

# Password Authentication Schemes with Smart Cards\*

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In this paper, two password authentication schemes with smart cards are proposed. In the schemes, users can change their passwords freely, and the remote system does not need the directory of passwords or verification tables to authenticate users. Once the secure network environment is set up, authentication can be handled solely by the two parties involved. For a network without synchronized clocks, the proposed nonce-based authentication scheme is able to prevent malicious reply attacks.

*Keywords:* password authentication, smart card, ID-based scheme, clock synchronization.

## 1. Introduction

The rapid progress of networks facilitates more and more computers connecting together to exchange great information and share system resources. Security is then an important issue for computer networks. There are two basic requirements for network security: secrecy and authentication. Secrecy protects sensitive data against eavesdropping and modification. Authentication prevents forgery and unauthorized network access. The common approach to provide authenticity is the use of passwords. Password authentication has been used for a long time, mainly because it is easy to implement and use.

In conventional password authentication schemes, each user has an identifier (ID) and a secret password (PW). If a user requests to enter a network system, he

must enter his ID and PW to pass the system authentication. A possible verification approach is to directly store and maintain a directory of users' IDs and PWs in the network system. Upon receipt of a user's login request, the network system searches the password directory table to verify whether or not the submitted password matches with the one stored in the table. If they match, the user is regarded as an authorized user and is permitted to enter the system. Otherwise, the login request is denied. Since the password is stored in plain-text form, this approach is clearly under the threat of revealing the password.

There are many schemes [Evans74, Lennon81] proposed to resolve the password revealing problem. These schemes often hash the password with a one-way function and store the hash value, instead of the plain password, in the directory table. In this way, the secrecy of passwords can be ensured even if contents of the directory table are disclosed. However, in the schemes, the system must protect the directory table against intruders' modification. Otherwise, the directory table may be replaced and users may be masqueraded. There are a number of authentication protocols [Kehne92, Kohl93, Neuman93, Otway87, Shieh96, Syverson93] which use a trusted third party to ensure authentication and security in an open network system. In these authentication protocols, secret information, such as secret keys, must be stored in a directory table on the authentication server. Therefore, the attacks to the directory table still exist in these authentication systems.

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Recently some enhanced authentication schemes [Chang91, Chang93, Okamoto89, Shieh97, Tsujii78, Wang96] are proposed to eliminate the drawback of using directory tables. These schemes all adopt the concept of ID-based signature scheme [Shamir85] in conjunction with smart cards [Peyret90]. The ID-based schemes have the following advantages: (1) neither secret nor public keys need be exchanged, (2) the public key directory table is not needed, and (3) the assistance of a third party is not needed. The first ID-based signature scheme was proposed by Shamir [Shamir85]. He uses the well-known public-key encryption algorithm RSA [Rivest78] with smart cards to implement ID-based signature. Shamir's ID-based scheme enables communicating parties to verify each other's signature without exchanging private or public keys.

In Shamir's ID-based scheme, the secret key corresponding to an ID is fixed, and cannot be changed. Thus, a user with an assigned ID cannot choose his secret key by himself. Since the concept of timestamps [Denning81] is not employed, the scheme is weak against the attack of replaying previously intercepted signature. It is hence not suitable for user authentication in network systems. Chang and Wu's scheme [Chang91] has a similar problem. A user's password is generated by the password generation center, rather than by the user himself. However, users are used to choosing their own passwords. This approach is against users' habit and may not be accepted by many users. Furthermore, the scheme suffers from the threat of password leakage [Chang93].

Based on Elgamal's signature [Elgamal85] and Shamir's ID-based schemes, Wang and Chang include the concept of timestamps in an improved authentication scheme [Wang96]. In their scheme, however, replay attacks cannot be avoided completely and user's identities may be forged. A legitimate user can impersonate other users and pass the system authentication. That is because the information about user identities is not included in the verification procedure of their scheme. The remote system can only determine validity of the authentication message, but cannot identify who really sent this message. Furthermore, these schemes are all based on ID-based schemes, they share

the problem that a user cannot change his password after registration. If a user's password is compromised, he can no longer use his current ID, but needs to apply for a new one. This makes users inconvenient to use in a real network system. Since some weaknesses exist in these schemes, a more secure and practical authentication scheme for network systems is proposed in the following section.

