A Novel Hybrid Coupler Based on Antiresonant Reflecting Optical Waveguides

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Abstract—A novel hybrid coupler based on the antiresonant reflecting optical waveguides (ARROW's) is presented. This device consists of two parallel antiresonant reflecting optical waveguides with a tapered outermost cladding layer. Such a device can provide advantageous features of low radiation loss, low crosstalk at the output end, and compatible core dimensions and indexes with single-mode optical fibers. The staircase approximation and the eigenmode expansion analysis are used to analyze and optimize this device. In our design on a Si-substrate, radiation losses below 0.38 dB and extinction ratios below -20 dB for two waveguide channels are achieved. The beam propagation method (BPM) is also used to verify our design and analysis results.

Index Terms—Optical beam splitting, optical coupling, optical power dividers/combiners, optical resonance, optical waveguides.

I. INTRODUCTION

BEAM splitters and beam combiners are basic elements to construct various optical circuits. Optical hybrid couplers, which can provided both of these functions in integrated optics, have been proposed and demonstrated [1]-[6]. Such versatile devices are attractive for applications in optical communications, optical signal processing, optical networks, and optical microsensing systems. A conventional waveguide hybrid coupler consists of a symmetric and an asymmetric Yjunctions connected directly. In each Y-junction, there exist two normal modes, even and odd modes, traveling along the propagation direction. For the input symmetric Y-junction, the amplitudes of the fields for both modes in two individual waveguides are the same; on the other hand, in the output asymmetric Y-junction, the field of the even mode is mainly confined in the wide-arm and the odd mode mainly in the narrow-arm, respectively. The branching angles of two Yjunctions are designed to be small enough so that the device is adiabatic. The input conditions of the optical fields will determine the outputs of the wide- and narrow-arms in the asymmetric Y-junction. However, for a conventional hybrid coupler, there exist inherent disadvantages of difficult alignment and low coupling efficiency when connected to optical fibers due to their incompatible core dimensions or indexes. Moreover, the separations between two arms at the input and output ends must be wide enough to reduce the crosstalk

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between two waveguide channels, and thus the device length is difficult to reduce.

The antiresonant reflecting optical waveguides (ARROW's) are promising to replace conventional hybrid couplers because of their flexible design rules of core and cladding dimensions [7]. In comparison with conventional waveguides, ARROW waveguides utilize antiresonant reflection as the guiding mechanism instead of total internal reflection. With this structure, ARROW devices can guide waves in low-index cores with large core sizes such that their core indexes and sizes can be compatible with single-mode fiber indexes and diameters, which provide efficient connections with fibers. In addition, the coupling length of a dual ARROW waveguide is not increasing but varies as a periodic function with the increasing waveguide separation such that a remote coupler can be realized [8], [9]. Based on our previous investigation, it is found that the maximum coupling efficiency of a dual parallel ARROW waveguide can be controlled from 100 to 0% by simply varying the outermost cladding thickness to change their symmetry [10]. In this paper, we present a novel hybrid coupler based on ARROW waveguides to provide the same functions as a conventional hybrid coupler [11]. The outermost cladding layer is tapered from the exact symmetric structure to the extremely asymmetric one, so that the fields of the symmetric and extremely asymmetric sides are similar to those in the input and output Y-junctions of a conventional hybrid coupler. Compatible core dimensions and indexes with single-mode fibers and a large separation thickness can be achieved by utilizing the periodic property of antiresonant conditions. The input and output coupling efficiency are thus significantly improved. In addition, by an optimum design of the outermost cladding thickness at the input and output ends, equal excitations of two normal modes at the input end and a low crosstalk at the output end can be achieved. Moreover, the surface scattering is relieved because only the thickness of the outermost cladding layer is changed along the device and the fields are mainly confined within the cores.

In Section II, the basic structure of an ARROW hybrid coupler and its operation principle are discussed. In Section III, the continuous tapered structure is modeled by dividing them into various segments with small step discontinuities [12]. The characteristic matrix method is applied to obtain the effective indexes, propagation losses, and field distributions of the propagation modes for each segment [9], [10]. The adiabatic invariance condition is verified by analyzing the mode transition of propagation modes using the abovementioned staircase approximation and eigenmode expansion analysis

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[13]. In Section IV, a design example and the simulation results using the eigenmode expansion analysis are given and the beam propagation method (BPM) is used to verify the theory and design [14]–[16]. Finally, a brief conclusion is given in Section V.

