# A PETRI NET APPROACH TO EARLY FAILURE DETECTION AND ISOLATION FOR PREVENTIVE MAINTENANCE

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#### SUMMARY

To improve preventive maintenance, this study uses a hybrid Petri net modelling method coupled with parameter trend and fault tree analysis to perform early failure detection and isolation. A Petri net arrangement is proposed that facilitates alarm, early failure detection, fault isolation, event count, system state description and automatic shutdown or regulation. These functions are very useful for health monitoring and preventive maintenance of a system. A fault diagnosis system for district heating and cooling facilities is employed as an example to demonstrate the proposed method. ©1998 John Wiley & Sons, Ltd.

KEY WORDS: hybrid Petri nets; early failure detection and isolation; preventive maintenance; trend chart; threshold; fault tree analysis

## INTRODUCTION

Preventive maintenance (PM) means all actions intended to keep equipment in good operating condition and to avoid failures [1]. PM should be able to indicate when a failure is about to occur, so that repair can be performed before such failure causes damage or capital investment loss. It is very important for any equipment whose failure may lead to severe consequences such as public hazard or financial loss. Such equipment includes nuclear power plants, passenger vehicles and semiconductor production lines. There are three main types of maintenance and three major divisions of PM, as illustrated in Figure 1 [1]. The most common strategy for maintenance is scheduled maintenance, i.e. maintenance is executed by time, by operation times, by material or by some other prescribed criterion. There are at least two drawbacks to this type of maintenance.

- 1. Criteria on which scheduled maintenance is based are statistical averages, e.g. mean time to failure. This makes the risk unavoidable that a system will fail before criteria are exceeded, i.e. a failure may occur unexpectedly.
- 2. The actual working lives of certain parts or modules may be longer than those averages, but such items are replaced during scheduled maintenance before they are worn out, resulting in waste.

In contrast, condition monitoring can be a better and more cost-effective type of maintenance than scheduled maintenance. However, it must be capable of detecting incipient failures prior to their occurrence.

The relationship between error, failure and fault is illustrated in Figure 2. The three terms are defined as follows [2].

1. *Error* is a discrepancy between a computed, observed or measured value or condition and

CCC 0748-8017/98/050319-12\$17.50 ©1998 John Wiley & Sons, Ltd. the true, specified or theoretically correct value or condition.

- 2. *Failure* is an event when a required function is terminated (exceeding the acceptable limits).
- 3. *Fault* is the state characterized by inability to perform a required function, excluding the inability during preventive maintenance or other planned actions or due to lack of external resources.

Based on the above statements, an error is not a failure and a fault is hence a state resulting from a failure. An error is sometimes referred to as an incipient failure [3]. Therefore PM action is taken when the system is still in an error condition, i.e. within acceptable deviation and before failure occurs. Thus, through the technique of PM, failure can be detected early.

There have been many methods proposed for early failure detection [4–6]. This study employs the Petri net modelling method coupled with parameter trend and fault tree analysis to perform early failure detection and isolation for PM. A fault diagnosis system for district heating and cooling facilities will be employed as an example to demonstrate the proposed Petri net method.

## THRESHOLD AND WARNING VALUE

A trend chart [7] is a chart that records the performance of a piece of equipment or a system by time. Methods for generating curves in a trend chart vary with different types of equipment, as depicted in Figure 3. Figure 4 shows a trend chart for a rotating machine. Trend charts are usually established by manufacturers when they run their tests in their laboratories to evaluate quality, reliability, maintainability and maintenance procedures. A threshold is a value used to judge whether an equipment failure occurs or not. It is prescribed as the measurement value that is taken just prior to or at the time of failure, i.e. the maximum allowed value in Figure 4. Life testing is one method to obtain such data, and may be performed by field engineers or users.

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Figure 1. Classification of maintenance



Figure 2. Error, failure and fault

Equipment	Methods		
Rotating machine	<ul><li>* Vibration analysis</li><li>* Oil analysis</li></ul>		
Power system	* Infrared thermography		
Induction motor	* Motor current signature analysis * Circuit analysis		
Pipeline	* Ultrasonic thickness measurement		

Figure 3. Methods for generating curves in trend charts

Once the threshold has been determined, a margin of safety should be added to account for variations in early failure detection. The warning value in Figure 4 is the edge of this margin. The safety margin can be determined by the requirement of lead time for PM or according to the physical properties and actual operating conditions of different systems. The lower the warning value is set, the greater is the assurance that PM will be done prior to failure [1], though more labour manpower and cost will have to be expended. Three standard deviations is one possible choice in prescribing a warning value [8]. On the basis of failure thresholds and warning values, a control chart [1] can be constructed to conduct limit control, as illustrated in Figure 5.

