

# Wideband Matched CMOS LNA Design Using R-L-C Loading Network

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**Abstract** This paper proposes a new methodology for designing and analyzing wideband matched CMOS LNA with *R-L-C* loading network, where validity of this new approach is supported by the agreement between the simulated input impedance of the LNA and its calculated counterpart. To demonstrate its feasibility, two wideband matched LNA's are designed using TSMC 0.18- $\mu\text{m}$  RF-CMOS process. One is for 3–8 GHz application and the second one targets at 8–25 GHz frequency range. The measured results of both circuits will then be presented.

**Keywords** Wideband · Input matching · Low noise amplifier · LNA

## 1 Introduction

Wide-band low-noise amplifiers (LNA's) have been a critical component for both scientific community and the communication industry, such as radio astronomy receivers for the former and ultra-wideband (UWB) technologies for the latter [1–3]. Among the different circuit design methodologies proposed for wideband amplifiers, the distributed one is probably the most straightforward in realizing broad bandwidth [4, 5]. However, it tends to consume a lot of power while providing only modest gain. An amplifier using common-gate transistor as input stage can indeed have wideband matched impedance; nonetheless, the resulting circuit will have poor power gain and large noise figure [6]. Adding a delicate *L-C* circuit in front of the amplifier can improve its input matching over a wide bandwidth, but at the cost of additional noise generated by these passive components and, especially in the case of silicon, this deterioration is pronounced [7–9]. Recently, it becomes popular

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applying current re-use method in designing wideband CMOS amplifiers; however, the stacking of one n-type and one p-type transistors requires a large bias voltage [10, 11].

In the case of high mobility transistor (HEMT), it has already been demonstrated that through the intrinsic gate-drain capacitor  $C_{gd}$ , the transistor's output  $R$ - $C$  loading can alter its input impedance to the intended value over a wide bandwidth [12]. In spite of that, implementation of this large loading equivalent resistance is not that easy in the CMOS circuit. Thus, the input matching mechanism for wideband matched COMS LNA needs to be re-examined and modified if necessary, and that prompts the research described in this paper.

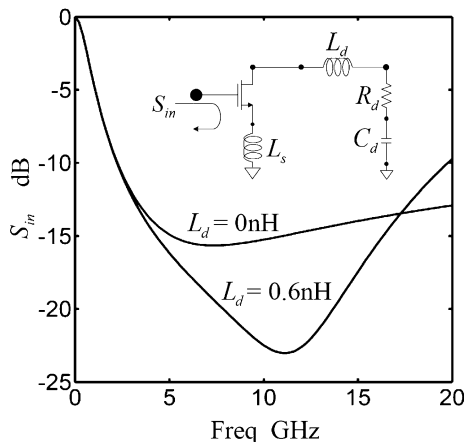
In the following section, after a brief review of the 0.18- $\mu\text{m}$  RF-CMOS transistor's small-signal modeling, we propose what should constitute the first-stage transistor's loading:  $L_d$ ,  $R_d$ , and  $C_d$ , as shown in Fig. 1, where  $L_d$  is an explicit element, and both  $R_d$  and  $C_d$  can be from the equivalent input circuit of the following-stage. Physically, the external source inductor  $L_s$  is critical in determining the low-frequency input matching, and the loading  $L_d$  starts playing a role as frequency increases. In both cases,  $C_d$  is used for setting  $\text{Re}[Z_{in}]$ , and proper choice of  $R_d$  helps lowering  $S_{11}$  at high frequency. If the high frequency range means infinite, then  $L_d$  can indeed be omitted; otherwise, the importance of this  $L_d$  cannot be overlooked for finite-bandwidth wideband LNA, as this  $L_d$  could improve the input matching at the intended high frequency range. Without inserting any complicated passive (and lossy) circuit in front of the first-stage transistor, superior noise performance is expected for this type of amplifier.

A 3–8 GHz LNA is therefore fabricated using TSMC (Taiwan Semiconductor Manufacturing Company) 0.18- $\mu\text{m}$  RF-CMOS process. To explore the high frequency performance of this commercial process, a second LNA targeting the 8–25 GHz frequency range is then designed. Measured results of both amplifiers will be presented too.