II. BASIC STRUCTURE AND OPERATION PRINCIPLE OF AN ARROW HYBRID COUPLER

The configuration of an ARROW hybrid coupler (n_a/n_{l_1}) $/n_{h_1}/n_{g_1}/n_{h_1}/n_{
m sep}/n_{h_2}/n_{g_2}/n_{h_2}/n_{l_2}/n_s)$ is depicted in Fig. 1, which consists of two parallel ARROW waveguides, a gradually tapered upper cladding layer, and a separation layer. The core layers of two ARROW waveguides are with low refractive indexes of n_{g_1} and n_{g_2} , and thickness of d_{g_1} and d_{g_2} , respectively. The upper waveguide is sandwiched between two high-index (n_{h_1}) cladding layers of thickness d_{h_1} , and atop this upper sandwiched waveguide is a tapered low-index (n_{l_1}) cladding layer of thickness d_{l_1} . The lower waveguide is sandwiched between two high-index (n_{h_2}) cladding layers of thickness d_{h_2} , and under this lower sandwiched waveguide is another low-index (n_{l_2}) cladding layer of thickness d_{l_2} . Between two ARROW waveguides there is a separation cladding layer with an index of $n_{\rm sep}$ and a thickness of $d_{\text{sep.}}$ The upper core index (n_{g_1}) and dimension (d_{g_1}) are flexibly chosen to be compatible with connected single-mode fibers, the core layer of the lower waveguide must satisfy the transverse resonance condition, and its thickness d_{g_2} is given as [7]

$$d_{g_2} = \frac{\lambda}{2n_{g_2}} \left[1 - \left(\frac{n_{g_1}}{n_{g_2}}\right)^2 + \left(\frac{\lambda}{2n_{g_2}d_{g_1}}\right)^2 \right]^{-(1/2)}.$$
 (1)

Except the upper cladding layer of d_{l_1} , all cladding layers satisfy the transverse antiresonance condition as

$$d_{j} = \frac{\lambda}{4n_{j}} \left[1 - \left(\frac{n_{g_{1}}}{n_{j}}\right)^{2} + \left(\frac{\lambda}{2n_{j}d_{g_{1}}}\right)^{2} \right]^{-(1/2)} \cdot (2P_{j} + 1), \qquad P_{j} = 0, 1, 2, 3, \cdots$$
(2)

where $j = h_1$ (and h_2), sep, and l_2 , representing corresponding high-index, separation and low-index cladding layers, respectively. P_j is the order of antiresonant condition, which can be arbitrarily chosen to adopt to butt-connection with singlemode fibers easily. Since the coupling strength between dual ARROW waveguides strongly depends on the degree of their symmetry, the thickness of the upper cladding layer can be adjusted to change the degree of their symmetry and thus the coupling efficiency between two guides can be varied. In our ARROW hybrid coupler device, the dual waveguides are exactly symmetric at the input end and extremely asymmetric at the output end. The thickness of the upper cladding layer (d_{l_1}) is thus gradually tapered from the input end to the output end as shown in Fig. 1.

Throughout the whole device there are two normal modes (one even and one odd modes) traveling along the propagation direction. The typical field distributions of two normal modes at several corresponding positions along the propagation direction are shown in Fig. 2. The peak amplitudes of the fields



Fig. 1. The schematic view of an ARROW hybrid coupler.



Fig. 2. The field distributions of two normal modes corresponding to the positions in Fig. 1.

for both modes in two individual waveguides are the same at the input end. The tapering angle is carefully designed to meet the adiabatic invariance condition such that the power resided in the initial modes at the beginning still remains in the same modes during traveling along the device [17]. The field of the even mode is mainly confined in the lower guide g_2 and the odd mode mainly in the upper guide g_1 at the output end, respectively. If two beams with the same amplitudes in phase are launched into two guides g_1 and g_2 at the input end, only the even mode can be excited and the power will be confined within guide 2 (g_2) at the output end. On the other hand, when two input beams with the same amplitudes are out of phase, only the odd mode will be excited and the power will be confined within guide 1 (g_1) at the output end as shown in Fig. 2. In such a way, the original power in two guide channels can be combined into one of these two guide channels depending on the phase difference between two input beams. In another case, if only single beam is launched into the input end of one of these two waveguides, even and odd modes are equally excited, and then adiabatically transferred into two guides $(g_1 \text{ and } g_2)$, respectively, and the device functions as a power divider.

