

# Effect of MgO addition on the electrical transport properties of highly Sb-doped BaTiO<sub>3</sub> ceramics

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BaTiO<sub>3</sub> ceramics doped with Sb donors and Mg acceptors have been fabricated. The lattice constant ratio  $c/a$  and the Curie point  $T_c$  decrease with increasing Sb concentration. The minimum room temperature resistivity  $\rho_{min}$  of the codoped BaTiO<sub>3</sub> occurs at a composition of 0.9 mole% Sb<sub>2</sub>O<sub>3</sub>-1 mole % MgO as compared to the literature reported  $\rho_{min}$  at 0.3 mole % antimony for the Sb<sub>2</sub>O<sub>3</sub>-doped BaTiO<sub>3</sub>. The Mg<sup>2+</sup> ion acts as an acceptor in the BaTiO<sub>3</sub> ceramics, which compensates the donor contribution from Sb<sup>3+</sup> and shifts the doped-BaTiO<sub>3</sub> semiconducting region to higher antimony content. The calculated donor concentration confirms the compensation effect of Mg acceptors over Sb donors. The temperature dependence of both barrier height and dielectric constant of specimens is discussed. © 1998 Chapman & Hall

## 1. Introduction

Barium titanate has attracted much attention in the field of electronic ceramics. Doped, n-type barium titanate ceramics exhibit an abrupt rise in resistivity near the Curie temperature ( $T_c$ ): the so-called positive temperature coefficient of resistivity (PTCR) effect. This anomaly of resistivity renders barium titanate useful in various applications [1, 2]. Many factors affect the PTCR phenomena of BaTiO<sub>3</sub> ceramics such as: the concentration and the distribution of the trace additives [2–6], the impurities in the raw materials, and the firing conditions [7–9].

The U-shaped relation between the dopant ion content and the resistivity of semiconducting BaTiO<sub>3</sub> is well known [5]. For Sb<sub>2</sub>O<sub>3</sub>-doped BaTiO<sub>3</sub>, the minimum resistivity exists at 0.3 mole % content of antimony dopant. However, an insulating BaTiO<sub>3</sub> is obtained beyond that range [10]. Previous work by Chiou *et al.* [7] reported that the Curie point of BaTiO<sub>3</sub>-based ceramics was altered by addition of Sb<sub>2</sub>O<sub>3</sub> and the dielectric peak was maintained by the presence of MgO additive. In addition, the presence of magnesium ions, which acted as acceptors, pushed the BaTiO<sub>3</sub> semiconducting region to higher Sb<sub>2</sub>O<sub>3</sub> content. However, the effect of MgO on Sb-doped BaTiO<sub>3</sub> is not well known.

In this study, the dielectric properties and PTCR effect of MgO-Sb<sub>2</sub>O<sub>3</sub> codoped BaTiO<sub>3</sub> are investigated. The antimony dopant content employed is larger than normally reported [11]. The doping concentrations in these specimens are 1 mole % MgO, 0.05 mole % MnO<sub>2</sub>, and 0.8 to 1.0 mole % Sb<sub>2</sub>O<sub>3</sub>. The addition of MnO<sub>2</sub> enhances the PTCR effect [7]. Manganese is an acceptor dopant. Ting *et al.* [12] reported that the acceptor effect of Mn<sup>2+</sup> became pronounced only at an Mn<sup>2+</sup> concentration of above

0.05 mole %. Illingsworth *et al.* [17] found that a small addition of Mn (0.04 mole %) to BaTiO<sub>3</sub> had negligible effect on both the bulk resistance and the dielectric constant above  $T_c$ . A 0.05 mole % MnO<sub>2</sub> addition in this study optimizes the PTCR phenomena while minimizing the acceptor effect of Mn<sup>2+</sup>. The possible role of Mg in the PTCR behaviour of highly Sb-doped BaTiO<sub>3</sub> is discussed.

## 2. Experimental procedures

Samples were prepared by a conventional ceramic fabrication process. Appropriate amounts of BaCO<sub>3</sub>, TiO<sub>2</sub>, MgO, MnO<sub>2</sub>, and Sb<sub>2</sub>O<sub>3</sub> (reagent grade, Merck & Co. Inc., Darmstadt, Germany), together with ethyl alcohol, were ball-milled for 24 h. The molar ratio of BaCO<sub>3</sub> and TiO<sub>2</sub> was 1:1.01, excess TiO<sub>2</sub> was added to obtain a TiO<sub>2</sub>-rich liquid phase during sintering [7]. After drying, the mixture was calcined in an alumina crucible at 1100 °C for 2 h, then crushed into powder and pressed into a disk-shape specimen, 10 mm in diameter and 1.5 mm in thickness. Sintering was carried out with an initial heating rate of 100 °C min<sup>-1</sup> to 1200 °C, and held at 1200 °C for 6 min, then heated to 1400 °C at 100 °C min<sup>-1</sup> and held at 1400 °C for 18 min. The two-stage firing resulted in a more uniform microstructure than a single-stage firing [7]. After sintering, electrodes were applied to the specimens by rubbing In-Ga (40:60) alloy on both surfaces to provide ohmic contacts.

