

# 國立交通大學

電子工程學系 電子研究所碩士班

碩士論文

用於 IEEE 802.16d 及 IEEE 802.11a/g 之  
CORDIC 多模同步電路設計



CORDIC Based Multimode Synchronization  
Circuit Design for IEEE 802.16d and  
802.11a/g systems

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中華民國九十七年六月

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## 摘要

本論文提出一個適用於 IEEE802.11a/g 及 IEEE802.16d 之多模同步電路。所提出的同步電路中可以細分為訊框偵測，分數載波頻率漂移估測，整數載波頻率漂移估測及符元邊界偵測。在訊框偵測中，本論文提出一個修改過的絕對值近似方法。這個方法可以使近似的誤差降低 2~3 倍。在分數載波頻率漂移估測中，本論文提出一個修改過的座標旋轉數位計算機電路。相對於傳統的方法，這個座標旋轉數位計算機電路可以使得硬體複雜度降低 46%。在整數載波頻率漂移中，本論文使用一個簡化的匹配濾波器以降低非共用電路所佔的比例。系統模擬是建構在 MathWorks 的 MATLAB 平台上。整個電路架構也已經在 Verilog 語言下實現出來。在 UMC 0.18 微米的製程環境下使用新思科技的 Design Compiler 所合成出來的結果顯示，多模同步電路的總 gate count 大約是 124k。

# CORDIC Based Multimode Synchronization Circuit Design for IEEE 802.16d and 802.11a/g systems

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## Abstract

In this thesis, a multimode synchronization circuit is presented. It consists of frame detection, fractional carrier frequency offset estimation, and integral carrier frequency offset estimation and symbol boundary detection. In frame detection, a modified absolute value approximation circuit (AVAC) is provided. It improves accuracy 2~3 times the accuracy of traditional method. In fractional carrier frequency offset estimation, a modified CORDIC circuit is proposed. The hardware reduction is at least 46% comparing to conventional method. In integral carrier frequency offset estimation, a reduced match filter is used. System simulation has done in Matlab. The architecture has been implemented in Verilog. By synthesizing to UMC 0.18um CMOS standard cell technology library with Synopsys Design Compiler, the overall gate count is about 124k.

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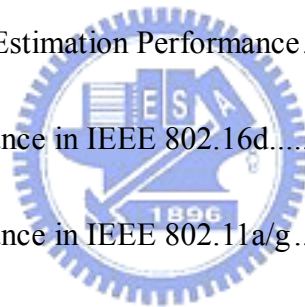
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# Chapter 1

## Introduction.

### 1.1. Motivation.

For the common human nature, there is an aspiration to have ability to communicate with people no matter where they are. In order to assuage the desire, people have developed several wired or wireless communication systems. Especially, wireless communication systems have been reached and developed enthusiastically. The institute of Electrical and Electronics Engineers (IEEE) has defined four different wireless standards. IEEE 802.11a/g standard is the widely used WLAN spec for now. The IEEE 802.11a/g system diagram is shown in Fig. 1.1. The major application of IEEE 802.11a/g is to provide a high data rate link in indoor environments, such as office buildings, library, coffee bar, etc. In many portable applications, IEEE 802.11a/g standard is adopted because of the need of internet access. In recent years, IEEE 802.16d standard has got a lot of interest for the sake of internet access anywhere. The IEEE 802.16d system diagram is shown in Fig. 1.2. IEEE 802.16d standard can make up the deficiency of IEEE 802.11a/g. If there is a portable device with these two standards, the device let people get internet information anywhere.



IEEE 802.11a/g and IEEE 802.16d have adopted OFDM as their key modulation scheme for high data rate transmissions. Because Synchronization is the most important functional block in OFDM systems, this thesis choose synchronization for IEEE 802.11a/g and IEEE 802.16d as research target.

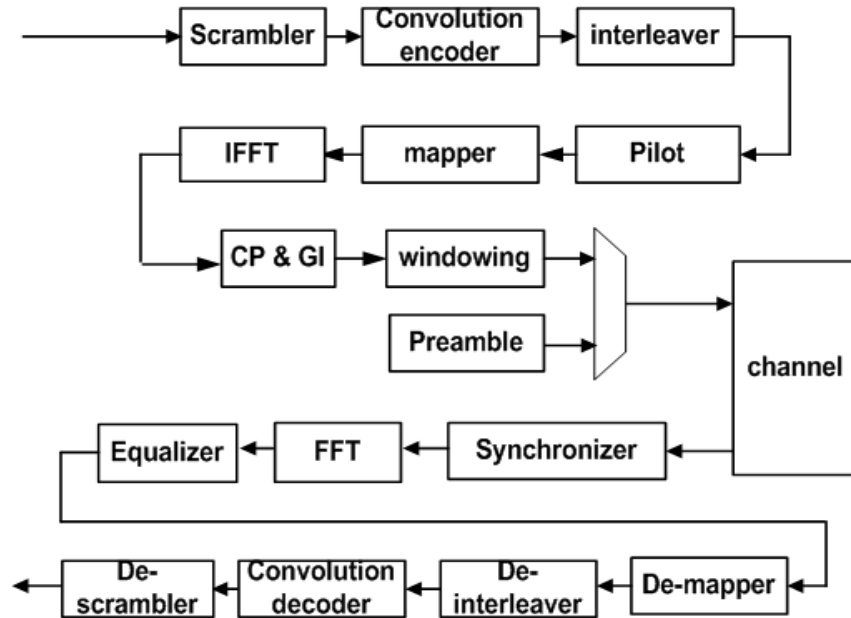


Figure 1.1 IEEE 802.11a/g system diagram

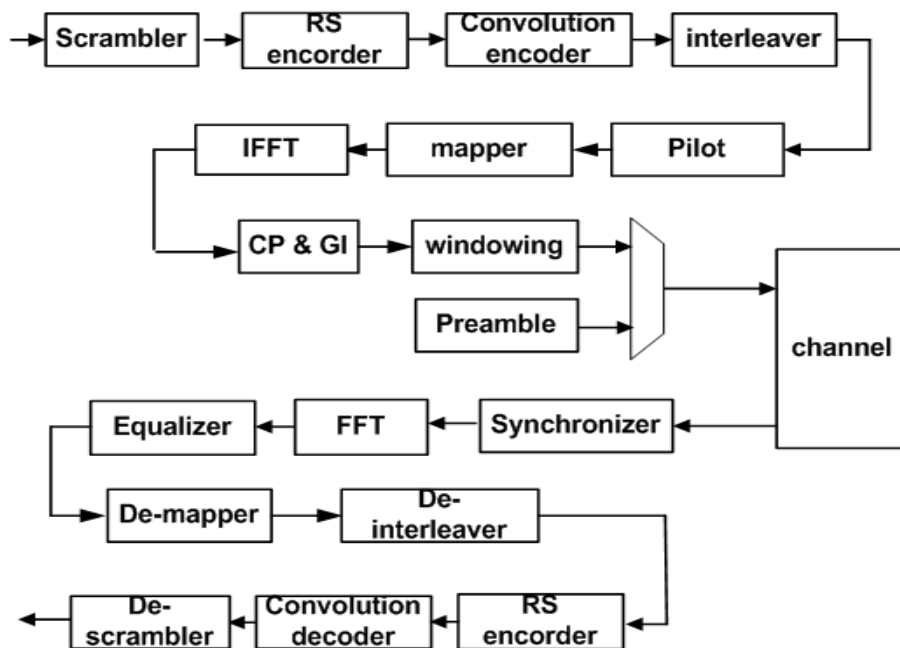
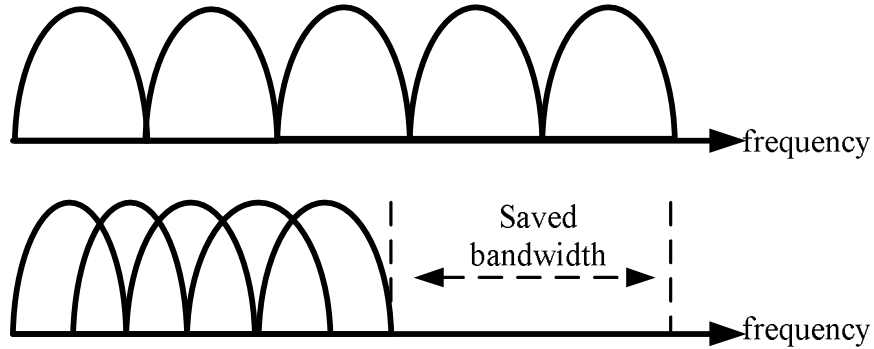


Figure 1.2 IEEE 802.16d system diagram

## 1.2. OFDM Basic.

Orthogonal frequency division multiplexing (OFDM) has been adopted in several standards such as IEEE 802.11a/g, IEEE 802.16d, HIPERLAN/2, DVB, DAB and so on. The main advantage of OFDM is its spectrum efficiency as depicted in Fig. 1.1



**Figure 1.3** Difference between OFDM system and traditional multicarrier system

OFDM systems can transmit a large number of data simultaneously via orthogonal subcarriers. By splitting high data-rate data stream into several low rate streams, OFDM systems have a larger symbol time and are more robust to timing errors. OFDM has many advantages such as better spectrum efficiency, better immunity against multipath effects and relaxed timing constraint. However, the main disadvantage of this technique is the sensitivity to carrier frequency offset (CFO). A small amount of CFO will cause loss of orthogonality and severely degrade system performance. The equivalent complex baseband OFDM symbol start at  $t=t_s$  can be written as [6]

$$x(t) = \sum_{k=-\frac{N_s}{2}}^{\frac{N_s}{2}-1} X_{k+\frac{N_s}{2}} \cdot e^{j2\pi\frac{k}{T}(t-t_s)} \cdot \Pi\left(\frac{t-t_s}{T}\right), t_s \leq t \leq t_s + T \quad (1.1)$$

$$x(t) = 0, t < t_s \text{ or } t > t_s + T$$

Where  $T$  is symbol duration,  $X_k$  is complex data symbol on  $k$ th subcarrier and the

pulse shaping filter is defined as

$$\Pi\left(\frac{t}{T}\right) = \begin{cases} 1, & \frac{-T}{2} \leq t \leq \frac{T}{2} \\ 0, & \text{otherwise} \end{cases} \quad (1.2)$$

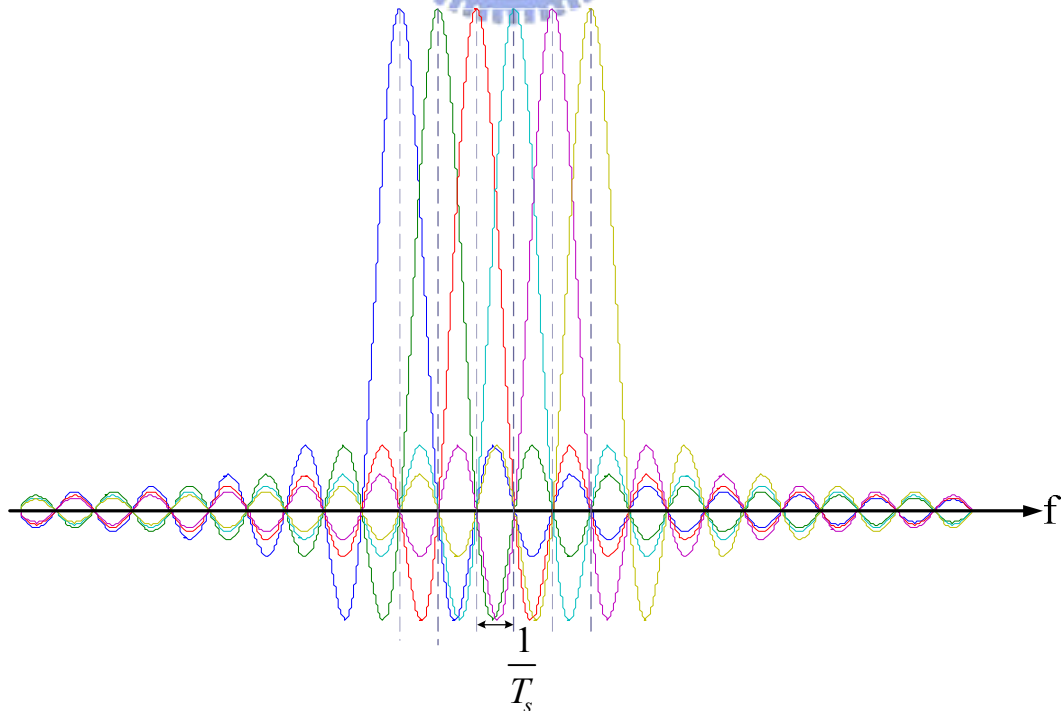
The orthogonality between subcarriers can be derived by integrating any two subcarriers within a symbol period

$$\int_{t=t_s}^{t_s+T} e^{j2\pi\frac{k}{T}(t-t_s)} e^{-j2\pi\frac{k'}{T}(t-t_s)} dt = \begin{cases} 1, & \text{for } k = k' \\ 0, & \text{for } k \neq k' \end{cases} \quad (1.3)$$

Because of the orthogonality, every OFDM data symbol can be demodulated by correlating with corresponding subcarrier.

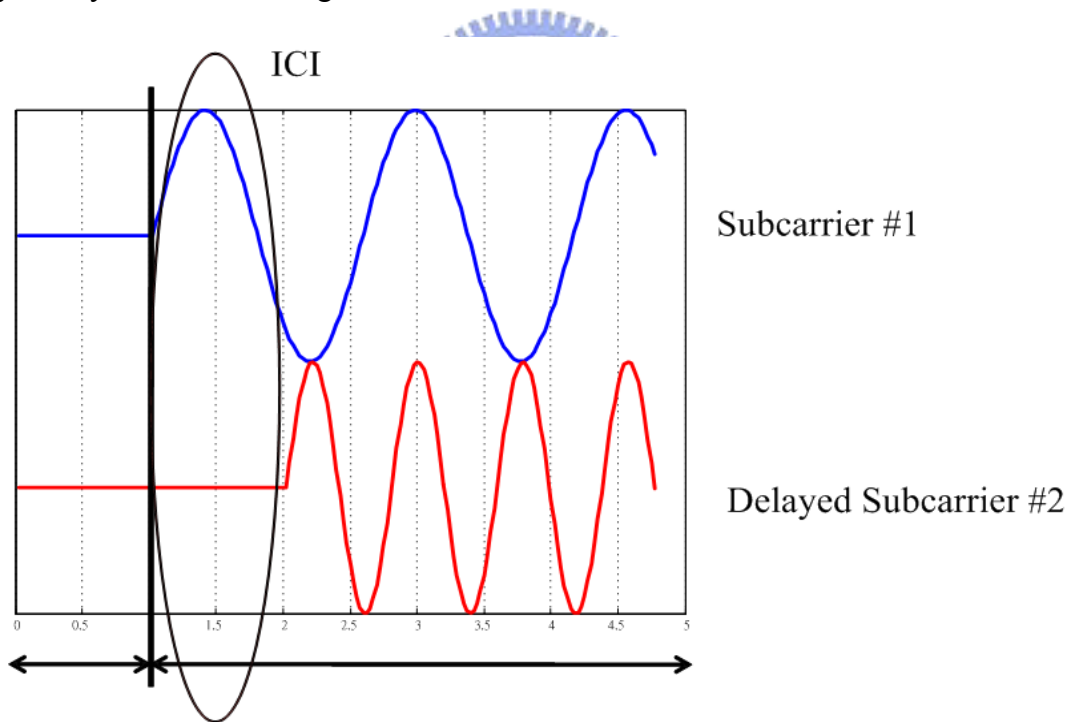
$$\begin{aligned} & \int_{t=t_s}^{t_s+T} x(t) \cdot e^{-j2\pi\frac{k}{T}(t-t_s)} dt, t_s \leq t \leq t_s + T \\ &= \sum_{k=-\frac{N_s}{2}}^{\frac{N_s}{2}-1} X_{k+\frac{N_s}{2}} \left( \int_{t=t_s}^{t_s+T} e^{j2\pi\frac{k-k'}{T}(t-t_s)} dt \right) = X_{k+\frac{N_s}{2}} \cdot N_s \end{aligned} \quad (1.4)$$

Thus, ideally each data symbol has no interfere from other data symbols.