Based on the reciprocity theorem, a reversed hybrid coupler can convert the original power combiner to a power divider when only one beam is input to guide 1 (g_1) or guide



Fig. 3. The staircase model of an ARROW hybrid coupler.

2 (g_2) . By combining these original and reversed hybrid couplers, an integrated-optical Michelson interferometer can be realized [2].

III. STAIRCASE APPROXIMATION AND EIGENMODE EXPANSION

In this section, staircase approximation and eigenmode expansion analysis are used to determine the adiabatic invariance condition [13]. In our analysis, the continuous tapered structure is divided into a series of staircase segments with small and abrupt discontinuities as shown in Fig. 3. The total number of segments is determined by satisfactory convergence when this number is enough increased. The field distributions and propagation losses of associated eigenmodes within each segment are obtained by applying the characteristic matrix method [9], [10]. The effective indexes of eigenmodes for our ARROW waveguides are solved in the complex plane due to their leaky characteristics. The imaginary parts of the effective indexes represent propagation losses of ARROW modes. The unphysical problem associated with the leaky mode representation can be relieved by the truncated method [18] with a suitable and systematic method to meet the orthogonality relation. Any field distribution f(x,z) at any position within the kth segment can be expressed by the summation of eigenmodes with their individual expansion coefficients as

$$f^{(k)}(x,z) = \sum_{g=e,o} a_g^{(k)} u_g^{(k)}(x) \exp\left(-j\beta_g^{(k)}z\right)$$
(3)

where $u_g^{(k)}(x), a_g^{(k)}$, and $\beta_g^{(k)}$ represent the normalized field distribution, propagation constant, and expansion coefficient of an eigenmode at the *k*th segment, respectively, and subscript g indicates a discrete guided mode which should be summed up. The normalized field distribution of the eigenmode $u_g^{(k)}(x)$ is multiplied by the phase term $\exp(-j\beta_g^{(k)}z)$ and its own expansion coefficient $a_g^{(k)}$ to express the wave propagation. In our case, only the first two modes, even and odd modes, are involved because only these modes can be efficiently excited by the fundamental mode from a single-mode fiber (or waveguide) input-coupling. The mode-conversion between these two modes can be simulated to determine the adiabatic invariance condition.

The boundary conditions at the step discontinuity give the relation as

$$\sum_{g=e,o} a_g^{(k)} u_g^{(k)}(x) \exp\left(-j\beta_g^{(k)} L^{(k)}\right)$$
$$= \sum_{g=e,o} a_g^{(k+1)} u_g^{(k+1)}(x) \tag{4}$$

where $L^{(k)}$ is the length of the *k*th segment. Here, it is assumed that the reflections of the next segments is negligible. This assumption is appropriate for our case since the fields of even and odd modes are mainly confined within the cores and only the thickness of the outermost cladding layer is changed. Combining the above equation with the orthogonal relations, the expansion coefficients of all modes at the (k+1)th segment can be reconstructed as

$$a_{g}^{(k+1)} = \sum_{h=e,o} a_{h}^{(k)} \exp\left(-j\beta_{g}^{(k)}L^{(k)}\right) \cdot \int u_{h}^{(k)}(x) \left[u_{g}^{(k+1)}(x)\right]^{*} dx \equiv \sum_{h=e,o} a_{h}^{(k)} \exp\left(-j\beta_{g}^{(k)}L^{(k)}\right) \left\langle u_{h}^{(k)}(x)|u_{g}^{(k+1)}(x)\right\rangle.$$
(5)

