port k has four possible circuits and each is dependent on the pair of integer n and k being even or odd, as shown in Fig. 3(c). They facilitate the determination of the  $V_{j,k}$  and  $I_{j,k}$ . Then,  $V_k$  and  $I_{r,k}$  of T-TLNS-n-m can be derived from (8)–(9). We define the notation of  $P_{r,k} = \frac{1}{2}V_k\overline{I}_{r,k}$  as the complex power transmitting toward the target  $R_L$  at each joint of the contour  $C_k$ , where  $\overline{I}_{r,k}$  is the complex conjugate of  $I_{r,k}$ . We summarize  $V_k$ ,  $I_{r,k}$ , and  $P_{r,k}$  for each joint on the contour  $C_k$  as follows.

For the T-TLNS-n-m having even n layers,
 a) if the joint on the odd contour C<sub>k</sub>, i.e., k is odd,

then

$$V_k = m^{(k-1)/2} \frac{I_S R_S Z_O^2}{m R_S R_L + Z_O^2} \exp\left(-j \frac{k-1}{2} \pi\right)$$
 (13)

$$I_{r,k} = m^{(k+1)/2} \frac{I_S R_S R_L}{m R_S R_L + Z_O^2} \exp\left(-j\frac{k-1}{2}\pi\right)$$
 (14)

$$P_{r,k} = \frac{1}{2} m^k \frac{|I_S|^2 R_S^2 R_L Z_O^2}{(mR_S R_L + Z_O^2)^2}$$
 (15)

b) if the joint on the even contour  $C_k$ , i.e., k is even, then

$$V_k = m^{k/2} \frac{I_S R_S R_L Z_O}{m R_S R_L + Z_O^2} \exp\left(-j \frac{k-1}{2} \pi\right)$$
 (16)

$$I_{r,k} = m^{k/2} \frac{I_S R_S Z_O}{m R_S R_L + Z_O^2} \exp\left(-j \frac{k-1}{2} \pi\right)$$
 (17)

$$P_{r,k} = \frac{1}{2} m^k \frac{|I_S|^2 R_S^2 R_L Z_O^2}{(mR_S R_L + Z_O^2)^2}.$$
 (18)

- 2) For the T-TLNS-*n*-*m* having odd *n* layers,
- a) if the joint on the odd contour  $C_k$ , i.e., k is odd, then

$$V_k = m^{(k-1)/2} \frac{I_S R_S R_L}{R_S + R_L} \exp\left(-j\frac{k-1}{2}\pi\right)$$
 (19)

$$I_{r,k} = m^{(k-1)/2} \frac{I_S R_S}{R_S + R_L} \exp\left(-j\frac{k-1}{2}\pi\right)$$
 (20)

$$P_{r,k} = \frac{1}{2} m^{k-1} \frac{|I_S|^2 R_S^2 R_L}{(R_S + R_L)^2}$$
 (21)

b) if the joint on the even contour  $C_k$ , i.e., k is even, then

$$V_k = m^{(k-2)/2} \frac{I_S R_S Z_O}{R_S + R_L} \exp\left(-j\frac{k-1}{2}\pi\right)$$
 (22)

$$I_{r,k} = m^{k/2} \frac{I_S R_S R_L}{Z_O(R_S + R_L)} \exp\left(-j\frac{k-1}{2}\pi\right)$$
 (23)

$$P_{r,k} = \frac{1}{2} m^{k-1} \frac{|I_S|^2 R_S^2 R_L}{(R_S + R_L)^2}.$$
 (24)