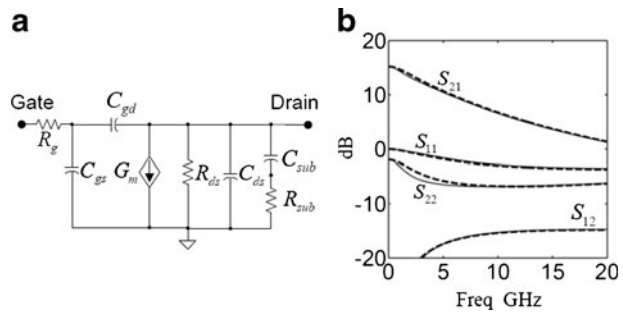
## 2 Analysis of wideband LNA design

To facilitate the circuit analysis,  $S$ -parameters of a TSMC 0.18- $\mu\text{m}$  RF-CMOS transistor need to be numerically fitted to find its equivalent small-signal model, as shown in Fig. 2, where the substrate effect due to  $C_{sub}$  and  $R_{sub}$  has been included. For this 216- $\mu\text{m}$  27-finger n-type transistor biased at  $V_{gs}=0.65$  Volt and  $I_d=7$  mA, our model is valid up to 20 GHz at least, and

**Fig. 1** The simulated input reflection coefficient  $S_{11}$  of the proposed transistor circuit with  $L_d=0$  and 0.6nH, respectively, while  $C_d=0.13$ pF,  $R_d=25\Omega$ , and  $L_s=0.3$ nH.



**Fig. 2** **a** Small-signal model of a TSMC 0.18- $\mu\text{m}$  RF-CMOS transistor biased at saturation region. **b** Simulated  $S$ -parameters from both the foundry provided design kit (solid lines) and our small-signal model (dashed lines).



the parameter values are tabulated in Table 1. Though  $S$ -parameter discrepancies can be observed with the omission of  $R_{gs}$ ,  $R_{ds}$ ,  $R_{sub}$ , and  $C_{sub}$ , they are relatively minor; thus, to retain the physical meaning while simplifying the mathematical derivation, these four parameters are removed from that used in the following circuit analysis.

Mathematically, the input impedance  $Z_{in}$ , as indicated in Fig. 3, can be expressed as

$$Z_m = \left[ Y_\alpha + \frac{1}{Z_\beta} \right]^{-1} \tag{1}$$

where  $Y_\alpha$  is the admittance looking into the  $C_{gd}$  branch, and  $Z_\beta$  is the impedance looking into the  $C_{gs}$  branch. Both  $Y_\alpha$  and  $Z_\beta$  can be derived as

$$Y_\alpha = \left[ \frac{1}{j\omega C_{gd}} + \frac{1}{j\omega C_d} + R_d + j\omega L_d \right]^{-1} + \left[ \left( \frac{1}{j\omega G_m R_{ds} C_{gd}} + \frac{1}{G_m} + j\omega L_s \right) + \left( \frac{1}{C_d / G_m C_{gd} + C_{gd} / j\omega L_s C_d} + \frac{1}{1 / j\omega G_m R_d C_{gd} + L_s / R_d C_{gd}} + \frac{1}{L_s / j\omega C_{gd} L_d - 1 / \omega^2 L_d C_{gd} G_m} \right) \right]^{-1} \tag{2}$$

and

$$Z_\beta = \frac{1}{j\omega C_{gs}} + \frac{G_m L_s}{C_{gs}} + j\omega L_s \tag{3}$$

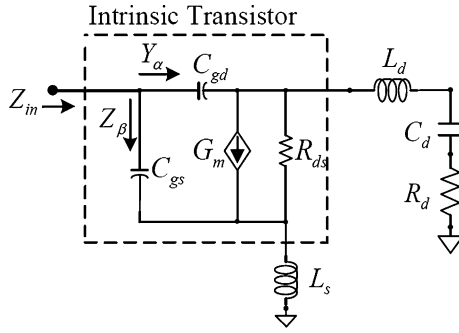
The corresponding equivalent circuit can be arranged as that of Fig. 4, where  $Y_\alpha$  is the dominant branch and  $Z_\beta$  offers some modification [12]. Again, it is the  $C_d$  that determines

