

# Deregistration Strategies for PCS Networks

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**Abstract**— This paper studies three deregistration strategies (explicit, implicit, and timeout (TO) deregistration) for personal communication service (PCS) networks to determine the network conditions under which each strategy gives the best performance. Two performance measures are considered: 1) the probability  $\alpha$  that a portable cannot register (and receive service) and 2) the number of deregistration messages sent in a strategy. For the same database size,  $\alpha$  is smaller for explicit deregistration (ED) than it is for TO or implicit deregistration (ID). On the other hand, ID does not create any deregistration message traffic. With an appropriate TO period, the deregistration message traffic for TO deregistration is much smaller than the traffic for ED. Suppose that there are  $N$  portables in a registration area (RA) on the average. To ensure that  $\alpha < 10^{-3}$ , our study indicates that if the database size is larger than  $4N$ , then the implicit scheme should be selected (to eliminate deregistration traffic). If the database size is smaller than  $1.5N$ , then the explicit scheme should be selected. Otherwise, the TO scheme should be selected to achieve the best performance.

**Index Terms**— Deregistration, home-location register, mobility management, personal communications services, registration, visitor-location register.

## I. INTRODUCTION

THIS PAPER studies three deregistration strategies for personal communication service (PCS) networks. In a PCS network, registration is the process by which portables inform the network of their current location (registration area or RA). We assume that a location database (i.e., visitor-location register or VLR) is assigned to exact one RA (although a VLR may cover several RA's in the existing PCS systems). A portable registers its location when it is powered on and when it moves between RA's. If the database is full when a portable arrives, the portable cannot access the services provided by the PCS network. When a portable leaves an RA or shuts off for a long period of time, the portable should be deregistered from the RA so that any resource previously assigned to the portable can be deallocated.

In IS-41 [1], [3], the registration process ensures that a portable registration in a new RA causes deregistration in the previous RA. This approach is referred to as explicit deregistration (ED). This approach to deregistration may create significant traffic in the network [8]. Also, ED does not provide a means of deregistering portables that are shut off, broken, or otherwise disabled for a significant period of time. Bellcore personal access communications systems (PACS's)

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[2] suggest that a portable be deregistered by default after a certain time period elapses without the portable reregistering. This scheme is referred to as timeout (TO) deregistration [11]. Another possibility is to perform deregistration *implicitly* [2], [7]. Suppose that the database is full when a portable  $p$  arrives at an RA. The implicit scheme selects a record based on some replacement strategy. This record is deleted and is then reassigned to  $p$ . Note that the record being replaced may be valid, in which case the corresponding portable is forced to deregister. Thus, the size of the registration database (i.e., the amount of resources) must be sufficiently large so as to ensure that the probability of a valid registration record being replaced is extremely low (say  $10^{-3}$ ). Lin and Noerpel [7] proposed an analytical model to determine the database size for an implicit scheme that selects the oldest record for replacement. This paper proposes analytical models to study the explicit scheme, implicit scheme with a new replacement strategy, and TO scheme.

## II. EXPLICIT DEREGISTRATION

In the explicit scheme, a registration record is deleted when the corresponding portable moves out of the RA. Thus, the database is full if and only if the number of portables in the RA is larger than the size of the database. To derive the probability that a portable cannot register at a particular RA, we first derive the distribution for the number of portables in an RA. Let  $N$  be the expected number of portables in an RA. Suppose that the residence time of a portable in an RA has a general distribution with the density function  $f(t)$  and mean  $1/\mu$ . In the steady state, the rate at which portables move into an RA equals the rate at which portables move out of the RA. In other words, the rate at which portables move into an RA is  $\eta = N\mu$ . The arrival of portables can be viewed as being generated from  $N$  input streams, which have the same general distribution with arrival rate  $\mu$ . If  $N$  is reasonably large in an RA, the net input stream is approximated as a Poisson process with arrival rate  $\eta$ . Thus, the distribution for the portable population can be modeled by an  $M/G/\infty$  queue with arrival rate  $\eta$  and mean residence time  $1/\mu$ . Let  $\pi_n$  be the steady-state probability that there are  $n$  portables in the RA. This model was validated against simulation experiments by Lin and Chen [6]. By the standard technique [4]

$$\pi_n = \frac{(\eta/\mu)^n e^{-(\eta/\mu)}}{n!} = \frac{N^n e^{-N}}{n!}. \quad (1)$$

Fig. 1(a) plots the population distribution when  $N = 50, 100,$  and  $150$ , respectively. Skew distributions are observed for small  $N$  values. We note that the typical number of portables

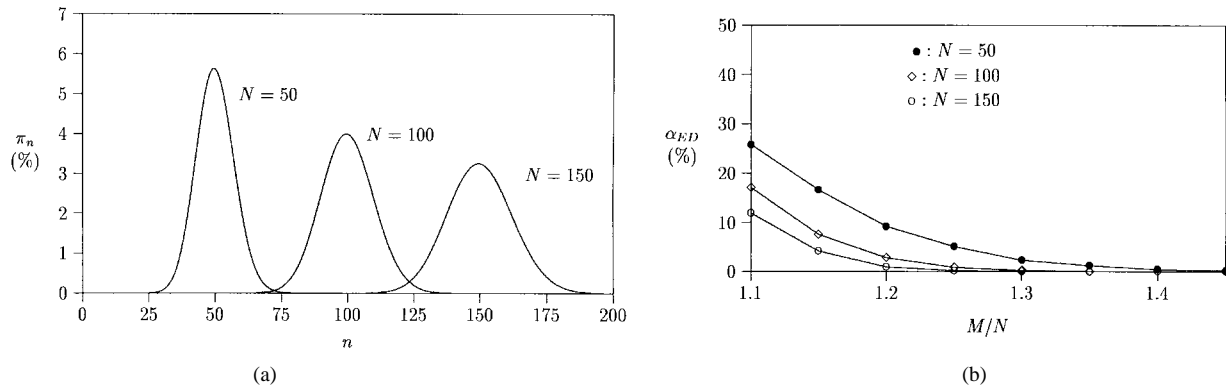


Fig. 1. The performance of the explicit scheme. (a) The population distribution. (b) The probability that a portable cannot register in the explicit scheme.

in a RA is much larger than 150. The numbers 50, 100, and 150 are selected only for the demonstration purpose.

Suppose that the size of the registration database is  $M$ . Let  $\alpha_{ED}$  be the probability that the registration database is full when a portable arrives (and thus the portable cannot register). Then

$$\alpha_{ED} = \sum_{M \leq n < \infty} \pi_n.$$

Fig. 1(b) plots  $\alpha_{ED}$  for different  $N$  values. The figure indicates that for  $M \geq 1.5N$  (where  $N > 50$ ), the explicit scheme can accommodate almost all arriving portables (i.e.,  $\alpha_{ED} < 10^{-3}$ ). Note that the rate of the deregistration messages sent in the network is  $N\mu$  per RA. The deregistration messages may significantly contribute to the PCS network traffic.