## C. Important Properties

Note that the ratio of  $|V_{k+1}|/|V_k|$  and  $|I_{r,k+1}|/|I_{r,k}|$  of T-TLNS-n-m are out of all relation to an internal impedance  $R_S$  of current cell. When the target load satisfies the condition of  $1/m < R_L/Z_0 < 1$ , the amplitudes of voltage  $V_k$  and current  $I_{r,k}$  increase in the direction of the target load, as derived from the conditions of  $|V_{k+1}|/|V_k| > 1$  and  $|I_{r,k+1}|/|I_{r,k}| > 1$ . It implies that cell units share the absolute minimum voltage and current rating of the complete system while the absolute maximum voltage and current in the complete T-TLNS-n-m occur at the target load. Moreover, the TL network itself linearly bears the difference between absolute extremes of voltage drop and current flow. Fig. 4 shows the simulation

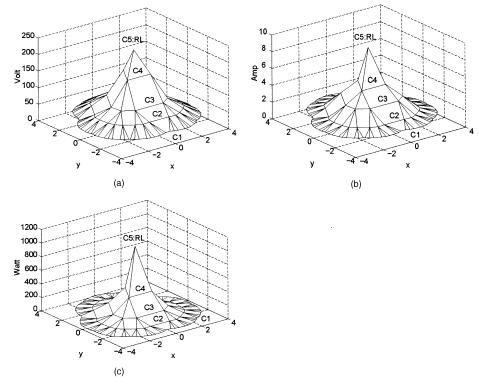


Fig. 4. Three-dimensional plots of (a)  $|V_k|$ , (b)  $|I_{r,k}|$ , (c)  $|P_{r,k}|$  of T-TLNS-5-3 at  $Z_O = 50\Omega$ ,  $R_L = 25\Omega$ ,  $I_S = 1 \exp(-j0)A$ , and  $R_S = \infty$ , where xy-plane represents position of cells or joints and z-axis stands for amplitude.

results of T-TLNS-5-3 at  $I_S = 1 \exp(-j0)A$ ,  $R_S = \infty$ ,  $Z_O = 50\Omega$ , and  $R_L = 25\Omega$  to illustrate the previous analysis.

Note that the maximum of  $|P_{r,k}|$  equals  $\frac{1}{8}3^{k-1}|I_S|^2R_S$ , which locates at the condition of  $mR_SR_L=Z_O^2$  for T-TLNS-n-m having even n layers and at the condition of  $R_L=R_S$  for T-TLNS-n-m having even n layers. For a fixed value of  $R_S$ ,  $R_L$  at the extreme point of  $|P_{r,k}|$  has relation to the number of branches m and the characteristic impedance  $Z_O$  for the systems having even n.

In addition,  $P_{r,k}$  is real because  $V_{r,k}$  is in phase with  $I_{r,k}$ . The magnitude of  $P_{r,k}$  is growing with increasing  $R_S$ ; that means that the larger the internal impedance  $R_S$  of nonideal cell, the more power the system collects. The fact of  $|P_{r,k+1}| = 3 \cdot |P_{r,k}|$  emphasizes that the T-TLNS-n-m is capable of accumulating the small power cell step by step in the direction of the system target  $R_L$  and forms large amount of power at  $R_L$ .

It had been shown that this tree-like network has the same efficiency as the conventional series-parallel combined dc networks. Moreover, one of the important features of T-TLNS-*n-m* is that when damaged cells appear and are short circuited, the self-stability makes some sources sustain additional power to compensate for the power which is supposed to be supplied by those damaged cells. It makes the tree-like network with some damaged cells provide almost the same amount of power as the system without any damaged cells. Although this network

system has the same collection efficiency as the optimum series-parallel networks, from other system points of view, the proposed tree-like T-TLNS-*n*-*m* is much better than the traditional series-parallel networks [9].