Failure detection can be carried out by comparing actual with nominal quantities, and fault isolation by comparing actual with fault quantities [9]. Consequently, an instrumentation system should be set up for the objective of PM to acquire actual quantities at measurement points. In addition to being used for comparison, acquired quantities can be stored to establish a database for modifying predetermined failure thresholds and warning values. The performance of some systems depends on external conditions. For example, the output current of a power generator varies with the load, which changes with time during a day. Hence thresholds and warning values may be varied according to a scheduled scheme that accomplishes adaptive adjustment for those values. The situation is called 'error' in this paper whenever the



Figure 5. A control chart

acquired quantity exceeds the prescribed warning value but falls within the high and low thresholds.

A fault diagnosis system for district heating and cooling facilities has been proposed [10]. This system is employed as an example for early failure detection and isolation using the method proposed in this study. The system diagram is shown in Figure 6. The facilities are composed of two heat pumps for producing heat, four storage tanks for storing hot and chilled water, two sets of supply pumps for supplying buildings with hot and chilled water respectively, and distribution pipes. The functions of the proposed fault diagnosis system for the facilities can be divided into two parts: reduced-capability diagnosis to prevent a failure and reduced-function diagnosis after a failure. They use the threshold of symptom detection to predict the fault time and a cause-effect tree diagram to find causes of faults. A trigger signal is generated which is a fault alarm or an upper or lower limit alarm once the measured data exceed a reference value. Reference values are presented in [10]. The value for condenser pressure, for example, is 0.1-0.7 kg cm<sup>-2</sup>, varying from September to December. The level of malfunction for this parameter is set at 15% up for the warning value and 20% up for the threshold. This system has been validated using real facilities.

Figure 7 depicts the fault tree of this system. Events 1–9 are measurable, whereas events 10–13 are phenomena which do not need to be measured. Since events 2-1 and 2-2 are the same event, they can be measured by the same sensor. In order to construct the Petri net dealing with system failure, nine sensors are selected to be installed at the associated test points depicted in the fault tree to acquire data. Sensor types, locations and associated sensing signals are depicted in Figure 6.

# PETRI NETS

A Petri net is a general-purpose mathematical tool for describing relations existing between conditions and events [11]. The basic symbols of Petri nets include [12]:

- *place*, drawn as a circle, denoting event
- *immediate transition*, drawn as a thin bar, denoting event transfer with no delay time
- timed transition, drawn as a thick bar, denoting event transfer with a period of delay time
- $\uparrow$  *arc*, drawn as an arrow, between places and transitions
- *token*, drawn as a dot, contained in places, denoting the data



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*inhibitor arc*, drawn as a line with a circle end, between places and transitions.

A transition is said to fire if input places satisfy an enabled condition. Transition firing will remove one token from each input place and put one token into each output place [13]. The basic structures of the logic relations for Petri nets are listed in Figure 8, where there are two types of input places for transition, namely specified and conditional. The former has a single output arc, whereas the latter has multiples. Tokens in a specified-type place have only one outgoing destination; that is, if the input place(s) holds a token, then the transition fires and gives the output place(s) a token. However, tokens in a conditional-type place have more than one outgoing path, which may lead the system to different situations. For the 'TRANSFER OR' Petri net in Figure 8, whether Q or R takes over a token from P depends on conditions such as probability, extra action and self-condition of the place.

There are three types of transitions that are classified based on time [11]. Transitions with no time delay due to transition are called immediate transitions, while those that need a certain constant period of time for transition are called timed transitions. The third type is called a stochastic transition and is used for modelling a process with random time. Owing to the variety of Petri nets [11], it is a powerful tool for modelling flexible manufacturing systems [14,15], multilevel hierarchical systems [16,17], multiprocessor systems [18,19], etc. Besides, Petri nets are capable not only of simulation [20,21], reliability analysis [22] and failure monitoring [23] but also of dynamic behaviour observation [24] and activity prediction [25].

