

國立交通大學  
電機與控制工程學系

碩士論文

應用於仿人眼視覺系統之  
智慧型深度偵測技術

Intelligent learning algorithm  
for depth detection applied to a  
humanoid vision system

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中華民國九十七年七月

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# 應用於仿人眼視覺系統之 智慧型深度偵測技術

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## 摘要




從兩台攝影機同時拍攝同景色的影像可以利用三角測量算出立體座標點。但是如果要用這種方法求得立體座標需要對攝影機有一些限制並且有一些參數是需要從實驗中獲得的。本論文提出用類神經網路去訓練出不需要相機參數的深度偵測系統，訓練資料由不同變化的目標點於兩張影像中的位置及其所對應的立體座標點構成。最後從誤差百分比可以知道傳統的深度偵測演算法的誤差遠遠大於本論文所提供的類神經網路深度偵測系統而且其準確度足以在立體視覺研究中被應用。

# Intelligent learning algorithm for depth detection applied to a humanoid vision system

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## ABSTRACT

The logo of National Chiao Tung University is a circular emblem with a gear-like border. Inside the circle, there is a stylized figure holding a torch, with the letters 'ES' and 'A' on either side. Below the figure, the year '1896' is inscribed.

Stereo-pair images obtained from two cameras can be utilized to compute world coordinate points by using triangulation. However, there are some restrictions from cameras and parameters need to be experimentally obtained, by applying this method. This thesis proposed that, for stereo vision applications which need to evaluate the actual depth, artificial neural networks be used to train the system such that the need for parameters of cameras are eliminated. The training set for our neural network consists of a variety of points in stereo-pair and their corresponding world coordinates. The percentage error obtained from the proposed architecture set-up is comparable with those obtained through traditional depth detection algorithm and that the system is accurate enough for most stereo vision applications.

# Acknowledgment

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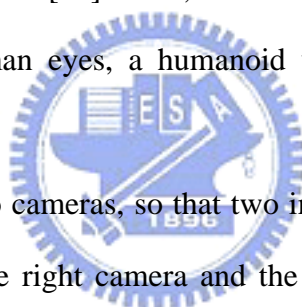


# Chapter 1

## Introduction

### 1.1 Preliminary

The human brain can process subtle differences between the images that are observed at the left and right eyes to perceive a three-dimensional (3-D) in the space effortlessly. This ability of perceiving 3-D is called stereo vision. Recently, applications of stereo vision systems which have been proposed in telecommunication [1], geoscience [2], [3], navigation [4], [5], and robotics [6], [7], [8], [9], [10], [11], [12]. Although the 3-D reconstruction also can be achieved from a single image, a priori information is still needed [13]. Thus, in order to simulate the ability of stereo vision that is similar to human eyes, a humanoid vision system (HVS) could be applied.



The HVS consists of two cameras, so that two images of the same scene can be taken at the same time by the right camera and the left camera from two different perspectives. The pair of these two images is called a stereo pair. The main problem in HVS is the perception of depth, because the depth information obtained from stereo vision is very useful for robot navigation in complex environments. Stereo vision consists of matching corresponding points in a stereo pair and estimating depth from their disparity which means the difference in positions of corresponding points. Usually in stereo vision systems, the depth is calculated from disparity by using the triangulation. The process of triangulation is needed to find the intersection of two known rays in space. This kind of classical technique needs careful calibration of the imaging system while calibration is an error sensitive process and it cannot always be performed online [13]. Therefore, there are some other approaches that calculating depth map without using camera parameter [12], [13]. In this thesis we have estimated

depth in a human visual system using neural networks. By using neural networks we have estimated depth without getting camera parameters and calibrating the imaging system.

## **1.2 Organization of the thesis**

The rest of the thesis is organized as follows in chapter 2 we have introduced the intelligent learning algorithm. In chapter 3 we have represented the traditional depth detection algorithm and ANN depth detection algorithm respectively. In chapter 4 experimental results and discuss are provided. At last, chapter 5 represents the conclusions and future works.