## III. IMPLEMENTATION OF AC CURRENT CELL

## A. Voltage Source to Current Source Converter

1) Quarter-Wave Lossless TL: A segment of quarter-wavelength lossless TL can be considered as a voltage source to current source converter (V-to-C converter). We define  $Z_{O,C}$  as the characteristic impedance of V-to-C converter. Fig. 5 shows that the V-to-C converter links the load  $R_{L,N}$  and the ac voltage source which has an open-circuit voltage  $V_{OC}$  and an internal source impedance  $R_{in}$ . The output current  $I_O$  through  $R_{L,N}$  is obtained by using (6):

$$I_O = \frac{Z_{O,C}^2}{Z_{O,C}^2 + R_{in}R_{L,N}} \cdot \frac{V_{OC}}{Z_{O,C}} \exp\left(-j\frac{\pi}{2}\right).$$
 (25)

The smaller value of  $R_{in}$  and the larger value of  $Z_{O,C}$  are chosen so that  $I_O$  approaches the phasor value  $V_{OC}/Z_{O,C} \exp(-j(\pi/2))$ . If  $10R_{in}R_{L,N} \leq Z_{O,C}^2$  holds, the magnitude of  $I_O$  can have less than 1% deviation from the value of  $|V_{OC}/Z_{O,C}|$ . In this way,  $I_O$  is almost independent of  $R_{L,N}$ . Therefore, the larger  $Z_{O,C}$  value is selected so that the V-to-C converter would convert

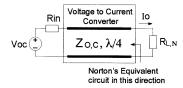


Fig. 5. Quarter-wave lossless TL is used for V-to-C converter.

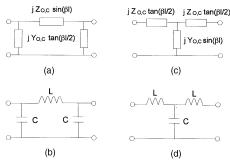


Fig. 6. (a) Equivalent  $\pi$  circuit, (b) nominal  $\pi$  circuit, (c) equivalent T circuit, (d) nominal T circuit of quarter-wave lossless TL.

one nonideal ac voltage source into one ac current source which is as close to the ideal case as possible.

2) Equivalent Lumped Circuits of Quarter-Wave Lossless TL: A segment of lossless TL used as the V-to-C converter, can be represented by the equivalent  $\pi$  circuit, as shown in Fig. 6(a), where the series arm has the impedance of  $jZ_{O,C}\sin(\beta l)$  and the two shunt arms have the same admittance of  $jY_{O,C}\tan(\beta l/2)$ . For the quarter-wave lossless TL, we have  $\beta l = \pi/2$ , and hence, the impedance of the series arm is  $jZ_{O,C}$  and the admittance of the shunt arm is  $jY_{O,C}$ .

The nominal  $\pi$  circuit in Fig. 6(b) at a frequency  $f_s = \omega_s/2\pi$  is requested to be equivalent to the equivalent  $\pi$  circuit of a quarter-wave lossless line, where  $f_s$  must satisfy the relationship of  $f_s \cdot \lambda = \mu_p$  and  $\mu_p$  is the phase velocity. Therefore, the series arm and the shunt arms satisfy the relations of  $j\omega_s L = jZ_{O,C}$  and  $j\omega_s C = jY_{O,C}$ , and we have the design formula as follows:

$$L = \frac{Z_{O,C}}{\omega_s} \quad \text{and} \quad C = \frac{1}{\omega_s Z_{O,C}}.$$
 (26)

Similarly, the equivalent T circuit shown in Fig. 6(c) can also be used as an equivalent circuit of the quarter-wave lossless line. The nominal T circuit in Fig. 6(d) is to have its shunt capacitor and series inductors satisfy the relationship of  $Z_{O,C} = \omega_s L = 1/\omega_s C$ . The values of series inductance L and the shunt capacitance C of the nominal T circuit are the same as those of the nominal  $\pi$  circuit.

# B. Phase-Controlled Full-Bridge Series-Resonant Voltage Inverter

We analyze the output equivalent circuit of the phase-controlled full-bridge series-resonant

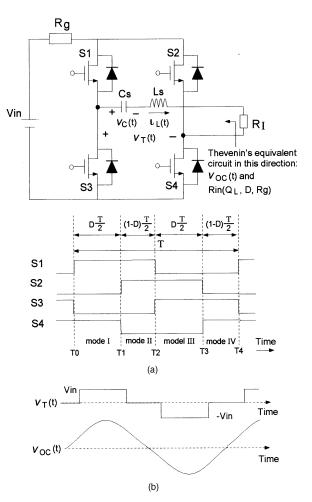


Fig. 7. (a) Phase-controlled full-bridge series-resonant voltage inverter. (b) Waveform of fundamental component of  $v_T(t)$  is output voltage  $v_{OC}(t)$  with  $R_I$  open circuited.