**Table 1** Parameters in the small-signal model of the 216-micron 27-finger tsmc n-type transistor.

$V_{gs}=0.65$  Volt,  $I_d=7$  mA

| parameter | value        | parameter | value   |
|-----------|--------------|-----------|---------|
| $R_g$     | 7 $\Omega$   | $C_{sub}$ | 0.3pF   |
| $R_{ds}$  | 452 $\Omega$ | $C_{ds}$  | 0.063pF |
| $R_{sub}$ | 180 $\Omega$ | $C_{gd}$  | 0.08pF  |
| $G_m$     | 64mS         | $C_{gs}$  | 0.2pF   |

**Fig. 3** The proposed transistor circuit used in the wideband analysis.



the matched  $\text{Re}[Z_{in}] (= C_d/G_m C_{gd})$ , as discussed in detail in [12]. With appropriate component values, the shape of the input reflection coefficient  $S_{in}$  resembles a hook, as shown in Fig. 5. The solid curve is the simulated result with  $C_d=0.13\text{pF}$ ,  $R_d=25\Omega$ ,  $L_d=0.6\text{nH}$ , and  $L_s=0.3\text{nH}$ ; the overlapping dashed curve is the calculated counterpart using (1). On the  $S_{in}$  trajectory, there are two marked frequency points where the corresponding input impedance is purely real and close to  $50\Omega$ , and thus are good indices for this circuit's (slightly larger) available frequency range. By setting  $\text{Im}[Y_\alpha]$  to zero, both  $f_L$  and  $f_H$  can be determined as

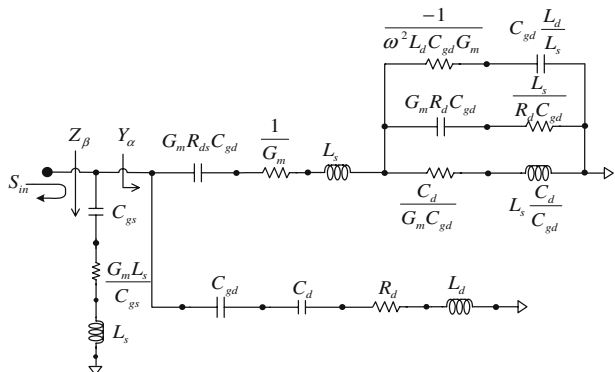
$$f_L = \frac{1}{2\pi\sqrt{L_s(C_{gd} + C_d)G_m R_{ds}}} \tag{4}$$

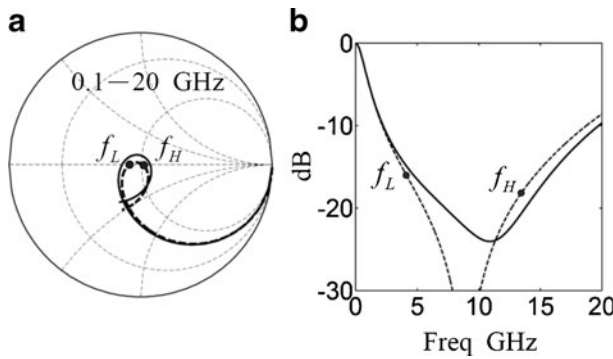
and

$$f_H = \frac{1}{2\pi\sqrt{(L_s + L_d)C_d}} \tag{5}$$

The calculated  $f_L$  and  $f_H$  are 4.09 GHz and 13.24 GHz in this case, and are very close to the simulated 5 GHz and 12.8 GHz, respectively. Apparently, with  $C_d$  used in determining  $\text{Re}[Z_{in}]$ ,  $f_L$  can now be set by  $L_s$  while  $f_H$  could be manipulated by  $L_d$ . Fig. 6 shows the simulated input reflection coefficient with different  $L_s$ , where curves 1–3 have  $L_s=0.3, 0.4,$  and  $0.5\text{nH}$ , and all have their  $C_d=0.13\text{pF}$ ,  $R_d=25\Omega$ , and  $L_d=0.6\text{nH}$ . Fig. 7 illustrates the impact of  $L_d$  on  $S_{in}$ , where curves 1–3 are with  $L_d=0.3, 0.6,$  and  $0.9\text{nH}$ , and all have their  $C_d=0.13\text{pF}$ ,  $R_d=25\Omega$ , and  $L_s=0.3\text{nH}$ . Figure 8 shows the simulated  $S_{in}$  with different  $R_{ds}$ .