# Chapter 2

## Intelligent learning algorithm

### 2.1 Introduction to ANNs

The human nervous system consists of a large amount of neurons, including somas, axons, dendrites and synapses. Each neuron is capable of receiving, processing, and passing electrochemical signals from one to another. To mimic the characteristics of the human nervous system, recently investigators have developed an intelligent algorithm, called artificial neural networks (ANNs), to construct intelligent machines capable of parallel computation. This thesis will apply ANNs to the depth detection in an eyeball system through learning.

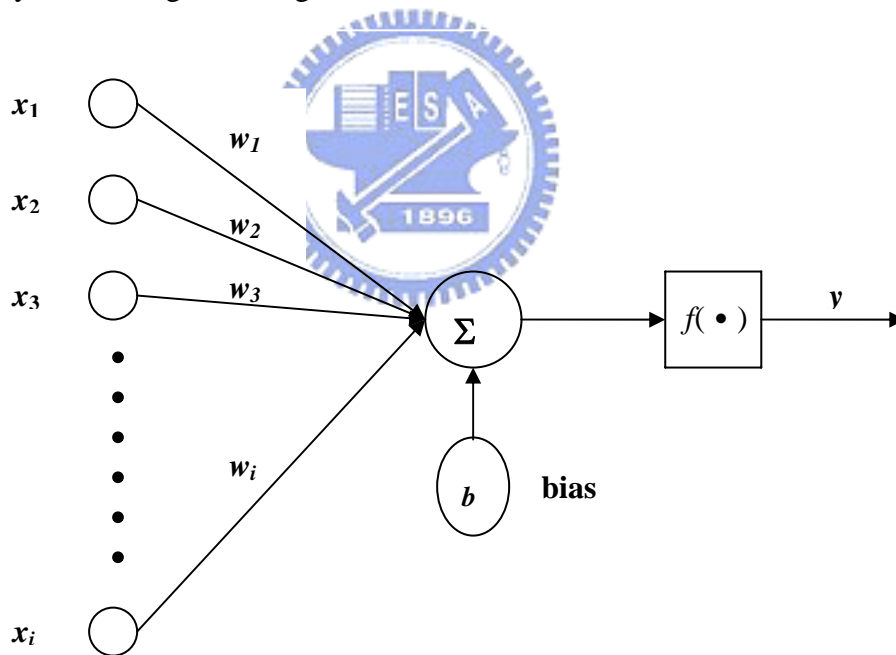


Fig. 2.1 Basic element of ANNs

ANNs can be divided into three layers which contain input layer, hidden layer, and output layer. The input layer receives signal from the outside world, which just includes input values without neuron. The neuron's number of output layer is depending on the output number. From the output layer, the response of the net can be

read. The neurons between input layer and output layer are belonging to hidden layer which does not exist necessarily. Here, each input is multiplied by a corresponding weight, analogous to synaptic strengths. The weighted inputs are summed to determine the activation level of the neuron. The connection strengths or the weights represent the knowledge in the system. Information processing takes place through the interaction among these units. The Basic element of ANNs, single layer net, is shown in Fig. 2.1 Basic element of ANNs which obeys the input-output relations

$$y = f\left(\sum_{i=1}^n w_i x_i + b\right) \quad (2.1-1)$$

where  $w_i$  is the weight at the input  $x_i$  and  $b$  is a bias term. The activation function  $f(\bullet)$  has many types cover linear and nonlinear. Note that the commonly used activation function is

$$f(x) = \frac{1}{1 + e^{-x}} \quad (2.1-2)$$

which is a sigmoid function. Base on the basic element, the commonest multilayer feed-forward net shown in Fig. 2.2 Multilayer feed-forward network, which contains input layer, output layer, and two hidden layers. Multilayer nets can solve more complicated problem than single layer nets, i.e. a multilayer nets is possible to solve some case that a single layer net cannot be trained to perform correctly at all. However, the training process of multilayer nets may be more difficult. The number of hidden layer and its neuron in the multilayer net are decided by complicated degree of the problem wait to solve.

