# Modeling Mis-Routing Calls Due to User Mobility in Wireless VoIP

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Abstract—This letter proposes an analytic model to study the mis-routing problem caused by user mobility in a wireless VoIP system. We derive the probability that there are n mis-routed calls when a subscriber moves from IP network to the GSM network. Our study indicates that if the user residence times in GSM location areas, inter-call origination times and the inter-call delivery times are of the same order, then the mis-routing effect can not be ignored.

Index Terms—GSM, mis-routing, user mobility, wireless VoIP.

# I. INTRODUCTION

UPPORTING telephony services over IP network is a promising trend in telecommunication business. Telephony services over IP network or the so called voice over IP (VoIP) can provide subscribers low cost telephony services. Thus, incorporating VoIP services into the existing telecommunication systems is essential. In particular, integrating mobile phone services with VoIP becomes an important issue, which has been intensively studied [1], [2].

Telecommunications and Internet Protocol Harmonization over Network (TIPHON) specifies the mechanism (i.e., a mediation gatekeeper) to provide the service control functions for convergence of IP networks, mobile networks, fixed wireless network, and the public switched telephone network (PSTN). Several scenarios are defined in TIPHON to illustrate different ways of integrating IP and mobile networks. In this paper, we use GSM as an example to describe a TIPHON mobile/IP integration, where the mobile signaling protocol is GSM MAP described in [3].

This TIPHON scenario is called iGSM [4] and its architecture is illustrated in Fig. 1. In this figure, iGSM gateway performs the conversion between GSM MAP and H.323 family protocols, and iGSM VLR (Gatekeeper) records location information as the visitor location register (VLR) in GSM network. iGSM supports user mobility for GSM subscribers to access VoIP services. By using various types of terminals, user mobility allows a user to move around the service area without losing contact with the system. That is, a GSM subscriber is able to keep the same identity to receive the service even if he/she changes the

Manuscript received July 21, 2000. The associate editor coordinating the review of this letter and approving it for publication was Prof. I. S. Venieris. This work was supported in part by MOE Program of Excellence Research under Contract 89-E-FA04-4, CCL/ITRI under Contract 2-10B, FarEastone, NSC, and the Lee and MTI Center for Networking Research, NCTU.

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Publisher Item Identifier S 1089-7798(00)11514-5.

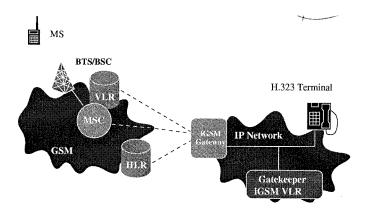


Fig. 1. The iGSM architecture.

terminal type from the GSM mobile station (MS) to the H.323 terminal. In Fig. 1, the incoming calls (call deliveries) are routed to the GSM MS when the person is in the GSM network (using GSM MS). On the other hand, the calls are routed to the H.323 terminal when the person is in the IP network (using H.323 terminal). We note that to make iGSM work, GSM periodic registration must be disabled for the iGSM subscribers. Otherwise, if an iGSM subscriber forgets to turn off the GSM MS when the subscriber switches to an H.323 terminal, the registration record of the H.323 terminal will be over-written by the periodic registration operation of the GSM MS.

To support user mobility, the subscriber needs to explicitly perform registration to inform the system which location area (LA) the MS resides when the subscriber changes the terminal. If the subscriber forgets to take this action, call deliveries to the subscriber may be mis-routed. This problem exists for all approaches based on the concept of *universal personal telecommunications* [5]. The mis-routing problem occurs in the following scenario.

Step I [Fig. 2(a)]: The subscriber p is in the GSM LA A and the home location register (HLR) indicates that the person is in LA A. The subscriber then moves to the IP network (LA B) without turning off the GSM MS.

Step II [Fig. 2(b)]:

The subscriber registers to IP network. After registration, the HLR record is modified and *p*'s record in VLR A is removed.

*Step III* [*Fig.* 2(*c*)]:

The subscriber moves back to the GSM MS at LA A. Since the GSM MS is still on, the subscriber *p* does not notice that an

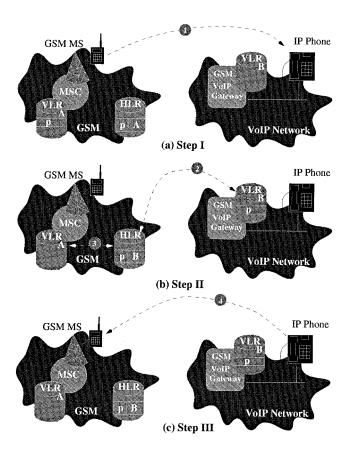


Fig. 2. Mis-routing in user mobility.

explicit registration is required. Thus, the HLR indicates that the subscriber p is still in LA B.