### III. IMPLICIT DEREGISTRATION

In the implicit scheme, no deregistration message is sent upon the movement of a portable. The obsolete record is kept in the database. When the database is full, the scheme reclaims a record (for the incoming portable) based on some strategy. A possible replacement strategy is described below.

#### A. Strategy ID

At time  $t$ , a portable  $p$  is said to be *inactive* for a time period  $\delta$  if  $p$  has not interacted (sending or receiving messages) with the RA since  $t - \delta$ . Define a threshold  $X$ . If  $p$  is inactive for a time period  $\delta > X$ , we may expect that  $p$  has already left the RA. On the other hand, if there is a phone call for  $p$  or  $p$  registers (i.e., moves into the RA) within the period  $X$ , then the implicit scheme assumes that  $p$  is still in the RA. The implicit deregistration (ID) strategy works as follows. When  $p_m$  arrives at an RA, let  $p_{m_1}$  and  $p_{m_2}$  be the oldest and the second oldest portables in the RA (i.e., for all the portables  $p_{m_3}$  in the RA, we have  $m_1 < m_2 < m_3$ ). When  $p_m$  arrives, the inactive time periods for  $p_{m_1}$  and  $p_{m_2}$  are  $\delta_1$  and  $\delta_2$ , respectively. If  $\delta_1 > X$ , ID assumes that  $p_{m_1}$  is not in the RA, and  $p_{m_1}$  is selected for replacement. Otherwise, if  $\delta_2 > X$ , then ID assumes that  $p_{m_2}$  is not in the RA and is selected for replacement. If  $\delta_1 < X$  (or  $t < X$ ) and  $\delta_2 < X$  (or  $t_2 < X$ ), then  $p_{m_1}$  is selected for replacement. In ID, more than two portables may be considered for replacement. For

demonstration purposes, here we consider only the oldest two portables. The following notation is introduced.

- 1)  $t$ : the time period between  $p_{m_1}$ 's arrival and  $p_m$ 's arrival [c.f. Fig. 2(a)].
- 2)  $t_1$ : the time period between  $p_{m_1}$ 's arrival and  $p_{m_2}$ 's arrival [c.f. Fig. 3(a)].
- 3)  $t_2$ : the time period between  $p_{m_2}$ 's arrival and  $p_m$ 's arrival [c.f. Fig. 3(a)]. Note that  $t_2 = t - t_1$ .
- 4)  $\tau_1$ : the residence time of  $p_{m_1}$  [c.f. Fig. 2(a)].
- 5)  $\tau_2$ : the residence time of  $p_{m_2}$  [c.f. Fig. 3(a)].
- 6)  $n$ : the number of portables that arrive in the period  $t$  (excluding  $p_{m_1}$ ). Note that  $n = m - m_1$ .
- 7)  $n_1$ : the number of portables that arrive in the period  $t_1$  (excluding  $p_{m_1}$ ). Note that  $n_1 = m_2 - m_1$ .
- 8)  $n_2$ : the number of portables that arrive in the period  $t_2$  (excluding  $p_{m_2}$ ). Note that  $n_2 = n - n_1 = m - m_2$ .
- 9)  $\delta_1$ : the time interval between the last phone call to  $p_{m_1}$  before  $p_m$ 's arrival and the time when  $p_m$  arrives [c.f. Fig. 2(b)]. Note that there is no phone call to  $p_{m_1}$  in the time period  $\delta_1$ .
- 10)  $\delta_2$ : the time interval between the last phone call to  $p_{m_2}$  before  $p_m$ 's arrival and the time when  $p_m$  arrives [c.f. Fig. 3(b)].
- 11)  $x_1$ : the time interval between the last phone call to  $p_{m_1}$  and the time when  $p_{m_1}$  moves out [c.f. Fig. 2(b)].
- 12)  $x_2$ : the time interval between the last phone call to  $p_{m_2}$  and the time when  $p_{m_2}$  moves out [c.f. Fig. 3(b)].

Since the portable arrivals to an RA form a Poisson process,  $t$  has an Erlang distribution with the density function

$$g_n(t) = \frac{(\eta t)^{n-1}}{(n-1)!} e^{-\eta t}.$$

Similarly,  $t_1$  and  $t_2$  have the Erlang density functions  $g_{n_1}(t_1)$  and  $g_{n_2}(t_2)$ , respectively. If we assume exponential portable residence times, then  $\tau_1$  and  $\tau_2$  have an identical density function

$$f(\tau) = \mu e^{-\mu\tau}.$$

Let the intercall arrival times to a portable be exponentially distributed with the density function

$$r(x) = \lambda e^{-\lambda x},$$

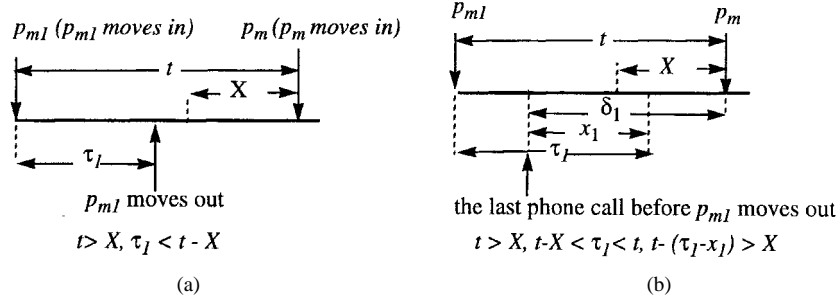


Fig. 2. The timing diagram for ID Case 1. (a)  $t > X, \tau_l < t - X$ . (b)  $t > X, t - X < \tau_l < t, t - (\tau_l - x_1) > X$ .

Since the movements of a portable are a Poisson process, a portable is a random observer of the call interarrival times when it moves out of the RA. From the random observer property of the Poisson process and the memoryless property of the exponential distribution, both  $x_1$  and  $x_2$  have the same density function  $r(\cdot)$ . Similarly, the arrival of  $p_m$  is a random observer of the call arrivals to  $p_{m_1}$  and  $p_{m_2}$ , and  $\delta_1$  and  $\delta_2$  also have the same density function  $r$ .

Let  $\gamma_1(m_1)$  be the probability that  $\delta_1 > X$  and  $p_{m_1}$  is not in the RA. Let  $\gamma_2(m_1, m_2)$  be the probability that  $\delta_1 < X$  (or  $t < X$ ),  $\delta_2 > X$ , and  $p_{m_2}$  is not in the RA. Let  $\gamma_3(m_1, m_2)$  be the probability that  $\delta_1 < X$  (or  $t < X$ ),  $\delta_2 < X$  (or  $t_2 < X$ ), and  $p_{m_1}$  is not in the RA. Then

$$\gamma_{ID} = \gamma_1(m_1) + \gamma_2(m_1, m_2) + \gamma_3(m_1, m_2)$$

is the probability that the portable (either  $p_{m_1}$  or  $p_{m_2}$ ) selected by ID is not in the RA.

The probability  $\gamma_{ID}$  is derived in the following three cases.

1) *Case 1:* ID assumes that  $p_{m_1}$  is not in the RA, and  $p_{m_1}$  is not in the RA.