In this paper, We propose two new password authentication schemes with smart cards. The proposed schemes can resolve the security problems in the above schemes [Chang91, Shamir85, Wang96]. Our method keeps the merits of ID-based schemes, but eliminates the weakness that users cannot change their passwords. In the new schemes, a user can freely choose and change his password at will. If his password is accidentally revealed, he can simply change it to another secure password without re-registering for a new ID. This paper is organized as follows. A new timestamp-based password authentication scheme is presented in section 2, which only needs one message for authentication. For the networks that clocks cannot be easily synchronized, we propose a nonce-based password authentication scheme in section 3. The security of our schemes will be analyzed in section 4. Finally, a conclusion is given in section 5.

## 2. Timestamp-Based Password Authentication Scheme

In the proposed scheme, we assume the existence of a trusted key information center in the network to issue personalized smart cards to users when joining the system. The proposed timestamp-based password authentication scheme can be divided into three phases. In the *registration phase*, the key information center sets up the authentication system and issues smart cards to the users who request registration. In the *login phase*, a user attaches his smart card to a terminal and keys in his identifier (ID) and password (PW). Then the terminal sends a login request message to the remote host. In the *verification phase*, the remote host verifies the correctness of submitted message and determines whether the login request should be accepted or not.

## Registration Phase

The key information center is not responsible for authenticating users, but for generating key information, issuing smart cards to new users and serving password-changing request for registered users. Let  $U_i$  denote the  $i$ th user who submits his identifier  $ID_i$  and chosen password  $PW_i$  to the key information center to request for registration. Here,  $PW_i$  must be sent over a secure channel. Upon receipt of the request, the key information center will perform the following steps:

1. Generate two large prime numbers  $p$  and  $q$ , and let  $n = p \cdot q$ . For security reasons, the length of  $p$  and  $q$  is recommended to be 512 bits at least.
2. Choose a prime number  $e$  and an integer  $d$  which satisfy

$$e \cdot d \pmod{(p-1) \cdot (q-1)} = 1. \quad (1.)$$

Here  $e$  is the public key of the key information center that should be published, and  $d$  is the secret key that must be kept privately.

3. Find an integer  $g$  which is a primitive element in both  $GF(p)$  and  $GF(q)$ , where  $g$  is the system's public information.
4. Calculate the user's secret information  $S_i$  as

$$S_i \equiv ID_i^d \pmod{n}. \quad (2.)$$

According to the encryption algorithm RSA [Rivest78], the following equation would be obtained.

$$ID_i \equiv S_i^e \pmod{n} \quad (3.)$$

Even if one knows  $ID_i$ ,  $e$ , and  $n$ , it is hard to crack  $S_i$  without the knowledge of  $d$ . This is a discrete logarithm problem [Adleman79]. The integer  $d$  can be evaluated only when  $n$  is factorized to  $p$  and  $q$ , which is very difficult because the length of  $n$  is 1024 bits.

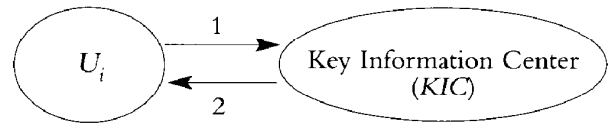
5. Generate the smart card's identifier  $CID_i$  of  $U_i$  and compute  $h_i$  by

$$h_i \equiv g^{PW_i \cdot d} \pmod{n} \quad (4.)$$

Here  $CID_i$  is for validating the legality of smart cards in the verification phase.

6. Write  $n, e, g, ID_i, CID_i, S_i$  and  $h_i$  to the memory of smart card and issue the card to  $U_i$ .

Once the authentication system is set up, the key information center is not needed except when new users request to join, or registered users request to change passwords. The integer pair  $p$  and  $q$  will not be used any more and should be thrown away secretly. When a new user requests to join, the center repeats step 4 through 6. The procedure of registration phase is shown in Figure 1.