The proposed fault tree of the facilities shown in Figure 7 can be transformed into the Petri net model shown in Figure 9. Since events 2-1 and 2-2 in the fault tree depicted in Figure 7 are the same, they have been combined into  $P_2$  in the Petri net depicted in Figure 9. As a result, each place in Figure 9 represents the associated fault event in Figure 7.

# EARLY FAILURE DETECTION AND ISOLATION ARRANGEMENT

An *early failure detection and isolation arrangement* (EFDIA) is proposed in this paper. It is a hybrid Petri net [11] that includes three kinds of Petri nets: ordinary, inhibitor arc and timed. In Figure 9, each place with a monitor sensor, i.e. each of the nine measurement points in Figure 6, will be equipped with an EFDIA that facilitates alarm, early failure detection, fault isolation, event count, system state description and automatic shutdown or regulation. EFDIA is shown in Figure 10, where the symbols are defined as follows:

- 1. n: total number of sensing points
- 2. *i*: sequence number,  $1 \le i \le n$
- 3.  $M(P)_k$ : marking of place *P* at state *k*, representing the token quantity of place *P* at state *k*, *k* = 1, 2, 3, ...
- 4.  $P_i$ : *i*th place of Petri net;  $M(P_i) = 1$  if  $P_i$  failure occurs.
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- 5. *T<sub>i</sub>*: *i*th transition of Petri net, representing the time duration due to transition
- 6.  $S_i$ : sensing signal for *i*th place;  $S_i$  generates a token such that  $M(S_i) = 1$  if the signal exceeds the prescribed warning value, i.e. an abnormal situation (error) occurs
- 7.  $T_{iE}$ : error transition of  $P_i$ ; immediate transition
- 8.  $T_{iL}$ : error times log transition of  $P_i$ ; immediate transition
- 9.  $T_{iM}$ : maintained transition, representing the transitional time from when the PM action for  $P_i$  is taken to when  $P_i$  is maintained, timed transition
- 10.  $T_{iP}$ : processing transition of  $P_i$ ; immediate transition
- 11.  $T_{iR}$ : reset transition of  $P_i$ ; immediate transition
- 12.  $T_{iS}$ : sensing transition of  $P_i$ ; immediate transition
- 13.  $T_{iT}$ : transfer transition of  $P_i$ ; immediate transition
- 14.  $T_{iU}$ : unprocessed transition of  $P_i$ , representing the transitional time from when the *i*th WARNING SIGNAL appears to when  $P_i$  failure occurs; timed transition
- 15.  $T_{iW}$ : warning times log transition of next lower level  $P^W$ ; immediate transition
- 16.  $P_i^{A}$ : PM action taken place for  $P_i$ ;  $P_i^{A}$  generates a token such that  $M(P_i^{A}) = 1$  if the PM action for  $P_i$  is taken
- 17.  $P_i^{Bj}$ : *j*th buffer place of  $P_i$ , for tokens to stay temporarily, j = 1, ..., x; *x* is the number of input arcs for  $P_i$
- 18.  $P_i^{\text{E}}$ : error indication place of  $P_i$ ;  $M(P_i^{\text{E}}) = 1$  after  $T_{i\text{E}}$  fires if the  $M(S_i) = 1$  situation is generated by  $P_i$  itself but not aroused by lower-level places (for fault isolation)
- 19.  $P_i^{\rm F}$ : failure counter place of  $P_i$ ;  $M(P_i^{\rm F})$  represents the failure times log number of  $P_i$ ;  $M(P_i^{\rm F})$  increases by one when  $P_i$  failure occurs
- 20.  $P_i^{\rm L}$ : error counter place of  $P_i$ ;  $M(P_i^{\rm L})$  represents the error times log number of  $P_i$ ;  $M(P_i^{\rm L})$  increases by one when  $P_i$  error occurs
- 21.  $P_i^{\mathrm{M}}$ : maintenance counter place of  $P_i$ ;  $M(P_i^{\mathrm{M}})$  represents the maintenance times log number of  $P_i$ ;  $M(P_i^{\mathrm{M}})$  increases by one when the  $M(S_i) = 1$  situation is maintained
- 22.  $P_i^{\rm P}$ : processing place of  $P_i$ , representing  $P_i$  in the being maintained situation
- 23.  $P_i^{\text{R}}$ : reset counter place of  $P_i$ ;  $M(P_i^{\text{R}})$  represents the warning times log number of  $P_i$  that are aroused by lower-level places, i.e. the reset times of the *i*th RESET R;  $M(P_i^{\text{R}})$  increases by one when the *i*th RESET R is triggered
- 24.  $P_i^{\text{T}}$ : transitional place of  $P_i$ , representing a transitional state inserted between  $S_i$  and  $P_i$ , of duration  $T_{i\text{S}}$  plus  $T_{i\text{T}}$ , which is the original path from  $S_i$  to  $P_i$  without EFDIA constructed
- 25.  $P_i^{\text{U}}$ : unprocessed place of  $P_i$ , representing the error of  $P_i$  not corrected
- 26.  $P_i^{W}$ : warning counter place of  $P_i$ ;  $M(P_i^{W})$  represents the warning times log number of  $P_i$  no matter from where warning cause arises;  $M(P_i^{W})$  increases by one when the *i*th RESET W is triggered
- 27. *i*th RESET E: reset E place of  $P_i$ , representing a reset signal for  $P_i^{\rm E}$ ; generates a token when it is triggered