**Fig. 4** Equivalent input schematic of the proposed transistor circuit.  $Y_\alpha$  is the admittance looking into  $C_{gd}$  branch,  $Z_\beta$  is the impedance looking into  $C_{gs}$  branch, and  $S_{in}$  is the overall input reflection coefficient.

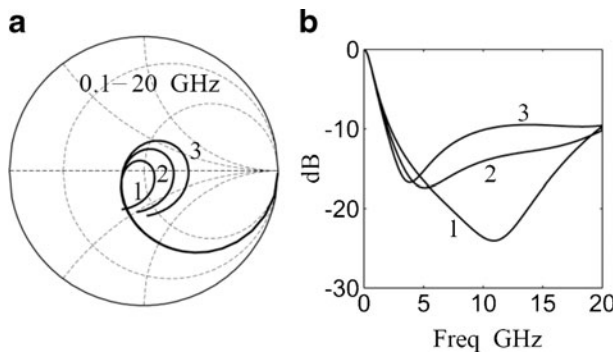




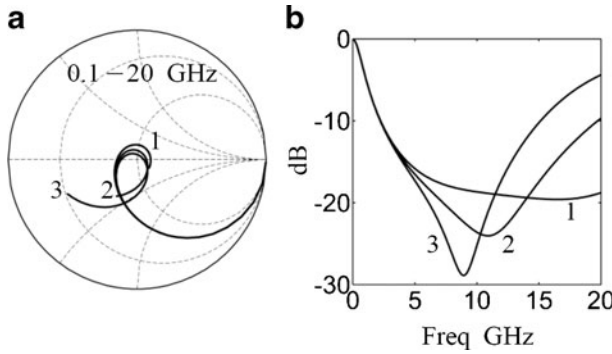
**Fig. 5** Calculated and simulated input reflection coefficient of the proposed transistor circuit. **a** The solid curve on the Smith chart is the simulated result while the dashed curve is its calculated counterpart. Here  $f_L$  and  $f_H$  are the resonant low- and high-frequency points. **b** The same results expressed in dB vs. frequency.

where curves 1–3 have  $R_d=25, 45,$  and  $65\Omega$ , and all have their  $C_d=0.13\text{pF}, L_s=0.3\text{nH},$  and  $L_d=0.6\text{nH}$ . Intuitive understanding of this matching mechanism can now be best described as follow:

- (a)  $f < f_L$  : As series  $R_d L_d C_d$  tends to be open-circuit at very low frequency and the effect of  $L_s$  is very small in this frequency range, the transistor’s loading is now dominated by channel resistance  $R_{ds}$  ( $= 452\Omega$ ). The resulting Miller capacitance  $G_m R_{ds} C_{gd}$  ( $= 2.31\text{pF}$ ) puts the location of  $S_{in}$  in the capacitive region of the Smith chart. As frequency increases, the real part of input impedance will start to be affected by the loading  $C_d$ , as  $\text{Re}[Z_{in}] = C_d / G_m C_{gd}$ . The  $S_{in}$  trajectory can be determined by  $C_d$  and moves along the constant resistance circle in the capacitive region [12].
- (b)  $f_L \leq f < f_H$ : As frequency continues to increase, the inductive voltage induced by  $L_s$  at the input is becoming more obvious, thus the inductive components of  $Z_{in}$  (originating from  $L_s$ ) will resonate out the aforementioned Miller capacitance  $G_m R_{ds} C_{gd}$ . On the Smith chart,  $S_{in}$  will now pass-by the zero point and enter the inductive region; therefore, it is apparently that  $f_L$  can be set by  $L_s$ . Since the loading resistor  $R_d$  ( $= 25\Omega$ ) can also generate a small Miller capacitance  $G_m R_d C_{gd}$  ( $= 0.125\text{pF}$ ), a further bending of the still-inductive  $S_{in}$  on the Smith chart can be observed in this frequency range.



**Fig. 6** Simulated input reflection coefficient of the wideband transistor circuit with different values of  $L_s$ . **a** On the Smith chart, curves 1–3 correspond to  $L_s=0.3, 0.4,$  and  $0.5,$  respectively, while  $C_d=0.13\text{pF}, R_d=25\Omega,$  and  $L_d=0.6\text{nH}$ . **b** The same results expressed in dB vs. frequency.