That is, ID assumes that  $p_{m_1}$  has moved out of the RA when  $p_m$  moves in, which implies that the inactive period  $\delta_1$  is longer than the threshold  $X$  when  $p_m$  arrives, and  $\delta_1 > X \Rightarrow t > X$ . Since  $p_{m_1}$  is not in the RA when  $p_m$  arrives, either  $\tau_l < t - X$  [c.f. Fig. 2(a)] or  $t - X < \tau_l < t$ , and  $\delta_1 = t - (\tau_l - x_1) > X$  [c.f. Fig. 2(b)]. The probability for Fig. 2(a) is

$$\begin{aligned} & \Pr[t > X, \tau_l < t - X] \\ &= \int_{t=X}^{\infty} \int_{\tau_l=0}^{t-X} g_n(t) f(\tau_l) d\tau_l dt \\ &= \int_{t=X}^{\infty} \frac{(\eta t)^{n-1}}{(n-1)!} e^{-\eta t} [1 - e^{-\mu(t-X)}] dt \\ &= \sum_{i=0}^{n-1} e^{-\eta X} \left\{ \frac{(\eta X)^i}{i!} - \left( \frac{\eta}{\eta + \mu} \right)^n \frac{[(\eta + \mu)X]^i}{i!} \right\}. \end{aligned} \quad (2)$$

(3) is derived from (2) based on the fact that

$$\int_{t=X}^{\infty} \frac{(\eta t)^{n-1}}{(n-1)!} e^{-\eta t} dt = \sum_{i=0}^{n-1} \frac{(\eta X)^i}{i!} e^{-\eta X}.$$

Since  $\delta_1 > X$  implies  $x_1 > \tau_l + X - t$ , the probability for Fig. 2(b) is

$$\begin{aligned} & \Pr[t > X, t - X < \tau_l < t, x_1 > \tau_l + X - t] \\ &= \int_{t=X}^{\infty} \int_{\tau_l=t-X}^t \int_{x_1=\tau_l+X-t}^{\infty} g_n(t) f(\tau_l) r(x_1) dx_1 \\ & \quad \cdot d\tau_l dt \\ &= \sum_{i=0}^{n-1} \left( \frac{\mu}{\mu + \lambda} \right) \left( \frac{\eta}{\eta + \mu} \right)^n \frac{[(\eta + \mu)X]^i}{i!} \\ & \quad \times [e^{-\eta X} - e^{-(\eta + \mu + \lambda)X}]. \end{aligned} \quad (4)$$

Thus,  $\gamma_1(m_1) = (3) + (4)$ .

2) *Case 2:* ID assumes that  $p_{m_1}$  is in the RA,  $p_{m_2}$  is not in the RA, and  $p_{m_2}$  is not in the RA. Since ID assumes that  $p_{m_2}$  is not in the RA when  $p_m$  moves in, it implies that the inactive period  $\delta_1$  is longer than the threshold  $X$ , and

$$\delta_2 > X \Rightarrow t_2 > X \Rightarrow t > X. \quad (5)$$

As in the situations described in Case 1, either  $\tau_2 < t_2 - X$  [c.f. Fig. 3(a) and (c)] or  $t_2 - X < \tau_2 < t_2$ , and  $\delta_2 = t_2 - (\tau_2 - x_2) > X$  [c.f. Fig. 3(b) and (d)]. Since ID assumes that  $p_{m_1}$  is in the RA and  $t_2 > X$ , it implies that  $t = t_1 + t_2 > X$  and  $\tau_1 > t - X$ . There are two cases.

3) *Case 2a:*  $\tau_1 > t$  and  $\delta_1 < X$  [c.f. Fig. 3(a) and (b)].

4) *Case 2b:*  $t - X < \tau_1 < t$  and  $\delta_1 = t - (\tau_1 - x_1) < X$  [c.f. Fig. 3(c) and (d)].

From (5) and Cases 2a and 2b, there are four combinations for Case 2, as illustrated in Fig. 3. The probability for Fig. 3(a) is

$$\begin{aligned} & \Pr[t_1 > 0, t_2 > X, \tau_1 > t, \delta_1 < X, \tau_2 < t_2 - X] \\ &= \int_{t_2=X}^{\infty} g_{n_2}(t_2) \int_{t_1=0}^{\infty} g_{n_1}(t_1) \int_{\tau_1=t_1+t_2}^{\infty} f(\tau_1) \\ & \quad \cdot \int_{\delta_1=0}^X r(\delta_1) \int_{\tau_2=0}^{t_2-X} f(\tau_2) d\tau_2 d\delta_1 d\tau_1 dt_1 dt_2 \\ &= \int_{t_2=X}^{\infty} g_{n_2}(t_2) \int_{t_1=0}^{\infty} g_{n_1}(t_1) e^{-\mu(t_1+t_2)} (1 - e^{-\lambda X}) \\ & \quad \cdot [1 - e^{-\mu(t_2-X)}] dt_1 dt_2 \\ &= (1 - e^{-\lambda X}) \int_{t_2=X}^{\infty} g_{n_2}(t_2) e^{-\mu t_2} [1 - e^{-\mu(t_2-X)}] \\ & \quad \cdot \int_{t_1=0}^{\infty} \frac{(\eta t_1)^{n_1-1}}{(n_1-1)!} e^{-(\eta+\mu)t_1} dt_1 dt_2 \end{aligned}$$