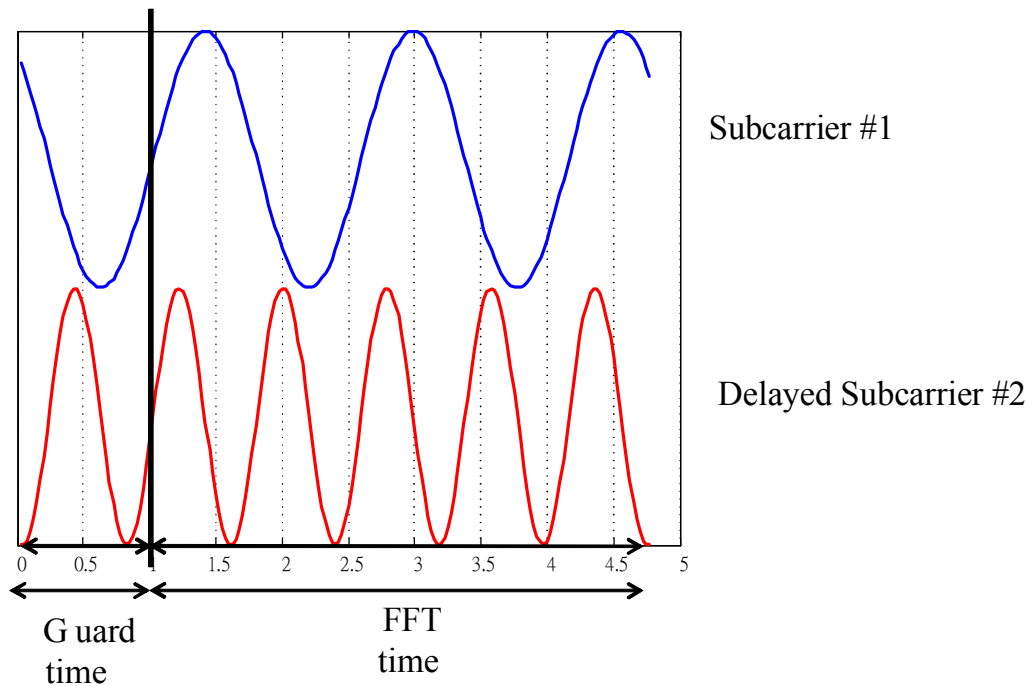
**Figure 1.4** Spectra of orthogonal subcarriers

Note that, from eq. (1.1), each subcarrier has an integer number of cycles in the interval  $T$ , and the number of cycles between adjacent subcarriers differs by exactly one. If there is no other impairment, each subcarrier is orthogonal and the spectral peak of each subcarrier will coincide with the zero crossing of all the other carriers as depicted in Fig. 1.2. Inter-symbol interference (ISI) will cause by convolution of transmitted signals and channel response. A guard time which is larger than the multipath delay spread is need for OFDM symbols. If guard time is zero padding as showed in Fig. 1.3 [13], there will be Inter-carrier interference (ICI) because of loss of orthogonality. In order to eliminate ICI, Fig. 1.4 shows that OFDM symbol is cyclically extended in the guard time.



**Figure 1.5** Effect of multipath with zero padding in the guard time





**Figure 1.6** OFDM symbol with cyclic extension

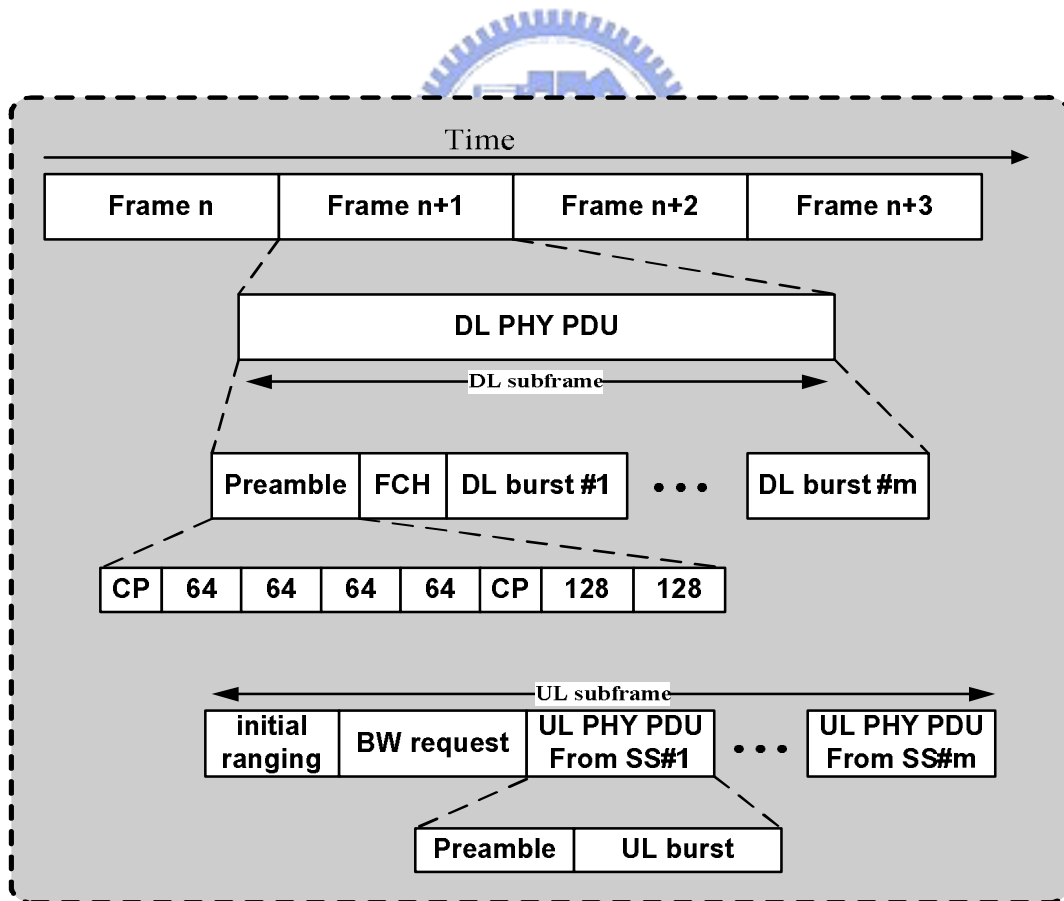
### 1.3 Overview of IEEE 802.16d System.

In IEEE 802.16d standard [1], the frame consists of a downlink subframe and an uplink subframe. According to different duplexing methods, there are two frame structures. Fig. 1.6 shows the FDD frame structure. The downlink PHY PDU starts with a long preamble. The preamble is followed by a FCH burst which specify burst profile and length of the one or several downlink bursts immediately following the FCH. After FCH, data bursts are transmitted.

The frequency domain sequences for preamble is derived from sequence  $PALL(-100:100) = \{1-j, 1-j, -1-j, 1+j, 1-j, 1-j, -1+j, 1-j, 1-j, 1-j, 1+j, -1-j, 1+j, 1+j, -1-j, 1+j, -1-j, -1-j, 1-j, -1+j, 1-j, 1-j, -1-j, 1+j, 1-j, 1-j, -1+j, 1-j, 1-j, 1-j, 1+j, -1-j, 1+j, 1+j, -1-j, 1+j, -1-j, -1-j, 1-j, -1+j, 1-j, 1-j, -1-j, 1+j, 1-j, 1-j, -1+j, 1-j, 1-j, 1-j, 1+j, -1-j, 1+j, 1+j, -1+j, 1+j, -1-j, -1-j, 1-j, -1+j, 1-j, 1-j, 1+j, -1-j, -1-j, -1-j, 1+j, -1-j, -1-j, -1-j, 1-j, 1-j, -1+j, 1-j, -1+j, 1-j, -1+j, -1+j, -1-j, 1+j, 0, -1-j, 1+j, -1+j, -1+j, -1-j, 1+j,$

$$\begin{aligned}
&1+j, 1+j, -1-j, 1+j, 1-j, 1-j, 1-j, -1+j, -1+j, -1+j, -1+j, 1-j, -1-j, -1-j, -1+j, 1-j, 1+j, 1+j, \\
&-1+j, 1-j, 1-j, 1-j, -1+j, 1-j, -1-j, -1-j, -1-j, 1+j, 1+j, 1+j, 1+j, -1-j, -1+j, -1+j, 1+j, -1-j, \\
&1-j, 1-j, 1+j, -1-j, -1-j, -1-j, 1+j, -1-j, -1+j, -1+j, -1+j, 1-j, 1-j, 1-j, 1-j, -1+j, 1+j, 1+j, \\
&-1-j, 1+j, -1+j, -1+j, -1-j, 1+j, 1+j, 1+j, -1-j, 1+j, 1-j, 1-j, 1-j, -1+j, -1+j, -1+j, 1-j, \\
&-1-j, -1-j, 1-j, -1+j, -1-j, -1-j, 1-j, -1+j, -1+j, -1+j, 1-j, -1+j, 1+j, 1+j, -1-j, -1-j, -1-j, \\
&-1-j, 1+j, 1-j, 1-j\} \tag{1.5}
\end{aligned}$$

The first preamble in the downlink PHY PDU consists of two consecutive OFDM symbols. The first OFDM symbol uses only subcarriers the indices of which are a multiple of four and the second OFDM symbol uses only even subcarriers. The resulting time domain structure of preamble is shown in Fig. 1.7



**Figure 1.7** IEEE 802.16d OFDM Frame structure with FDD

**Table 1.1** IEEE 802.16d system parameter list

NFFT	256
Nused	200
Bandwidth	BW
F <sub>s</sub>	Floor(n *BW/8000)*8000 (2~32 MHz)
Subcarrier spacing	F <sub>s</sub> /N <sub>F<sub>FT</sub></sub> (7.8125~125 KHz)
Sampling factor	8/7
G	1/4, 1/8, 1/16, 1/32
T <sub>b</sub>	1/subcarrier spacing
T <sub>g</sub>	G*T <sub>b</sub>
T <sub>s</sub>	T <sub>b</sub> +T <sub>g</sub> (31.25~500ns)
Number of lower frequency guard subcarriers	28
Number of higher frequency guard subcarriers	27

**Table 1.2** IEEE 802.16d available bandwidth list

BW		T <sub>b</sub>	T <sub>g</sub> =T <sub>b</sub> /32	T <sub>g</sub> =T <sub>b</sub> /16	T <sub>g</sub> =T <sub>b</sub> /8	T <sub>g</sub> =T <sub>b</sub> /4
n=8/7	1.75	128	4	8	16	32
	3.5	64	2	4	8	16
	7.0	32	1	2	4	8
	14.0	16	0.5	1	2	4
	28.0	8	0.25	0.5	1	2

## 1.4 Overview of IEEE 802.11a/g System.

Fig. 1.7 shows the PPDU frame format defined in IEEE 802.11a/g [2]. It includes the OFDM PLCP preamble, OFDM PLCP header, PSDU, tail bits, and pad bits. The PLCP preamble contains ten short symbols and two long symbols. A short OFDM training symbol consists of 12 subcarriers which are modulated by the elements of the sequence S, given by

$$S_{-26,26}(\sqrt{13/6})\{0,0,1+j,0,0,0,-1-j,0,0,0,1+j,0,0,0, \\ -1-j,0,0,0,-1-j,0,0,0,1+j,0,0,0,0,0,0,-1-j,0, \\ 0,0,-1-j,0,0,0,-1-j,0,0,0,1+j,0,0,1+j,0,0,1+j,0,0\}$$
(1.6)

A long symbol consists of 53 subcarriers which are modulated by the elements of the sequence L, given by

$$L_{-26,26} = \{1,1,-1,-1,1,1,-1,1,-1,1,1,1,1,1,-1,-1, \\ ,1,1,-1,1,-1,1,1,1,0,1,-1,-1,1,1,-1,1,-1,1,-1 \\ , -1,-1,-1,-1,1,1,-1,-1,1,-1,1,-1,1,1,1\}$$
(1.7)

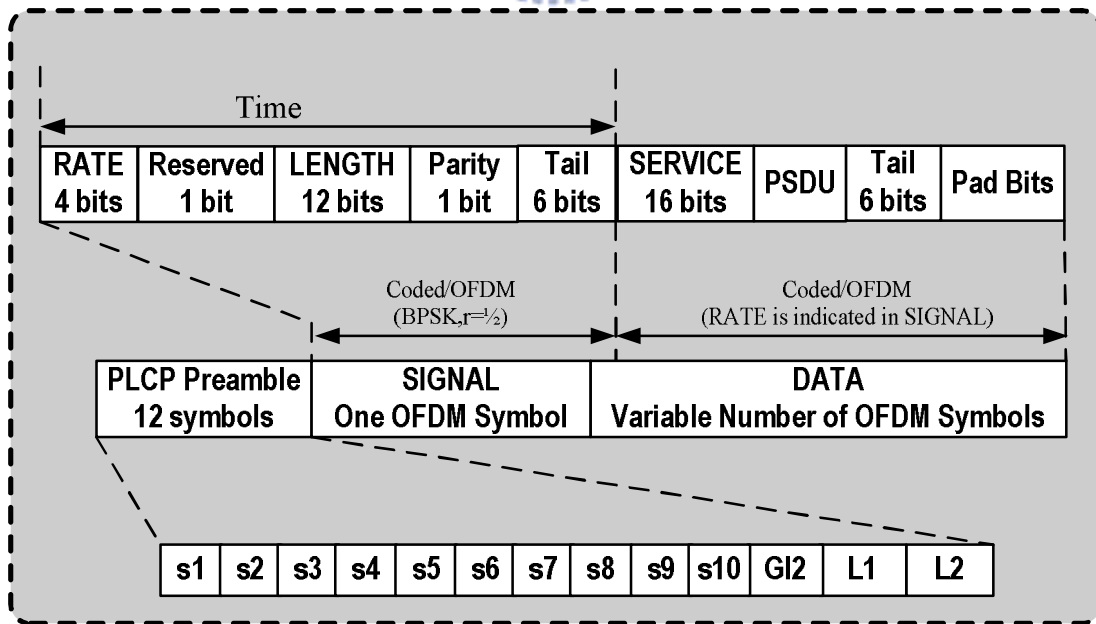


Figure 1.8 IEEE 802.11a/g OFDM Frame structure

From Table 3, eight different kinds of data rates from 6 up to 54 Mbps, Table 4 shows the timing related parameters and the reason why 802.11a/g has a maximum data rate of 54 Mbps is derived in eq. (1.8)

$$data\ rate = 6 \times 48 \times \frac{3}{4} \times 250k = 54Mbps \quad (1.8)$$

**Table 1.3** IEEE 802.11a/g rate-dependent parameters

Data rate (Mbits/s)	Modulation	Coding rate	Coded bits per subcarrier	Coded bits per OFDM symbol	Data bits per OFDM symbol
6	BPSK	1/2	1	48	24
9	BPSK	3/4	1	48	36
12	QPSK	1/2	2	96	48
18	QPSK	3/4	2	96	72
24	16 QAM	1/2	4	192	96
36	16 QAM	3/4	4	192	144
48	64 QAM	2/3	6	288	192
54	64 QAM	3/4	6	288	216

**Table 1.4** IEEE 802.11a/g Timing-related parameters

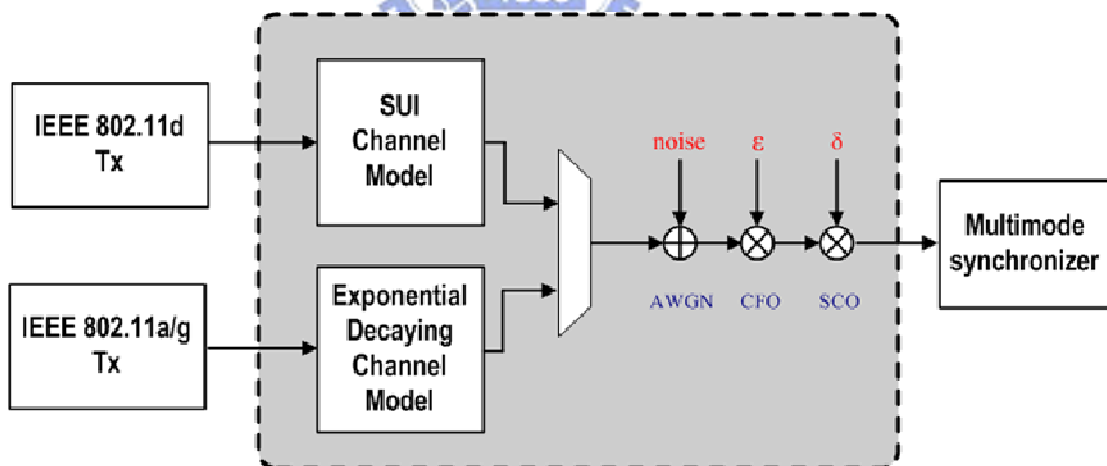
Parameter	Value
N <sub>SD</sub> : Number of data subcarriers	48
N <sub>SP</sub> : Number of pilot subcarriers	4
N <sub>ST</sub> : Number of subcarriers, total	52
Subcarrier spacing	0.3125MHz

$T_{\text{FFT}}$	3.2ms
$T_{\text{PREAMBLE}}$	16ms
$T_{\text{SIGNAL}}$	4ms
$T_{\text{GI}}$	0.8ms
$T_{\text{GI2}}$	1.6ms
$T_{\text{SYM}}$	4ms
$T_{\text{SHORT}}$	8ms
$T_{\text{LONG}}$	8ms

## 1.5 Channel Model

### 1.5.1 Simulation Channel

The simulation channel used is showed in Fig. 1.9 and three non-ideal effects are shown below.