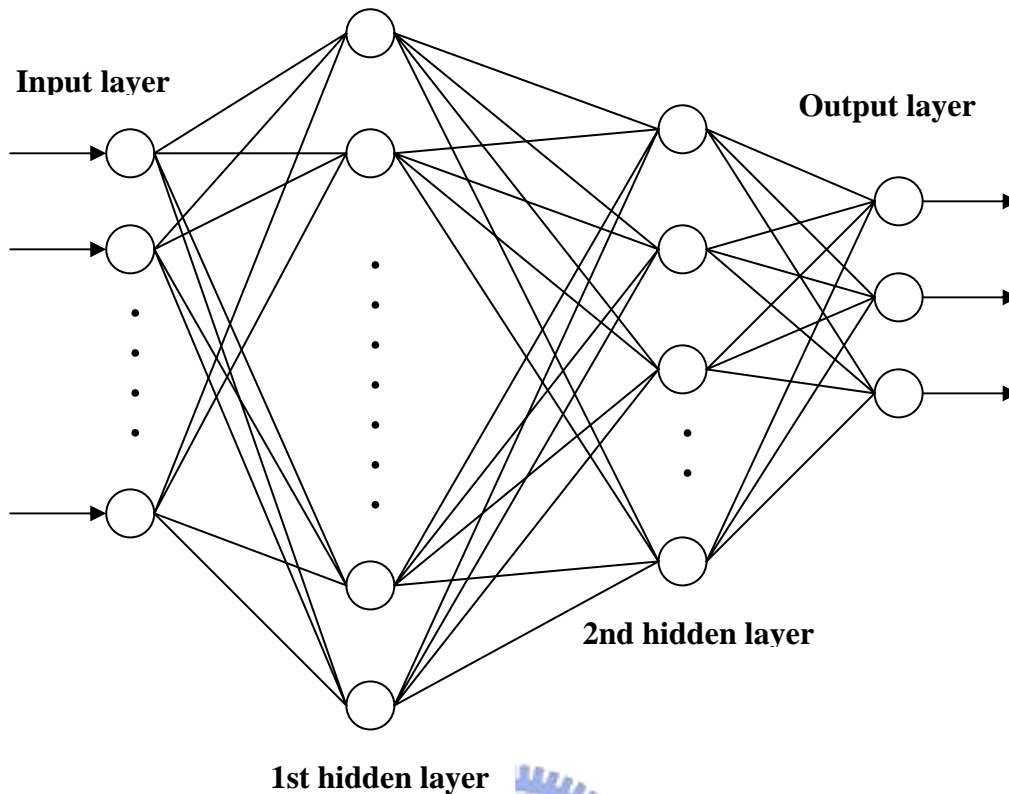


Fig. 2.2 Multilayer feed-forward network

In addition to the architecture, the method of setting the values of the weights is an important matter of different neural net. For convenience, the training for a neural network mainly classified into supervised learning and unsupervised learning. Training of supervised learning is mapping a given set of inputs to a specified set of target outputs. The weights are then adjusted according to various learning algorithms. Another type, unsupervised learning, can self-organize neural nets group similar input vectors together without the used of training data to specify what a typical member of each group looks like or to which group each vector belongs. For unsupervised learning, a sequence of input vector is provided, but no target vectors are specified. The net modifies the weights so that the most similar input vectors are assigned to the same output unit. In addition, there are nets whose weights are fixed without iterative training process, called structure learning, which change the network structure to achieve reasonable responses. In this thesis, the neural network learns the behavior by

many input-output pairs, hence that is belongs to supervised learning.

## 2.2 Back-Propagation Network

In supervise learning, the back propagation learning algorithm, is widely used in most application. The back propagation, BP, algorithm was proposed in 1986 by Rumelhart, Hinton and Williams, which is based on the gradient steepest descent method for updating the weights to minimize the total square error of the output. The training by BP mainly is applied to multilayer feed-forward network which involves three stages: the feed-forward of the input training pattern, the calculation and back-propagation of the associated error, and the adjustment of the weights. Fig. 2.3 Back-propagation network shows a back-propagation network contains input layer with  $N_{inp}$  neurons, one hidden layer with  $N_{hid}$  neurons, and output layer with  $N_{out}$  neurons. In Fig. 2.3 Back-propagation network,  $\mathbf{x} = [x_1 \ x_1 \ \cdots \ x_{N_{inp}}]^T$ ,  $\mathbf{h} = [h_1 \ h_2 \ \cdots \ h_{N_{hid}}]^T$ , and  $\mathbf{y} = [y_1 \ y_2 \ \cdots \ y_{N_{out}}]^T$  respectively represent the input, hidden, and out note of the network. In addition,  $v_{ij}$  is the weight form the  $i$ -th neuron in the input layer to  $j$ -th neuron in the hidden layer and  $w_{gh}$  is the weight form the  $g$ -th neuron in the hidden layer to  $h$ -th neuron in the output layer.