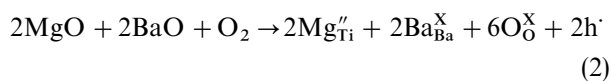
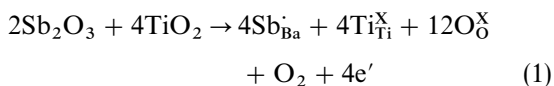
The resistance of samples was measured with a pA meter (HP4140B, Hewlett Packard). The impedance of samples was measured with an impedance analyser (HP4192A). The densities of the sintered specimens were determined by the Archimedes method. Microstructure and elemental distribution of the samples

were examined with a scanning electron microscope (SEM, Hitachi, S-570) and an electron microprobe analyser (EPMA, JEOL JCXA-733, Japan). Phase identification of the samples was carried out with an X-ray diffractometer. The average grain size of the sample was determined by the linear intercept method from the scanning electron micrograph of the as-fired surface.

### 3. Results and discussion

The microstructures for  $\text{Sb}_2\text{O}_3$ -doped  $\text{BaTiO}_3$  are shown in Fig. 1. The average grain size is 9.2, 7.0, and 5.0  $\mu\text{m}$  for samples doped with 0.8, 0.9, and 1.0 mole %  $\text{Sb}_2\text{O}_3$ , respectively. Addition of  $\text{Sb}_2\text{O}_3$  inhibits the grain growth of  $\text{BaTiO}_3$  ceramics. The X-ray diffraction (XRD) patterns indicate that the specimens are of perovskite structure. The lattice constant as a function of  $\text{Sb}_2\text{O}_3$  concentration is calculated on the basis of the XRD results and shown in Fig. 2. In contrast to the decrease in lattice constant  $c$ , lattice constant  $a$  increases and the  $c/a$  ratio decreases with increasing Sb content. At room temperature  $a$  and  $c$  for pure  $\text{BaTiO}_3$  are 0.3992 nm and 0.4035 nm, respectively. These values are not obtained by extrapolating data in Fig. 2 at 0 mole %  $\text{Sb}_2\text{O}_3$ , because two other additives, MgO and  $\text{MnO}_2$ , are present in  $\text{BaTiO}_3$  ceramics. The theoretical density  $D_{th}$  is calculated from the lattice constants. Table I lists the grain size and the measured and theoretical density of the specimens. The percentage of the  $D_{th}$  increases with  $\text{Sb}_2\text{O}_3$  content, the 97.5%  $D_{th}$  is obtained for the 1.0 mole %  $\text{Sb}_2\text{O}_3$  sample. Figs 3 and 4 show the temperature variation of the dielectric constant and dissipation factor of the  $\text{Sb}_2\text{O}_3$ -doped  $\text{BaTiO}_3$ , respectively. The Curie temperatures are 64  $^\circ\text{C}$ , 60  $^\circ\text{C}$ , and 55  $^\circ\text{C}$  for the 0.85, 0.9, and 1.0 mole % specimens, respectively.

The resistivity  $\rho$  as a function of temperature is given in Fig. 5. The resistivity decreases initially and then increases as the  $\text{Sb}_2\text{O}_3$  content increases from 0.85 mole % to 1.0 mole %. The specimen with 0.9 mole %  $\text{Sb}_2\text{O}_3$  has the lowest resistivity. The room temperature resistivity for the 0.9 mole %  $\text{Sb}_2\text{O}_3$ -MgO codoped sample is  $\sim 240 \Omega \text{ cm}$  which is comparable to the minimum resistivity reported for the  $\text{Sb}_2\text{O}_3$ -doped  $\text{BaTiO}_3$  [10]. The ionic radii of  $\text{Ba}^{2+}$ ,  $\text{Sb}^{3+}$ ,  $\text{Ti}^{4+}$ , and  $\text{Mg}^{2+}$  ions are 0.135, 0.076, 0.065, and 0.069 nm, respectively [13]. The trivalent  $\text{Sb}^{3+}$  ions tend to occupy the position of  $\text{Ba}^{2+}$  in preference to  $\text{Ti}^{4+}$  ions, while  $\text{Mg}^{2+}$  would replace  $\text{Ti}^{4+}$  instead  $\text{Ba}^{2+}$ , as expected from the radii. Possible defect reactions are as follows [12]:



Magnesium ions behave as electron acceptors in  $\text{BaTiO}_3$  and compensate some of the donor  $\text{Sb}^{3+}$  ions. Consequently, the antimony content for minimum resistivity of  $\text{Sb}_2\text{O}_3$ -MgO codoped  $\text{BaTiO}_3$  is higher than that for  $\text{Sb}_2\text{O}_3$ -doped  $\text{BaTiO}_3$ .

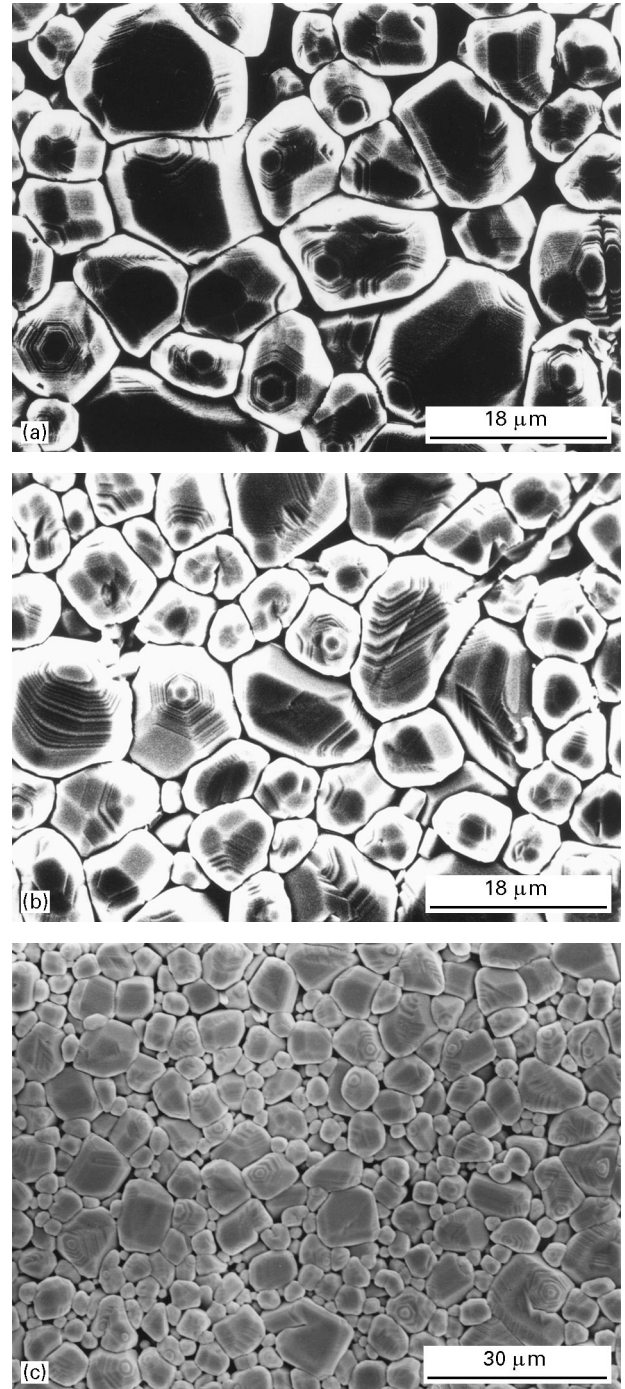


Figure 1 SEM micrographs for  $\text{BaTiO}_3$  doped with 1.0 mole % MgO, 0.05 mole %  $\text{MnO}_2$  and  $x$  mole %  $\text{Sb}_2\text{O}_3$ . (a)  $x = 0.8$ , (b)  $x = 0.9$ , and (c)  $x = 1.0$ .

The values of  $\rho_{r,t}$ ,  $\rho_{max}$ ,  $\rho_{max}/\rho_{r,t}$ , and  $T_{max}$  are summarized in Table II. The 0.9 mole %  $\text{Sb}_2\text{O}_3$  sample has the smallest resistivity increase  $\rho_{max}/\rho_{r,t}$  and the largest  $T_{max}$  among the compositions studied. Also, a strong NTCR effect is noticeable for the specimen with 1.0 mole %  $\text{Sb}_2\text{O}_3$  after the maximum resistivity is reached at about 200  $^\circ\text{C}$ , as shown in Fig. 5.