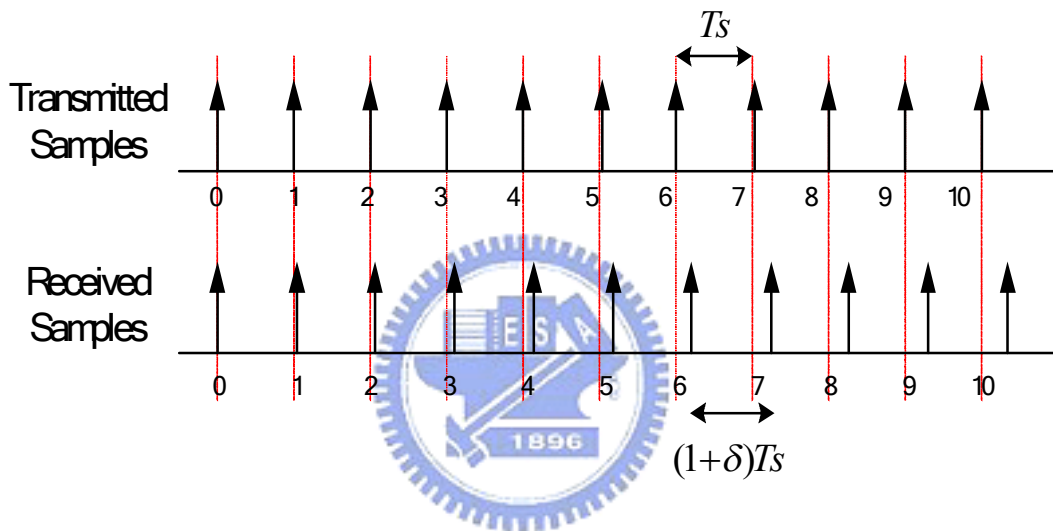


**Figure 1.9** Simulation channel diagram

In real implementation, the frequency difference between transmitter oscillator and receiver oscillator is impossible to be zero. This non-ideal effect will cause ICI and severely degrade system if no compensation process is used. Eq. 1.12 shows the CFO influence on transmitted data samples.

$$\begin{aligned}
r_n &= x_n e^{j(2\pi f_i nT)} e^{-j(2\pi f_r nT)} \\
&= x_n e^{j(2\pi(f_i - f_r)nT)} \\
&= x_n e^{j(2\pi(\Delta f)nT)}
\end{aligned} \tag{1.9}$$

where  $f_i$  and  $f_r$  are the frequencies of oscillator at transmitter and receiver respectively. SCO is caused by the mismatch between ADC/DAC sampling frequencies, as illustrated in Fig. 1.9.



**Figure 1.10** Mismatches between ADC/DAC sample frequencies.

Assume  $T_s$  is the transmitted sampling period,  $\delta$  is the sampling clock offset value, and  $(1+\delta)T_s$  is the received sampling period. In frequency domain, SCO enlarging or narrowing the spectrum in horizontal destroys the orthogonality in OFDM, thus induces ICI in OFDM systems. To simulate the non-ideal effect, received signal is interpolated by using a raised cosine filter.

$$h_{\text{interp}}(\tau) = \frac{\cos(\alpha(n+\tau))}{1 - (2\alpha(n+\tau)/\pi)^2} \text{sinc}(n+\tau) \times w(n+N), \quad n = -N/2, \dots, N/2 \tag{1.10}$$

Where  $\alpha$  is the roll off factor. Additional White Gaussian Noise (AWGN) is a complex

Gaussian random variable with zero mean and variance  $\sigma^2 = N_0/2$ , where  $N_0 = E_s / SNR$ , and  $E_s$  is defined as the average energy of one OFDM symbol.

## 1.5.2 SUI Channel model

In 802.16d system, a series of Stanford University Interim (SUI) channel selected for three terrain types [3]. These models are very suitable for fixed broadband wireless applications. According to the difference in terrain and tree density, the six SUI channels can be assort into three categories as showed in table 5.

**Table 1.5** Classification of SUI channel models

Model	Category
SUI5,SUI66	Hilly terrain with moderate-to-heavy tree densities
SUI3,SUI4	Hilly terrain with light tree densities
SUI1,SUI2	Flat terrain with light tree densities

In small scale fading, K-factor is a key parameter in defining the fading distribution. It is defined as the ratio of fixed-component power and the scatter-component power. A K-factor model is presented as follows

$$K = F_s F_h F_b K_o d^\gamma u \quad (1.11)$$

Where  $F_s$  is a seasonal factor,  $F_s=1$  in summer (leaves):2.5 in winter (no leaves)

$F_h$  is the receive antenna height factor,  $F_h = (h/3)^{0.46}$

$F_b$  is the beamwidth factor,  $F_b = (b/17)^{-0.62}$

$K_o$  and  $\gamma$  are regression coefficients,  $K_o=10$ ;  $\gamma=-0.5$

$u$  is a lognormal variable which has zero dB mean and standard deviation of 8 dB



If K-factor equal to zero, the multipath fading tap is Rayleigh distributed. On the other hand, multipath fading tap is Ricean distributed with nonzero K-factor. Table 6 shows a parameter list of SUI channels

**Table 1.6** SUI channel model parameters

Model	RMS delay (us)	Parameter	Tap1	Tap2	Tap3	K-factor
SUI-1	0.111	Delay(us)	0	0.4	0.9	[4 0 0]
		Power(dB)	0	-15	-20	
		Doppler Frequency (Hz)	0.4	0.3	0.5	
SUI-2	0.202	Delay(us)	0	0.4	1.1	2 0 0]
		Power(dB)	0	-12	-15	
		Doppler Frequency (Hz)	0.2	0.15	0.25	
SUI-3	0.264	Delay(us)	0	0.4	0.9	[1 0 0]
		Power(dB)	0	-5	-10	
		Doppler Frequency (Hz)	0.4	0.3	0.5	
SUI-4	1.257	Delay(us)	0	1.5	4	[0 0 0]
		Power(dB)	0	-4	-8	
		Doppler Frequency (Hz)	0.2	0.15	0.25	
SUI-5	2.842	Delay(us)	0	4	10	[0 0 0]
		Power(dB)	0	-5	-10	
		Doppler Frequency (Hz)	2	1.5	2.5	
SUI-6	5.240	Delay(us)	0	14	20	[0 0 0]
		Power(dB)	0	-10	-14	
		Doppler Frequency (Hz)	0.4	0.3	0.5	

The multipath fading taps generated from table 6 have a white spectrum since they are independent of each other. Considering the Doppler Effect, these taps should pass Doppler filter with power spectral density defined as follows:

$$S(f) = \begin{cases} 1 - 1.72f_0^2 + 0.785f_0^4, & |f_0| \leq 1 \\ 0, & |f_0| > 1 \end{cases} \quad \text{where } f_0 = \frac{f}{f_m} \quad (1.12)$$

After passing through the Doppler filter, a normalized factor needs to apply to these multipath fading taps. In order not to change the total power of transmitted signal, the total power of the Doppler filter has to be normalized to one. Table 7 shows the normalization factor of each SU channel model. Finally with the knowledge of Tap delay and system bandwidth, the channel impulse response can be generated.

**Table 1.7** Normalization factor list

SUI Channel Models	Normalization Factor (dB)
SUI-1	-0.1771
SUI-2	-0.3930
SUI-3	-1.5113
SUI-4	-1.9218
SUI-5	-1.5113
SUI-6	-0.5683

### 1.5.3 Exponentially decaying Channel Model

The channel model used is recommended by IEEE 802.11a/g standard specification.

Eq. 1.11 shows the channel impulse response.

$$h_k = N(0, \frac{1}{2}\sigma_k^2) + jN(0, \frac{1}{2}\sigma_k^2)$$

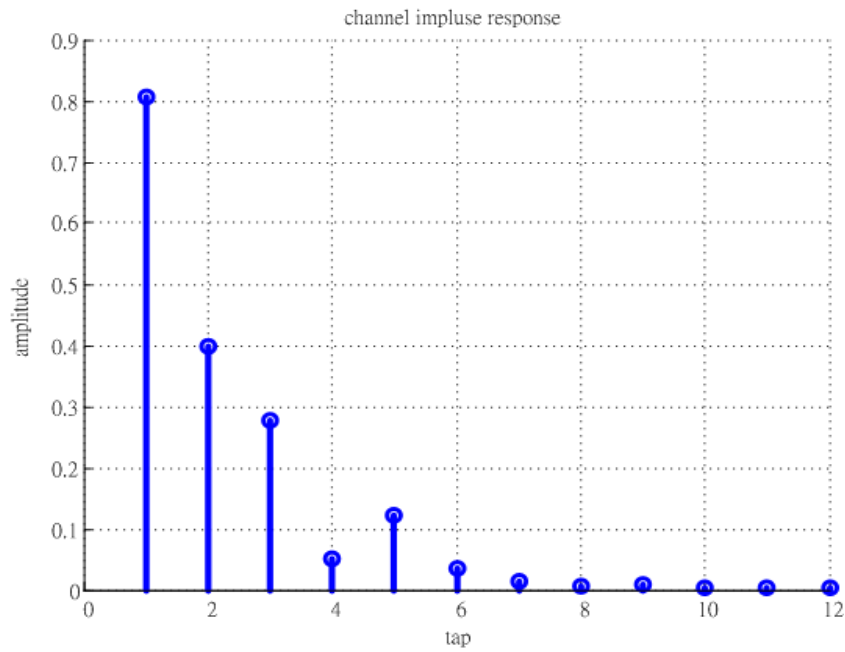
$$\sigma_0^2 = 1 - e^{-T_s/\tau_{RMS}}$$

$$\sigma_k^2 = \sigma_0^2 e^{-kT_s/\tau_{RMS}}$$
(1.13)

Where  $N(0, \frac{1}{2}\sigma_k^2)$  is a zero mean Gaussian random variable with variance  $\frac{1}{2}\sigma_k^2$

and  $\sigma_0^2 = 1 - e^{-T_s/\tau_{RMS}}$  is chosen such that  $\sum_{k=0}^L \sigma_k^2 = 1$  is satisfied the constant average

received power. Fig. 1.8 shows the amplitude response of the recommended model.



**Figure 1.11** Cir of the exponential decaying model with rms delay spread 50ns

# Chapter2

## Multimode Synchronization Architecture Design



### 2.1 Synchronization Scheme

Basically, a synchronization block consists of three tasks: Frame detection: finding a data frame. CFO estimation and compensation: correcting CFO effect. Symbol boundary detection: selecting a correct FFT window. According to the different bandwidth and different frequency offset tolerance, the CFO estimation function block is different from each other. The estimation range of conventional method [] is two times subcarrier spacing. Table 2.1 shows the frequency difference between IEEE 802.16d and IEEE 802.11a/g. In IEEE 802.11a/g, the maximum carrier offset is derived in eq. (2.1) and the CFO estimation range is derived in eq. (2.2).

$$500(\text{MHz}) \times (20 + 20) (\text{ppm}) = 200(\text{KHz}) \quad (2.1)$$

$$2 \times \frac{1}{50(ns) \times 64} = 625(KHz) \quad (2.2)$$

From eq. (2.1) and (2.2), the CFO estimation range is larger than the maximum carrier offset and so the conventional method is suitable for IEEE 802.11a/g. However, In IEEE 802.16d, the maximum carrier offset is derived in eq. (2.3) and the minimum CFO estimation range is derived in eq. (2.4).

$$10.68(MHz) \times (8 + 8) (ppm) = 170.88(KHz) \quad (2.3)$$

$$2 \times \frac{1}{250(ns) \times 256} = 31.25(KHz) \quad (2.4)$$

**Table 2.1** Frequency offset analysis

	802.16d				802.11a/g
BW	3.5	7.0	14.0	28.0	20
n	8/7				1
Ts(ns)	250	125	62.5	31.25	50
$\Delta f(KHz)$	15.625	31.25	62.5	125	312.5
Fractional estimation range(KHz)	$\pm 31.25$	$\pm 62.5$	$\pm 125$	$\pm 320$	$\pm 625$
Center frequency tolerance (ppm)	$\pm 8$				$\pm 20$
Carrier frequency(GHz)	10.68				5
Maximum carrier offset(KHz)	$\pm 170.888$				$\pm 200$

From eq. (2.3) and (2.4), the CFO estimation range is smaller than the maximum carrier offset and there will be another frequency offset estimation in IEEE 802.16d.

## 2.2 Synchronization Architecture for IEEE 802.11a/g System

In 802.11a/g system, two structures can be used to accomplish synchronization as shown in Fig. 2.1 and Fig. 2.2. In Fig. 2.1, received data is processed by symbol boundary detection, and then correct its frequency offset [4]. Symbol boundary detection block can be done before the CFO estimation block because of the real value long preamble. However, received data corrects its frequency offset, and then finds out the symbol boundary in Fig. 2.2 [5].

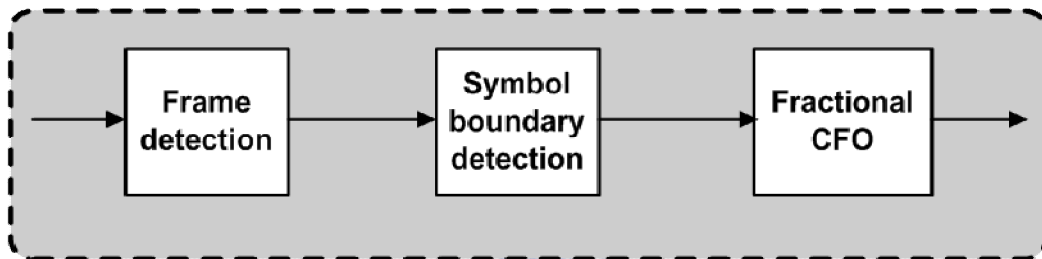


Figure 2.1 IEEE 802.11a/g synchronization architecture 1

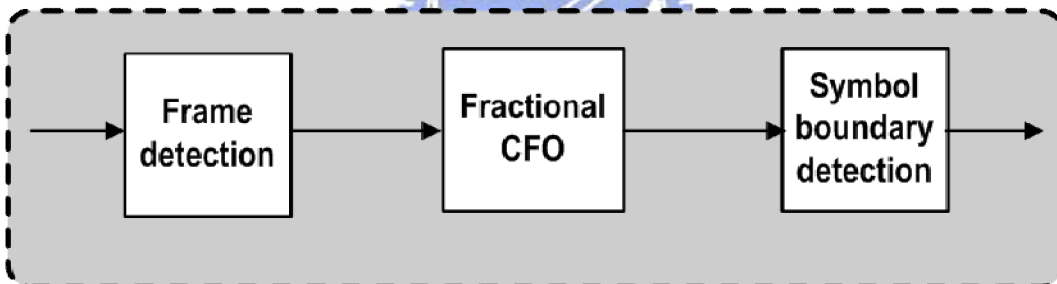
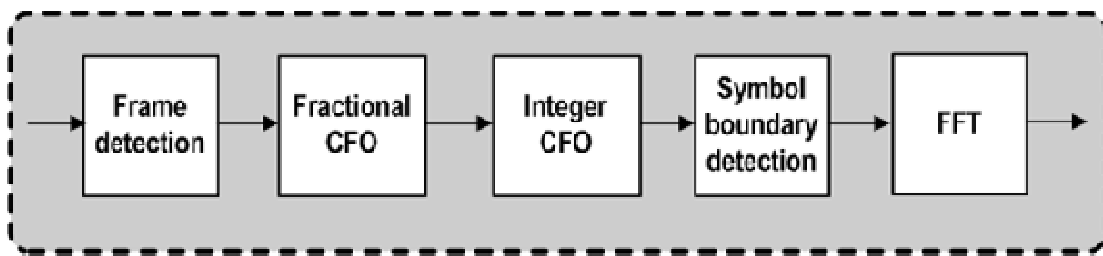


Figure 2.2 IEEE 802.11a/g synchronization architecture 2

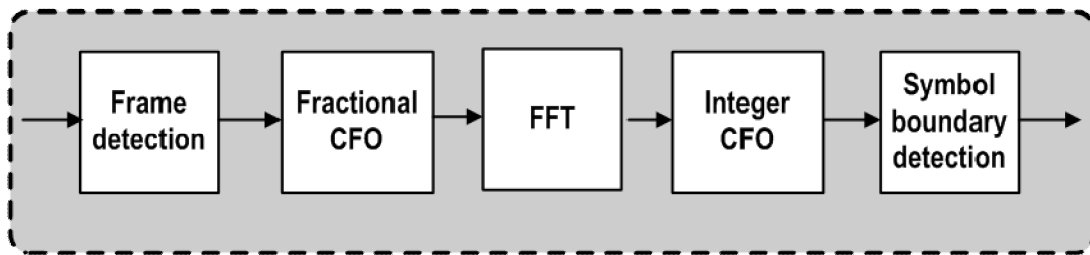
## 2.3 Synchronization Architecture for IEEE 802.16d System

In IEEE 802.16d system, there are also two architectures. The two architectures shown in Fig. 2.3 and Fig. 2.4 are like the architecture in Fig. 2.2. The symbol timing can't be acquired before the two frequency correction blocks because of complex value long preamble. So the synchronization is done by correcting system frequency offset, and then finding out the symbol boundary. The difference between these two

architectures is at the last two functional blocks. Architecture shown in Fig. 2.3 uses time domain operation of integral CFO estimation and time domain operation of symbol boundary detection [11]. Architecture shown in Fig. 2.4 utilizes frequency domain operation of integral CFO estimation and frequency domain operation of symbol boundary detection [12]. Frequency domain operation of integral CFO estimation cost more hardware than time domain operation because of several complex multiplications. Moreover, frequency domain operation of symbol boundary detection is also more complex because it needs another FFT block to translate channel frequency response to channel impulse response.