At this point, the subscriber is in LA A. However, the incoming calls to the user (without explicit registration) are misrouted to LA B until one of the following events occurs.

- Case 1) The subscriber originates a call. In this case VLR A finds that the VLR record for the subscriber does not exist. VLR A will ask the MS to perform a registration operation as described in the VLR failure restoration procedure [3]
- Case 2) The subscriber moves to another LA in the GSM network. Registration is automatically initiated by the GSM MS.

To avoid mis-routing calls, the H.323 terminal may be designed with appropriate SIM slot. In this approach, the service provider requests that the SIM card must be inserted in the H.323 terminal when it is in use, and be removed when the subscriber moves back to the GSM MS. By doing so, mis-routing will not occur when switching from the H.323 terminal to the GSM MS. However, from an engineering and marketing study conducted by a GSM service provider, we found that hardware modifications to H.323 terminals will seriously increase the cost of iGSM, which is not commercially feasible. The only solution is to keep operator related confidential information (including SIM) in the H.323 gateway.

In this paper, we propose an analytic model to study misrouting due to user mobility in iGSM. The purpose of this study

is to investigate how serious mis-routing will be if the subscriber does not perform an explicit registration.

## II. THE ANALYTIC MODEL

This section proposes an analytic approach to model misrouting due to user mobility in iGSM. We derive the probability  $\Pr[K=n]$  that there are n mis-routed calls when a subscriber moves from IP network to the GSM network as follows.

Let call originations and deliveries be Poisson process. Let  $\tau_o$  and  $\tau_t$  be the inter-arrival times for call originations and deliveries, respectively. Then  $\tau_o$  and  $\tau_t$  have exponential distributions with rate  $\lambda_o$  and  $\lambda_t$ . Let  $\tau_t$ , n be the inter-arrival time for n consecutive call deliveries. Then  $\tau_t$ , n has an Erlang distribution with mean  $n/\lambda_t$ .

Let  $\tau_r$  be the time that the iGSM subscriber stays in an LA. Suppose that  $\tau_r$  is a random variable with a general density function  $f_r(\,\cdot\,)$ , distribution function  $F_r(\,\cdot\,)$  and Laplace transform  $f_r^*(s)$ . Any call deliveries occur during the period  $\min(\tau_o,\,\tau_r)$  are mis-routed. Let K be the number of mis-routed call deliveries. Then for  $n\geq 0$ ,

$$\Pr[K \ge n] = \Pr[\tau_o > \tau_{t,n}, \tau_r > \tau_{t,n}]$$

$$= \int_{\tau_{t,n}=0}^{\infty} \left\{ \left[ \frac{\lambda_t^n}{(n-1)!} \right] \tau_{t,n}^{n-1} e^{-\lambda_t \tau_{t,n}} \right.$$

$$\times \left[ \int_{\tau_o = \tau_{t,n}}^{\infty} \lambda_o e^{-\lambda_o \tau_o} d\tau_o \right]$$

$$\times \left[ \int_{\tau_r = \tau_{t,n}}^{\infty} f_r(\tau_r) d\tau_r \right] \right\} d\tau_{t,n}$$

$$= \left[ \frac{\lambda_t^n}{(n-1)!} \right] \left\{ \int_{\tau_{t,n}=0}^{\infty} \tau_{t,n}^{n-1} e^{-(\lambda_t + \lambda_o)\tau_{t,n}} \right.$$

$$\times \left[ 1 - F_r(\tau_{t,n}) \right] d\tau_{t,n} \right\}$$

$$= \left( \frac{\lambda_t}{\lambda_t + \lambda_o} \right)^n + \left[ \frac{(-\lambda_t)^n}{(n-1)!} \right]$$

$$\times \left\{ \frac{d^{n-1} \left[ \frac{f_r^*(s)}{s} \right]}{ds^{n-1}} \right\} \right|_{s = \lambda_t + \lambda_o}$$

$$= \left( \frac{\lambda_t}{\lambda_t + \lambda_o} \right)^n + \left[ \frac{(-\lambda_t)^n}{(\lambda_t + \lambda_o)(n-1)!} \right]$$