The PTCR effect has been confirmed to originate from the grain boundary property and to be associated with the ferroelectric-paraelectric phase transition in semiconducting barium titanate ceramics [8, 14]. According to Heywang's [10, 11] model, the presence of grain boundary depletion layers consisting

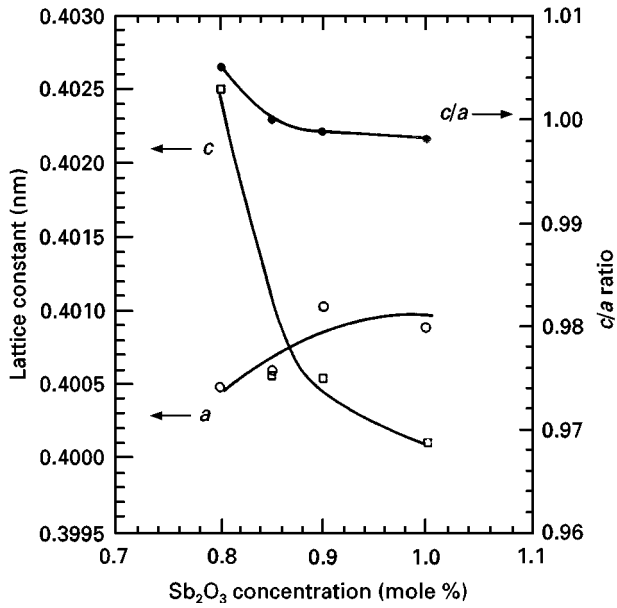


Figure 2 Lattice constant as a function of  $\text{Sb}_2\text{O}_3$  concentration.

TABLE I Average grain size and density for  $\text{BaTiO}_3$  doped with 1.0 mole %  $\text{MgO}$ , 0.05 mole %  $\text{MnO}_2$  and various amounts of  $\text{Sb}_2\text{O}_3$

$\text{Sb}_2\text{O}_3$ (mol %)	Average grain size ( $\mu\text{m}$ )	Theoretical density ( $\text{g cm}^{-3}$ )	Measured density ( $\text{g cm}^{-3}$ )	$D_{th}$ (%)
0.8	9.2	5.99	5.66	94.5
0.9	7.0	6.00	5.75	95.8
1.0	5.0	6.01	5.86	97.5

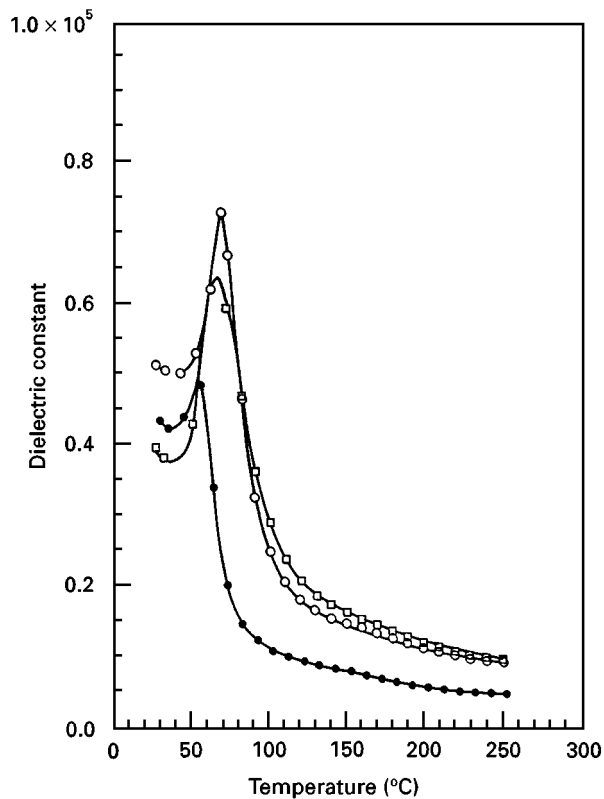


Figure 3 Apparent dielectric constant as a function of temperature for  $\text{BaTiO}_3$  doped with 1.0 mole %  $\text{MgO}$ , 0.05 mole %  $\text{MnO}_2$ , and  $x$  mole %  $\text{Sb}_2\text{O}_3$ , where  $x = 0.85$  ( $\circ$ ),  $0.9$  ( $\square$ ) and  $1.0$  ( $\bullet$ ).