Therefore, we obtain

$$A^{(k+1)} = A^{(k)} \cdot P^{(k)} \cdot C^{(k,k+1)}$$
(6)

where $A^{(k)}$ is the input expansion matrix, which is composed of expansion coefficients of even and odd modes at the beginning of the *k*th segment, i.e., $A^{(k)} = [a_e a_o]^{(k)}; P^{(k)}$ describes the propagation phenomena of all modes in the *k*th segment given as

$$\boldsymbol{P}_{ij}^{(k)} = \left[\exp(-j\beta_i^{(k)}L^{(k)}) \right] \cdot \delta_{ij} \tag{7}$$

where δ_{ij} is the Kronecker delta function and $C^{(k,k+1)}$ is the coupling matrix describing the coupling phenomena between modes in two adjacent segments at the corresponding step discontinuity, defined as

$$\mathcal{C}_{ij}^{(k,k+1)} = \left\langle u_i^{(k)}(x) | u_j^{(k+1)}(x) \right\rangle.$$
(8)

Whenever the expansion matrix at the input end is determined, the output expansion matrix is obtained segment by segment from (6) as

$$\boldsymbol{A}^{(N)} = \boldsymbol{A}^{(1)} \cdot \left[\boldsymbol{P}^{(1)} \cdot \boldsymbol{C}^{(1,2)} \cdot \boldsymbol{P}^{(2)} \cdot \boldsymbol{C}^{(2,3)} \cdots \right] \cdot \boldsymbol{C}^{(N-1,N)} \cdot \boldsymbol{P}^{(N)} = \boldsymbol{A}^{(1)} \cdot \boldsymbol{T} \qquad (9)$$

where N is the total number of divided segments and T is the system transfer matrix. Once the tapered structure is modeled by the staircase approximation, the length of a segment $L^{(k)}$ can be changed when the tapering angle is varied, such that it is not necessary to recalculate the coupling matrices.

The mode-conversion effect can be observed by the phase behavior of even and odd modes. We can now extract the phase term in (9) to describe such effects. First, we observe the mode-conversion phenomena of an even mode. In this case, the input field is assumed to be the normalized even mode, i.e., $A^{(1)} = [1 \ 0]$. If the adiabatic invariance condition holds, i.e., no cumulative mode conversion occurs, the mode coefficient a_o at the output end will be very low. According to (5) and (6), the mode coefficient a_o of the (k + 1)th segment can be represented as

$$a_{o}^{(k+1)} = a_{e}^{(k)} \exp\left(-j\beta_{e}^{(k)}L^{(k)}\right) \cdot C_{eo}^{(k,k+1)} + a_{o}^{(k)} \exp\left(-j\beta_{o}^{(k)}L^{(k)}\right) \cdot C_{oo}^{(k,k+1)}.$$
 (10)

Each variable of the above equation is separated into the amplitude term multiplied by the phase term as

$$|a_{o}^{(k+1)}| \exp\left(j\phi_{o}^{(k+1)}\right) = \left[|a_{e}^{(k)}| \exp\left(j\phi_{e}^{(k)}\right)\right] \exp\left(-j\beta_{e}^{(k)}L^{(k)}\right) \\ \cdot \left[|C_{eo}^{(k,k+1)}| \exp\left(j\phi_{C_{eo}}\right)\right] \\ + \left[|a_{o}^{(k)}| \exp\left(j\phi_{o}^{(k)}\right)\right] \exp\left(-j\beta_{o}^{(k)}L^{(k)}\right) \\ \cdot \left[|C_{oo}^{(k,k+1)}| \exp\left(j\phi_{C_{oo}}\right)\right]$$
(11)

where ϕ_i represents the corresponding phase term. Rearranging the above equation, we obtain

$$|a_{o}^{(k+1)}| = |a_{e}^{(k)}| \cdot |C_{eo}^{(k,k+1)}| \cdot \exp(j\phi_{eo}) + |a_{o}^{(k)}| \cdot |C_{oo}^{(k,k+1)}| \cdot \exp(j\phi_{oo})$$
(12)

where ϕ_{eo} and ϕ_{oo} represent $(\phi_e^{(k)} - \beta_e^{(k)}L^{(k)} + \phi_{C_{eo}} - \phi_o^{(k+1)})$ and $(\phi_o^{(k)} - \beta_o^{(k)}L^{(k)} + \phi_{C_{oo}} - \phi_o^{(k+1)})$, respectively. The real part of (12) is expressed as

$$|a_o^{(k+1)}| = |a_e^{(k)}| \cdot |C_{eo}^{(k,k+1)}| \cdot \cos \phi_{eo} + |a_o^{(k)}| \cdot |C_{oo}^{(k,k+1)}| \cdot \cos \phi_{oo}.$$
(13)

Thus, the degree of mode conversion can be observed by the phase behavior as described in (13) [13]. If the phase term $\cos \phi_{eo}$ is locked near 1 or -1 especially in the region where the coupling coefficient $|C_{eo}^{(k,k+1)}|$ is relatively large along the propagation direction, substantial mode conversion from the even mode to the odd mode will occur. On the contrary, if the phase term oscillates rapidly across zero, $|a_o^{(k)}|$ will not cumulatively increase and mode conversion does not occur. The above analysis is also valid when the input field is an odd mode.