inverter whose four switches operate at the same frequency as the series-resonant load. Fig. 7 shows the phase-controlled full-bridge series resonant voltage inverter and the gate drive voltage waveforms of the four switch transistors in the bridge. Switching leg, including  $S_1$  and  $S_3$ , is loaded capacitively. Switches  $S_1$  and  $S_3$  are thus zero-current switching (ZCS) and suffer from turn-on loss but no turn-off loss. Additionally, switches  $S_2$  and  $S_4$  are zero-voltage switching (ZVS), and they have the turn-off loss and no turn-on loss, because the other switch leg is loaded inductively.

It is assumed that the components  $L_S$ ,  $C_S$ , and four switches are lossless, and  $R_g$  is an internal impedance of dc voltage source. The four switches operate at the same frequency  $f_{sw}$  as the load series-resonant frequency  $f_r$ . D is defined as the duty cycle of the quasi-square wave applied to the tank, and (1-D) corresponds to the relative phase shift among the switches of the bridge. We control the output load voltage by varying D.

The equivalent output circuit of the voltage inverter contains the open-circuit voltage,  $v_{QC}(t)$ , and

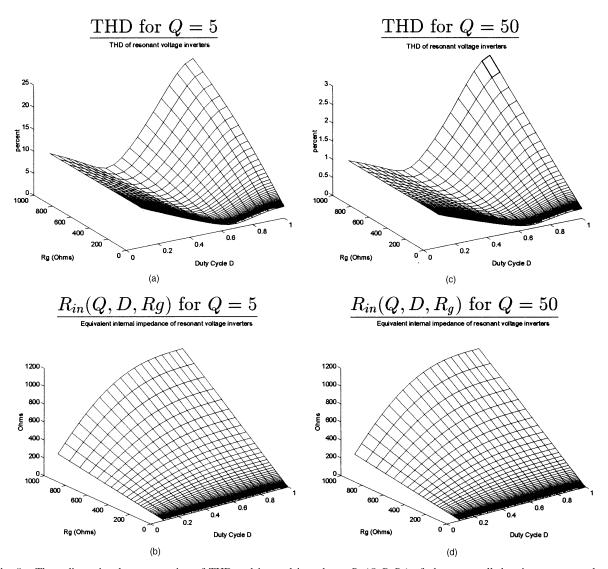


Fig. 8. Three-dimensional representation of THD and internal impedance  $R_{in}(Q,D,R_g)$  of phase-controlled series-resonant voltage inverter versus D and  $R_g$  at (a)–(b) Q=5 and (c)–(d) Q=50.

the output impedance,  $R_{in}$ , connected in series. Since  $f_{sw} = f_r$ , the series resonant tank has zero phase shift at fundamental frequency, and the output impedance of inverter is purely resistive and is a function of Q, D, and  $R_g$ . We denote the output impedance by  $R_{in}(Q,D,R_g)$ .

To determine  $v_{OC}(t)$  mathematically, let the series-resonant inverter operating at  $f_{sw} = f_r$  have the loaded quality factor Q:

$$Q = \frac{\omega_r L_S}{R_I} = \frac{1}{\omega_r C_S R_I}$$
 (27)

where  $\omega_r = 2\pi f_r = 1/\sqrt{L_S C_S}$ . It is assumed that Q is such a large value that the high-frequency harmonics at the output of the inverter are negligible. With  $R_I$  open-circuited, the fundamental component of the voltage  $v_T(t)$  applied to the tank is equal to  $v_{QC}(t)$ 

$$v_{OC}(t) = \frac{4}{\pi} \cdot V_{in} \cdot \sin\left(\frac{\pi}{2}D\right) \cdot \sin(2\pi f_{sw}t). \tag{28}$$

The magnitude of  $v_{OC}(t)$  is controlled by the duty cycle D and is proportional to the sin function of D. The phase-controlled voltage inverter is inherently a voltage source because  $v_{OC}(t)$  does not vary with the load  $R_I$  under high Q.