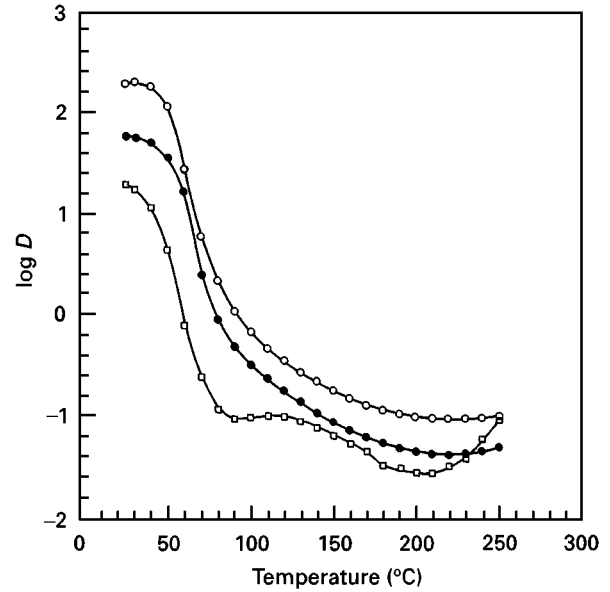


Figure 4 Dissipation factor as a function of temperature for  $\text{BaTiO}_3$  doped with 0.1 mole %  $\text{MgO}$ , 0.05 mole %  $\text{MnO}_2$  and  $x$  mole %  $\text{Sb}_2\text{O}_3$  at 1 kHz: ( $\bullet$ )  $x = 0.85$ , ( $\circ$ )  $x = 0.9$ , and ( $\square$ )  $x = 1.0$ .

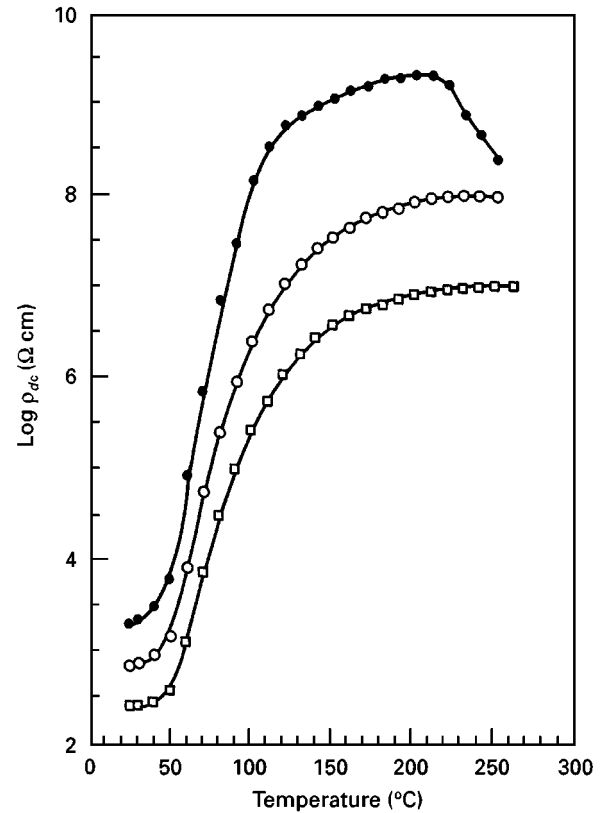


Figure 5 Resistivity as a function of temperature for  $\text{BaTiO}_3$  doped with 1.0 mole %  $\text{MgO}$ , 0.05 mole %  $\text{MnO}_2$  and  $x$  mole %  $\text{Sb}_2\text{O}_3$ : ( $\circ$ )  $x = 0.85$ , ( $\square$ )  $x = 0.9$ , and ( $\bullet$ )  $x = 1.0$ .

of two-dimensional surface acceptor states gives rise to a potential barrier at the grain boundary as a result of the upward bending of the conduction band, as shown schematically in Fig. 6 [15].

The charge in the surface states equals the charge in the depletion region. Below  $T_c$ , the potential barrier is compensated by the charges arising from the

TABLE II Logarithm of room temperature resistivity  $\rho_{r,t}$ , maximum resistivity  $\rho_{max}$ , resistivity increase  $\rho_{max}/\rho_{r,t}$  and temperature of maximum resistivity  $T_{max}$  for BaTiO<sub>3</sub> doped with 1.0 mole % MgO, 0.05 mole % MnO<sub>2</sub> and various amounts of Sb<sub>2</sub>O<sub>3</sub>

Sb <sub>2</sub> O <sub>3</sub> (mol %)	log $\rho_{r,t}$ ( $\Omega$ cm)	log $\rho_{max}$ ( $\Omega$ cm)	log $\rho_{max}/\rho_{r,t}$	$T_{max}$ ( $^{\circ}$ C)
0.85	2.8	8.0	5.2	230
0.9	2.4	7.0	4.6	250
1.0	3.3	9.2	5.9	200