$$\times \left\{ \frac{d^{n-1} f_r^*(s)}{ds^{n-1}} - (n-1) \right.$$

$$\times \left\{ \frac{d^{n-2} \left[ \frac{f_r^*(s)}{s} \right]}{ds^{n-2}} \right\} \right\} \right\}$$

$$= (1)$$

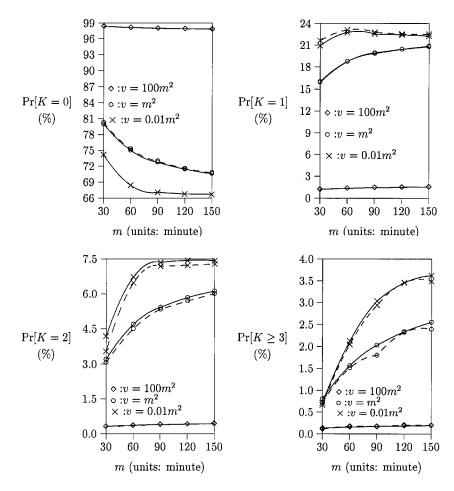


Fig. 3. Mis-routing probabilities (dashed: simulation; solid: analytic analysis).

where by convention [6]

$$\frac{d^0f_r^*(s)}{ds^0} = f_f^*(s), \quad \text{and} \quad \frac{d^{-1}f_r^*(s)}{ds^{-1}} = \frac{d^{-2}f_r^*(s)}{ds^{-2}} = 0.$$

For  $n \geq 0$ , we have

$$\Pr[K = n] = \Pr[K \ge n] - \Pr[K \ge n + 1] \tag{2}$$

where  $\Pr[K \geq 0] = 1$ .

If  $\tau_r$  has a Gamma distribution with mean m and variance v, then

$$f_r^*(s) = \left[\frac{(1/m)}{(1/m) + (v/m^2)s}\right]^{m^2/v}$$
 and 
$$\frac{d^k f_r^*(s)}{ds^k} = \left(\frac{1}{m}\right)^{m^2/v} \left[\prod_{i=0}^{k-1} \left(-\frac{m^2}{v} - i\right)\right]$$
$$\times \left(\frac{1}{m} + \frac{vs}{m^2}\right)^{-(m^2/v) - k} \left(\frac{v}{m^2}\right)^k. \tag{3}$$

# III. NUMERICAL RESULTS

This section investigates the performance of mis-routing of user mobility in iGSM based on the analytic model developed in the previous section. Fig. 3 plots Pr[K=0], Pr[K=1],

 $\Pr[K=2]$ , and  $\Pr[K\geq 3]$  where the call originations occur every 30 minutes and the call deliveries occur every 60 minutes. The user's LA residence times are assumed to have a Gamma distribution with mean m and variance v. Gamma distribution is used in our study because this distribution can approximate many other distributions as well as measured data obtained from the mobile network field trials. In Fig. 3, the solid curves are for analytic analysis and the dashed curves are for simulation. It is clear that our analytic analysis is consistent with the simulation results

The figure indicates that the mis-routing probabilities increase as the variance v of the user LA residence time decreases. The figure also indicates that if the user LA residence times, the inter-call origination times and the inter-call delivery times are of the same order, then the mis-routing effect can not be ignored. Thus, to avoid the mis-routing problem, the iGSM subscribers must be responsible to perform the explicit registration operation. That is, the subscriber should turn off their MS when moving to the IP network. The "turn-off" action results in a detach GSM message to de-register the MS. When the subscriber turns on the MS in the GSM coverage area, an explicit registration is performed, and the person is considered to move back to the GSM network.

It is clear that if the subscribers originate calls much more frequently than receiving calls, then the mis-routing effect is insignificant.

# IV. CONCLUSIONS

This paper proposed an analytic model to investigate the misrouting problem caused by user mobility in iGSM. The study indicated that the variance of the user LA residence time significantly affects the number of mis-routed calls to a user. We observed that if the user LA residence times, the inter-call origination times and the inter-call delivery times are of the same order, then the mis-routing effect can not be ignored.

As a final remark, mis-routed calls are not necessarily lost. With call forwarding on no reply, these calls can be forwarded to an appropriate destination or mailbox.

### ACKNOWLEDGMENT

The authors would like thank the two anonymous reviewers. Their comments have significantly improved the quality of this letter.

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