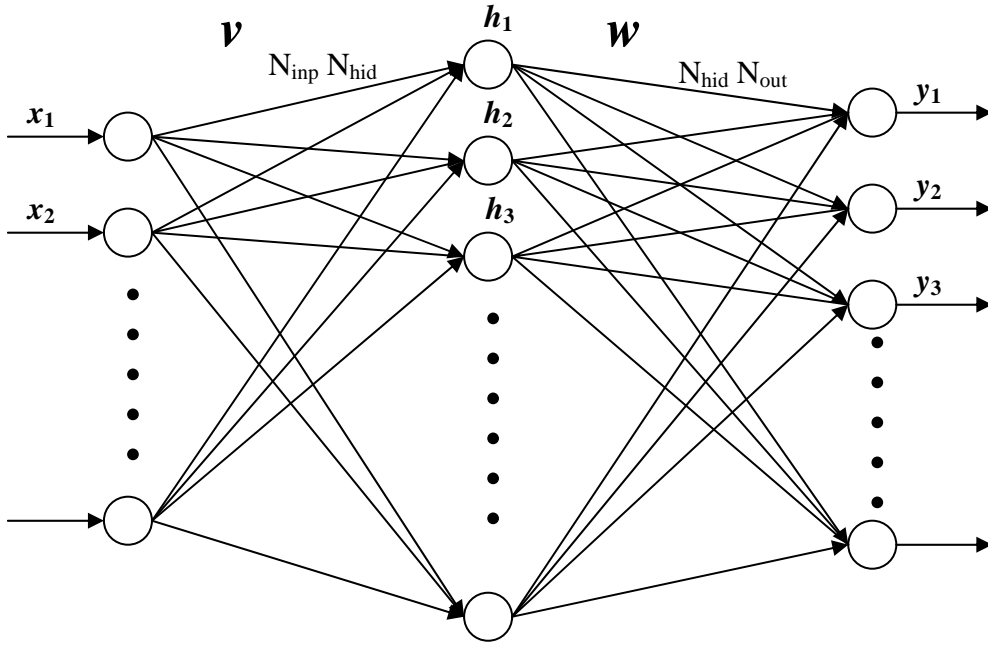


Fig. 2.3 Back-propagation network

The learning algorithm of BP is elaborated on below:

**Step 1:** Input the training data of input  $\mathbf{x} = [x_1 \ x_2 \ \dots \ x_{N_{inp}}]^T$  and desired output  $\mathbf{t} = [t_1 \ t_2 \ \dots \ t_{N_{inp}}]^T$ . Set the maximum tolerable error  $E_{max}$  and leaning rate  $\eta$  which between 0.1 and 1.0 to reduce the computing time or increase the precision.

**Step 2:** Set the initial weight and bias value of the network at random.

**Step 3:** Calculate the output of the  $m$ -th neuron in hidden layer

$$h_m = f_h \left( \sum_{k=1}^{N_{inp}} v_{km} x_k \right), m = 1, 2, \dots, N_{hid} \quad (2.1-3)$$

where  $f_h(\bullet)$  is the activation function of the neuron and the output of the  $i$ -th neuron in output layer

$$y_n = f_y \left( \sum_{q=1}^{N_{hid}} w_{qn} h_q \right), n = 1, 2, \dots, N_{out} \quad (2.1-4)$$



where  $f_y(\bullet)$  is the activation function of the neuron.

**Step 4:** Calculate the error function between network output and desired output.

$$E(\mathbf{w}) = \frac{1}{2} \sum_{n=1}^{N_{out}} (d_n - y_n)^2 = \frac{1}{2} \sum_{n=1}^{N_{out}} \left[ d_n - f_y \left( \sum_{q=1}^{N_{hid}} w_{mq} h_q \right) \right]^2 \quad (2.1-5)$$

where  $y_n$  is the network output and  $d_n$  is the desired output.