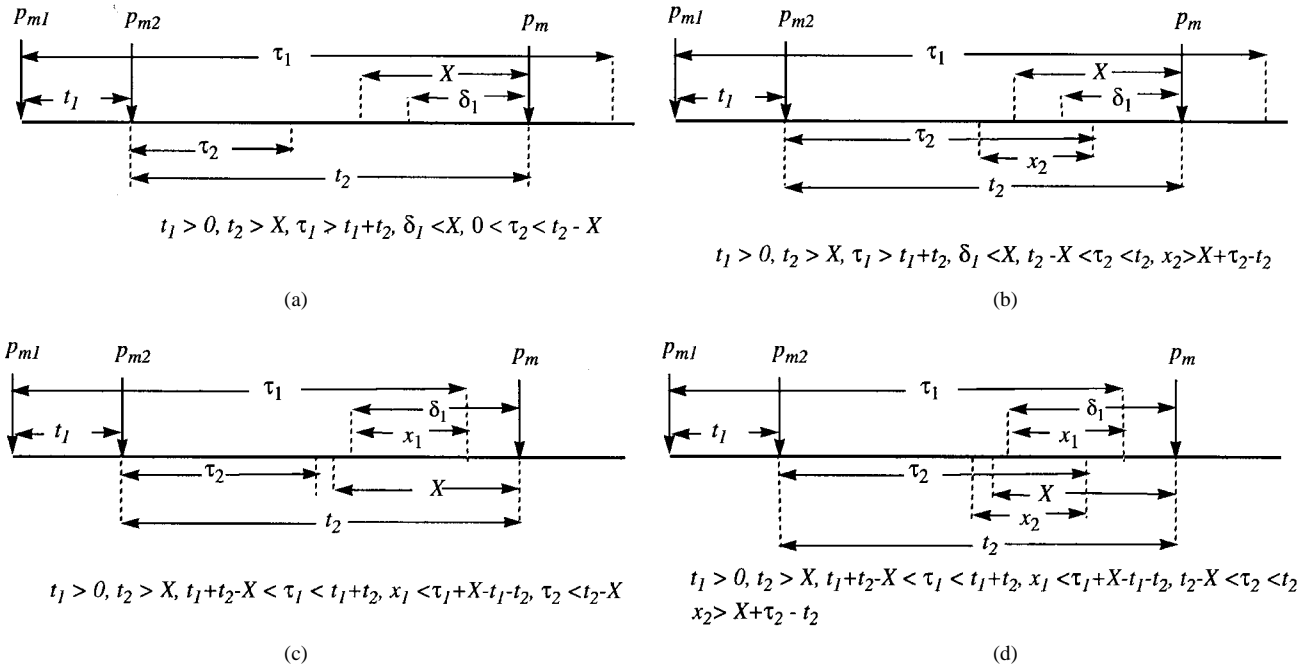


Fig. 3. The timing diagram for ID Case 2. (a)  $t_1 > 0, t_2 > X, \tau_1 > t_1 + t_2, \delta_1 < X, 0 < \tau_2 < t_2 - X$ . (b)  $t_1 > 0, t_2 > X, \tau_1 > t_1 + t_2, \delta_1 < X, t_2 - X < \tau_2 < t_2, x_2 > X + \tau_2 - t_2$ . (c)  $t_1 > 0, t_2 > X, t_1 + t_2 - X < \tau_1 < t_1 + t_2, x_1 < \tau_1 + X - t_1 - t_2, \tau_2 < t_2 - X$ . (d)  $t_1 > 0, t_2 > X, t_1 + t_2 - X < \tau_1 < t_1 + t_2, x_1 < \tau_1 + X - t_1 - t_2, t_2 - X < \tau_2 < t_2, x_2 > X + \tau_2 - t_2$ .

$$\begin{aligned}
&= \left( \frac{\eta}{\eta + \mu} \right)^{n_1} (1 - e^{-\lambda X}) \int_{t_2=X}^{\infty} \frac{(\eta t_2)^{n_2-1}}{(n_2-1)!} \\
&\quad \cdot [e^{-(\eta+\mu)t_2} - e^{-(\eta+2\mu)t_2+\mu X}] dt_2 \\
&= \sum_{i=0}^{n_2-1} \left( \frac{\eta}{\eta + \mu} \right)^{n_1} (1 - e^{-\lambda X}) e^{-(\eta+\mu)X} \\
&\quad \cdot \left\{ \left( \frac{\eta}{\eta + \mu} \right)^{n_2} \frac{[(\eta + \mu)X]^i}{i!} \right. \\
&\quad \left. - \left( \frac{\eta}{\eta + 2\mu} \right)^{n_2} \frac{[(\eta + 2\mu)X]^i}{i!} \right\}. \quad (6)
\end{aligned}$$

The probability for Fig. 3(b) is

$$\Pr [t_1 > 0, t_2 > X, \tau_1 > t, \delta_1 < X,$$

$$\begin{aligned}
& t_2 - X < \tau_2 < t_2, x_2 > X + \tau_2 - t_2] \\
&= \int_{t_1=0}^{\infty} g_{n_1}(t_1) \int_{t_2=X}^{\infty} g_{n_2}(t_2) \int_{\tau_1=t_1+t_2}^{\infty} f(\tau_1) \\
&\quad \cdot \int_{\delta_1=0}^X r(\delta_1) \int_{\tau_2=t_2-X}^{t_2} f(\tau_2) \\
&\quad \times \int_{x_2=X+\tau_2-t_2}^{\infty} r(x_2) dx_2 d\tau_2 d\delta_1 d\tau_1 dt_2 dt_1 \\
&= \sum_{i=0}^{n_2-1} \left( \frac{\eta}{\eta + 2\mu} \right)^{n_2} \left( \frac{\eta}{\eta + \mu} \right)^{n_1} \\
&\quad \cdot \left( \frac{\mu}{\lambda + \mu} \right) \frac{[(\eta + 2\mu)X]^i}{i!} \\
&\quad \times e^{-(\eta+\mu)X} (1 - e^{-\lambda X}) [1 - e^{-(\lambda+\mu)X}]. \quad (7)
\end{aligned}$$

The probability for Fig. 3(c) is

$$\begin{aligned}
&\Pr [t_1 > 0, t_2 > X, t - X < \tau_1 < t, \\
&\quad x_1 < \tau_1 + X - t, \tau_2 < t_2 - X] \\
&= \int_{t_1=0}^{\infty} g_{n_1}(t_1) \int_{t_2=X}^{\infty} g_{n_2}(t_2) \int_{\tau_1=t_1+t_2-X}^{t_1+t_2} f(\tau_1) \\
&\quad \times \int_{x_1=0}^{\tau_1+X-t_1-t_2} r(x_1) \int_{\tau_2=0}^{t_2-X} f(\tau_2) d\tau_2 dx_1 d\tau_1 \\
&\quad \cdot dt_2 dt_1 \\
&= \sum_{i=0}^{n_2-1} \left( \frac{\eta}{\eta + \mu} \right)^{n_1} e^{-\eta X} \left\{ \left( \frac{\eta}{\eta + \mu} \right)^{n_2} \frac{[(\eta + \mu)X]^i}{i!} \right. \\
&\quad \left. - \left( \frac{\eta}{\eta + 2\mu} \right)^{n_2} \frac{[(\eta + 2\mu)X]^i}{i!} \right\} \\
&\quad \times \left\{ 1 - e^{-\mu X} - \left( \frac{\mu}{\lambda + \mu} \right) [1 - e^{-(\lambda+\mu)X}] \right\}. \quad (8)
\end{aligned}$$

The probability for Fig. 3(d) is

$$\begin{aligned}
&\Pr [t_1 > 0, t_2 > X, t - X < \tau_1 < t, x_1 < \tau_1 \\
&\quad + X - t, t_2 - X < \tau_2 < t_2, x_2 > X + \tau_2 - t_2] \\
&= \int_{t_2=X}^{\infty} g_{n_2}(t_2) \int_{t_1=0}^{\infty} g_{n_1}(t_1) \int_{\tau_1=t_1+t_2-X}^{t_1+t_2} f(\tau_1) \\
&\quad \times \int_{x_1=0}^{\tau_1+X-t_1-t_2} r(x_1) \int_{\tau_2=t_2-X}^{t_2} f(\tau_2) \\
&\quad \times \int_{x_2=X+\tau_2-t_2}^{\infty} r(x_2) dx_2 d\tau_2 dx_1 d\tau_1 dt_1 dt_2
\end{aligned}$$