IV. DESIGN EXAMPLE AND SIMULATION RESULTS

In this section, our design example is based on a Sisubstrate ($n_s = 3.5$) and the operating wavelength is $\lambda = 0.6328 \ \mu m$. SiO₂ with a refractive index of 1.46 is used for guiding layers, the separation layer and low-index cladding layers, i.e., $n_{g_1} = n_{g_2} = n_{sep} = n_{l_1} = n_{l_2} = 1.46$, and the glass mixture of BaO and SiO₂ with a refractive index of 1.50 is used as high-index cladding layers, i.e., $n_{h_1} = n_{h_2} = 1.5$.



Fig. 4. The dispersion relation versus the thickness of the upper cladding layer d_{l_1} . The parameters are $n_{g_1} = n_{g_2} = n_{\text{sep}} = n_{l_1} = n_{l_2} = 1.46$, $n_{h_1} = n_{h_2} = 1.5$, $d_{g_1} = d_{g_2} = 4\mu$ m, $d_{\text{sep}} = d_{l_2} = 2 \mu$ m, $d_{h_1} = d_{h_2} = 0.448 \mu$ m and $\lambda = 0.6328 \mu$ m.

The upper waveguide thickness d_{g_1} is 4 μ m such that this large core is compatible with single-mode optical fibers [9], [10]. Based on (1) and (2) we obtain $d_{g_2} = 4 \ \mu m$, $d_{l_2} = 2 \ \mu m$, and $d_{h_1} = d_{h_2} = 0.448 \ \mu \text{m}$ for $\lambda = 0.6328 \ \mu \text{m}$. Also based on (2) the thickness of the separation layer can be adjusted as $d_{sep} = 2 \ \mu m \times (2P_j + 1)$ for easy alignment to optical fibers. In our analysis the minimum value of $d_{\rm sep} = 2 \ \mu {
m m}$ is chosen for numerical convenience. The effective indexes of even and odd modes as functions of the upper cladding thickness are illustrated in Fig. 4. We then determine the thickness of the upper cladding layer, which will influence the symmetric degree of the dual ARROW waveguides. From the dispersion results shown in Fig. 4, it can be seen that, in the symmetric region, i.e., $d_{l_1} = d_{l_2}$, both even and odd modes are described by nondispersive curves which imply symmetric field distributions for two modes, and optical power can efficiently exchange between two ARROW waveguides. In the asymmetric region, i.e., d_{l_1} approach zero, the dispersive curves imply asymmetric field distributions for two modes. The maximum coupling efficiency as a function of the upper cladding thickness is shown in Fig. 5 [10]. It is observed that efficient coupling occurs in a symmetric structure and weak coupling in an asymmetric structure. Since our ARROW hybrid coupler is tapered from an exactly symmetric structure to an extremely asymmetric structure, we choose the initial value of d_{l_1} to be 1.91 μ m such that the maximum coupling efficiency is high and both the even mode and odd modes are equally distributed into two cores, and the final value of d_{l_1} to be 0.1 μ m such that the maximum coupling efficiency is sufficiently low and both modes reside mainly in two individual cores. The mode conversion along the whole device is then analyzed by eigenmode propagation as described in the previous section to find the optimized tapering angle. In our



Fig. 5. Maximum coupling efficiency as a function of the upper cladding layer thickness d_{l_1} . The parameters are $n_{g_1} = n_{g_2} = n_{\text{sep}} = n_{l_1} = n_{l_2} = 1.46$, $n_{h_1} = n_{h_2} = 1.5$, $d_{g_1} = d_{g_2} = 4 \ \mu\text{m}$, $d_{\text{sep}} = d_{l_2} = 2 \ \mu\text{m}$, $d_{h_1} = d_{h_2} = 0.448 \ \mu\text{m}$, and $\lambda = 0.6328 \ \mu\text{m}$.