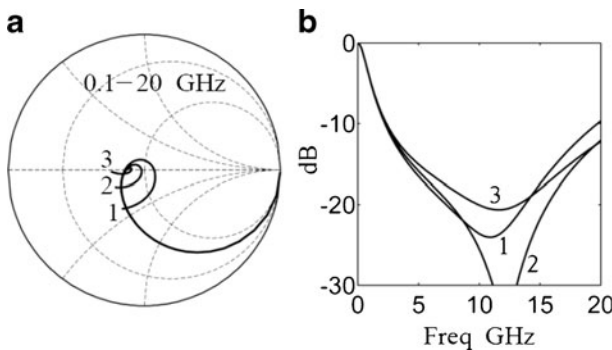


**Fig. 7** Simulated input reflection coefficient of the wideband transistor circuit with different values of  $L_d$ . **a** On the Smith chart, curves 1–3 correspond to  $L_d=0.3, 0.6,$  and  $0.9\text{nH}$ , respectively, while  $C_d=0.13\text{pF}$ ,  $R_d=25\Omega$ , and  $L_s=0.3\text{nH}$ . **b** The same results expressed in dB vs. frequency.

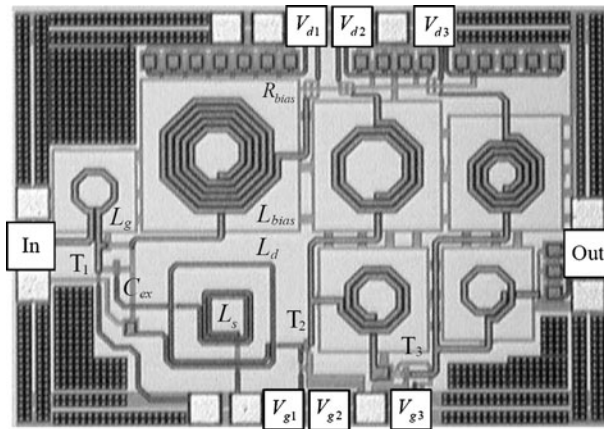
(c)  $f \geq f_H$ : When the inductor  $L_d$  begins to resonate out  $C_d$ , the loading circuit can be approximated as  $R_d$  at the resonance frequency; therefore,  $Z_{in}$  is predominated by the corresponding Miller capacitance  $G_m R_d C_{gd}$ , which means  $S_{in}$  on the Smith chart can be easily dragged into the capacitive region. A complete loop around the zero point is now constructed and we know that  $f_H$  can be changed by  $L_d$ . If the high frequency range means infinite, this  $L_d$  can indeed be omitted; otherwise, the importance of this  $L_d$  cannot be ignored in the case of finite-bandwidth wideband LNA. Thus far, the roles played by  $C_d$ ,  $L_s$ ,  $L_d$ , and  $R_d$  in achieving wideband input matching are well explained and can be easily understood.

### 3 Wideband LNA design

With the wideband matching mechanism fully analyzed, two CMOS LNA's, one covers the more common 3–8 GHz as an initial verification and the other the more challenging 8–25 GHz for exploring this type of circuits' potential and limitation, are designed and fabricated using TSMC 0.18- $\mu\text{m}$  RF-CMOS process. Both the  $S$ -parameters and noise



**Fig. 8** Simulated input reflection coefficient of the wideband transistor circuit with different values of  $R_d$ . **a** On the Smith chart, curves 1–3 correspond to  $R_d=25; 45,$  and  $65\Omega$ , respectively, while  $C_d=0.13\text{pF}$ ,  $L_s=0.3\text{nH}$ , and  $L_d=0.6\text{nH}$ . **b** The same simulated results in dB vs. frequency.



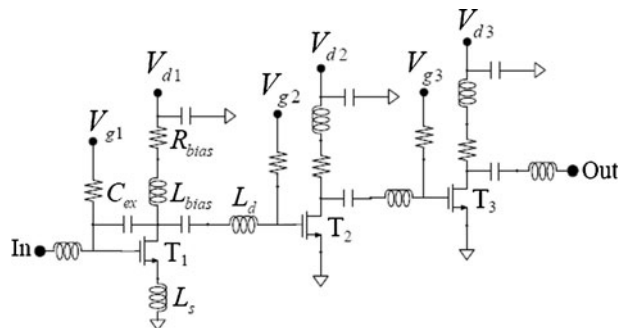
**Fig. 9** Photograph of the 3–8 GHz LNA. The chip size is  $1400 \times 1000 \mu\text{m}^2$ .  $T_1$ ,  $T_2$ , and  $T_3$  are the three transistors.