1.  $U_i \rightarrow KIC : ID_i, PW_i$
2.  $KIC \rightarrow U_i : \text{a smartcard containing } \{ID_i, CID_i, n, e, g, S_i, h_i\}$

Figure 1. Registration Phase

## Login Phase

When  $U_i$  wishes to login a remote host, he must insert the smart card into a card reader and enter his identity  $ID_i'$  and password  $PW_i'$ . If  $ID_i'$  is identical to the  $ID_i$  which is kept in the memory of the smart card, the smart card will perform the following steps:

1. Generate a random number  $ri$  and calculate the following two integers:

$$X_i \equiv g^{ri \cdot PW_i'} \pmod{n} \quad (5.)$$

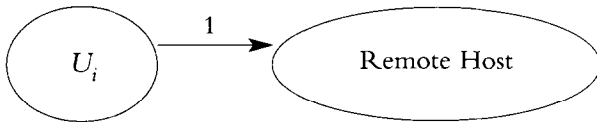
$$Y_i \equiv S_i \cdot h_i^{ri \cdot f(CID_i, T)} \pmod{n} \quad (6.)$$

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Where  $T$  is the current time used as a time-stamp and  $f(x, \gamma)$  is a one-way function. The one-way function is a function relatively easy to compute but significantly harder to undo or reverse. That is, given  $(x, \gamma)$  it is easy to compute  $f(x, \gamma)$ , but given  $f(x, \gamma)$  it is very difficult to compute  $x$ .

2. Send a login request message  $M$  containing  $ID_i, CID_i, X_i, Y_i, n, e, g$  and  $T$  to the remote host.

In Figure 2, the transaction of *login phase* is depicted.



1.  $U_i \rightarrow \text{host} : M = \{ ID_i, CID_i, X_i, Y_i, n, e, g, T \}$

$$X_i \equiv g^{n_i \cdot PW_i'} \pmod{n}$$

$$Y_i \equiv S_i \cdot h_i^{n_i \cdot f(CID_i, T)} \pmod{n}$$

Figure 2. Log-in Phase

## Verification Phase

The *verification phase* is executed by the remote host to determine whether  $U_i$  is allowed to login or not. Let  $T'$  be the time when the remote host receives the message  $M$ . Upon receipt of message  $M$ , the remote host will perform the following steps to verify the correctness of  $M$ .

1. Verify that  $ID_i$  is a valid user identity and  $CID_i$  is a legal smart card identity. If not, the log-in request is rejected.
2. Compare  $T$  with  $T'$ , if the difference between  $T$  and  $T'$  is longer than the valid period,  $M$  is considered as an invalid message and the host computer will reject the login request. According to different network environments, the length of the valid period can be adjusted.

3. Check whether the following equation holds:

$$Y_i^e = ID_i \cdot X_i^{f(CID_i, T)} \quad (7.)$$

The equation will hold when the password  $PW_i'$ , keyed in by  $U_i$ , matches  $PW_i$  registered in the key information center. That is because:

$$\begin{aligned} Y_i^e &= (S_i \cdot h_i^{n_i \cdot f(CID_i, T)})^e = S_i^e \cdot (g^{PW_i \cdot d})^{n_i \cdot f(CID_i, T) \cdot e} \\ &= ID_i \cdot (g^e \cdot d)^{n_i \cdot PW_i \cdot f(CID_i, T)} \\ &= ID_i \cdot g^{n_i \cdot PW_i \cdot f(CID_i, T)} \end{aligned} \quad (8.)$$

and

$$ID_i \cdot X_i^{f(CID_i, T)} = ID_i \cdot g^{n_i \cdot PW_i \cdot f(CID_i, T)} \quad (9.)$$

4. If the equation holds, the remote host believes that the message  $M$  is sent by  $U_i$ , and the password  $PW_i'$  matches  $PW_i$ . Therefore,  $U_i$  is allowed to log in the remote host, otherwise the login request is rejected.

Comparing to other schemes, our authentication scheme allows users to freely change their passwords at will. If a user  $U_i$  wants to change his password, he can submit his smart card and newly chosen password  $PW_i^*$  to the key information center over a secure channel. The center will compute the new  $hi'$  as

$$h_i' \equiv g^{PW_i^* \cdot d} \pmod{n} \quad (10.)$$

and write it into  $U_i$ 's smart card to replace the original  $h_i$ . After getting the updated smart card,  $U_i$  is able to use the new password  $PW_i^*$  to login the network system.