analysis, the continuous structure is divided into N sections with small abrupt steps as shown in Fig. 3. The length of each section $L^{(k)}$ as a function of the tapering angle is

$$L^{(k)} = \frac{\Delta d_{l_1}}{N \cdot \tan \alpha} \tag{14}$$

where Δd_{l_1} is the total tapered thickness of the upper cladding layer and α is the tapering angle. In this case, it is found that N = 180 is sufficiently large to describe the mode conversion effect of the original continuous structure. As described in the previous section, the input field is assumed to be the normalized even mode, i.e., $A^{(1)} = \begin{bmatrix} 1 & 0 \end{bmatrix}$. Fig. 6 shows the mode coefficients a_e and a_o as functions of d_{l_1} when the input beam is propagating along the whole device for various tapering angles. The proper tapering angle is chosen to avoid mode conversion between two normal modes and prevent two normal modes from conversion into radiation modes. In Fig. 6, it is observed that a substantial mode conversion from the even mode to the odd mode occurs when $\alpha = 0.05^{\circ}$, whereas nearly adiabatic invariance is achieved when $\alpha = 0.03^{\circ}$. Fig. 7 shows the phase term $\cos \phi_{eo}$ in (13) versus d_{l_1} for various tapering angles. The coupling coefficients C_{eo} are simultaneously shown in this figure. It is found that the phase term oscillates rapidly in the case of $\alpha = 0.01^{\circ}$, whereas it is locked near -1 in the region of a large C_{eo} when $\alpha = 0.05^{\circ}$. In comparison with Figs. 6 and 7, a_o oscillates as $\cos \phi_{eo}$ does when $\alpha = 0.01^{\circ}$, and thus no cumulative mode conversion occurs. On the other hand, the cumulative mode conversion is serious when $\alpha = 0.05^{\circ}$. In Fig. 8, the mode expansion coefficients at the output end for $0.001^{\circ} < \alpha < 0.1^{\circ}$ are given. It can be seen that a_e decreases dramatically as α becomes very small because the radiation loss of the ARROW modes into substrate increases as the device length is very long.



Fig. 6. The mode coefficients a_e and a_o as functions of the thickness of the upper cladding layer for the tapering angles $\alpha = 0.01, 0.03$, and 0.05° . The input field is an even mode. BPM simulation results for $\alpha = 0.03^{\circ}$ are also given for comparison. The parameters are $n_{g_1} = n_{g_2} = n_{\text{sep}} = n_{l_1} = n_{l_2} = 1.46$, $n_{h_1} = n_{h_2} = 1.5$, $d_{g_1} = d_{g_2} = 4 \,\mu\text{m}$, $d_{\text{sep}} = d_{l_2} = 2 \,\mu\text{m}$, $d_{h_1} = d_{h_2} = 0.448 \,\mu\text{m}$, and $\lambda = 0.6328 \,\mu\text{m}$.



Fig. 7. The phase behavior associated with Fig. 6.

However, the mode conversion occurs when α becomes large as mentioned. The optimum tapering angle is chosen as 0.03° for this device.

The beam propagation method (BPM) with a transparent boundary condition (TBC) and an efficient interface condition is also used to verify our design and analysis [14]–[16]. An even mode with a unit power is launched into our ARROW hybrid coupler with $\alpha = 0.03^{\circ}$, and the overlap integral between the calculated field and the eigenmode fields (one



Fig. 8. The cumulative mode coefficients at the end of this device as functions of the tapering angle. The parameters are $n_{g_1} = n_{g_2} = n_{\text{sep}} = n_{l_1} = n_{l_2} = 1.46$, $n_{h_1} = n_{h_2} = 1.5$, $d_{g_1} = d_{g_2} = 4 \ \mu\text{m}$, $d_{\text{sep}} = d_{l_2} = 2 \ \mu\text{m}$, $d_{h_1} = d_{h_2} = 0.448 \ \mu\text{m}$, d_{l_1} is tapered from 1.91 μm to 0.01 μm , $\alpha = 0.03^\circ$, and $\lambda = 0.6328 \ \mu\text{m}$.