Figure 7. Fault tree of heating and cooling facilities

Logic relation	TRANSFER	AND	OR	TRANSFER AND	TRANSFER OR	INHIBITION
Description	If P then Q	If P AND Q then R	If P OR Q then R	If P then Q AND R	If P then Q OR R	If P AND Q' then R
<b>Boolean function</b>	Q=P	R=P*Q	R=P+Q	Q=R=P	Q+R=P	R=P*Q'
Petri nets	Q + P	R P Q	P Q	Q R P	Q R P	R P Q

Figure 8. Basic structures of logic relations for Petri nets

- 28. *i*th RESET R: reset R place of  $P_i$ , representing a reset signal for  $P_i^{R}$ ; generates a token when it is triggered
- 29. *i*th RESET W: reset W place of  $P_i$ , representing a reset signal for  $P_i^{\rm B}$ ; generates a token when it is triggered; the number of the *i*th RESET W should equal number of inhibitor arcs of transition  $T_{i\rm E}$
- 30. ASFM: automatic shutdown or feedback mechanism; for instance, an air-conditioning or ventilation system is a feedback mechanism for an over temperature module
- 31. *i*th WARNING SIGNAL: warning signal place for  $P_i$

32. CLOCK: a clock is embedded to record the time of event occurrence

The operational steps for EFDIA are described as follows.

1. Transition  $T_{iS}$  fires if  $S_i$  exceeds the prescribed warning value. Subsequently, each of  $P_i^{B1}$ , *i*th WARNING SIGNAL,  $P_i^{T}$  and next higher  $P^{B2}$ obtains a token. As defined in the previous paragraph, M(P) is the marking of place P. Thus  $M(P_i^{T}) = 1$  represents this  $S_i$  monitored subsystem (module) at a transitional state. Similarly, M(ith WARNING SIGNAL) = 1 represents that the *i*th



Figure 9. Petri net of Figure 7



Figure 10. Early failure detection and isolation arrangement (EFDIA)

WARNING SIGNAL goes on, which may be a light, a beep or some other form, to indicate that  $S_i$  exceeds the prescribed warning value.

- 2. There are two paths to follow.
  - (a)  $T_{iP}$  fires if  $P_i^A$  generates a token, i.e. PM action is taken. The tokens in  $P_i^A$  and the *i*th WARN-ING SIGNAL move to  $P_i^P$ , i.e. the subsystem (module) is being maintained. Otherwise,  $T_{iU}$ fires if  $P_i^A$  does not generate a token during the transition time of  $T_{iU}$ , such that  $P_i^U$  acquires a token.
  - (b)  $T_{iE}$  fires if  $P_i^{B2}$  has no token, i.e. this error is not caused by the next lower subsystem (module) but by the *i*th-level subsystem (module) itself, such that  $P_i^E$  obtains a token. On the other hand, if  $P_i^{B2}$  holds a token, i.e. this error results from the next lower subsystem (module), then  $T_{iE}$  does not fire, such that the token from  $S_i$  will be held in  $P_i^{B1}$ . The error is hence isolated.