**Figure 2.3** IEEE 802.16d synchronization architecture 1

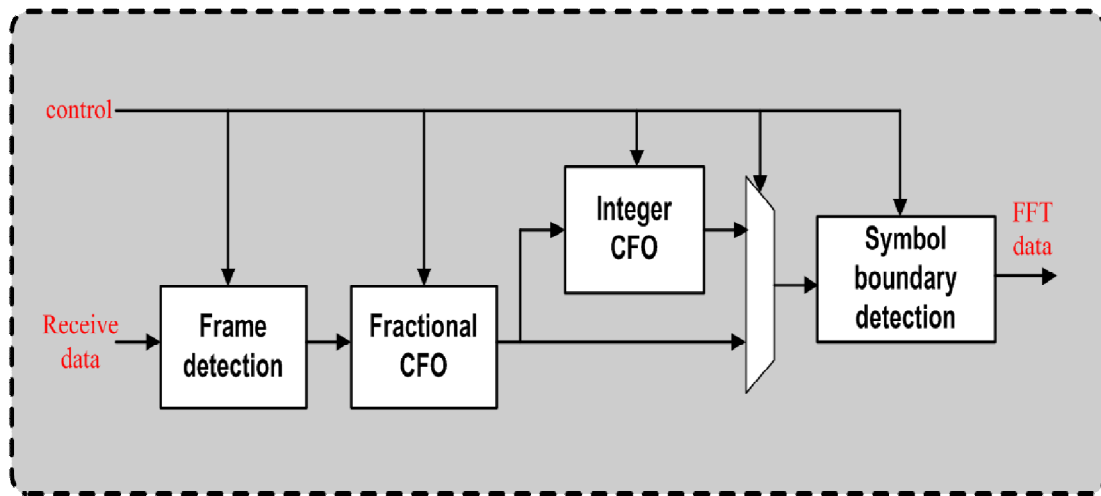


**Figure 2.4** IEEE 802.16d synchronization architecture 2

## 2.4 Proposed Multimode Synchronization Architecture

Multimode synchronization architecture is proposed as shown in Fig. 2.5. the architecture 2 in Fig. 2.2 and architecture 1 in Fig. 2.3 is combined. The integral CFO block is overhead in IEEE 802.11a/g mode. In order to balance the hardware cost of

these standards, the proposed multimode synchronization architecture has a low complexity integral CFO block.



**Figure 2.5** Proposed multimode synchronization architecture



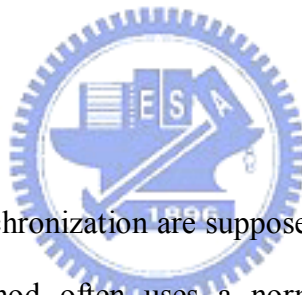


# Chapter3

## Circuit Design for Multimode Synchronization Blocks

### 3.1 Frame Detection

#### 3.1.1 Algorithm

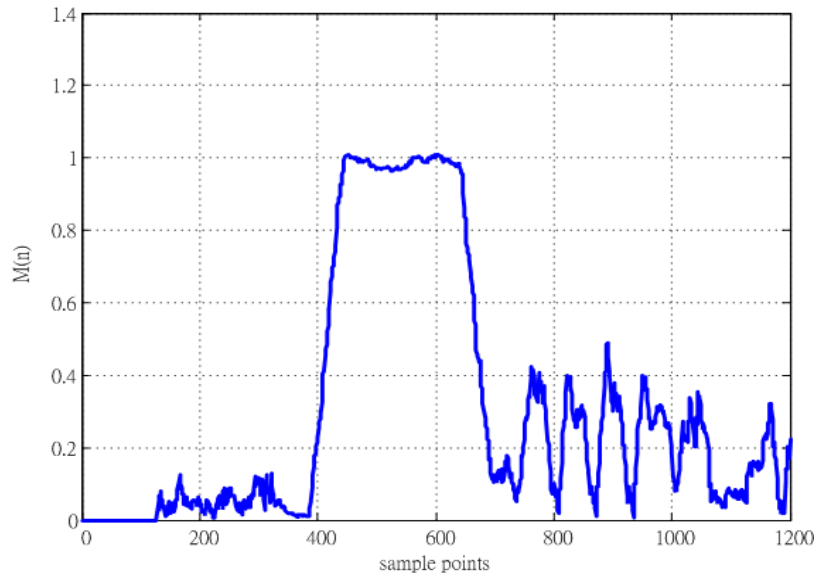


The AGC and clock synchronization are supposed to be performed before frame detection. Conventional method often uses a normalized autocorrelation with a predefined threshold to detect the incoming frame [14]. Normalized autocorrelation is shown in eq. 3.1 to eq. 3.3 where  $r(n)$  are received data samples and  $D$  is delay between two sequence and  $L$  is the accumulating window length. The advantage of Conventional method is more robust to multipath fading channel. Fig. 3.1 shows the normalized autocorrelation diagram .

$$M(n) = \frac{|C(n)|^2}{P(n)} \quad (3.1)$$

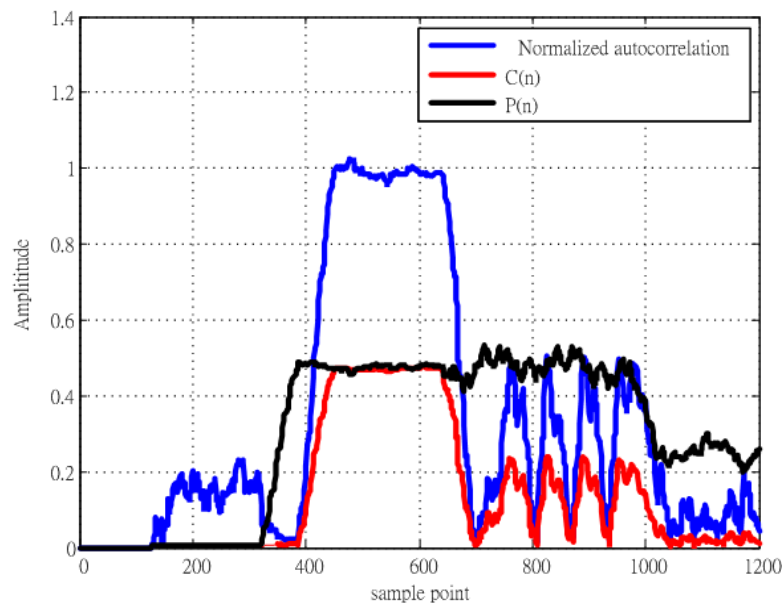
$$C(n) = \sum_{i=0}^{L-1} r_{n+i} r_{n+i+D}^* \quad (3.2)$$

$$P(n) = \sum_{i=0}^{L-1} |r_{n+i+D}|^2 \quad (3.3)$$



**Figure 3.1** Normalized autocorrelation diagram

The hardware complexity of normalized autocorrelation is high because of the division. However, a modified frame detection algorithm is proposed. The correlation term and power term shown in eq. 3.2 and eq.3.3 are calculated in step 1. The delay ( $D$ ) is 64 for IEEE 802.16d and 16 for IEEE 802.11a/g. The accumulating window length ( $L$ ) is 64 for these two standards. Fig. 3.2 shows the Correlation diagram.



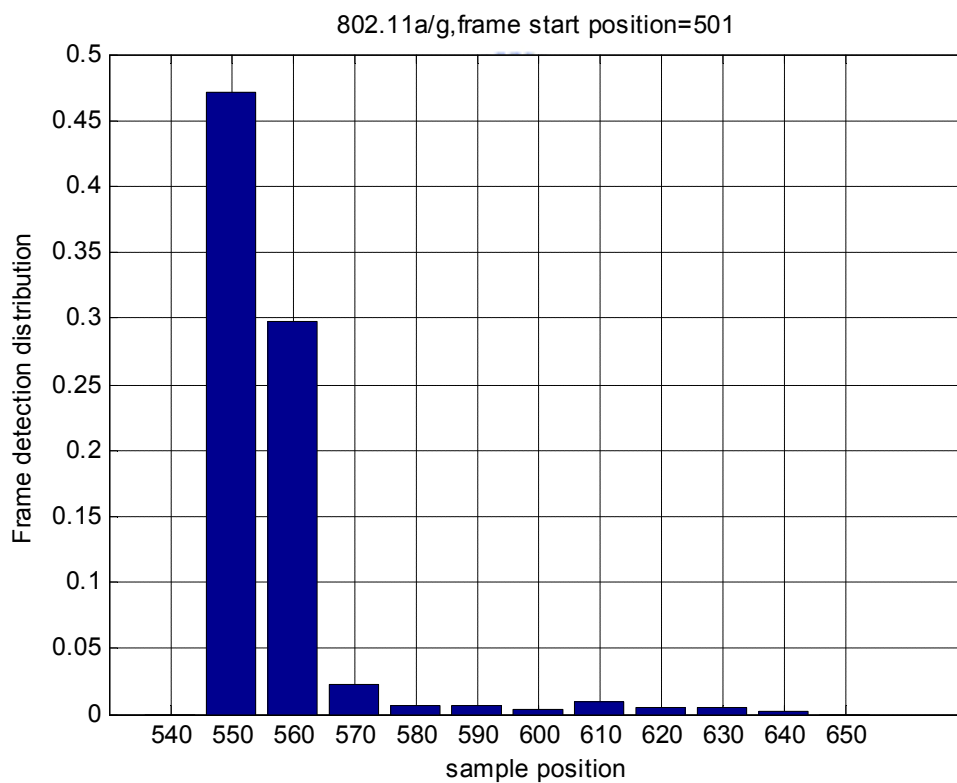
**Figure 3.2** Correlation diagram

We can see that the amplitude of correlation in eq. 3.2 will be influenced by multipath fading channel. If a fixed threshold is used to detect the frames, the position that indicates where the frame starts will vary for a large range. In step 2, eq. 3.4 is used to find out whether a frame is coming or not.

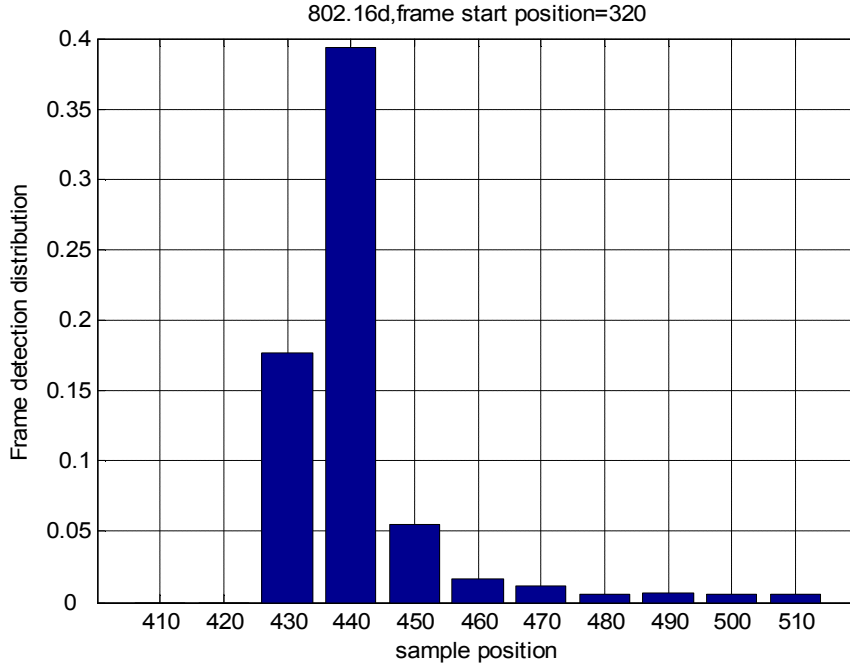
$$n_{frame} = \arg \min_n [|c(n)| > \max(P(n')) \times 0.8]$$

where  $n' \leq n$  (3.4)

By comparing the correlation term and power term, the detection will be robust to multipath path fading. Fig. 3.3 and Fig. 3.4 show the frame detection distribution diagrams in IEEE 802.11a/g and IEEE 802,16d respectively.

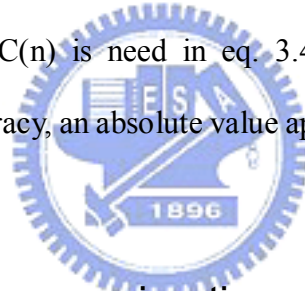


**Figure 3.3** Frame detection distribution in IEEE 802.11a/g



**Figure 3.4** Frame detection distribution in IEEE 802.16d

Note that absolute value of  $C(n)$  is needed in eq. 3.4. In order to reduce hardware complexity and maintain accuracy, an absolute value approximation circuit is proposed.



### 3.1.2 Absolute value approximation circuit

The absolute value of a complex number  $(I+jQ)$  is shown in eq. 3.6 and an absolute value approximation is shown in eq. 3.7. By comparing these two eq.s, we can find out the approximation error as shown in eq. 3.8

$$a = \max(|I|, |Q|), b = \min(|I|, |Q|) \quad (3.5)$$

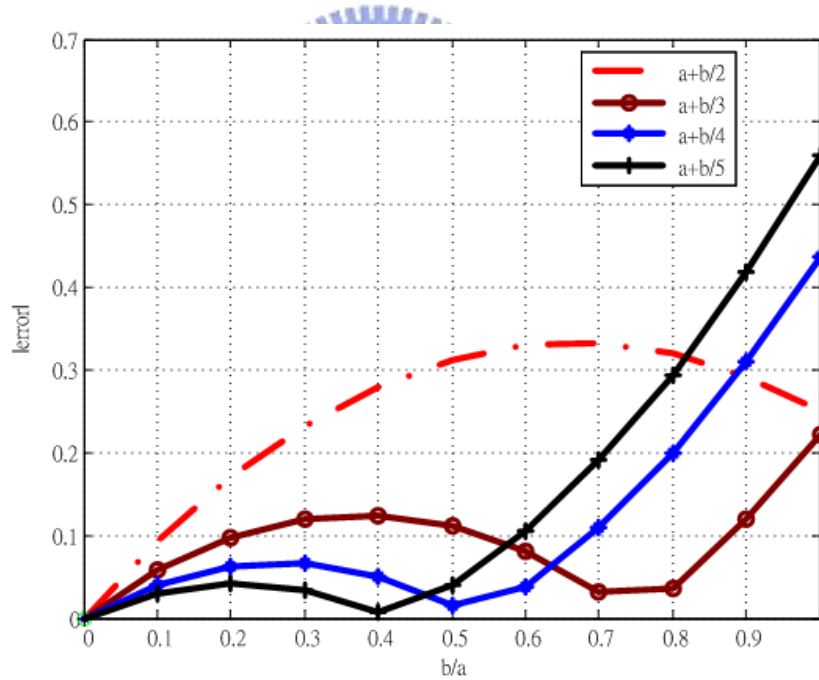
$$|a + bj| = \sqrt{a^2 + b^2} = \sqrt{a^2(1 + \frac{b^2}{a^2})} = a\sqrt{1 + (\frac{b^2}{a^2})} \quad (3.6)$$

$$a + \frac{b}{index} = a\sqrt{1 + 2\sqrt{\frac{b^2}{(index)^2 a^2}} + \frac{b^2}{(index)^2 a^2}} \quad (3.7)$$

$$error\_index = \frac{b^2}{a^2} - \left( 2\sqrt{\frac{b^2}{(index)^2 a^2}} + \frac{b^2}{(index)^2 a^2} \right) \quad (3.8)$$

By investigating the index from 2 to 5, we can get the approximation error functions in eq. 3.9. The approximation error plot as a function of b/a is shown in Fig. 3.5.