With  $R_I$  connected, the fundamental component of  $i_L(t)$  is denoted by  $i_{L,f}(t)$ . We get  $R_{in}(Q,D,R_g)$  by using the following relation

$$i_{L,f}(t) = \frac{v_{OC}(t)}{R_{in}(Q, D, R_g) + R_I}$$

$$\Rightarrow R_{in}(Q, D, R_g) = \frac{v_{OC}(t)}{i_{L,f}(t)} - R_I.$$
 (29)

The voltage inverter is simulated under the conditions of different values of  $R_g$ , D, and Q. Fig. 8 shows the total harmonic distortion (THD) of the output current through  $R_I$  and an internal impedance  $R_{in}$  versus  $R_g$  and D at Q = 5 and Q = 50. Note that THD is decreased with increasing Q and the minimum

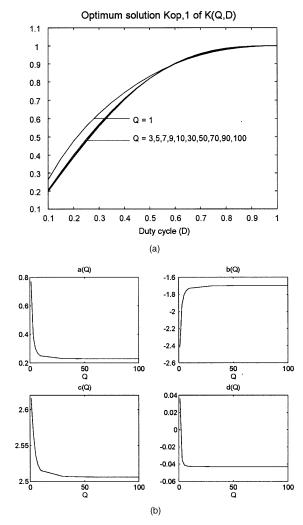


Fig. 9. Optimum solution  $K_{op,1}(Q,D)$  of K(Q,D) of  $R_{in}(Q,D,R_g) = K(Q,D) \cdot R_g$  in least-square error sense. (b) Polynomial of  $a \cdot Q^3 + b \cdot Q^2 + c \cdot Q + d$  is used to fit curves of  $K_{op,1}$  in least-square error sense.

of THD locates at about D=0.7. The curves of  $R_{in}(Q,D,R_g)$ , which are linearly increased with  $R_g$ , is to be fitted with the relation of  $R_{in}(Q,D,R_g)=K(Q,D)\cdot R_g$  in a least-square error sense. The optimum solutions of K(Q,D), denoted by  $K_{op,1}$ , are plotted in Fig. 9(a). To describe it mathematically, we define a polynomial of degree 3 as  $K_{op,2}=a\cdot D^3+b\cdot D^2+c\cdot D+d$ . and let  $K_{op,2}=K_{op,1}(Q,D)$ , after solving the coefficients of the polynomial in a least-square error sense to each case of Q. Fig. 9(b) shows the plots of the coefficients a,b,c, and d versus Q and coefficients approach the constant value for high Q values. We can estimate the output impedance  $R_{in}$  of the inverter for  $Q \geq 5$  as:

$$R_{in}(Q, D, R_g) = (0.3D^3 - 1.8D^2 + 2.5D - 0.04) \cdot R_g.$$
(30)

The effect of the internal impedance  $R_g$  of dc voltage source on the output impedance of the inverter is nonlinear. The output equivalent circuit of the

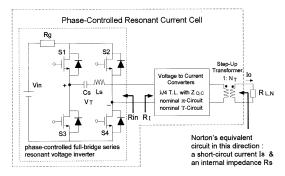


Fig. 10. Phase-controlled resonant current cell contains three cascaded stages of phase-controlled full-bridge series-resonant voltage inverter, V-to-C converter, and step-up transformer.

inverter is therefore determined and is described by (28) and (30).