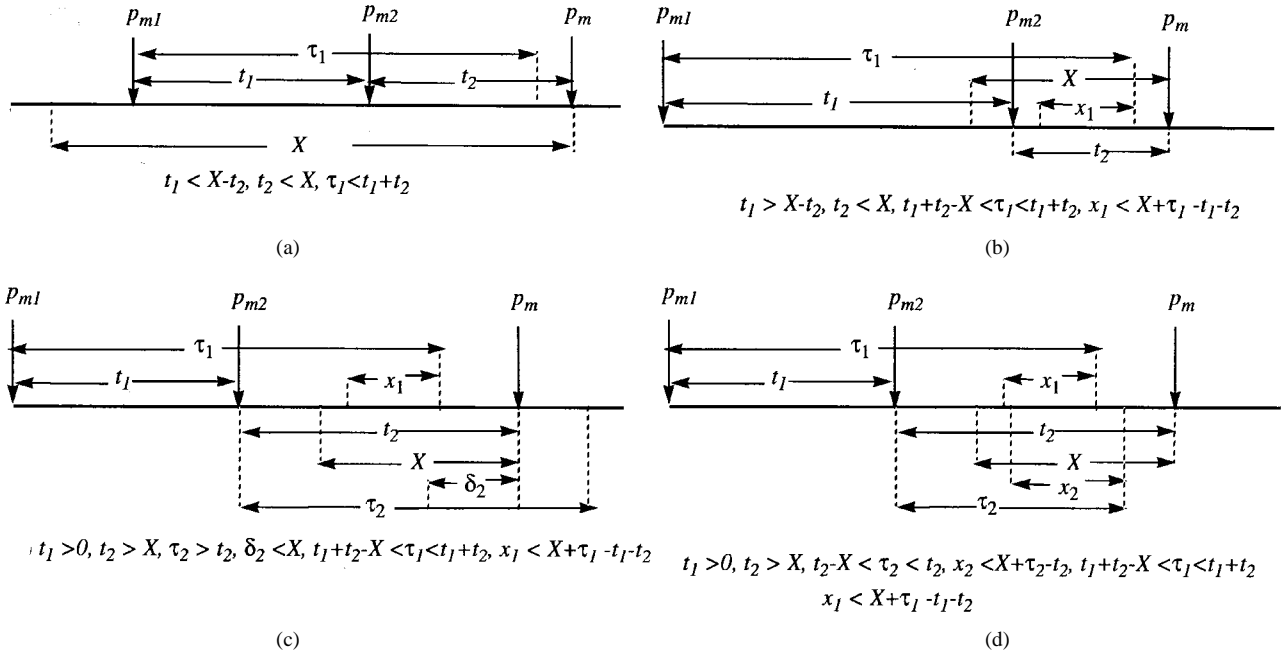


Fig. 4. The timing diagram for ID Case 3.

$$\begin{aligned}
 &= \sum_{i=0}^{n_2-1} \left( \frac{\eta}{\eta + \mu} \right)^{n_1+n_2} \frac{[(\eta + \mu)X]^i}{i!} \\
 &\cdot e^{-\eta X} [1 - e^{-(\lambda + \mu)X}] \\
 &\times \left\{ 1 - e^{-\mu X} - \left( \frac{\mu}{\lambda + \mu} \right) [1 - e^{-(\lambda + \mu)X}] \right\}. \quad (9)
 \end{aligned}$$

Thus,  $\gamma_2(m_1, m_2) = (6) + (7) + (8) + (9)$ .

5) **Case 3: ID assumes that both  $p_{m_1}$  and  $p_{m_2}$  are in the RA, but  $p_{m_1}$  is not in the RA.** Note that  $\tau_1 < t$ . ID assumes that  $p_{m_2}$  is in the RA, which implies that  $\delta_2 < X$  or  $t_2 < X$ . There are three possibilities.

•  $t_2 < X$  [c.f. Fig. 4(a) and (b)]. Since ID assumes that  $p_{m_1}$  is in the RA, we have  $\delta_1 < X$  or  $t_1 < X$ . There are two cases.

6) **Case 3a:  $t < X \Rightarrow t_1 < X - t_2$ ,** as shown in Fig. 4(a). The probability is

$$\begin{aligned}
 &\Pr[\tau_1 < t_1 + t_2 < X] \\
 &= \int_{t_2=0}^X g_{n_2}(t_2) \int_{t_1=0}^{X-t_2} g_{n_1}(t_1) \int_{\tau_1=0}^{t_1+t_2} f(\tau_1) d\tau_1 \\
 &\cdot dt_1 dt_2 \\
 &= 1 - \left( \frac{\eta}{\eta + \mu} \right)^{n_1+n_2} - \sum_{j=0}^{n_2-1} \left( \frac{X^j e^{-\eta X}}{j!} \right) \\
 &\cdot \left[ \eta^j - \left( \frac{\eta}{\eta + \mu} \right)^{n_1+n_2} (\eta + \mu)^j e^{-\mu X} \right] \\
 &- \sum_{i=0}^{n_1-1} \frac{X^{n_2+i} \eta^{n_2} e^{-\eta X}}{(n_2+i)!} \left[ \eta^i - \left( \frac{\eta}{\eta + \mu} \right)^{n_1} \right. \\
 &\quad \left. \cdot (\eta + \mu)^i e^{-\mu X} \right]. \quad (10)
 \end{aligned}$$

7) **Case 3b:  $t > X \Rightarrow t_1 > X - t_2$ .** Since  $\delta_1 < X$ , we have  $t - (\tau_1 - x_1) < X$  and  $t - X < \tau_1 < t$ , as shown in Fig. 4(b). The probability is

$$\begin{aligned}
 &\Pr[t_1 > X - t_2, t_2 < X, t - X < \tau_1 < t, x_1 < X + \tau_1 - t] \\
 &= \int_{t_2=0}^X g_{n_2}(t_2) \int_{t_1=X-t_2}^{\infty} g_{n_1}(t_1) \int_{\tau_1=t_1+t_2-X}^{t_1+t_2} f(\tau_1) \\
 &\times \int_{x_1=0}^{X+\tau_1-t_1-t_2} r(\delta_1) d\delta_1 d\tau_1 dt_1 dt_2 \\
 &= \sum_{i=0}^{n_1-1} \left( \frac{\eta}{\eta + \mu} \right)^{n_1} \frac{\eta^{n_2} (\eta + \mu)^i X^{n_2+i}}{(n_2+i)!} e^{-\eta X} \\
 &\times \left\{ 1 - e^{-\mu X} - \left( \frac{\mu}{\lambda + \mu} \right) [1 - e^{-(\lambda + \mu)X}] \right\}. \quad (11)
 \end{aligned}$$