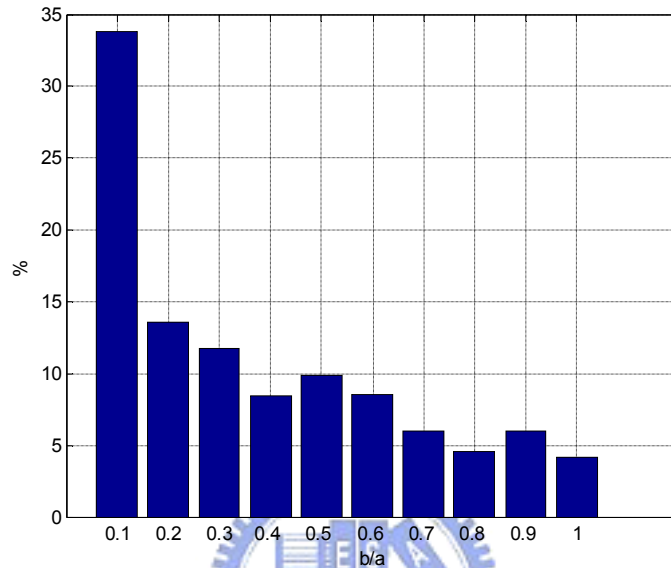
$$\begin{aligned} error2 &= \frac{b^2}{a^2} - \left( 2\sqrt{\frac{b^2}{2^2 a^2}} + \frac{b^2}{2^2 a^2} \right) \\ error3 &= \frac{b^2}{a^2} - \left( 2\sqrt{\frac{b^2}{3^2 a^2}} + \frac{b^2}{3^2 a^2} \right) \\ error4 &= \frac{b^2}{a^2} - \left( 2\sqrt{\frac{b^2}{4^2 a^2}} + \frac{b^2}{4^2 a^2} \right) \\ error5 &= \frac{b^2}{a^2} - \left( 2\sqrt{\frac{b^2}{5^2 a^2}} + \frac{b^2}{5^2 a^2} \right) \end{aligned} \quad (3.9)$$



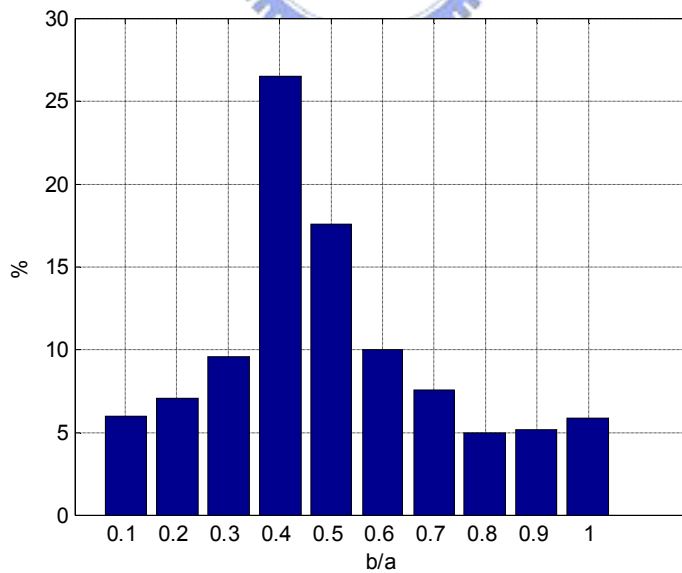
**Figure 3.5** Approximation error plots

By system simulation, the distribution of b/a can be found for IEEE 802.16d and IEEE 802.11a/g. Fig. 3.6 and Fig. 3.7 shows the distribution for these two standards. The product of error value and distribution in Fig. 3.6 and 3.7 is used to estimate approximation performance. Table 3.1 and Table 3.2 show the approximation

performance for IEEE 802.16d and IEEE 802.11a/g respectively. From table 3.1 and table 3.2 , the best approximation is  $a+b/4$  in both standards. The approximation accuracy is 2~3 times the accuracy of  $a+b/2$  [10].



**Figure 3.6** Distribution of IEEE 802.11a/g



**Figure 3.7** Distribution of IEEE 802.16d

Table 3.1 Approximation performance of IEEE 802.11a/g

802.11a/g	
	error*distribution
a+b/2	22.6873
a+b/3	9.5150
a+b/4	9.1302
a+b/5	10.6549

Table 3.2 Approximation performance of IEEE 802.16d

802.16d	
	error*distribution
a+b/2	23.9383
a+b/3	9.4477
a+b/4	7.3156
a+b/5	7.7097

### 3.1.3 Multimode Circuit Design for Frame Detection

The multimode circuit for frame detection is shown in Fig. 3.8. First of all, the autocorrelation circuit is implemented in an iterative form. The circuit only uses one complex multiplier and two complex adders. The proposed AVAC circuit follows the autocorrelation circuit. The  $n''$  is used to indicate incoming frames. The  $Max\_c$  is the maximum that is used to estimate CFO.

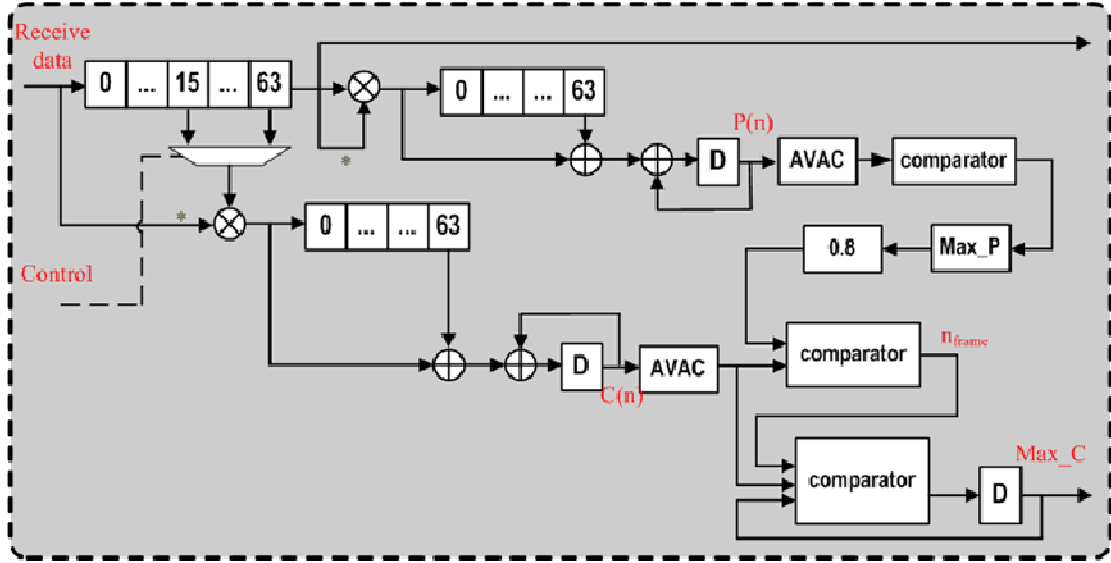
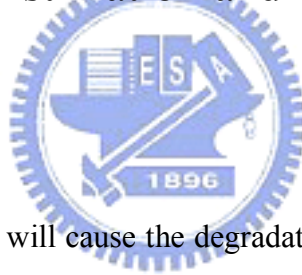


Figure 3.8 Multimode frame detection circuit

## 3.2 Fractional CFO Estimation and Compensation

### 3.2.1 Algorithm



Inter-Carrier Interference will cause the degradation of system performance. The degradation in SNR was approximated by eq. 3.10 [15].

$$SNR_{Loss} = \frac{10}{3 \ln 10} (\pi T \Delta f)^2 \frac{E_s}{N_0} \quad (3.10)$$

where  $\Delta f$  is the frequency offset as a fraction of the subcarrier spacing and  $T$  is the sampling period.. Thus, the carrier frequency offset needs to be compensated before the received data go through FFT. The received data are expressed as

$$r(n) = s(n)e^{-\frac{j2\pi n\varepsilon}{N}} + w(n), \varepsilon = \varepsilon_f + \varepsilon_i \quad (3.11)$$

Where  $s(n)$  are transmitted data and  $w(n)$  are AWGN noise and  $\varepsilon_f$  is fractional CFO and  $\varepsilon_i$  is integral CFO. A simple algorithm shown in eq. 3.12 can be used to estimate fractional CFO [5]. The CFO compensation show in eq. 3.13 can be done by rotating the received data with its corresponding angle.



$$\varepsilon_f = \frac{-N}{2\pi D} \angle \max(c(n)) = \frac{-N}{2\pi D} \angle \max\left(\sum_{i=0}^{L-1} r_{n+i} r_{n+i+D}^*\right) \quad (3.12)$$

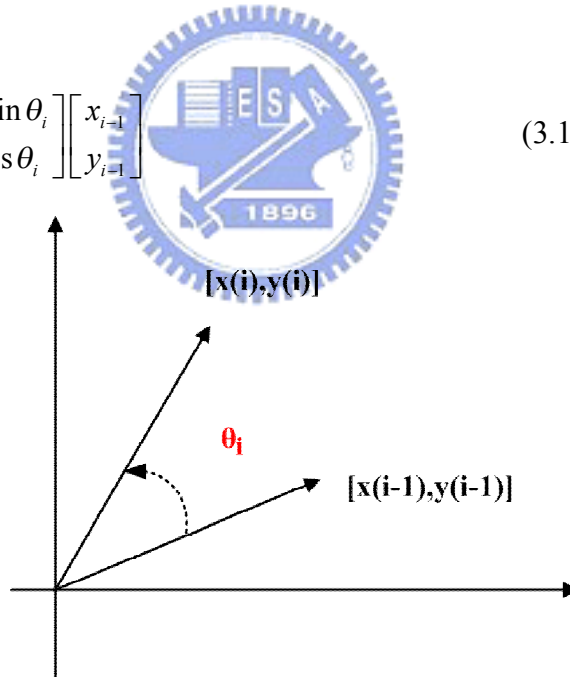
$$r(n)' = r(n) e^{\frac{j2\pi n \varepsilon_f}{N}} \quad (3.13)$$

The common used hardware implementation of fraction CFO estimation uses a CORDIC circuit. The hardware implementation of fraction CFO compensation uses a look-up table (LUT) with a complex multiplier. However, one modified CORDIC circuit is used for both CFO estimation and CFO compensation.

### 3.2.2 CORDIC Cell Circuit Design

The rotation of a vector  $[x_{i-1}, y_{i-1}]$  with angle  $\theta_i$  is shown in Fig. 3.9. The CORDIC is based on the rotation matrix in eq. 3.14. The equation can be modified as shown in eq. 3.15.

$$\begin{bmatrix} x_i \\ y_i \end{bmatrix} = \begin{bmatrix} \cos \theta_i & -\sin \theta_i \\ \sin \theta_i & \cos \theta_i \end{bmatrix} \begin{bmatrix} x_{i-1} \\ y_{i-1} \end{bmatrix} \quad (3.14)$$



**Figure 3.9** Rotation in Cartesian coordinate system

$$\begin{bmatrix} x_i \\ y_i \end{bmatrix} = \frac{1}{\sqrt{1 + \tan^2 \theta_i}} \begin{bmatrix} 1 & -\tan \theta_i \\ \tan \theta_i & 1 \end{bmatrix} \begin{bmatrix} x_{i-1} \\ y_{i-1} \end{bmatrix} \quad (3.15)$$

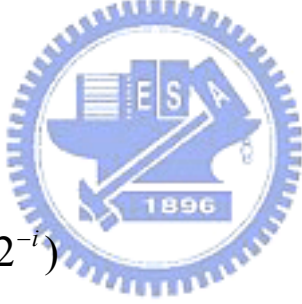
By using the simplification in eq. 3.16, a reduced form of eq. 3.15 is shown in eq. 3.17.

$$\tan \theta_i = 2^{-i} \quad (3.16)$$

$$\begin{bmatrix} x_i \\ y_i \end{bmatrix} = \frac{1}{\sqrt{1+2^{-2i}}} \begin{bmatrix} 1 & -2^{-i} \\ 2^{-i} & 1 \end{bmatrix} \begin{bmatrix} x_{i-1} \\ y_{i-1} \end{bmatrix} \quad (3.17)$$

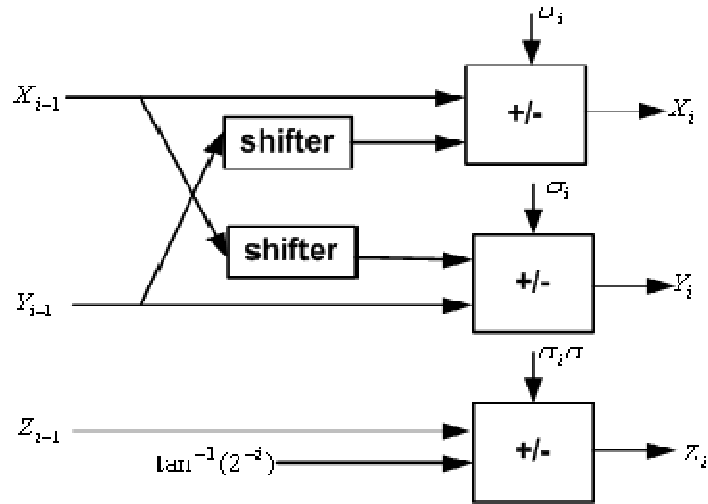
Based on eq. 3.17, the equation used for fractional CFO estimation is shown in eq. 3.18 and the compensation equation is shown in eq. 3.19 where  $z_{i-1}$  is the angle of vector  $[x_{i-1}, y_{i-1}]$ .

$$\begin{aligned} x_i &= x_{i-1} - \sigma_i 2^{-i} y_{i-1} \\ y_i &= y_{i-1} + \sigma_i 2^{-i} x_{i-1} \\ z_i &= z_{i-1} - \sigma_i \tan^{-1}(2^{-i}) \\ \sigma_i &= \begin{cases} -1, & y_{i-1} \geq 0 \\ 1, & y_{i-1} < 0 \end{cases} \end{aligned} \quad (3.18)$$

$$\begin{aligned} x_i &= x_{i-1} - \sigma_i 2^{-i} y_{i-1} \\ y_i &= y_{i-1} + \sigma_i 2^{-i} x_{i-1} \\ z_i &= z_{i-1} + \sigma_i \tan^{-1}(2^{-i}) \\ \sigma_i &= \begin{cases} -1, & z_{i-1} \geq 0 \\ 1, & z_{i-1} < 0 \end{cases} \end{aligned} \quad (3.19)$$


In order to combine the two equations above, a parameter  $\sigma$  is added and a CORDIC cell with estimation and compensation is shown in eq. 3.20. Fig. 3.10 shows the CORDIC cell circuit diagram.

$$\begin{aligned} x_i &= x_{i-1} - (\sigma_i) 2^{-i} y_{i-1} \\ y_i &= y_{i-1} + (\sigma_i) 2^{-i} x_{i-1} \\ z_i &= z_{i-1} - (\sigma_i \sigma) \tan^{-1}(2^{-i}) \\ \sigma_i &= \begin{cases} -1, & y_{i-1} \text{ or } z_{i-1} \geq 0 \\ 1, & y_{i-1} \text{ or } z_{i-1} < 0 \end{cases}, \sigma = \begin{cases} 1, & \text{estimation} \\ -1, & \text{compensation} \end{cases} \end{aligned} \quad (3.20)$$



**Figure 3.10** Modified CORDIC cell

### 3.2.3 Angle Consideration of Estimation

At CFO estimation, the angle of a detected vector needs to be found. The possible range of the angle is from  $-\pi$  to  $\pi$ . However, the estimation angle can be reduced to  $\pi/2$  by a mirror step. Thus, the estimation angle must be larger than  $\pi/2$ . The estimation angle depends on two factors: number of stages and sequence of elementary rotations. The number of stage is ten because CFO estimation needs high accuracy. The rule that must obey in deciding sequence of elementary rotations is shown in eq. 3.21.

$$\tan^{-1}(2^{-i}) < (\tan^{-1}(2^{-i+1}) + \tan^{-1}(2^{-i+2}) + \dots) \quad (3.21)$$

Under this constraint, Table 3.3 gives the optimum sequence of elementary rotations.