**Step 5:** According to gradient steepest descent method, determining the correction of weights.

$$\Delta w_{mn} = -\eta \frac{\partial E}{\partial w_{mn}} = -\eta \frac{\partial E}{\partial y_n} \frac{\partial y_n}{\partial w_{mn}} = \eta (d_n - y_n) \left[ f_y' \left( \sum_{q=1}^{N_{hid}} w_{mq} h_q \right) \right] h_m = \eta \delta_{mn} h_m \quad (2.1-6)$$

and

$$\begin{aligned} \Delta v_{km} &= -\eta \frac{\partial E}{\partial v_{km}} = -\eta \sum_{n=1}^{N_{out}} \left( \frac{\partial E}{\partial y_n} \frac{\partial y_n}{\partial h_m} \frac{\partial h_m}{\partial v_{km}} \right) \\ &= \eta \sum_{n=1}^{N_{out}} \left[ (d_n - y_n) f_y' \left( \sum_{q=1}^{N_{hid}} w_{mq} h_q \right) w_{mn} \right] f_h' \left( \sum_{k=1}^{N_{inp}} v_{km} x_k \right) x_k = \eta \delta_{kmn} x_k \end{aligned} \quad (2.1-7)$$

where  $\delta_{mn} = (d_n - y_n) \left[ f_y' \left( \sum_{q=1}^{N_{hid}} w_{mq} h_q \right) \right]$  and

$$\delta_{kmn} = \sum_{n=1}^{N_{out}} \left[ (d_n - y_n) f_y' \left( \sum_{q=1}^{N_{hid}} w_{mq} h_q \right) w_{mn} \right] f_h' \left( \sum_{k=1}^{N_{inp}} v_{km} x_k \right) x_k.$$

**Step 6:** Propagate the correction backward to update the weights.

$$\begin{cases} w(n+1) = w(n) + \Delta w \\ v(n+1) = v(n) + \Delta v \end{cases} \quad (2.1-8)$$

**Step 7:** Check whether the whole training data set have learned already.

Networks learn whole training data set once called a learning circle. If the network not goes through a learning circle, return to Step 1; otherwise, go

to Step 8.

**Step 8:** Check whether the network converge. If  $E < E_{max}$ , terminate the training process; otherwise, begin another learning circle by going to Step 1.

BP learning algorithm can be used to model various complicated nonlinear functions. Recently years The BP learning algorithm is successfully applied to many domain applications, such as: pattern recognition, adaptive control, clustering problem, etc. In the thesis, the BP algorithm was used to learn the input-output relationship for depth function.



# Chapter 3

## Intelligent depth detection for a humanoid vision system

### 3.1 Humanoid Vision System Description

The HVS is built with two cameras and five motors to emulate human eyeballs as shown in Fig. 3.1. These five motors, FAULHABER DC–servomotors, are used to drive the two cameras to implement the eye movement, one for the conjugate tilt of two eyes, two for the pan of two eyes, and two for the pan and tilt of the neck correspondingly. The control of DC–servomotors is executed by the motion control card, MCDC 3006 S, in a positioning resolution of  $0.18^\circ$ . With these 5 degrees of freedom, the HVS would track the target whose position is determined from the image processing of the two cameras. In addition, these two cameras, QuickCam<sup>TM</sup> Communicate Deluxe, have specifications listed below. [19]

- 1.3-megapixel sensor with RightLight<sup>TM</sup>2 Technology
- Built-in microphone with RightSound<sup>TM</sup> Technology
- Video capture: Up to 1280 x 1024 pixels (HD quality) (HD Video 960 x 720 pixels)
- Frame rate: Up to 30 frames per second
- Still image capture: 5 megapixels (with software enhancement)
- USB 2.0 certified
- Optics: Manual focus

In this proposed system structure, the baseline  $2d$  is set as constant equal to 10.5cm. The control and image process are both implemented in personal computer with 3.62 GHz CPU.