## C. Phase-Controlled Resonant Current Cell

It has been found that the phase-controlled series and series-parallel resonant inverter in [12–13] have much smaller output impedance than the phase-controlled parallel resonant inverter in [14]. It is noted that cells in T-TLNS-n-m should have large output impedance to improve the power collection efficiency. A simple voltage inverter is not qualified for our tree-like network system. The phase-controlled series-resonant voltage inverter in this work has the output impedance as nonlinear function of the internal resistance  $R_{o}$  of dc voltage source, and its output impedance is usually low because large stabilized shunt capacitor is used to represent dc source. One of the main purposes of this section is to present a method to change the low output impedance of the voltage inverter into the high output impedance.

Fig. 10 shows that the voltage inverter is cascaded with the V-to-C converter and the step-up transformer with a ratio of  $N_T$ . Equation (25) states that the V-to-C converter can convert the voltage source with low output impedance into the current source with high output impedance by increasing  $Z_{O,C}$ . The step-up transformer magnifies the impedance again in addition to providing the electric isolation. We call the circuit in Fig. 10 a practical ac current source cell.

Based on (6), (28), and (30), we can obtain the equivalent output circuit of the current cell for  $Q \ge 5$  as follows:

$$I_{S} = \frac{V_{oc}}{N_{T}Z_{O,C}} \exp\left(-j\frac{\pi}{2}\right)$$

$$= \frac{4V_{in}}{\pi N_{T}Z_{O,C}} \sin\left(\frac{\pi}{2}D\right) \exp\left(-j\frac{\pi}{2}\right) \qquad (31)$$

$$R_{S} = \frac{N_{T}^{2}Z_{O,C}^{2}}{R_{in}(Q,D,R_{g})}$$

$$= \frac{N_{T}^{2}Z_{O,C}^{2}}{(0.3D^{3} - 1.8D^{2} + 2.5D - 0.04) \cdot R_{g}}. \qquad (32)$$

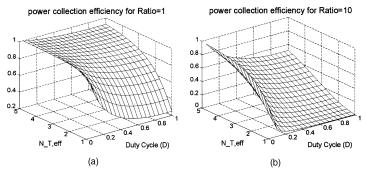


Fig. 11. Three-dimensional representation of power collection efficiency  $\psi_{N,L}$  of T-TLNS-*n-m* versus  $N_{t,eff}$  and D at (a) Ratio = 1 and (b) Ratio = 10.

The current cell is required to have larger internal impedance  $R_S$  so as to behave closer to that of the ideal ac current source. It can be achieved by selecting the small value of  $R_g$  and large value of D or increasing  $Z_{O,C}$  and the ratio  $N_T$ .

It is found that if the current cell contains the low-Q phase-controlled series-resonant voltage inverter and a quarter-wavelength lossless TL section as the V-to-C converter, the choice of low Q value in the voltage inverter achieves high efficiency, but low Q circuit is rich in harmonics which is not good for the power collection system. Since the TL section does not reduce the hamonics effectively, the low-pass nominal  $\pi$  or T circuit in Fig. 6 are used as the V-to-C converter to filter out the harmonics and to obtain a synchronous, single frequency current cell system.

## IV. SIMULATED RESULTS

By substituting k=n into (18) and (21), the derived  $P_{r,n}$  is the the power received by the target  $R_L$  in T-TLNS-n-m. The notation of  $P_{L,ideal}$  represents the power received by  $R_L$  under  $R_L \neq 0$  and  $R_S = \infty$ . The denotation of  $\psi_{N,L}$  is defined as the ratio of  $P_{r,n}$  to  $P_{L,ideal}$  and called the power collection efficiency of T-TLNS-n-m. As the resonant current inverter in Fig. 10 is in place of all cells in T-TLNS-n-m, we can obtain  $\psi_{N,L}$ :

$$\psi_{N,L} = \left(1 + \frac{f(D)}{N_{T,eff}^2} \cdot \text{Ratio}\right)^{-2} \tag{33}$$

where

$$f(D) = 0.3D^3 - 1.8D^2 + 2.5D - 0.04$$
 (34)

$$N_{T,eff} = \begin{cases} \sqrt{m} \cdot N_T & \text{for an even integer } n \\ N_T & \text{for an odd integer } n \end{cases}$$
(35)
$$\text{Ratio} = \begin{cases} \frac{R_g \cdot Z_O^2}{R_L \cdot Z_{O,C}^2} & \text{for an even integer } n \\ \frac{R_g \cdot R_L}{Z_{O,C}^2} & \text{for an odd integer } n \end{cases} .$$