Table 3.3 Sequence of elementary rotations for estimation

stage	arctan
i=0	<b>0.7854</b>
i=1	<b>0.4636</b>
i=2	<b>0.2450</b>
i=3	<b>0.1244</b>
i=4	<b>0.0624</b>

i=5	<b>0.0312</b>
i=6	<b>0.0156</b>
i=7	<b>0.0078</b>
i=8	<b>0.0039</b>
i=9	<b>0.0020</b>
	<b>1.7413</b>

### 3.2.4 Angle Consideration of Compensation

The constraint of compensation is that rotation angle must be larger than  $\pi$  because the angle of vector is possible in the range of  $-\pi$  to  $\pi$ . The sequence of elementary rotations must be modified under the constraint shown in eq. 3.21. The rotation angle can be larger if the number of  $i=0$  increases. Table 4 show a sequence of elementary rotations which angle is larger than  $\pi$ .

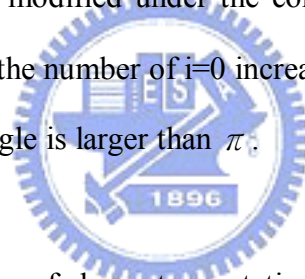


Table 3.4 Sequence of elementary rotations for compensation

stage	arctan
i=0	<b>0.7854</b>
i=0	<b>0.7854</b>
i=0	<b>0.7854</b>
i=1	<b>0.4636</b>
i=2	<b>0.2450</b>
i=3	<b>0.1244</b>
i=4	<b>0.0624</b>
i=5	<b>0.0312</b>
i=6	<b>0.0156</b>
i=7	<b>0.0078</b>
	<b>3.3063</b>

While the compensation accuracy of the sequence in table 3.4 is only 0.0078, the accuracy reduction will also result system performance degradation. In order to improve compensation without increasing hardware, a sequence of elementary rotation is proposed in table 3.5

Table 3.5 Proposed sequence of elementary rotations for compensation

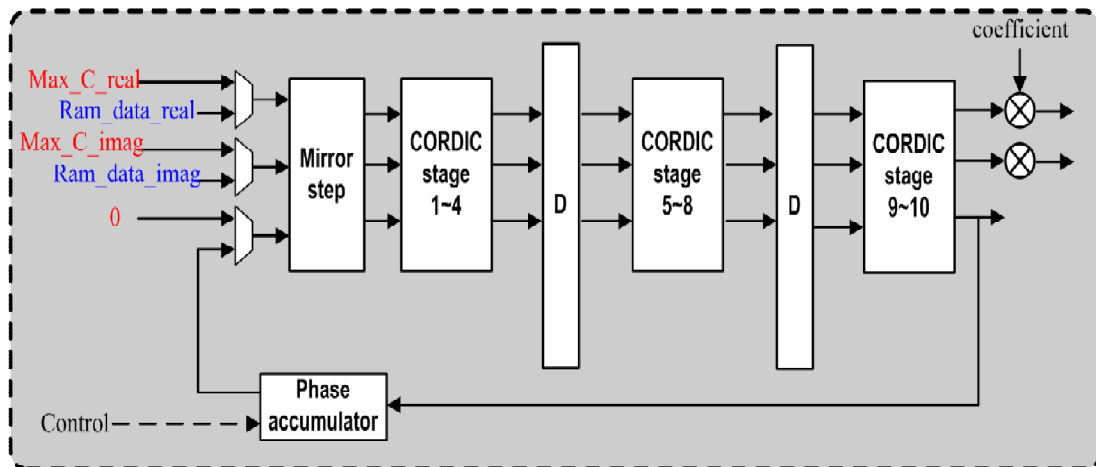
stage	arctan
i=-3	<b>1.4464</b>
i=0	<b>0.7854</b>
i=1	<b>0.4636</b>
i=2	<b>0.2450</b>
i=3	<b>0.1244</b>
i=4	<b>0.0624</b>
i=5	<b>0.0312</b>
i=6	<b>0.0156</b>
i=7	<b>0.0078</b>
i=8	<b>0.0039</b>
	<b>3.1858</b>

### 3.2.5 Multimode Circuit Design for Fractional CFO

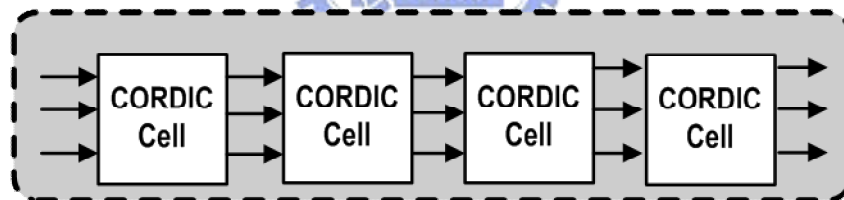
#### Estimation and Compensation

A CORDIC based fractional CFO estimation and compensation circuit is shown in Fig. 3.11 and Fig. 3.12 shows the cascaded CORDIC stage. Considering the system clock constraint, the ten CORDIC stages is divided into three pipeline stages. First of all, the Max\_c signal from frame detection goes through the ten CORDIC stages which are working in estimation mode. The initial angle used in estimation is zero. After

finishing the estimation, the received data from RAM is passing into ten CORDIC stages which are working in compensation mode. At this time, the initial angle is the output of phase accumulator. The phase accumulator is adjusted by the control signal which is different in different standards.



**Figure 3.11** CORDIC based fractional CFO estimation and compensation circuit



**Figure 3.12** Cascaded CORDIC stage

### 3.3 Integral CFO Estimation

#### 3.3.1 Algorithm

The received data after fractional CFO compensation is shown in eq. 3.22. The maximum of integral CFO will be different in different standards. In IEEE 802.16d the Integral CFO is restricted in the range of -12 subcarrier spacing to 12 subcarrier

spacing.

$$r(n)' = s(n)e^{\frac{j2\pi\varepsilon_i n}{N}}, \varepsilon \in \{\dots, -12, -8, -4, 0, 4, 8, 12, \dots\} \quad (3.22)$$

The algorithm used to estimate Integral CFO is shown in eq. 3.23 [11]

$$\varepsilon_i = \max(M1, M2, M3, M4, M5, M6, M7) \quad (3.23)$$

$$M1 = \sum_{k=1}^{64} r(n+k)' p_1(k), \dots, M7 = \sum_{k=1}^{64} r(n+k)' p_7(k)$$

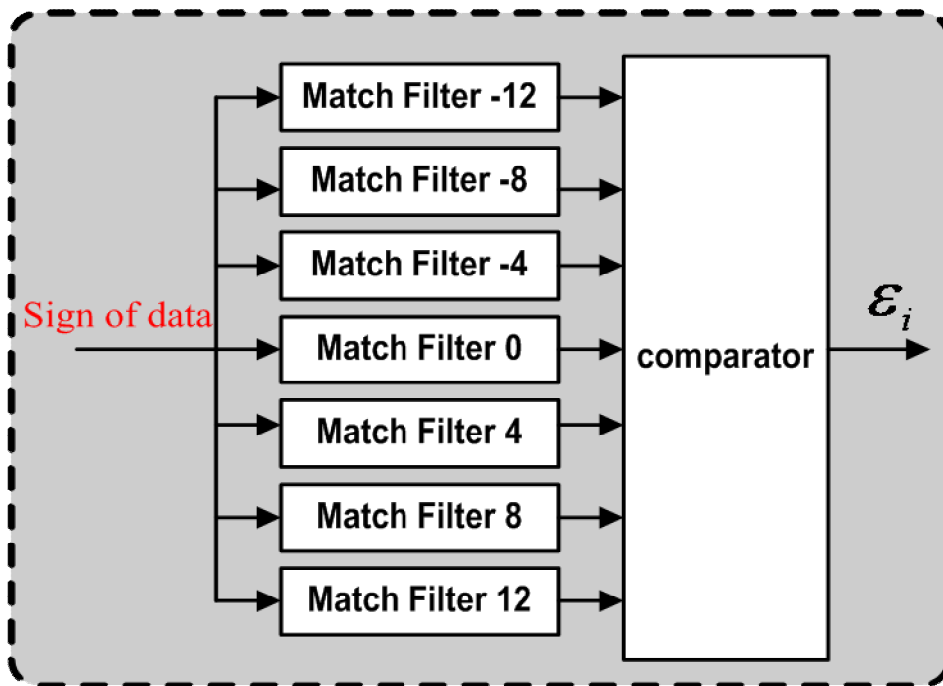
Where p1, p2, p3, p4, p5, p6, p7 are a first 64 data samples of long preamble with different integral CFO. The p1 sequence has been influenced by integral CFO of -12 times of subcarrier spacing. The p2 sequence has been influenced by integral CFO of -8 times of subcarrier spacing. The p3 sequence has been influenced by integral CFO of -4 times of subcarrier spacing. The p4 sequence has not been influenced by integral CFO. The p5 sequence has been influenced by integral CFO of 4 times of subcarrier spacing. The p6 sequence has been influenced by integral CFO of 8 times of subcarrier spacing. The p7 sequence has been influenced by integral CFO of 12 times of subcarrier spacing.

### 3.3.2 Circuit Design for Integral CFO Estimation

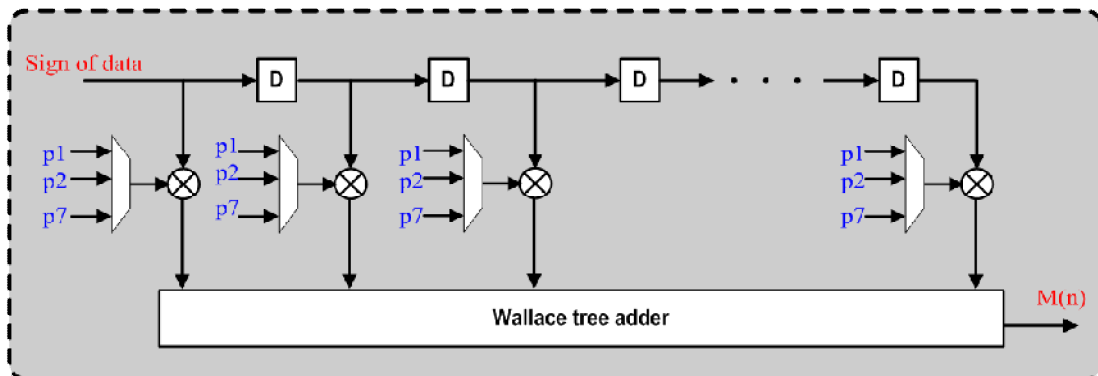
A match filter based integral CFO estimation is shown in Fig. 3.13. The sign of each received data is used for the sake of complexity reduction. The match filter circuit is shown in Fig. 3.14 and the reduced multiplier is shown in Fig. 3.15. the function of gate level selection is shown in table 3.6

**Table 3.6** Gate level selection

selection	Condition
0	Real_data = Real_p    Imag_data=Imag_p
1	Imag_data= real_p    Real_data=imag_p
2	Real_data = ~real_p    Imag_data=~imag_p
3	Imag_data = ~real_p    Real_data =imag_p



**Figure 3.13** Integral CFO Estimation circuit



**Figure 3.14** Match Filter circuit



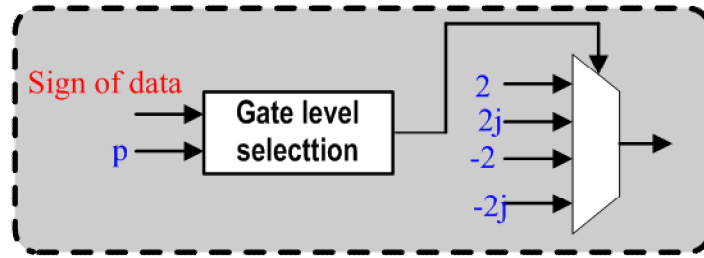


Figure 3.15 Reduced multiplier

### 3.4 Symbol boundary Detection

#### 3.4.1 Algorithm

The purpose of symbol boundary detection is to find the ISI-free window for each symbol. A modified symbol boundary detection algorithm is proposed. The conventional cross correlation method shown in eq. 3.24 is used in step 1.

$$M_{SBD}(n) = \sum_{k=1}^{64} r''(n+k)p^*(k) \quad (3.24)$$

Where p sequence are the first 64 points of long preamble and r'' are data samples after frequency correction. If the method in step 1 is used without any adjustment, the symbol boundary detection is possible to find the ISI window rather than ISI-free window. Fig. 3.16 shows the ISI effect caused by wrong symbol boundary detection when the signal in path 2 has maximum power.

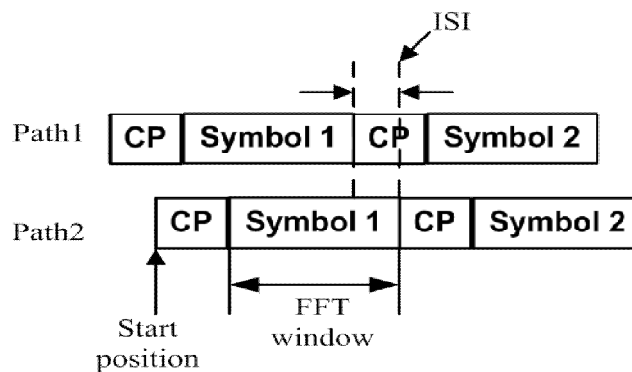


Figure 3.16 Multipath effect on symbol boundary detection

In step 2, eq. 3.25 and eq. 3.26 express where the reference symbol boundary is. The response of  $M_{SBD}(n)$  and  $MM_{SBD}(n)$  is shown in Fig. 3.17 [7]

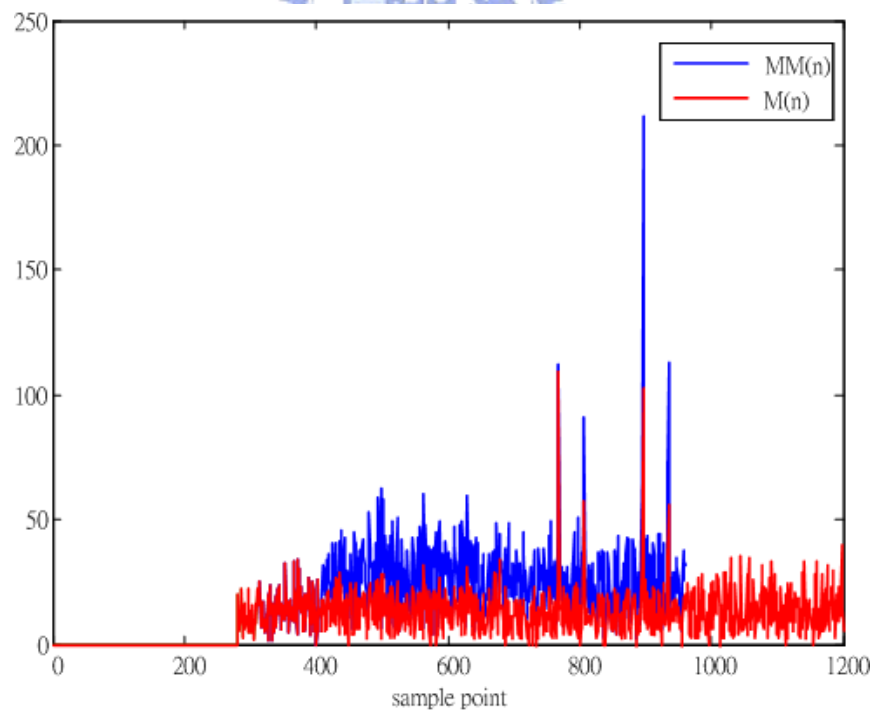
$$MM_{SBD}(n) = M_{SBD}(n) + M_{SBD}(n + D) \quad (3.25)$$

$$n_{ref} = \arg \max_n [MM_{SBD}(n)] \quad (3.26)$$

The delay (D) is 128 for IEEE 802.16d and 64 for IEEE 802.11a/g. Eq. 3.27 is used to find out the correct symbol boundary detection if the signal with largest power is not on path 1. It searches the ten data samples in front of the reference symbol boundary and finds the data sample that is larger than a half of  $\max(M_{SBD})$  with minimum timing index.

$$n_{SBD} = \arg \min_{n'} [M_{SBD}(n') > \frac{\max(M_{SBD})}{2}] \quad (3.27)$$

$$n' \subset [n \mid n_{ref} - 10 \leq n \leq n_{ref}]$$



**Figure 3.17** Response of  $M_{SBD}(n)$  and  $MM_{SBD}(n)$

### 3.4.2 Multimode Circuit Design for Symbol Boundary Detection

The multimode circuit for symbol boundary is shown in Fig. 3.18. If the MM\_MAX is updated, the FFT position functional block will update simultaneously. The correct FFT data will be passed to the next stage when the counter\_SBD reaches the predefined value.