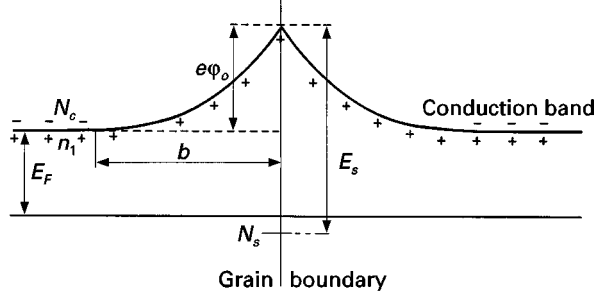


Figure 6 Energy level diagram near a grain boundary [15].

spontaneous polarization, rendering the whole material conductive. Above  $T_c$ , the spontaneous polarization disappears and the resistivity is controlled by the potential barrier. The barrier height  $\Phi_o$  is [6, 7, 16]

$$\Phi_o = en^2/8\epsilon_o n\epsilon_r \quad (3)$$

and the barrier thickness  $b$  is

$$b = n_s/2n \quad (4)$$

where  $e$  is the electron charge,  $n$  ( $\text{cm}^{-3}$ ) the effective donor concentration within the grain,  $\epsilon_o$  the permittivity of free space,  $n_s$  number of electrons trapped in the surface states (number is  $N_s$  at a distance  $E_s$  below the conduction level),  $\epsilon_r$  the relative permittivity, and

$$\epsilon_r = C/T - T_c \quad (5)$$

where  $C$  is the Curie constant and  $T$  is the absolute temperature. The measured dielectric constant  $\epsilon_m$  of a material consisting of insulating grain-boundary layers and a semiconducting grain is [18]

$$\epsilon_m = \epsilon_{gb}d/t \quad (6)$$

where  $d$  is the average grain size of the dielectric and  $\epsilon_{gb}$  and  $t$  are the dielectric constant and thickness of the insulating grain boundary layer, respectively. In this case,

$$t = 2b \quad (7)$$

$$\epsilon_{gb} = \epsilon_r \quad (8)$$

and

$$\epsilon_m = \epsilon_r (d/2b) \quad (9)$$

The dielectric constants of samples in this study are one to two orders of magnitude larger than those of the undoped BaTiO<sub>3</sub> at  $T_c$  (i.e. 1000 ~ 5000) [11]. Yamamoto and Takao [19] estimated a grain boundary layer of  $\sim 0.26 \mu\text{m}$  thickness for a PTC thermi-

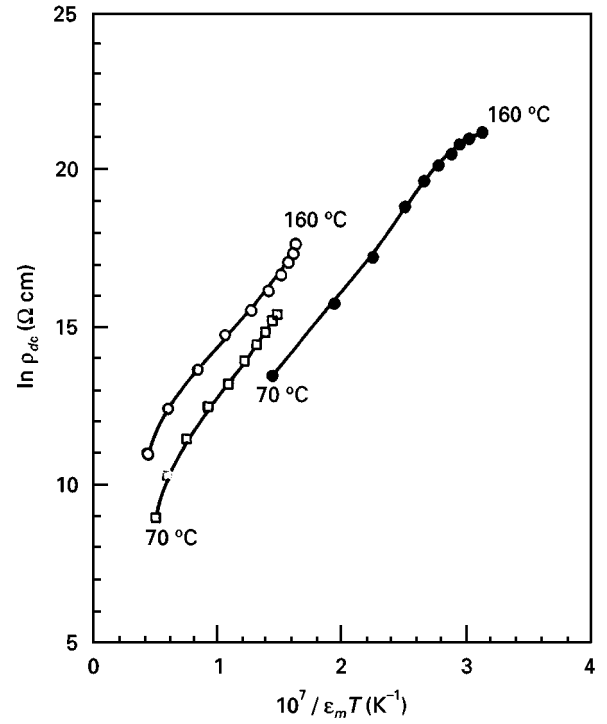


Figure 7 Plots of  $\ln(\rho_{dc})$  against  $1/\epsilon_m T$  for BaTiO<sub>3</sub> doped with 1.0 mole % MgO, 0.05 mole % MnO<sub>2</sub>, and  $x$  mole % Sb<sub>2</sub>O<sub>3</sub>: (○)  $x = 0.85$ , (□)  $x = 0.9$ , and (●)  $x = 1.0$ . Dielectric constant  $\epsilon_m$  is measured at 1 kHz.