The simulated results of the power collection efficiency of T-TLNS-n-m are shown in Fig. 11. The power collection efficiency for a small Ratio value is higher than that for a large Ratio value. And, the efficiency is very sensitive to the variations of  $N_{T,eff}$  and D at the case of the large Ratio.

For the case of T-TLNS-5-3, it is assumed that all transmission lines in the tree-like network have  $Z_O = 50\Omega$  and the system target load is  $R_L = 50\Omega$ . Note that the load impedance of current cell is  $R_{L,N} = V_1/I_{r,1} = R_L$ , as derived from dividing (19) by (20), and the load impedance of voltage inverter equals  $R_I = Z_{O,C}^2/R_{L,N}$ . The circuit parameters of the phase-controlled full bridge series-resonant voltage inverter are  $V_{in} = 100$  V,  $R_g = 10\Omega$ , D = 0.26,  $f_{sw} = 1$  MHz and Q = 5, and  $L_S = 0.159$  mH and  $C_S = 796$  pF are obtained by (27). Additionally, the V-to-C converter has  $Z_{O,C} = 100\Omega$ , and its nominal  $\pi$ -circuit and nominal T circuit have L = 15.9 uH and C = 159 pF as given by (26). The turn ratio of the step-up transformer is set to  $N_T = 1$ . It is derived that the current cell has the short-circuit current  $I_S = 0.5 \cdot \exp(-j(\pi/2))$  A and the output impedance  $R_S = 2026\Omega$ , as obtained by (31)–(32).

The SPICE simulation results of T-TLNS-5-3 described above are shown in Fig. 12. It has excellent agreement with the previous analysis of T-TLNS-n-m. Additionally, the caculated efficiency of T-TLNS-5-3 is  $\psi_{LN}$  = 98.6%. The THD is calculated by taking into account from the second harmonic to the tenth harmonic together. The simulation results in Fig. 12 point out that THD of  $v_k(t)$  and  $i_{r,k}(t)$  of T-TLNS-n-m for the lump-type low-pass V-to-C converter, such as the nominal  $\pi$  and T circuit, is much small than that for the TL-type V-to-C converter. Note that if the low-pass nominal  $\pi$ - or T-circuit are used for the V-to-C converter in the current cell, the low-Q series-resonant voltage inverter is selected to achieve high efficiency and the harmonics from the low-Q voltage inverter can be reduced effectively by the next stage of the low-pass  $\pi$  or T circuit. Thus the high-efficiency and low-harmonic characteristics can be obtained by cascading low-O series-resonant

(36)