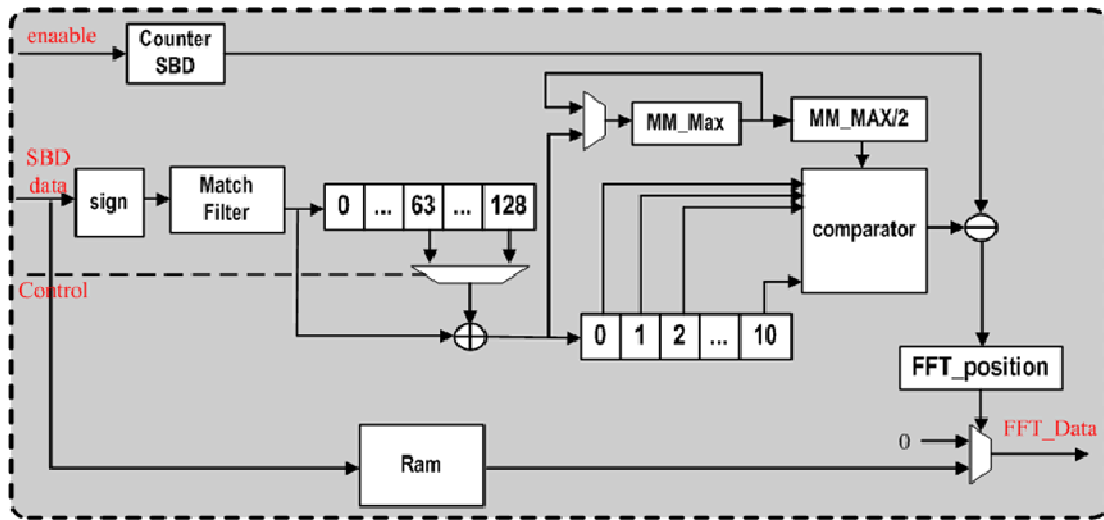


Figure 3.18 Multimode circuit design for symbol boundary detection

# Chapter4

## Simulation and FPGA Emulation

### 4.1 Simulation Result and Performance Analysis

#### 4.1.1 Simulation Setup

Fig. 4.1 shows the simulation setup for this section. The hardware we proposed will be substituted the ideal synchronization. The multipath channel presented in section 1.5 generates SUI channel impulse response and exponentially decaying channel impulse response, respectively. During the simulation, there is an assumption that AGC has been processed.

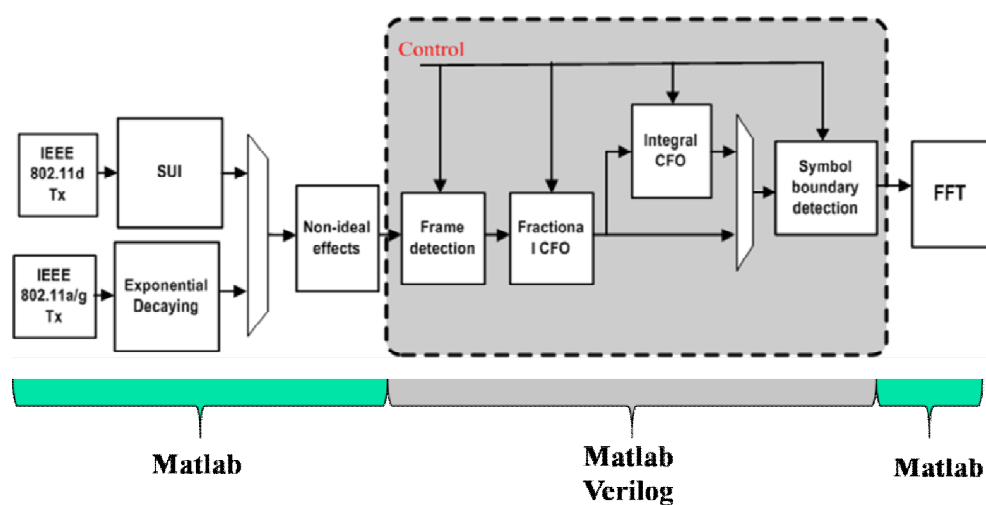
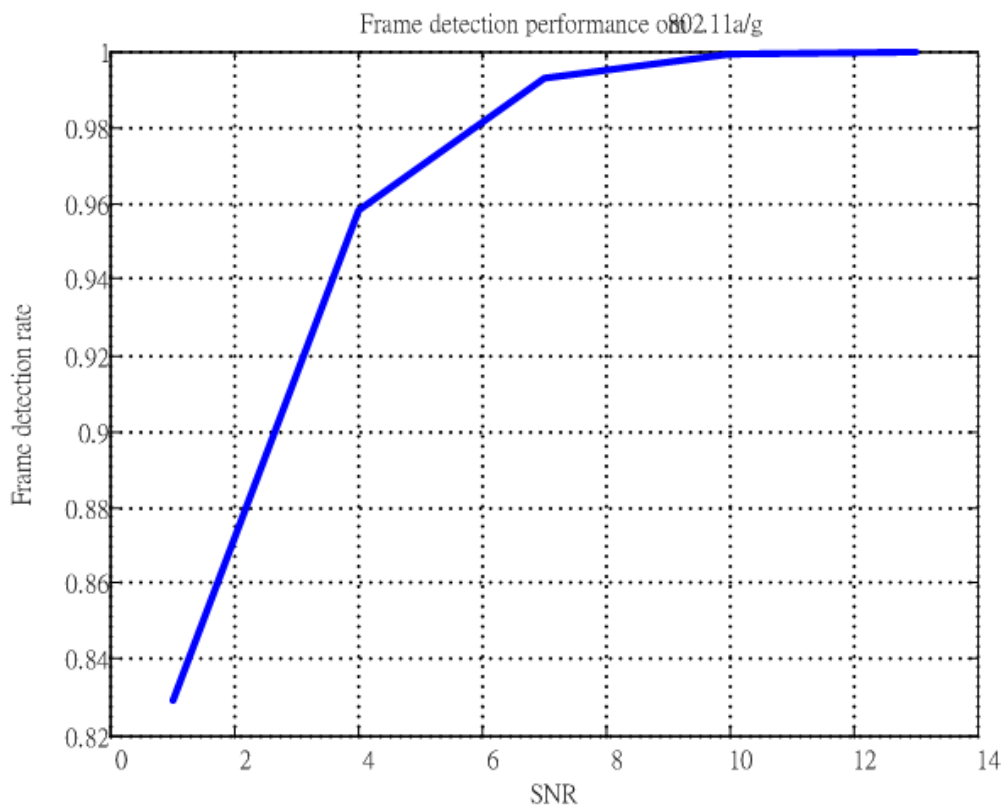


Figure 4.1 Simulation setup

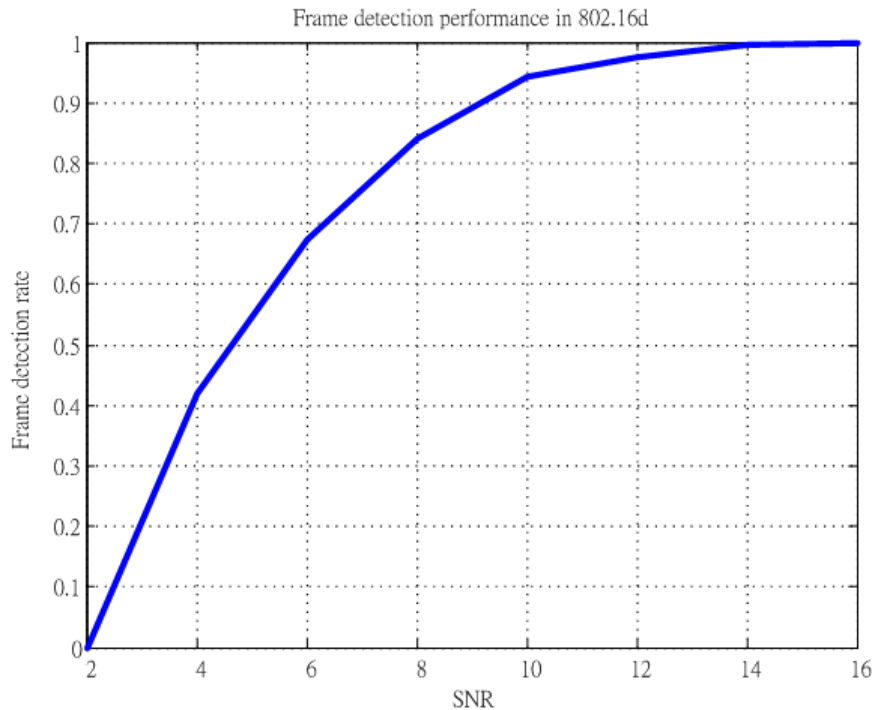
## 4.1.2 Frame Detection Performance

Fig. 4.2 shows the frame detection performance in IEEE 802.11a/g. The simulation condition is under transmitting 1000 packets and multipath channel with rms delay spread 50 ns. The suitable frame detection rate must be larger than 90% because the system PER must be lower than 10%. Thus, the SNR of suitable frame detection rate is about 2.5 dB.



**Figure 4.2** Frame detection performance in 802.11a/g

Fig. 4.3 shows the frame detection performance in IEEE 802.16d. The simulation condition is under transmitting 1000 frames, SUI-3 multipath channel, qpsk modulation and bandwidth is 7 MHz. From Fig. 4.3, we can see that the SNR of suitable frame detection rate is about 9 dB because the system BER must be lower than  $10^{-6}$ .

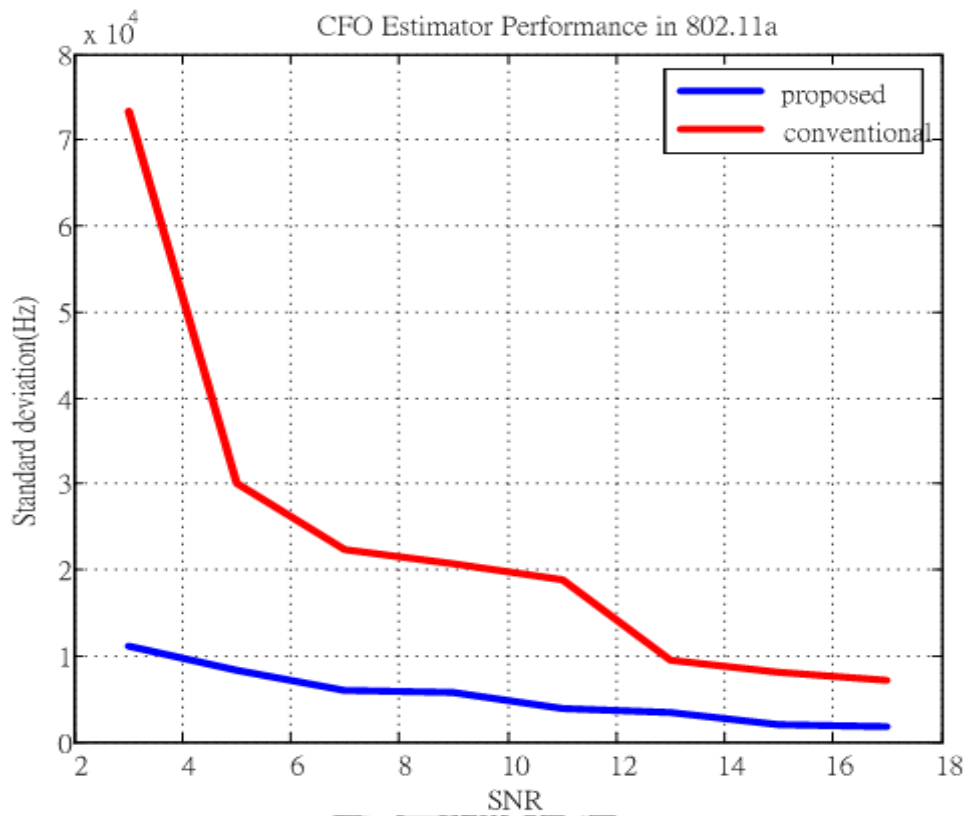


**Figure 4.3** frame detection performance in 802.16d

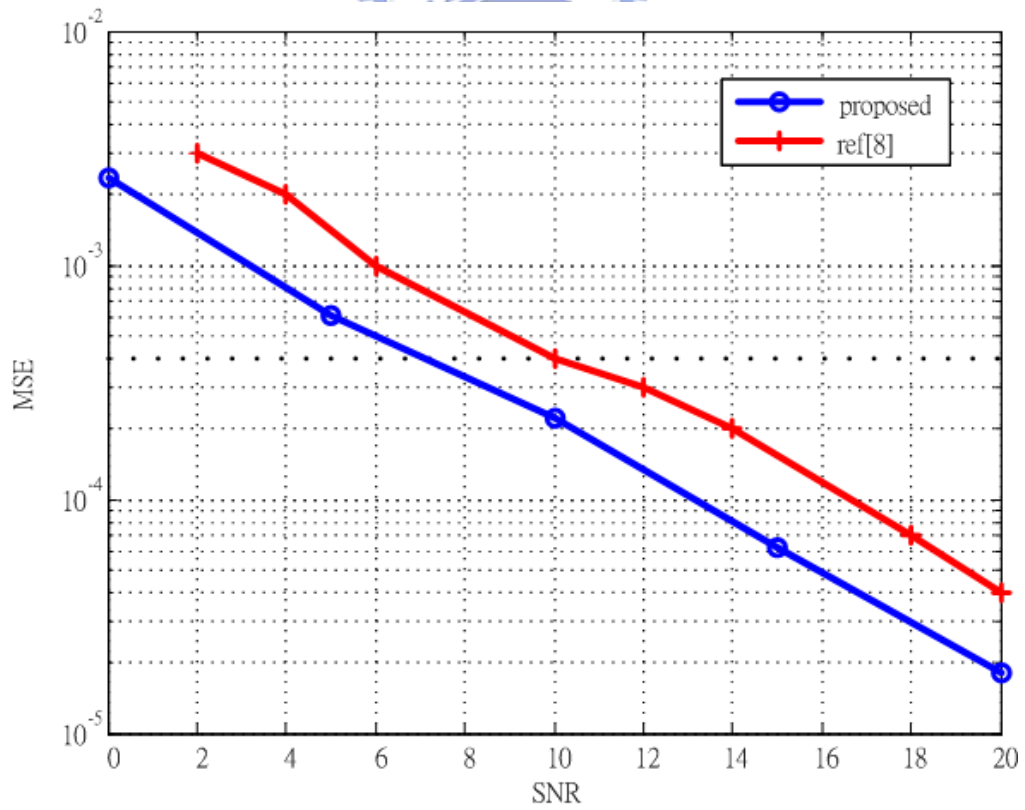


### 4.1.3 Fractional CFO Estimation Performance

The fractional CFO estimation Performance of IEEE 802.11a/g is shown in Fig. 4.3. The simulation condition is under maximum CFO value and multipath channel with rms delay spread 50 ns. The conventional method [4] described in Fig. 4.3 a two step estimation approach. The two step estimation uses an autocorrelation which length equals to 16 first, and then uses the autocorrelation which length is 64. The proposed method uses only one autocorrelation which length equal to 64. Actually the proposed method in IEEE 802.11a/g is exactly the method in IEEE 802.16d. The fractional CFO estimation performance is shown in Fig. 4.4. The simulation condition is under CFO of 5.75 times subcarrier spacing, SUI-3 multipath channel, qpsk modulation and bandwidth is 7 MHz. We can see that the performance in IEEE 802.16d is about the same the performance of other methods [8].