stor. The average grain size of the 0.9 mole % Sb<sub>2</sub>O<sub>3</sub>-doped sample is  $7.0 \mu\text{m}$ . Substituting these data into Equation 9 one obtains  $\epsilon_m$  values of around  $1.3 \times 10^4$  to  $6.7 \times 10^4$  which are in agreement with the measured data shown Fig. 3. This suggests that the BaTiO<sub>3</sub> ceramic exhibits the characteristics of the so-called grain boundary barrier layer (GBBL) capacitors [18]. From semiconductor theory, the resistivity of the depletion layer  $\rho_L$  is given by

$$\rho_L = \rho_o \exp(e\Phi_o/kT) \quad (10)$$

For a polycrystalline sample with semiconducting grain and insulating barrier layers, the resistivity can be expressed as

$$\rho = \rho_g + \rho_L \approx \rho_L \quad (11)$$

where  $\rho_g$  is the resistivity of the grain.

Combining Equations 4, 9, 10 and 11 into Equation 3, one has

$$\begin{aligned} \rho &= \rho_o \exp(e\Phi_o/kT) \\ &= \rho_o \exp(A n_s / \epsilon_m T) \end{aligned} \quad (12)$$

$$A = e^2 d / 8 k \epsilon_o \quad (13)$$

Fig. 7 is the  $\ln(\rho_{dc})$  versus  $1/\epsilon_m T$  plots. It is seen that the slopes of the curves decrease as temperature increases from  $T_c$  to  $T_{max}$ . This suggests a decrease of the grain boundary acceptor states  $n_s$  with temperature.

Previous work reported a value of  $n_s$  to be about  $10^{14} \text{cm}^{-2}$  and  $n$  of  $\sim 3 \times 10^{19} \text{cm}^{-3}$  for BaTiO<sub>3</sub> doped with 0.07 wt % Sb<sub>2</sub>O<sub>3</sub> [19]. In this study, the  $n_s$  at  $T_c$  is  $\sim 4 \times 10^{13} \text{cm}^{-2}$  which is of the same order as literature reported data [19]. However, the effective donor concentration  $n$ , estimated on the basis of

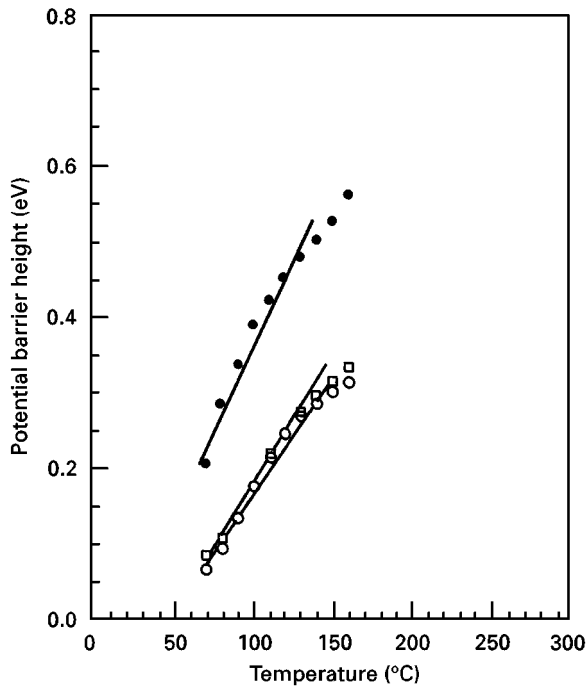


Figure 8 The potential barrier height as a function of temperature for BaTiO<sub>3</sub> doped with 1.0 mole % MgO, 0.05 mole % MnO<sub>2</sub>, and x mole % Sb<sub>2</sub>O<sub>3</sub>: (○) x = 0.85, (□) x = 0.9, and (●) x = 1.0.

dielectric data in Fig. 4 and Equations 4 and 9, is  $\sim 2 \times 10^{17} \text{ cm}^{-3}$  which is much smaller than reported data [19]. This confirms that not all of the Sb<sub>2</sub>O<sub>3</sub> addition was effective in making the ceramics semiconducting. Only part of the Sb<sub>2</sub>O<sub>3</sub> addition was effective as donors. Magnesium ions behave as electron acceptors in BaTiO<sub>3</sub> ceramics, and compensate some of the donor Sb<sup>3+</sup> ions.