•  $t_2 > X, \tau_2 > t_2$  and  $\delta_2 < X$  [c.f. Fig. 4(c)]. Since  $t = t_1 + t_2 > X$  and ID assumes that  $p_{m_1}$  is in the RA, the situation is the same as in Case 3b (i.e.,  $t - X < \tau_1 < t$  and  $\delta_1 = t - (\tau_1 - x_1) < X$ ), and

$$\begin{aligned}
 &\Pr[t_1 > 0, t_2 > X, \tau_2 > t_2, \delta_2 < X, t - X < \tau_1 < t, \\
 &\quad x_1 < X + \tau_1 - t] \\
 &= \int_{t_2=X}^{\infty} g_{n_2}(t_2) \int_{t_1=0}^{\infty} g_{n_1}(t_1) \int_{\tau_2=t_2}^{\infty} f(\tau_2) \\
 &\cdot \int_{\delta_2=0}^X r(\delta_2) \int_{\tau_1=t_1+t_2-X}^{t_1+t_2} f(\tau_1) \times \int_{x_1=0}^{X+\tau_1-t_1-t_2} \\
 &\cdot r(x_1) dx_1 d\tau_1 d\delta_2 \\
 &\cdot d\tau_2 dt_1 dt_2 \\
 &= \sum_{i=0}^{n_2-1} \left( \frac{\eta}{\eta + 2\mu} \right)^{n_1+n_2} \frac{[(\eta + 2\mu)X]^i}{i!} \\
 &\cdot e^{-(\eta + \mu)X} (1 - e^{-\lambda X})
 \end{aligned}$$

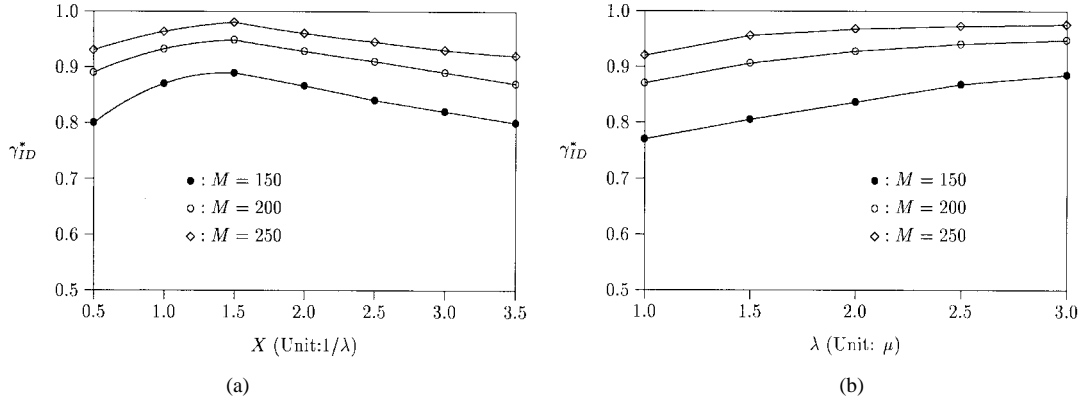


Fig. 5. Performance of ID. (a) The effect of  $X$  on ID ( $\lambda = 2\mu$ ). (b) The effect of  $\lambda$  on ID ( $X = 1.5/\lambda$ ).

$$\times \left[ 1 - e^{-\mu X} - \left( \frac{\mu}{\lambda + \mu} \right) (1 - e^{-(\lambda + \mu)X}) \right]. \quad (12)$$

•  $t_2 > X$ ,  $t_2 - X < \tau_2 < t_2$ , and  $\delta_2 = t_2 - (\tau_2 - x_2) < X$  as shown in Fig. 4(d). Since  $t = t_1 + t_2 > X$  and ID assumes that  $p_{m_1}$  is in the RA, the situation is the same as Case 3b (i.e.,  $t - X < \tau_1 < t$  and  $\delta_1 = t - (\tau_1 - x_1) < X$ ), and

$$\begin{aligned} & \Pr[t_1 > 0, t_2 > X, t_2 - X < \tau_2 < t_2, x_2 < X + \tau_2 - t_2, \\ & \quad t - X < \tau_1 < t, x_1 < X + \tau_1 - t] \\ &= \int_{t_2=0}^X g_{n_2}(t_2) \int_{t_1=0}^{\infty} g_{n_1}(t_1) \int_{\tau_2=t_2-X}^{t_2} f(\tau_2) \\ & \quad \cdot \int_{x_2=0}^{X+\tau_2-t_2} r(x_2) \int_{\tau_1=t_1+t_2-X}^{t_1+t_2} f(\tau_1) \int_{x_1=0}^{\tau_1+X-t_1-t_2} \\ & \quad \cdot r(x_1) dx_1 d\tau_1 dx_2 d\tau_2 dt_1 dt_2 \\ &= \sum_{i=0}^{n_2-1} \left( \frac{\eta}{\eta + \mu} \right)^{n_1} \left( \frac{\eta}{\eta + 2\mu} \right)^{n_2} \frac{[(\eta + 2\mu)X]^i}{i!} e^{-\eta X} \\ & \quad \times \left[ 1 - e^{-\mu X} - \left( \frac{\mu}{\lambda + \mu} \right) (1 - e^{-(\lambda + \mu)X}) \right]^2. \quad (13) \end{aligned}$$

Thus,  $\gamma_3(m_1, m_2) = (10) + (11) + (12) + (13)$ .

Suppose that the size of the database is  $M$ . For the oldest portable  $p_{m_1}$ , it is apparent that  $m_1 \leq m - M$ . Similarly, for the second oldest portable  $p_{m_2}$ ,  $m_2 \leq m - M + 1$ . Since

$$\begin{aligned} & \gamma_1(m_1) + \gamma_2(m_1, m_2) + \gamma_3(m_1, m_2) \\ & > \gamma_1(m - M) + \gamma_2(m - M, m - M + 1) \\ & \quad + \gamma_3(m - M, m - M + 1) \end{aligned}$$

a lower bound  $\gamma_{ID}^*$  for  $\gamma_{ID}$  is

$$\begin{aligned} \gamma_{ID}^* &= \gamma_1(m - M) + \gamma_2(m - M, m - M + 1) \\ & \quad + \gamma_3(m - M, m - M + 1). \end{aligned}$$

Fig. 5(a) illustrates the effect of  $X$  on  $\gamma_{ID}^*$ . The figure indicates that the maximum value for  $\gamma_{ID}^*$  occurs when  $X \approx 1.5$  (for  $\lambda = 2\mu$ ). The figure indicates that erring on the side of an  $X$  value that is too large will degrade performance less than erring on the side of an  $X$  value that is too small. It is apparent that the performance of ID improves as  $\lambda$  increases. Fig. 5(b) illustrates that  $\gamma_{ID}^*$  is an increasing function of  $\lambda$ .

Let  $\alpha_{ID}$  be the probability that a portable (either  $p_{m_1}$  or  $p_{m_2}$ ) cannot register (i.e., is forced to deregister) when  $p_m$  arrives. An upper bound  $\alpha_{ID}^*$  for  $\alpha_{ID}$  is

$$\alpha_{ID} \leq \alpha_{ID}^* = 1 - \gamma_{ID}^*.$$

Fig. 9(a) indicates that  $\alpha_{ID}^* < 10^{-3}$  for  $M > 4N$ .