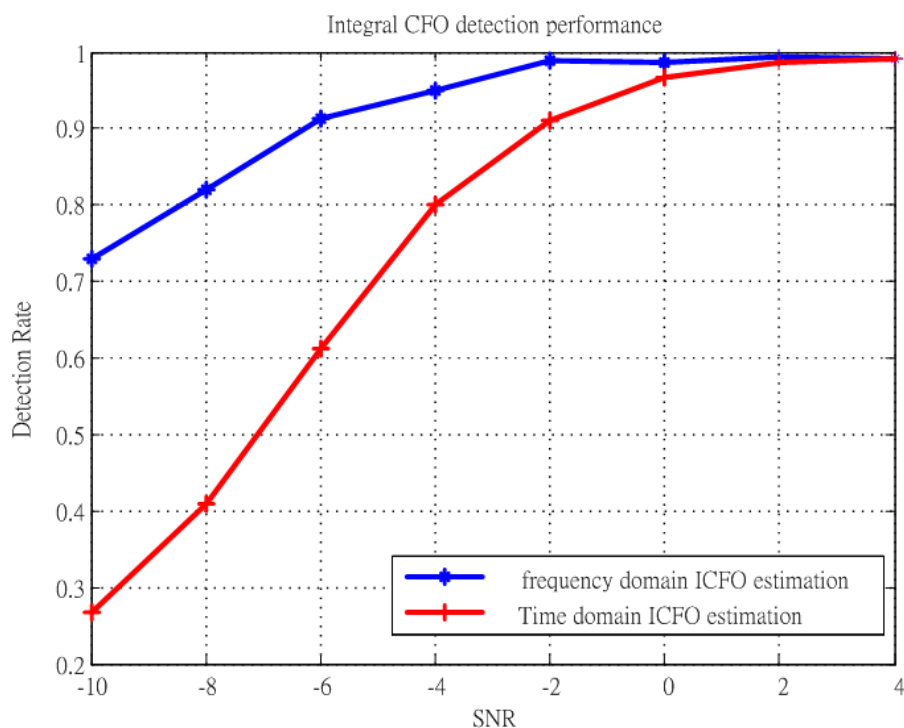
**Figure 4.4** Fraction CFO estimation performance in 802.11a/g



**Figure 4.5** Fractional CFO Estimation performance in 802.16d

#### 4.1.4 Integral CFO Estimation Performance

The Integral CFO Estimation performance is shown in Fig. 4.5. The performance of frequency domain integral CFO estimation is better than the performance of time domain estimation under negative SNR. However, the performance is almost the same if SNR is larger than zero. In consideration of compensation, the hardware complexity of time domain approach must less than frequency domain approach.



**Figure 4.6** Integral CFO Estimation performance in 802.16d

#### 4.1.5 BER Performance in IEEE 802.16d

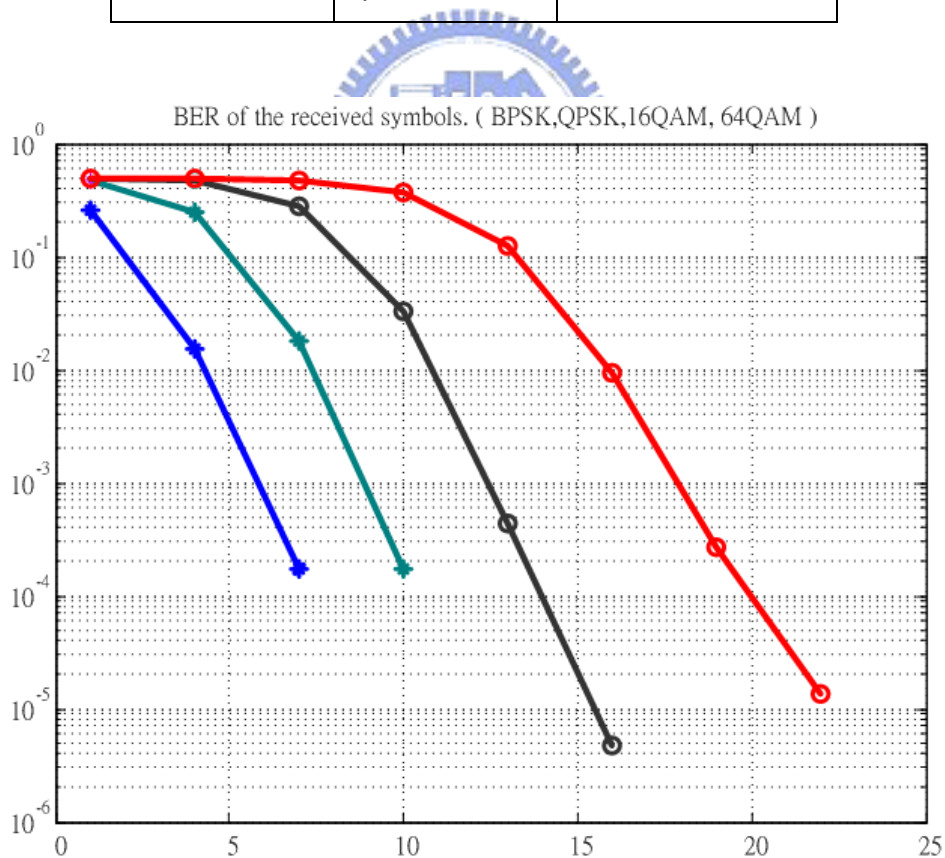
The BER performance in IEEE 802.16d is shown in Fig. 4.6. The simulation



condition is under CFO of 5.75 times subcarrier spacing, SUI-3 multipath channel, 1/2 coding rate and bandwidth is 7 MHz. comparing Fig. 4.6 to table 4.1 ,we can find that the BER performance can conform to the system simulation constraint.

**Table 4.1** System simulation constraint of IEEE 802.16d

modulation	Coding rate	Receiver SNR (dB)
BPSK	1/2	11.4
QPSK	1/2	14.4
	3/4	16.2
16QAM	1/2	21.4
	3/4	23.2
64QAM	1/2	27.7
	3/4	29.4



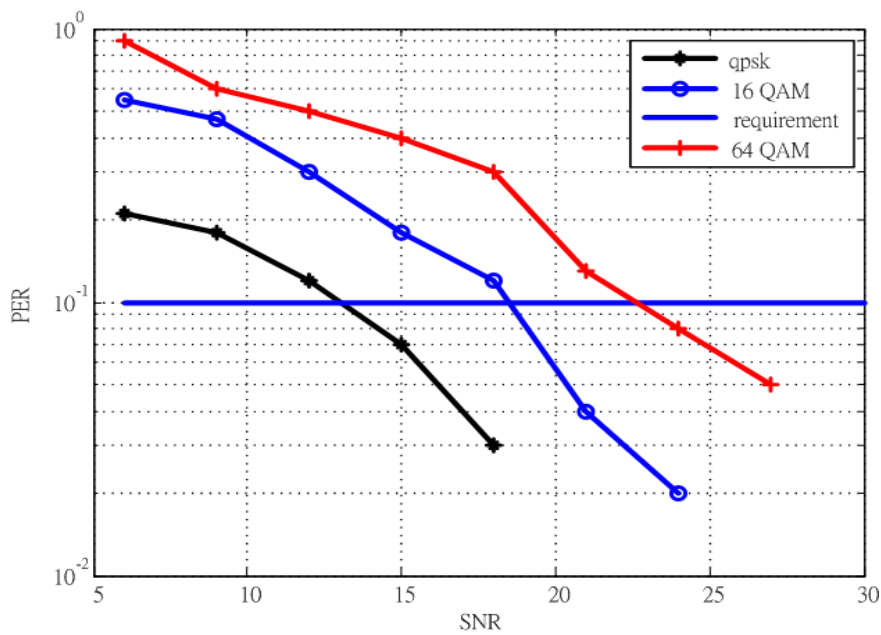
**Figure 4.7** BER performance of IEEE 802.16d

### 4.1.6 BER Performance in IEEE 802.11a/g

The PER performance in IEEE 802.11a/g is shown in Fig. 4.7. The simulation condition is under maximum CFO value, multipath channel with rms delay spread 50 ns and 3/4 coding rate. comparing Fig. 4.7 to table 4.2 ,we can find that the PER performance can conform to the system simulation constraint of IEEE 802.11a/g.

**Table 4.2** System simulation constraint of IEEE 802.11a/g

modulation	Coding rate	Receiver SNR (dB)
BPSK	1/2	9
	3/4	10
QPSK	1/2	12
	3/4	14
16QAM	1/2	17
	3/4	21
64QAM	2/3	25
	3/4	26



**Figure 4.8** PER performance of IEEE 802.11a/g

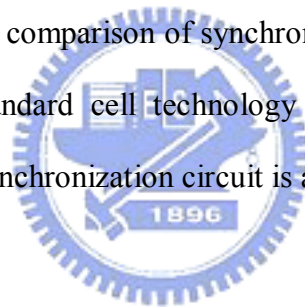
## 4.2 Hardware comparison

Table 4.3 shows the hardware comparison of fractional CFO estimation and compensation. The gate count of the proposed design is less than the reference design at least 46%.

**Table 4.3** Hardware comparison of fractional CFO estimation and compensation

	proposed	CORDIC +LUT or Sinusoid generator+ Complex multiplier[16]
Gate Count	62799.1	116816.5+LUT or Sinusoid generator

Table 4.4 shows the hardware comparison of synchronization circuit. By synthesizing to UMC 0.18um CMOS standard cell technology library with Synopsys Design Compiler, the gate count of synchronization circuit is about 124k

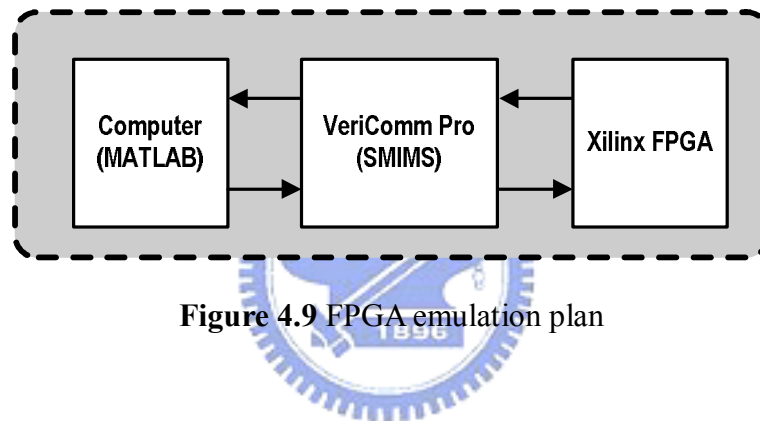


**Table 4.4** Hardware comparison of synchronization circuit

	Proposed WLAN & WiMax	[6] WLAN	[4] WLAN	[9] WiMax
Frame Detection	58168	16032	22800	N/A
Fractional CFO Estimation and Compensation	6279	136339	10100	N/A
Integral CFO Estimation	38147	none	none	N/A
Symbol boundary Detection	20411	8161	8800	N/A
Total	124072	160532	74200	82017

## 4.3 FPGA Emulation

FPGA emulation plan is shown in Fig. 4.9. We transmit data to Xilinx FPGA via VeriComm Pro software. The VeriComm Pro software and the Xilinx FPGA is presented in Fig. 4.10. The FPGA synthesis report is provided in Fig. 4.11. The total equivalent gate count of design includes register file. In this design, four 12x256 bits of register file and four 12x300 bits of register file are used. Fig. 4.12 shows the RTL simulation result and the FPGA emulation result.



**Figure 4.9** FPGA emulation plan



**Figure 4.10** VeriComm Pro software and the Xilinx FPGA

Device Utilization Summary				
Logic Utilization	Used	Available	Utilization	Note(s)
<b>Total Number Slice Registers</b>	29,571	53,248	55%	
Number used as Flip Flops	29,568			
Number used as Latches	3			
Number of 4 input LUTs	22,531	53,248	42%	
<b>Logic Distribution</b>				
Number of occupied Slices	26,160	26,624	98%	
Number of Slices containing only related logic	26,160	26,160	100%	
Number of Slices containing unrelated logic	0	26,160	0%	
<b>Total Number 4 input LUTs</b>	22,545	53,248	42%	
Number used as logic	22,531			
Number used as a route-thru	14			
Number of bonded IOBs	52	640	8%	
Number of BUFG/BUFGCTRLs	1	32	3%	
Number used as BUFGs	1			
Number used as BUFGCTRLs	0			
Number of DSP48s	9	64	14%	
<b>Total equivalent gate count for design</b>	402,875			
Additional JTAG gate count for IOBs	2,496			

Figure 4.11 FPGA synthesis report

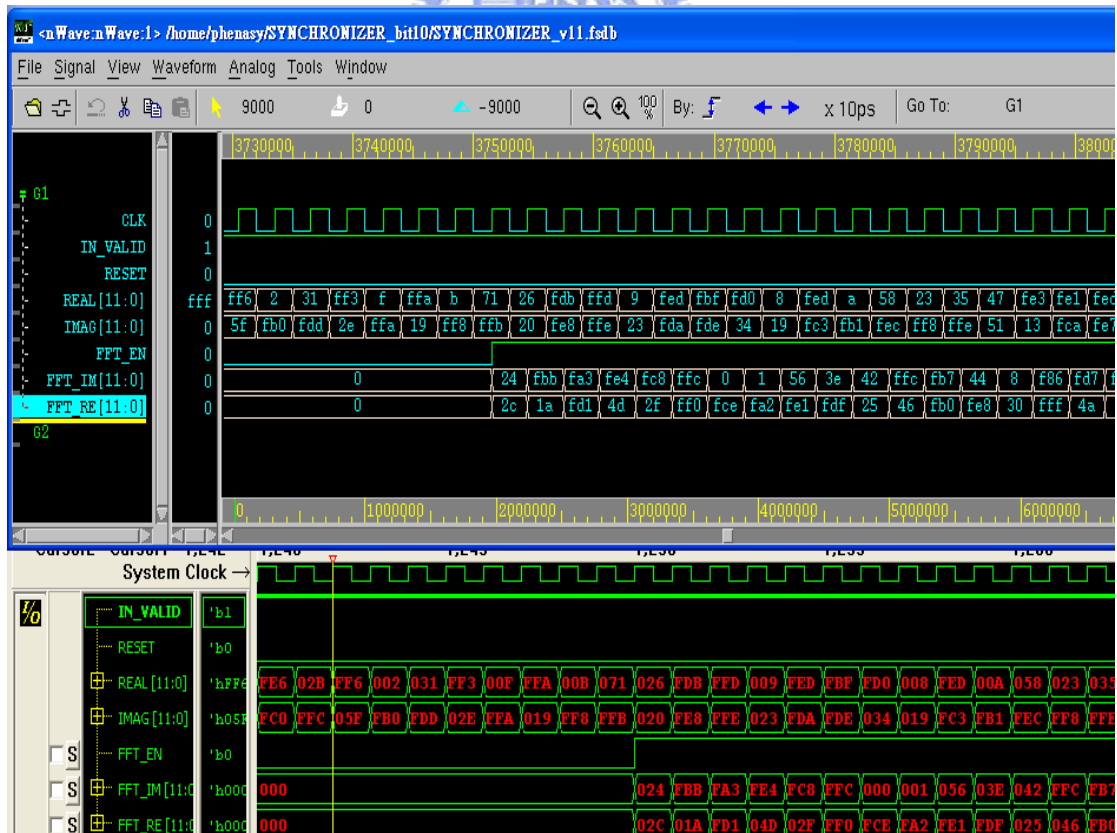


Figure 4.12 Waveform of FPGA and RTL design

# Chapter5

## Conclusions and Future Work

### 5.1 Conclusions

In the thesis, a multimode synchronization circuit is designed for both IEEE 802.16d and IEEE 802.11a/g systems. The performance of the multimode circuit can conform to the two receiver requirements. A modified absolute value approximation circuit (AVAC) that improves accuracy 2~3 times the accuracy of traditional method is provided. The fractional CFO estimator can have outstanding performance while the system is under IEEE802.11a/g mode. A modified CORDIC circuit for fraction CFO estimation and compensation is presented. After integral CFO estimation, the integral CFO compensation uses the same modified CORDIC circuit. The CORDIC circuit can be used other standards directly. The hardware of the multimode synchronization circuit is low and suitable for SOC integration. The multimode synchronization circuit has been verified by software simulation on Matlab platform and hardware implementation on FPGA with Virtex 4.

### 5.2 Future Work

There are still many non-ideal effects, including phase noise, IQ imbalance and power amplifier nonlinearity. In the presence of these non-ideal effects, the estimator and detector performance will degrade. Future work is to complete the multimode

synchronization circuit design in consideration of those non-ideal effects and then to complete the multimode receiver design by integrating channel estimator, equalizer and outer receiver.



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論文題目：CORDIC Based Multimode Synchronization Circuit Design for IEEE

802.16d and 802.11a/g systems

用於 IEEE 802.16d 及 IEEE 802.11a/g 之 CORDIC 多模同步電路設計