- 3. There are again two paths to follow.
  - (a)  $T_{iM}$  fires if the PM action is finished, such that the tokens in  $P_i^P$  and in  $P_i^T$  move to  $P_i^M$ , i.e. this error has been corrected. Otherwise,  $T_{iT}$  fires if  $P_i^U$  obtains a token resulting from the firing of  $T_{iU}$ , i.e. PM action was not taken in time, such that tokens in  $P_i^U$  and  $P_i^T$  move to  $P_i$ , i.e.  $P_i$  failure occurs. As a consequence, both  $P_i^F$ and ASFM also obtain a token. Accordingly, the failure times log number increases by one and the ASFM is triggered. This mechanism can be optional for different systems.
  - (b)  $T_{iL}$  fires if  $P_i^E$  holds a token and the *i*th RESET E is triggered, such that  $P_i^L$  obtains a token, i.e. the error times log number of  $P_i$  increases by one. Otherwise, the token in buffer place  $P_i^{B1}$ will move to  $P_i^R$  when  $T_{iR}$  fires by triggering the *i*th RESET R, i.e. this error is not caused by  $P_i$ and the reset times log number of  $P_i$  increases



Figure 11. Flow chart of EFDIA

by one. Similarly, the *i*th RESET W triggers to fire  $T_{iW}$  such that the token in the other buffer place,  $P_i^{B2}$ , moves to the next lower  $P^W$ , i.e. the warning times log number of the next lower  $P^W$  increases by one.

Conventionally, a flow chart is an easier representation for understanding the operational steps. Therefore the above descriptions are summarized into a flowchart for clarity, as shown in Figure 11.

EFDIA is composed of several small arrangements, each of which has a specific function.

1. *Reset.* The *i*th RESET E and  $P_i^E$  together with  $T_{iL}$  form a logic AND relation. The *i*th RESET E generates a token whenever this reset button has been triggered, so as to fire  $T_{iL}$  and remove a token from  $P_i^E$  to  $P_i^L$  whenever  $P_i^E$  holds a token and needs to be reset. In a similar manner, the *i*th RESET R and *i*th RESET W are designed to reset  $P_i^{B1}$  and  $P_i^{B2}$  respectively.

- 2. *Inhibition*. Both  $T_{iE}$  and  $T_{iU}$  are transitions with an inhibitor arc. This arrangement is designed to inhibit the firing of  $T_{iE}$  and  $T_{iU}$  whenever the place where the inhibitor arc is connected, i.e.  $P_i^{B2}$  and  $P_i^A$  respectively, holds a token.
- 3. Conditional place. Any place that has more than one outgoing arc is called a conditional place. Tokens contained in a conditional place will move to an output place through the transition which is firstly enabled among all the output transitions of the transitional places. A conditional place models a conditional state of a system or process. In EFDIA,  $P_i^{A}$ ,  $P_i^{B1}$ ,  $P_i^{B2}$ ,  $P_i^{T}$  and the *i*th WARNING SIGNAL are conditional places.
- 4. *Counter*.  $P_i^{\bar{F}}$ ,  $P_i^L$ ,  $P_i^M$ ,  $P_i^R$  and  $P_i^W$  perform as counters to accumulate occurrence times of associated events.
- Event flag. Several places are designed as event flags. Each of them represents an associated event once the marking of the place becomes unity.
  - (a)  $P_i$  denotes the failure of the *i*th place.

- (b) P<sub>i</sub><sup>E</sup> denotes the error located at the *i*th place.
  (c) P<sub>i</sub><sup>T</sup> denotes the *i*th place at a transitional state.
- (d) The *i*th WARNING SIGNAL denotes the *i*th monitored signal exceeding the warning value.
- (e) ASFM means the automatic shutdown function or feedback mechanism is triggered.

#### PROPERTIES OF EFDIA

This section presents the capabilities of EFDIA and the invariants derived from EFDIA.