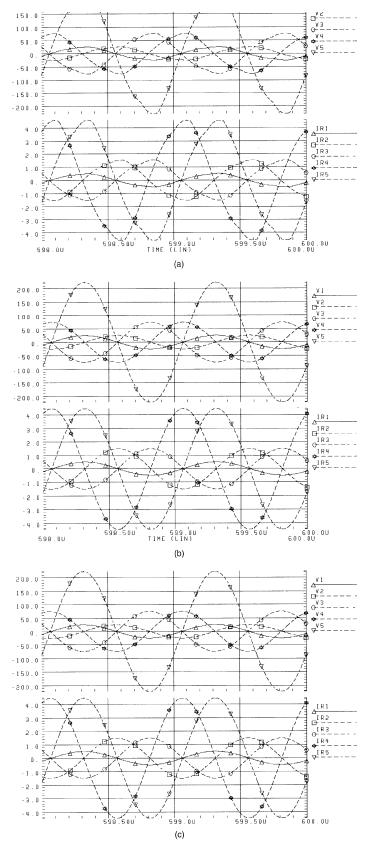


Fig. 12. SPICE simulation results of T-TLNS-5-3, where every resonant current cell has  $f_{sw}=1$  MHz, D=0.26,  $V_{in}=100$  V,  $R_g=10\Omega$ , Q=5,  $L_S=0.159$  mH,  $C_S=796$  pF,  $Z_{O,C}=100\Omega$  (L=15.9 uH and C=159 pF) and  $N_T=1$ , and tree-like network has  $Z_O=50\Omega$  and target  $R_L=50\Omega$ . Simulated results of T-TLNS-5-3 are under different types of V-to-C converters: (a) quarter-wave lossless TL section, (b) nominal  $\pi$  circuit, and (c) nominal T circuit. THD of  $v_k(t)$  and  $i_{r,k}(t)$  are about (a) 6.2%, (b) 0.22%, (c) 0.33%. Upper panel: waveforms of  $v_k(t)$ . Lower panel: waveforms of  $i_{r,k}(t)$ .

voltage inverter with the lump-type low-pass  $\pi$  or T filter

Another important fact is that the equivalent load impedance,  $R_I$ , of the series-resonant voltage inverter is  $R_I = Z_{O,C}^2/R_{L,N}$ . The Q value of the voltage inverter can be reduced by increasing  $Z_{O,C}$ , that is, the V-to-C converter equivalently increase the efficiency of the voltage inverter. It is obvious that the low-pass  $\pi$  or T filter with high- $Z_{O,C}$  is used in the current cell to improve the efficiency of the voltage inverter, to filter out the harmonics, and to increase the output impedance of the whole current cell.

Therefore, those inverters which have lower output impedance can be increased to high value by cascading the low-pass type  $\pi$  or T circuit and the step-up transformer. Thus, a new system of high power collection efficiency, low cost in maintenance and easy in implementation is presented conceptually.

## V. CONCLUSIONS

This paper present a new generalized tree-like TL network system for automatically accumulating identically small power cells, which are distributed over very large areas, into large power amount at the target load along a special TL network. The tree-like network system has the attractive features of simple structure, easy construction and maintenance, and low cost, because only two kinds of parts, ac current sources and *m*-to-1 TL branch connection parts, are used in the whole system, and they are suitable for the mass production and should be passed through a hard reliability test process before shifting out. Thus, the system is low cost and reliable in nature that is suitable for use in future space craft.

It has been shown that the higher the output impedance of current cell, the better the power collection efficiency of T-TLNS-*n-m*. We propose a method to increase the output impedance of inverters by cascading the V-to-C converter and the step-up transformer. For example, the proposed phase-controlled resonant current cell, which is constructed by cascading three stages of the phase-controlled full-bridge series-resonant voltage inverter, the V-to-C converter and the step-up transformer, can achieve the high output impedance.

Increasing the characteristic impedance of the V-to-C converter is equivalent to lower the loaded quality factor, i.e., to increase the efficiency of the series-resonant voltage inverter. The harmonics resulting from the low-Q series-resonant voltage inverter should be avoided entering the tree-like TL network and forming the standing wave in network, which could damage the sources. Reducing the interference of harmonics and improving high efficiency of the series-resonant voltage inverter can

be achieved by cascading the low-pass nominal  $\pi$  or T circuit with high characteristic impedance.

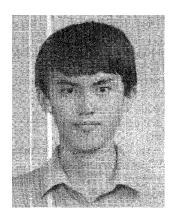
This work contributes to the important concept that there exist other methods than that of the conventional series-parallel combined dc power collection system that is used to collect many small power cells. The new one proposed here can also effectively collect the power. A practical implementation of the T-TLNS-*n-m* to prove its feasibility and to check its excellence and reliability are expected in a future work.

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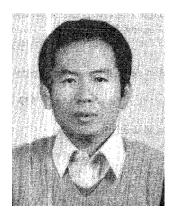
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