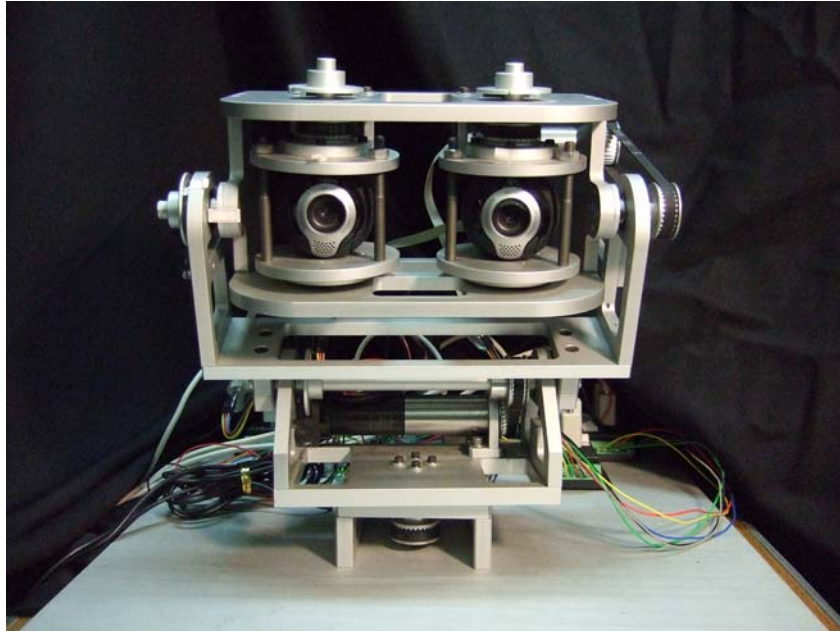


Fig. 3.1 Humanoid vision system



## 3.2 Depth Detection

### 3.2.1 Traditional depth detection algorithm

Before introducing depth computing, the triangulation for one camera will be introduced first [20]. Fig. 3.2 illustrates the relation of a world point with world coordinates  $(X, Y, Z)$ , which is projected onto camera coordinates  $(x, y)$  and onto image coordinates  $(u, v)$  in the image plane. The mapping between the camera coordinates  $(x, y)$  and the world coordinates  $(X, Y, Z)$  is formed by means of similar triangles as

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{f}{Z} \begin{bmatrix} X \\ Y \end{bmatrix} \quad (3.1-1)$$

where  $f$  is the focal length of the camera. The origin of the camera frame is located at the intersection of the optical axis with the image plane, while the origin of the image frame is located at the top left corner of the image. The transformation between the image frame and the camera frame is given by

$$\begin{cases} u = \text{round}(k_u x) + u_0 \\ v = \text{round}(k_v y) + v_0 \end{cases} \quad (3.1-2)$$

where  $k_u$  and  $k_v$  are the scale factors in  $\text{m}^{-1}$  of the horizontal and vertical pixels, respectively. Besides,  $(u_0, v_0)$  are the image coordinates of the origin of the camera frame and the function  $\text{round}(\bullet)$  rounds the element to its nearest integer.

It is known that mapping a 3-D scene onto an image plane is a multiple-to-one transformation, i.e., an image point may represent different locations in world coordinate. To derive the world coordinate information uniquely, two cameras should be used. With the triangulation theory and the disparity of a pair of corresponding object points in two camera's frames, the real location of an object can be reconstructed.