#### IV. TIMEOUT DEREGISTRATION

In the TO scheme, a portable sends a reregistration message to the RA for every time period  $T$ . The TO scheme is better than the explicit scheme if the reregistration traffic (in TO) is less than the deregistration traffic [in ED]. This section derives the number of reregistration messages sent in the TO scheme. Let  $E[K]$  be the expected number of reregistration messages sent before a portable leaves an RA. Let  $f(\tau)$  be the portable residence time distribution (with mean  $1/\mu$ ). Then

$$E[K] = \sum_{k=0}^{\infty} k \int_{\tau=kT}^{(k+1)T} f(\tau) d\tau. \quad (14)$$

For the exponential residence time distribution, (14) is rewritten as

$$E[K] = \sum_{k=0}^{\infty} \int_{\tau=kT}^{(k+1)T} k \mu e^{-\mu\tau} d\tau = \frac{e^{-\mu T}}{1 - e^{-\mu T}}.$$

For the uniform residence time distribution in  $[0, 2/\mu]$

$$\begin{aligned} E[K] &= \sum_{k=0}^{\lfloor 2/\mu T \rfloor - 1} \int_{\tau=kT}^{(k+1)T} k \frac{\mu}{2} d\tau + \int_{\tau=\lfloor 2/\mu T \rfloor T}^{2/\mu} k \frac{\mu}{2} d\tau \\ &= \left\lfloor \frac{2}{\mu T} \right\rfloor \left( \frac{\mu}{2} \right) \left[ \frac{T}{2} \left( \left\lfloor \frac{2}{\mu T} \right\rfloor - 1 \right) \right] \\ & \quad + \left( \frac{2}{\mu} - \left\lfloor \frac{2}{\mu T} \right\rfloor T \right). \end{aligned}$$

Fig. 6(a) plots  $E[K]$  against  $T$ . The figure indicates that  $E[K] < 0.24$  if  $T > 1.8/\mu$  for the exponential residence times and  $T > 1.52/\mu$  for the uniform residence times. In the explicit scheme, a deregistration message is sent when a portable moves out of the RA. On the other hand, in the TO scheme, the number of reregistration messages sent by a portable is  $E[K]$ . Thus, the deregistration traffic in the explicit scheme is  $\frac{1}{E[K]}$  times the reregistration traffic in the TO scheme. For

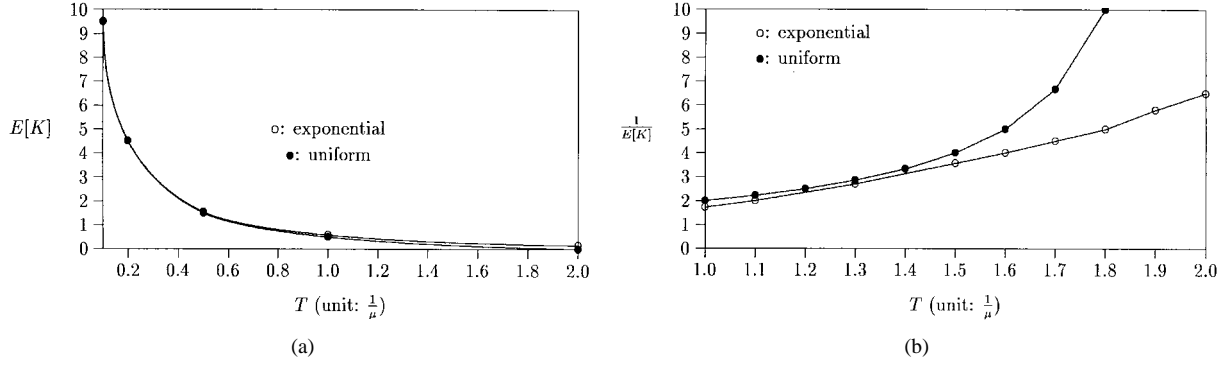


Fig. 6. The expected number of reregistration messages. (a) The registration message overhead in the TO scheme. (b) Comparison of the de(re)registration message overhead for the explicit scheme and the TO scheme.

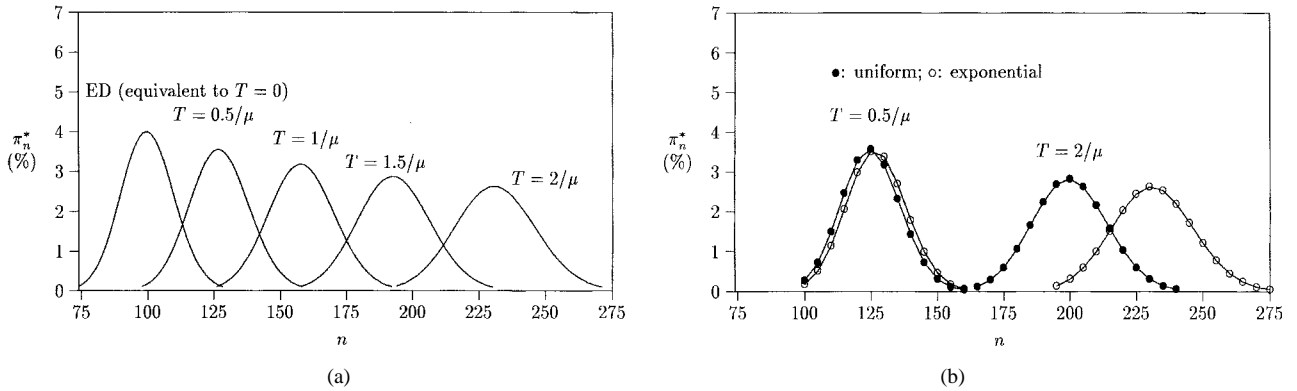


Fig. 7. The portable distribution seen by the TO scheme. (a) The impact of  $T$ . (b) The impact of the residual time distributions.

example, if  $T = 1.8/\mu$ , the deregistration traffic generated by the explicit scheme is about four–five times the traffic generated by the TO scheme assuming exponential residence times [c.f. Fig. 6 (b)]. In other words, if  $T$  is sufficiently large, then the TO scheme significantly reduces the network traffic due to deregistration (compared with the explicit scheme).

The portable residence time  $\tau^*$  seen by the TO scheme is different from the true portable residence time  $\tau$  (the TO scheme only differentiates on multiples of  $T$ ). Since  $\tau^* = \lceil \tau/T \rceil T$ , the expected residence time  $E[\tau^*]$  seen by the TO scheme is

$$E[\tau^*] = \sum_{k=0}^{\infty} \int_{\tau=kT}^{(k+1)T} (k+1)T f(\tau) d\tau = (E[K] + 1)T.$$

For the exponential residence time distribution

$$E[\tau^*] = \frac{T}{1 - e^{-\mu T}}. \quad (15)$$

From (15) and the  $M/G/\infty$  model described in Section II, the steady-state probability  $\pi_n^*$  that the TO scheme sees  $n$  portables in the RA is

$$\pi_n^* = \left( \frac{N\mu T}{1 - e^{-\mu T}} \right)^n \frac{e^{-(N\mu T/(1 - e^{-\mu T}))}}{n!}.$$