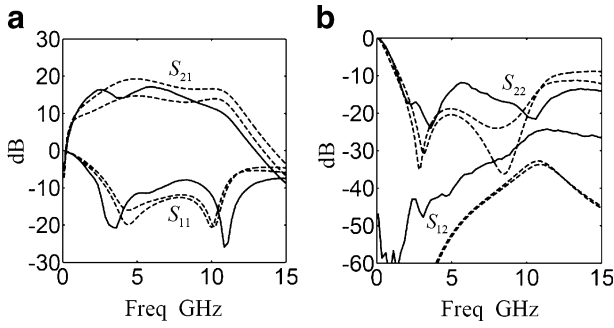
figures of these two circuits are measured on-wafer at room temperature. Description of the circuits and their measured results will be presented below.

Figures 9 and 10 are the photograph and schematic of the 3–8 GHz LNA. It is mainly the InH source inductor  $L_s$ , 1.5nH inter-stage  $L_d$ , and 0.2pF loading capacitor  $C_d$ , that contribute to the wideband input matching. The coupling between  $L_s$  and  $L_d$  allows the reduction of the chip size. To reduce its power consumption, a slightly smaller transistor is used for the first stage. To ensure that the equivalent  $C_{gd}$  is still sufficient to sustain the wideband matching mechanism, an external capacitor  $C_{ex}$  is added. The large inductor  $L_{bias}$  on the drain branch is for DC bias purpose and has small impact on  $S_{11}$  in 3–8 GHz. Since this  $L_{bias}$  tends to introduce a negative  $\text{Re}[Z_{in}]$  at very low frequency,  $R_{bias}$  is used to stabilize this amplifier.

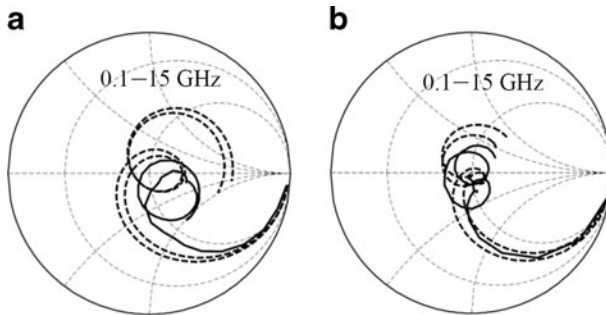
Figure 11 shows the measured and simulated  $S$ -parameters of this 3–8 GHz LNA where the both the  $S_{11}$  and  $S_{22}$  are below -10dB,  $S_{21}$  around 15dB, and  $S_{22}$  far below -20dB. For each measured scattering parameter, there are two simulated counterparts, technically SS and TT corners, to account for the inevitable process variation. The bias is set at  $V_{d1} = 1\text{V}$  and  $I_{d1} = 9.5\text{ mA}$  for the first-stage transistor,  $V_{d2} = 1\text{V}$  and  $I_{d2} = 7.5\text{ mA}$  for the second stage, and  $V_{d3} = 1\text{V}$  and  $I_{d3} = 7.4\text{ mA}$  for the last stage. Figure 12 shows the same  $S_{11}$  and  $S_{22}$  on the Smith chart, and both resemble the familiar wideband hook shape. Figure 13

**Fig. 10** Schematic of the 3–8 GHz LNA.

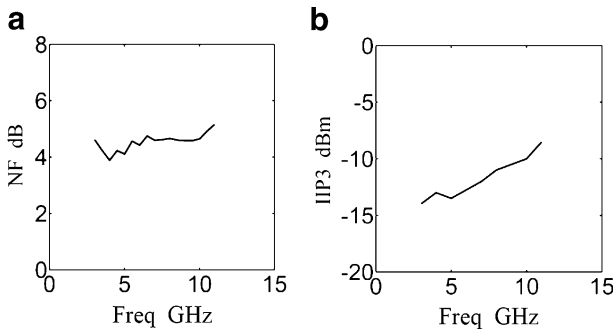




**Fig. 11** Measured and simulated  $S$ -parameters of the 3–8 GHz wideband LNA. **a**  $S_{21}$  and  $S_{11}$  where the solid curves are the measured results and the dashed curves are their simulated counterparts in two circumstances. **b**  $S_{12}$  and  $S_{22}$ .