The proposed password authentication scheme can withstand the problems that have appeared in other schemes [Chang91, Shamir85, Wang96]. With the timestamp  $T$ , the attack of replaying previously intercepted messages is avoided. However, note that if system clocks are not well synchronized, and transmission delay is long and unpredictable in a network environment (e.g., a wide area network) [Gong92], a potential replay attack exists in all schemes that employ the concept of timestamps. In the next section, we will propose a nonce-based authentication scheme to protect users against this attack in this network environment.

### 3. Nonce-Based Password Authentication Scheme

The nonce-based password authentication scheme is an extended version of the timestamp-based scheme. In the nonce-based scheme, the timestamp  $T$  is replaced with a nonce number  $N$  to withstand the replay attack. The nonce-based scheme consists of three phases. The *registration phase* is the same as the timestamp-based scheme described in the previous section, hence the description of the phase is skipped. The *login phase* and *verification phase* are described as follows respectively.

#### Login Phase

In order to login a remote host,  $U_i$  inserts his smart card into a terminal and enters his identity  $ID_i$  and password  $PW_i'$ . If  $ID_i$  matches the one kept in the memory of smart card, the following steps will be performed.

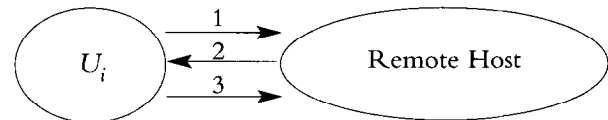
1. The smart card sends an initial message  $M_1 = \{ID_i, CID_i\}$  to request for a login session.
2. Upon receipt of the message  $M_1$ , the remote host verifies the validity of  $ID_i$  and  $CID_i$ . If any one of these two is not valid, the login request is rejected and the connection will be closed. Otherwise, the remote host reserves  $ID_i$  and  $CID_i$  for the *verification phase*, and then evaluates a session nonce  $N = f(CID_i, rj)$  and sends it back to the smart card. Here,  $rj$  is a random number and  $f(x,y)$  is a one-way hash function. The session nonce  $N$  will be kept for future use.
3. Upon receipt of the session nonce  $N$ , the smart card generates another random number  $ri$  and calculates the following two integers:

$$X_i \equiv g^{ri \cdot PW_i'} \pmod{n} \quad (11.)$$

$$Y_i \equiv S_i \cdot h_i^{ri \cdot N} \pmod{n} \quad (12.)$$

4. The smart card sends an authentication message  $M_2$  containing  $X_i, Y_i, n, e$  and  $g$  to the remote host.

In the nonce-based scheme, three message transmissions are required to complete the login phase. The transaction of the new *log-in phase* is depicted in *Figure 3*.



1.  $U_i \rightarrow \text{host} : M_1 = \{ID_i, CID_i\}$
2.  $\text{host} \rightarrow U_i : N = f(CID_i, rj)$
3.  $U_i \rightarrow \text{host} : M_2 = \{X_i, Y_i, n, e, g\}$   
 $X_i \equiv g^{ri \cdot PW_i'} \pmod{n}$

$$Y_i \equiv S_i \cdot h_i^{ri \cdot N} \pmod{n}$$

Figure 3. Log-in phase in the nonce-based scheme

#### Verification Phase

Upon receipt of message  $M_2$ , the remote host will do the following steps to decide whether  $U_i$  is permitted to log in or not.

1. Check whether the following equation holds:

$$Y_i^e = ID_i \cdot X_i^N \quad (13.)$$

Where  $ID_i$  and  $CID_i$  are derived from the smart card and  $N$  is the session nonce generated by the remote host in the *login phase*.

2. If the equation holds, the remote host believes that:
  - (a) the authentication message  $M_2$  is truly sent by  $U_i$ ,
  - (b) the password  $PW_i'$ , keyed in by  $U_i$ , matches  $PW_i$  registered in the key information center,
  - (c) and the session nonce  $N$  that the smart card used to evaluate  $Y_i$  is identical to the one the remote host generated. That is, message  $M_2$  is fresh and is not a replay message.