The  $\pi_n^*$  distribution is plotted in Fig. 7 for different  $T$  values. Fig. 7(a) indicates that the portable seen by the TO scheme increases as  $T$  increases. Fig. 7(b) indicates that the number of portables seen by the TO registration scheme is closer to the true number for the uniform residence times than for the exponential residence times. Let  $\alpha_{TO}$  be the probability that the TO scheme sees a full registration database in an RA when a portable arrives. Then

$$\alpha_{TO} = \sum_{n=M}^{\infty} \pi_n^*.$$

Suppose that  $p$  is not allowed to register if the TO scheme sees a full database at  $p$ 's arrival. Then  $\alpha_{TO}$  is the probability that a portable (i.e.,  $p$ ) cannot register (and receive services). Fig. 8 plots  $\alpha_{TO}$  against  $M$ . It is clear that  $\alpha_{TO}$  is a decreasing function of the database size  $M$  and is an increasing function of  $T$  [c.f. Fig. 8(a)]. It is interesting to note that for the same  $M/N$  ratio, the  $\alpha_{TO}$  value for a small  $N$  is smaller than the  $\alpha_{TO}$  for a large  $N$  when  $M/N < 2.17$ . The opposite is true when  $M/N > 2.17$  [c.f. Fig. 8(b)]. Fig. 9(a) compares  $\alpha_{TO}$  with  $\alpha_{ID}^*$ . For  $M > 2.5N$  (where  $N = 100$ ),  $\alpha_{TO} < \alpha_{ID}^*$ . Note that  $\alpha_{TO} < 10^{-3}$  for  $M > 2.5N$ . However, when  $M < 2N$ ,  $\alpha_{TO}$  is much larger than  $\alpha_{ID}^*$ .

Other replacement strategies can be used if the TO scheme sees a full database when a portable  $p$  arrives. Let us consider

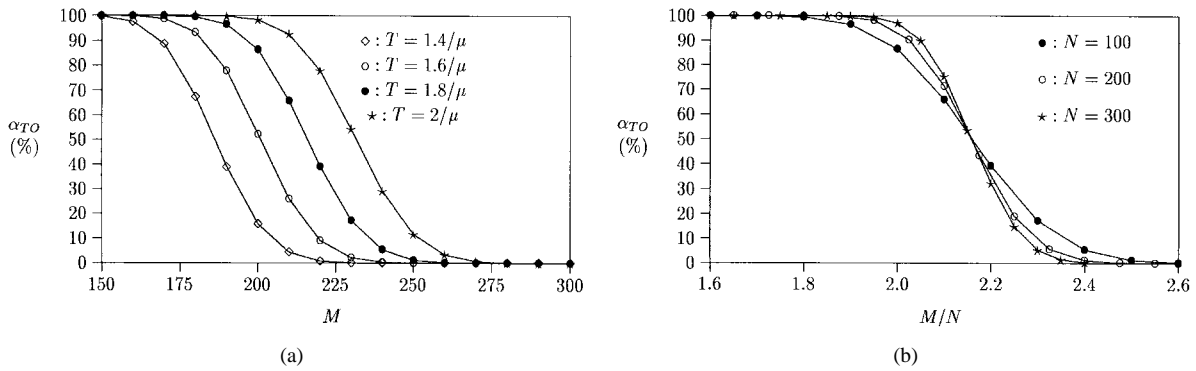


Fig. 8. The probability that the TO scheme sees a full registration database when a portable arrives. (a) The impact of  $T$  ( $N = 100$ ). (b) The impact of  $N$  ( $T = 1.8$ ).

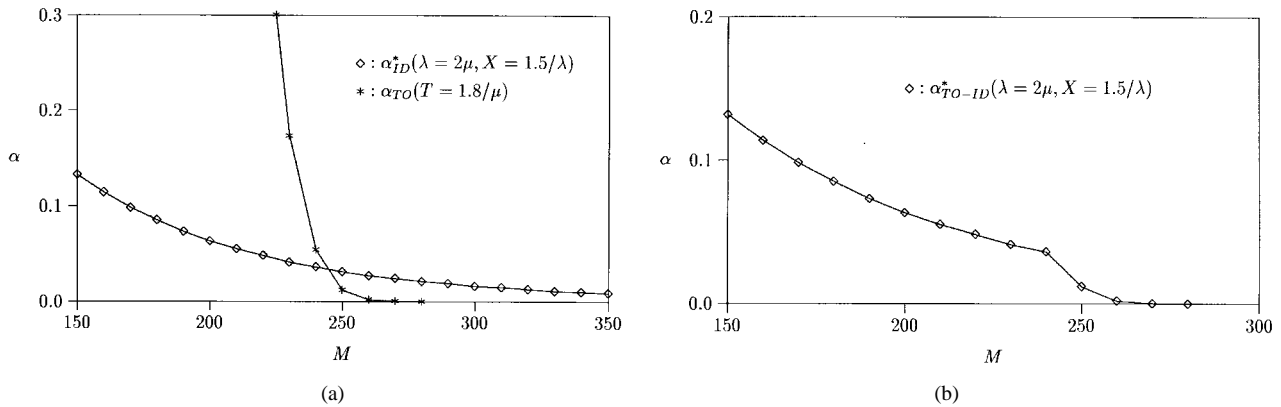


Fig. 9. Performance for different deregistration schemes ( $N = 100$ ). (a) The  $\alpha$  values for different schemes. (b) The performance for the TO scheme with different replacement strategies ( $T = 1.8/\mu$ ).

the replacement strategies used in ID in the previous section. Let  $\alpha_{TO-ID}$  be the probability that  $p$  cannot register in the TO scheme with the ID replacement strategy. Then

$$\alpha_{TO-ID} < \alpha_{TO-ID}^* = \min(\alpha_{TO}, \alpha_{ID}^*).$$

Fig. 9(b) plots  $\alpha_{TO-ID}^*$ . The figure indicates that with the ID replacement strategy, the performance of the TO scheme is significantly improved.

## V. CONCLUSIONS

This paper has studied three deregistration strategies for PCS networks. Two output measures were considered: the number of messages sent in the deregistration strategies and the probability  $\alpha$  that a portable cannot register (and receive service). Assume 100 portables in an RA on the average. To satisfy the constraint that  $\alpha < 10^{-3}$ , the size of the database required in the explicit scheme is  $M \simeq 1.5N$ , which is smaller than the database size for the implicit scheme ( $M \simeq 4N$ ) and the TO scheme ( $M \simeq 2.5N$ ). On the other hand, the number of deregistration messages sent in the explicit scheme is four–five times the number of messages sent in the TO scheme (with the registration period  $T = 1.8/\mu$ ). In the implicit

scheme, neither deregistration nor reregistration messages are sent. Our study indicates that if the database size is expected to be large, then the implicit scheme should be used to eliminate the deregistration message traffic. If the database size has to be small, on the other hand, then the explicit scheme should be used to achieve a low  $\alpha$  value. If the database size is between  $2.5\text{--}4N$ , then the TO scheme with the ID replacement strategy should be used to ensure a reasonably small  $\alpha$  value and a low level of reregistration message traffic.

In summary, ID and ED are mutually exclusive. TO deregistration is a useful tool to clean up registration databases and can be combined with either one of the ID or ED approaches. In PACS [5], [10], polling reregistration was introduced so that the system can poll the portables to see if the portables are still in the RA [9]. A combination of TO deregistration, ID, and polling reregistration might be best in all circumstances. Performance modeling of such a combination will be one of our future research directions.

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