The barrier height  $\Phi_0$  is calculated on the basis of Equation 3 and plotted as a function of temperature, as shown in Fig. 8. Combining Equations 3 and 5, one has

$$\Phi_0 = en_s (T - T_c) / 8Cn\epsilon_0 \quad (14)$$

which indicates that, for given values of  $n$  and  $n_s$ ,  $\Phi_0$  is directly proportional to temperature. However, since  $n_s$  decreases as temperature increases, the increase of  $\Phi_0$  with temperature is not as great at elevated temperatures. Hence, a slower increase in  $\Phi_0$  is observed at temperatures higher than 140 °C, as shown in Fig. 8. In addition, the barrier height increases as the Sb<sub>2</sub>O<sub>3</sub> concentration is raised from 0.9 mole % to 1.0 mole %.

The relation between  $1/\epsilon_m$  and temperature at  $T > T_c$ , exhibited in Fig. 9, indicates that the Curie–Weiss law is obeyed at temperatures in the range between 70 °C and 130 °C. At higher temperatures,  $1/\epsilon_m$  still increases linearly, but more slowly with temperature, giving a second region with smaller slope. The number of surface states  $n_s$  can be expressed as [15]:

$$n_s = N_s / \{1 + \exp[(E_f + e\Phi - E_s) / kT]\} \quad (15)$$

Equation 9 can be rewritten as:

$$\epsilon_m = \epsilon_r (dn/n_s) \quad (16)$$

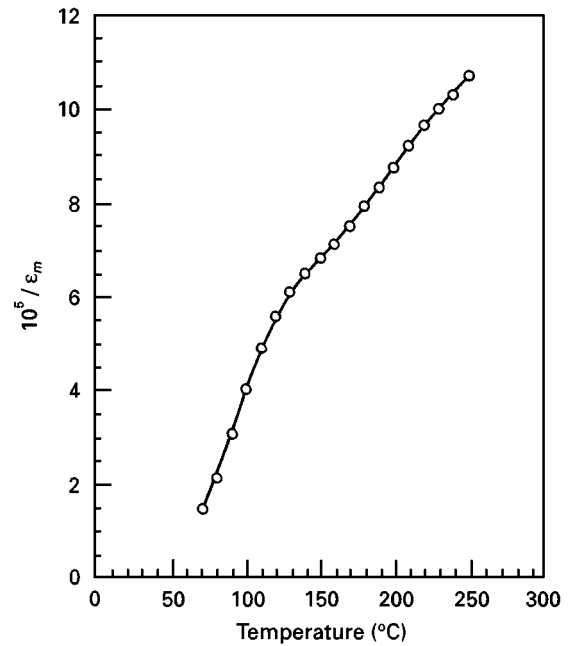


Figure 9 Reciprocal of the dielectric constant as a function of temperature for BaTiO<sub>3</sub> doped with 1.0 mole % MgO, 0.05 mole % MnO<sub>2</sub>, and 0.85 mole % Sb<sub>2</sub>O<sub>3</sub>.

At lower temperatures, the acceptor states at the grain surface are almost fully ionized, i.e.  $n_s \approx N_s$ , and  $\epsilon_m$  is expected to follow the Curie–Weiss law. However, at sufficiently high temperatures,  $E_f + e\Phi$  approaches  $E_s$  and depopulation of surface states occurs (Fig. 6). The decrease in  $n_s$  with rising temperature counteracts the reduction of  $\epsilon_m$ . Hence,  $1/\epsilon_m$  rises more slowly with temperature once depopulation of the surface states begins.

#### 4. Conclusions

1. BaTiO<sub>3</sub> doped with 1.0 mole % MgO, 0.05 mole % MnO<sub>2</sub>, and various amounts of Sb<sub>2</sub>O<sub>3</sub> were fabricated with a two-stage firing profile. The Curie temperature and grain size decrease with the increase of Sb<sub>2</sub>O<sub>3</sub> content.
2. For the Sb<sub>2</sub>O<sub>3</sub>–MgO codoped samples, the minimum resistivity, smallest resistivity increase  $\rho_{max}/\rho_{r,t}$  and the largest  $T_{max}$  occur at 0.9 mole % Sb<sub>2</sub>O<sub>3</sub> for 1 mole % MgO addition.
3. Magnesium ions, substituting as the Ti<sup>4+</sup> sites, behave as electron acceptors in BaTiO<sub>3</sub> and compensate some of the donor Sb<sup>3+</sup> ions. This results in smaller donor concentrations than in other reported work.
4. The measured dielectric constant  $\epsilon_m$  is inversely proportional to temperature as predicted by the Curie–Weiss law. However, as depopulation of surface states occurs,  $1/\epsilon_m$  rises more slowly with temperature at higher  $T$ .

#### Acknowledgment

This work is supported by the National Science Council, Taiwan, under the contract NO. NSC 85-2216-E-009-012.

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*Received 18 April  
and accepted 23 July 1997*