Since  $M_2$  is proved as a legal and fresh authentication message,  $U_i$  is allowed to login the remote host. With the session nonce  $N$ , the nonce-based password

authentication scheme can protect users against the replay attack even if the system clocks are not synchronized. In the next section, we will analyze the security of the two proposed schemes.

## 4. Security Analysis and Discussions

The strength of our schemes can be demonstrated by the following security attacks. In the proposed timestamp-based scheme, if a forger wants to masquerade  $U_i$  to pass the system authentication, he must find two integers  $x$  and  $y$  that satisfy the following equation.

$$y^e = ID_i \cdot x^{f(CID_i, T)} \quad (14.)$$

Although the forger can get a pair of integers  $(y^e, x^{f(CID_i, T)})$  that make the equation hold. The pair  $(y, x)$  is unattainable because computing  $(y, x)$  from  $(y^e, x^{f(CID_i, T)})$  is a discrete logarithm problem. In another case, assume that the smart card  $CID_i$  of  $U_i$  is exposed to an intruder, say  $U_j$  ( $j \neq i$ ). In this case,  $U_j$  cannot access the network systems since he does not have  $PW_i$ . One possible way for  $U_j$  to acquire  $PW_i$  is to crack  $h_i \equiv g^{PW_i \cdot d} \pmod{n}$ . This is infeasible, because  $h_i$  is stored in the tamper-proof smart card and cannot be retrieved directly. Even if  $U_j$  can compromise  $h_i$ ,  $PW_i$  remains secure because of the discrete logarithm problem. As to  $U_j$ , he can use the same  $ID_i$  to re-register a new smart card  $CID_i'$  to the key information center. From then on, the old smart card  $CID_i$  that  $U_j$  obtained is automatically disabled.

In the nonce-based scheme, the potential replay attack will not succeed. Considering the following scenario, an intruder eavesdropped an old authentication message from a login session of  $U_i$  associated with a session nonce  $N$ . He may replay the old authentication message to request for a new log-in session. Following the steps of *login phase*, the intruder first sends  $M_1 = \{ID_i, CID_i\}$  to the remote host. Upon receipt of  $M_1$ , the remote host generates a new session nonce  $N'$  and replies it to the intruder. Then the intruder replays intercepted authentication message  $M_2$  to the remote host. The login procedure will fail in the *verification*

*phase*, because the verification equation does not hold as follows:

$$Y_i^e = ID_i \cdot X_i^N \neq ID_i \cdot X_i^{N'} \quad (15.)$$

The authentication message  $M_2$  that the intruder replayed is considered invalid. Consequently, the login request is rejected and the attack fails.

Exponential computation is considered to be very time-consuming. In our schemes, only two exponential computations are needed for the smart card to initialize a login session. This feature makes our schemes effective, since the smart cards usually do not support powerful computation capability. It is noticeable that the remote host performs the verification of users without any prior knowledge, and all the elements used in the *verification phase* are generated or provided on users' side. It means that the remote host does not need to register in the same key information center as users. Therefore, our authentication schemes are suitable for cross-domain network applications, such as electronic commerce systems.

## 5. Conclusions

In this paper, two practical password authentication schemes are proposed which are based on the concepts of ID-based schemes and the smart cards. These schemes do not need the directory of passwords or verification tables to authenticate users. Their security is based on the difficulty of factoring a large number and the discrete logarithm problem. Once the secure network system is set up, the authentication can be handled solely by the two parties involved. Unlike in other ID-based authentication schemes, users are permitted to choose and change their passwords freely in the two proposed schemes.

The proposed timestamp-based scheme needs only one message for authentication, but requires synchronous clocks. And the proposed nonce-based scheme is immune from the replay attack, but requires three authentication messages. In the networks with tightly synchronized system clocks, such as local area networks, the timestamp-based scheme is advised. On the other hand, the nonce-based

scheme is suitable for a large network where clock synchronization is difficult, such as wide area networks, mobile communication networks, and satellite communication networks.

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