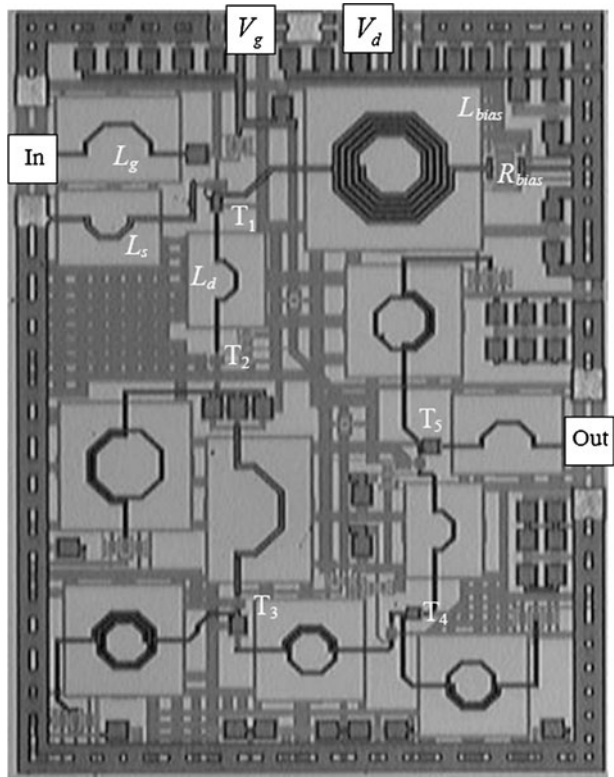
**Fig. 12** Measured and simulated  $S_{11}$  and  $S_{22}$  of the 3–8 GHz wideband LNA on the Smith chart. **a** The solid curve is the measured  $S_{11}$  and the two dashed curves are the simulated counterparts. **b** Measured and simulated  $S_{22}$ .



**Fig. 13** The measured noise figure and IIP3 of the 3–8 GHz wideband LNA. **a** Noise figure. **b** IIP3.



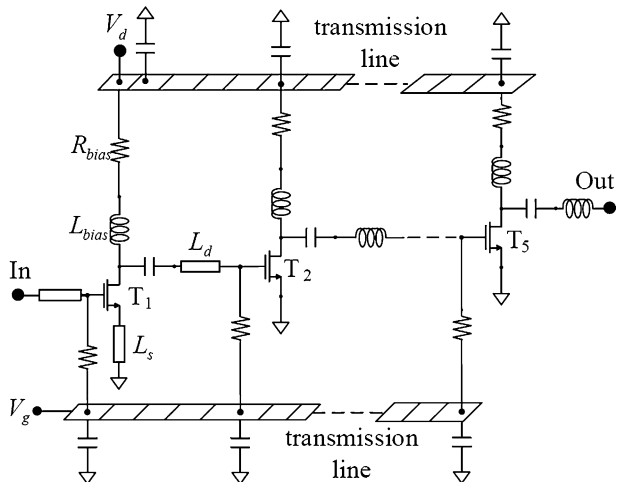
**Fig. 14** Photograph of the 8–25 GHz CMOS LNA. The chip size is  $945 \times 1245 \mu\text{m}^2$ .  $T_1$ ,  $T_2$ ,  $T_3$ ,  $T_4$ , and  $T_5$  are the five transistors.

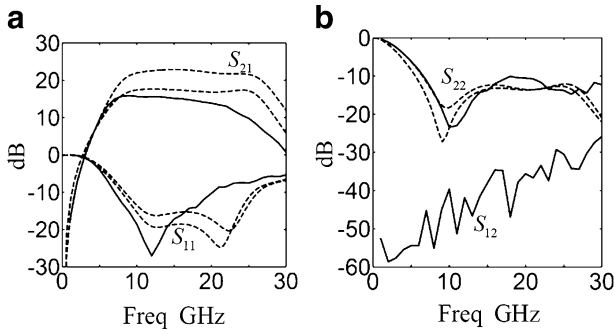


shows the measured noise figure and the linearity (IIP3) of this circuit. The total power consumption of this amplifier is 24.4mW.