#### Capabilities

- 1. Alarm. EFDIA provides alarm capability whenever an over-warning-value situation occurs, by triggering the *i*th WARNING SIGNAL for the associated place.
- 2. Early failure detection. EFDIA is capable of early failure detection, since the alarm function operates whenever the acquired signal exceeds a prescribed warning value but not the failure threshold. This means that the abnormal situation is detected before failure occurs. As shown in Figure 5, the lead time of early detection can be obtained by extrapolating the curve in a control chart with a line slope that is constructed by the last two sampled points on the curve [10]. The lead time is the period between the time point where the warning value is exceeded and the intersection of the extended line and time axis.
- 3. Fault isolation. The cause(s) of malfunction of a system can be located anywhere within the system. However, since malfunction causes are constrained by the logic relations of the fault tree, they can be isolated by the inhibit transition  $T_{iE}$  via the indication of the event flag  $P_i^{\rm E}$ . The error is located at the *i*th place if  $M(P_i^{\rm E}) = 1$ . Otherwise, the error of the *i*th place arises from the lower-level place(s) even if the *i*th WARNING SIGNAL appears.
- 4. Event count. All the counters designated in EFDIA record the associated occurrence times of events. By incorporating a time clock, the associated rates can be obtained at the same time. The following items can be derived from EFDIA:
  - (a) failure rate of the *i*th place:  $M(P_i^F)/t$
  - (b) error rate of the *i*th place:  $M(P_i^{\rm L})/t$
  - (c) maintenance rate of the *i*th place:  $M(P_i^{\rm M})/t$
  - (d) alarm rate of the *i*th place:  $M(P_i^W)/t$ .

From these rates, two advantages can be obtained.

- (a) If the *i*th subsystem is maintained whenever an error is detected, the failure rate of the *i*th place can be minimized such that the system reliability is promoted.
- (b) All the rates can be recorded as historical data so as to perform statistical prediction for system failure (by failure rate and error rate), and the time needed for maintenance (by maintenance rate) of each subsystem can be derived.
- 5. System state description. The system state is clearly visible by the indication of every place in EFDIA. The following parameters are defined to account for

the system state:

- (a)  $\mathbf{M}_k$ : marking of the Petri net at state k,  $\mathbf{M}_k =$  $[M(P_1), M(P_2), \dots, M(P_n)]^{\mathrm{T}}$
- (b)  $S_k$ : sensing signal matrix at state k,  $\mathbf{S}_{k} = [M(S_{1}), M(S_{2}), \dots, M(S_{n})]^{\mathrm{T}}$
- (c)  $\mathbf{L}_k$ : maintenance log matrix at state k,  $\mathbf{L}_k =$  $[M(P_1^{\rm M}), M(P_2^{\rm M}), \dots, M(P_n^{\rm M})]^{\rm T}$
- (d)  $\mathbf{F}_k$ : failure times log matrix at state k,  $\mathbf{F}_k =$  $[M(P_1^{\rm F}), M(P_2^{\rm F}), \dots, M(P_n^{\rm F})]^{\rm T}$
- (e)  $\mathbf{E}_k$ : error indication matrix at state k,  $\mathbf{E}_k = [M(P_1^{\rm E}), M(P_2^{\rm E}), \dots, M(P_n^{\rm E})]^{\rm T}$ ; the ith entry indicates that the error is located at the *i*th place if the *i*th entry value is unity.
- 6. Auto shutdown or regulation. Automatic shutdown or regulation capability can be provided by EFDIA through triggering the ASFM place.
- 7. Time recording. The time at which each event occurs can be recorded by the embedded CLOCK. This is required for failure analysis.

#### Invariants

According to the properties of EFDIA, the following invariants can be derived:

- 1.  $M(P_i^{\rm L})k + M(P_i^{\rm R})k = M(P_i^{\rm W})k$ . The number of warning signals for the *i*th place at state k is equal to the summation of the error times log number and the reset times log number at state k for the *i*th place.
- 2.  $M(P_i^{\rm F})k + M(P_i^{\rm M})k = M(P_i^{\rm W})k$ . For the *i*th place at state k, failure times plus maintenance times equal the warning times log number.
- 3. At basic places,  $M(P^{R})k = 0$  and  $M(P^{L})k =$  $M(P^{W})k$ . Since there is no place lower than basic places, the error times log number and the warning times log number are equal at basic places.
- 4.  $M(P_i^{\rm P})k + M(P_i^{\rm U})k = 1$ . Since the conditions that an error place is maintained and not maintained are mutually exclusive, at state k either the marking for  $P_i^{\rm P}$  or that for  $P_i^{\rm U}$  is unity.

## **EXAMPLE**

The Petri net for the heating and cooling facilities endowed with EFDIA is shown in Figure 12. It is a result of appending an EFDIA to each place with a monitor sensor in Figure 9, i.e.  $P_1$  to  $P_9$ . The logic relations among all places in Figure 9 are still retained in Figure 12. At basic places, i.e.  $P_1$  to  $P_6$ , the function for testing whether the error cause is from the next lower place or not becomes unnecessary. The following two situations are used to demonstrate the function of EFDIA in the employed system.