even and one odd modes) along the propagation direction is plotted in Fig. 6 as well. It is shown that BPM simulation results agree with the results of our previous analysis. The field evolution profiles with the input field of an even mode and an odd mode are shown in Fig. 9(a) and (b), respectively. To evaluate the performance of our hybrid coupler, the extinction ratios for two modes are defined as

$$\xi_{o,e} = 10 \log_{10} \frac{P_o \text{ at the output end}}{P_e \text{ at the input end}},$$

with the even mode as the input field
$$\xi_{e,o} = 10 \log_{10} \frac{P_e \text{ at the output end}}{P_o \text{ at the input end}}$$

with the odd mode as the input field (15)

where P_e and P_o are optical power of the even mode and the odd mode, respectively. The extinction ratios $\xi_{e,o}$ and $\xi_{o,e}$ should be very small when the device is nearly adiabatic and radiation losses are small. In our case, $\xi_{o,e} = -23.10$ dB and $\xi_{e,o} = -22.87$ dB. The radiation losses are 0.38 dB and 0.31 dB, respectively, as desired. Finally, further simulations with a unit-power even mode and odd mode as the input field from the original output end are performed to verify the reciprocity law as shown in Fig. 10(a) and (b), respectively. The extinction ratios of $\xi_{o,e} = -23.05$ dB and $\xi_{e,o} = -24.30$ dB are obtained, and the radiation losses are 0.34 and 0.25 dB, respectively. All these results verify the function of our devices.

V. CONCLUSION

A novel hybrid coupler based on antiresonant reflecting optical waveguides (ARROW's) is proposed. This ARROW



Fig. 9. The power evolution profile with an input field of a normal mode along the propagation distance for an ARROW hybrid coupler. The parameters are $n_{g_1} = n_{g_2} = n_{\text{sep}} = n_{l_1} = n_{l_2} = 1.46$, $n_{h_1} = n_{h_2} = 1.5$, $d_{g_1} = d_{g_2} = 4 \,\mu\text{m}$, $d_{\text{sep}} = d_{l_2} = 2 \,\mu\text{m}$, $d_{h_1} = d_{h_2} = 0.448 \,\mu\text{m}$, d_{l_1} is tapered from 1.91 μ m to 0.01 μ m, $\alpha = 0.03^{\circ}$, and $\lambda = 0.6328 \,\mu\text{m}$. (a) An even mode input.

hybrid coupler consists of two parallel antiresonant reflecting optical waveguides with a tapered outermost cladding layer. Compatible core dimensions and indexes with singlemode fibers and a large separation thickness between two waveguide channels of an ARROW hybrid coupler can be



Fig. 10. The power evolution profile with an input field of a normal mode along the propagation distance for a reversed ARROW hybrid coupler. The parameters are $n_{g_1} = n_{g_2} = n_{\text{sep}} = n_{l_1} = n_{l_2} = 1.46$, $n_{h_1} = n_{h_2} = 1.5$, $d_{g_1} = d_{g_2} = 4 \,\mu\text{m}$, $d_{\text{sep}} = d_{l_2} = 2 \,\mu\text{m}$, $d_{h_1} = d_{h_2} = 0.448 \,\mu\text{m}$, d_{l_1} is increased from 0.01 μ m to 1.91 μ m, $\alpha = 0.03^\circ$, and $\lambda = 0.6328 \,\mu\text{m}$. (a) An even mode input and (b) an odd mode input.

achieved by utilizing the periodic property of the antiresonant conditions. The input and output coupling efficiency are thus significantly improved compared to a conventional waveguide hybrid coupler. With an optimum design of the outermost cladding layer thickness, equal excitations for two normal modes (one even and one odd modes) at input end can be realized and the crosstalk at the output end is low. In addition, the surface scattering is relieved because only the thickness of outermost cladding layer is gradually changed. The tapering angle is designed to ensure the adiabatic invariance condition. Eigenmode expansion analysis is used to design this device and the beam propagation method is used to verify the device characteristics. A design example based on a Si-substrate is given. The extinction ratios of -23.10 and -22.87 dB with an input for an even mode and an odd mode are obtained, respectively, and the corresponding radiation losses of 0.38 and 0.31 dB are also obtained. This versatile optical device can be efficiently applied to optical communications, optical signal processing, and optical microsensing systems.

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