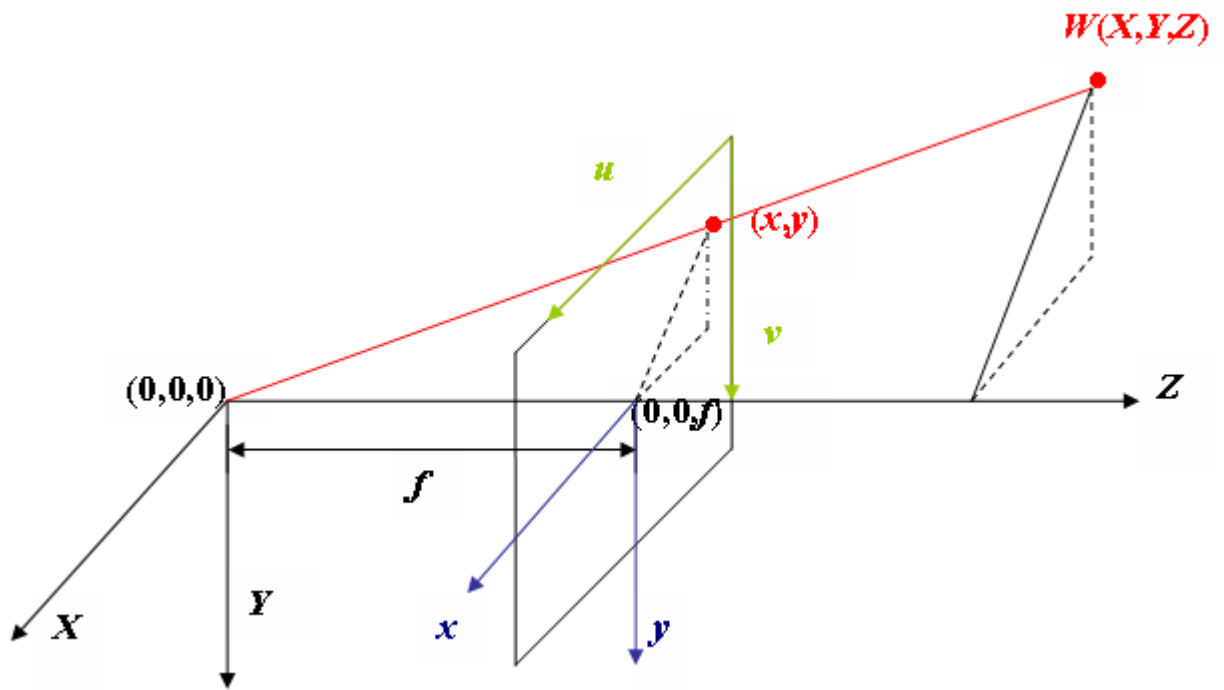
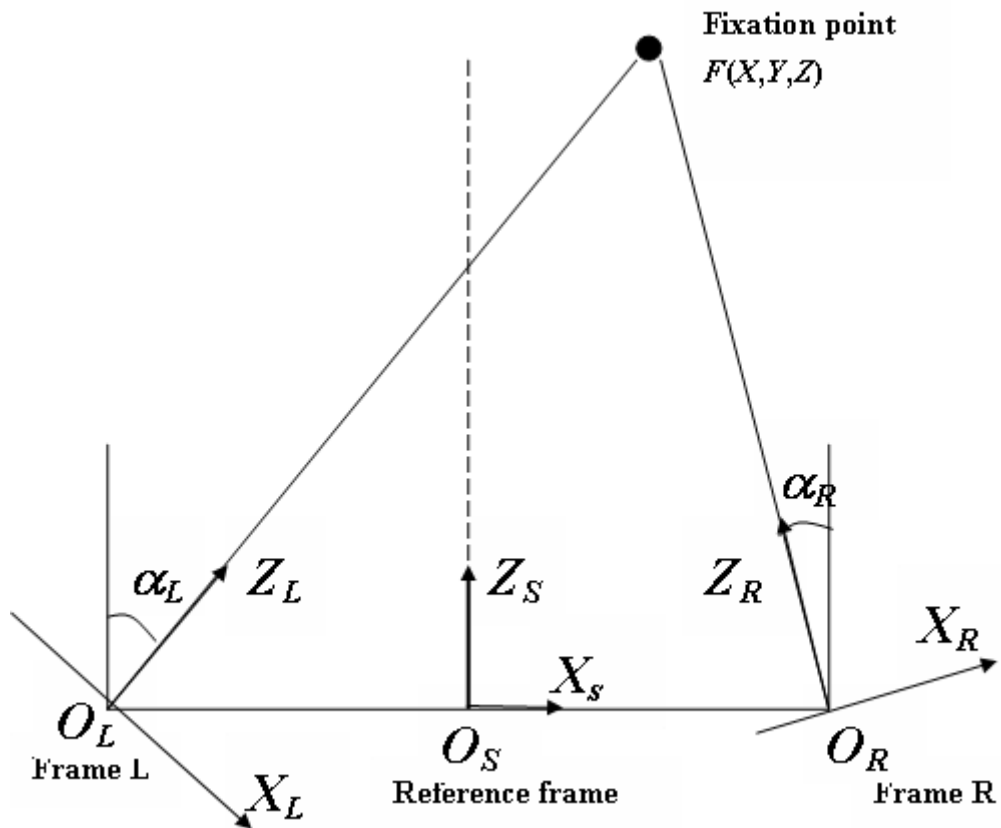