1. Suppose the monitored signal for cooling water flow, i.e.  $S_1$  in Figure 12, exceeds the prescribed warning value. Subsequently,  $T_{1S}$  fires such that the 1st WARNING SIGNAL goes on and each of  $P_1^{\rm T}$ ,  $P_7^{\rm B3}$ and  $P_1^{\rm E}$  obtains a token.  $M(P_1^{\rm T}) = 1$  represents the cooling water flow rate that is in an error situation and it is a transitional state between normal and faulty. There is a lead time from then until  $P_1$  failure



Figure 12. Petri net for DHC facilities endowed with EFDIA

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really happens. If the PM action takes place during the lead time, then  $P_1^A$  generates a token such that  $T_{1P}$  fires so as to make the tokens in  $P_1^A$  and the 1st WARNING SIGNAL move to  $P_1^P$ . The subsystem is being maintained and the 1st WARNING SIGNAL goes off at this moment.  $T_{1M}$  fires if the PM action is finished. Subsequently, the tokens in  $P_1^P$  and  $P_1^T$ move to  $P_1^{\rm M}$ , i.e. this error has been corrected. The marking of  $P_1^{\rm M}$ , i.e. the maintenance times log number for  $P_1$ , increases by one. On the other hand, if the PM action does not take place in time, then  $T_{1U}$ fires such that  $P_1^U$  obtains a token. Consequently, the tokens in  $P_1^U$  and  $P_1^T$  move to  $P_1$ . Hence  $P_1$  failure occurs. At the same time,  $P_1^F$  obtains a token, i.e. the failure times log number increases by one. Because of the logic relation between  $P_1$  and  $P_7$ , the monitored signal for  $P_7$ , i.e.  $S_7$ , exceeds the prescribed warning value due to  $P_1$  failure. Accordingly, the 7th WARNING SIGNAL goes on and each of  $P_7^{\rm T}$ ,  $P_7^{\rm B1}$ and  $P_7^W$ , obtains a token.  $T_{7E}$  is inhibited by the token in  $P_7^{B3}$ , such that the tokens in  $P_7^{B1}$  and  $P_7^{B3}$  move to  $P_7^R$  and  $P_1^W$  after triggering the 7th RESET R and 7th RESET W1 respectively. Hence this error is located at  $P_1$ , whereas  $M(P_7^{\rm L})$  does not increase.

2. Suppose the monitored signal for condenser pressure, i.e.  $S_7$ , exceeds the prescribed warning value spontaneously while both  $S_1$  and  $S_2$  are at normal condition. As a result,  $T_{7S}$  fires such that the 7th WARNING SIGNAL goes on. Simultaneously, each of  $P_7^T$ ,  $P_7^{B1}$  and  $P_7^W$  obtains a token. In a similar manner, as  $S_1$  exceeds the prescribed warning value,  $M(P_7^M)$  increases by one if the PM action for  $P_7$  takes place in time. Otherwise,  $P_7$  failure occurs such that  $M(P_7^F)$  increases by one. However, since  $P_7^{B2}$  and  $P_7^{B3}$  are both empty,  $T_{7E}$  fires such that  $P_7^E$  obtains a token. As a result,  $M(P_7^L)$ , i.e. the error times log number for  $P_7$ , increases by one.

ASFM is to prevent higher-level fault or system breakdown from happening by automatic shutdown or regulation. It should be incorporated with the places that may cause safety problems in a Petri net. In this example it can be triggered by either  $P_6$  or  $P_7$  failure, i.e. excess pump energy increased or condenser pressure high.

#### CONCLUSIONS

This paper has presented an early failure detection and isolation scheme for PM via the heating and cooling facilities example, by using a hybrid Petri net modelling method coupled with parameter trend and fault tree analysis. The Petri net dealing with system failure has to be constructed beforehand. The next task is to obtain trend charts for all fault places in the Petri net in order to prescribe thresholds and allowable margins. With these prerequisites the present method can be applied to any system. The proposed Petri net approach can not only achieve early failure detection and isolation for fault diagnosis but also facilitates event count, system state description and automatic shutdown or regulation. These capabilities can be very useful for health monitoring and preventive maintenance of a system.

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