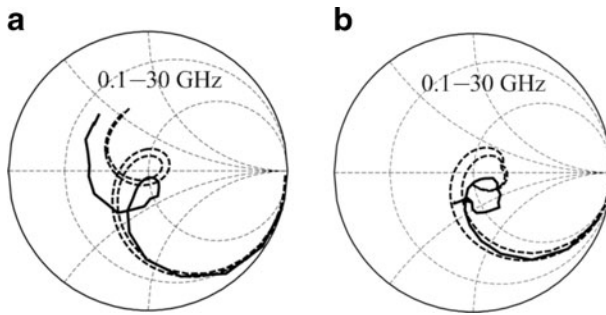
Figures 14 and 15 are the photograph and schematic of the 8–25 GHz five-stage LNA where the design methodology is similar to that of the 3–8 GHz one. To simplify the bias

**Fig. 15** Schematic of the 8–25 GHz CMOS LNA. There is only one drain bias and one gate bias needed for this 5-stage circuit.

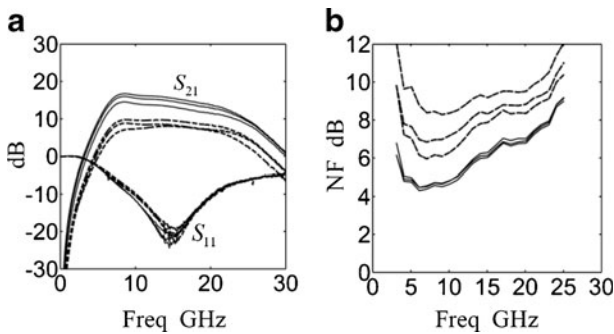




**Fig. 16** Measured and simulated  $S$ -parameters of the 8–25 GHz wideband LNA. **a** Measured (solid) and simulated (dashed)  $S_{21}$  and  $S_{11}$ . **b** Measured and simulated  $S_{12}$  and  $S_{22}$ .



**Fig. 17** Measured and simulated  $S_{11}$  and  $S_{22}$  of the 8–25 GHz wideband LNA on the Smith chart. **a** The solid curve is the measured  $S_{11}$  and the dashed curves are the simulated counterparts. **b** Measured and simulated  $S_{22}$ .



**Fig. 18** Measured  $S_{21}$ ,  $S_{11}$  and noise figure of the 8–25 GHz LNA. **a** Measured  $S_{21}$  and  $S_{11}$  where the solid curves are with  $V_d = 2V$ ,  $I_d$  is 37, 50, and 62 mA; the dashed curves are with  $V_d = 1V$ ,  $I_d$  is 31, 42, and 53 mA, **b** Measured noise figure with  $V_d = 2V$  (solid) and  $V_d = 1V$  (dashed) with different bias current.

scheme, only one drain bias and one gate bias are used. Isolation along the common drain bus between each stage is provided by the long transmission lines that surround the periphery of this chip. A small chip size of  $945 \times 1245 \mu\text{m}^2$  can thus be obtained. With  $V_d = 1.8\text{V}$  and  $I_d = 62 \text{ mA}$ , both the measured and simulated  $S_{11}$  and  $S_{22}$  are below  $-10 \text{ dB}$ ,  $S_{21}$  around  $15 \text{ dB}$ , and  $S_{22}$  far below  $-20\text{dB}$ , as shown in Figs. 16 and 17. Apparently, an increase of the input inductor by the use of bond-wire can easily move the  $S_{11}$  loop upward on the Smith chart and surround the zero point, therefore, lowers the input reflection coefficient further. The total power consumption is  $112\text{mW}$ . To explore this circuit's performance under different bias conditions, Fig. 18 shows the measured input reflection coefficient, gain, and noise figure at different bias conditions where the solid curves are at  $V_d = 2\text{V}$ ,  $I_d$  is 37, 50, and 62 mA; the dashed curves are with  $V_d = 1\text{V}$  and  $I_d$  is 31, 42, and 53 mA, respectively.

## 4 Conclusion

In this paper, the input matching technique for common source wideband LNA design has been thoroughly analyzed. The agreement between the simulated input impedance of the LNA and its calculated counterpart confirms the accuracy of our analysis. To demonstrate its wideband potential, both the 3–8 GHz and 8–25 GHz low noise amplifiers using TSMC 0.18- $\mu\text{m}$  RF-CMOS process are designed, fabricated and measured.

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