Fig. 3.2 Relation of a world point projected onto an image plane



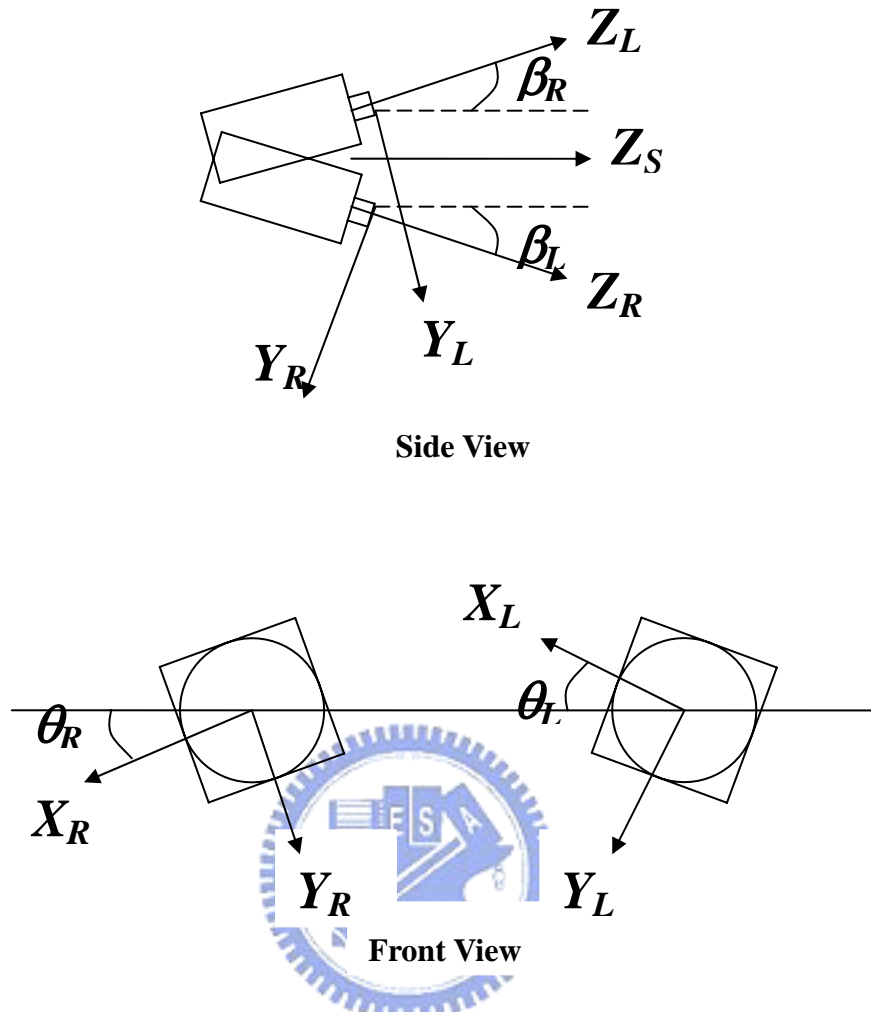


Fig. 3.3 Configuration of a HVS with binocular cameras

A HVS is implemented by two cameras with fixed focal length as shown in Fig. 3.3. The baseline of the two cameras is  $2d$ , where  $d$  is the length from the center of baseline to the camera, left or right. Let the pan angles of the left and right cameras be denoted by  $\alpha_L$  and  $\alpha_R$ , respectively. Since the cameras may not be placed precisely, there often exists a small tilt angle  $2\beta_0$  and a small roll angle  $2\phi_0$  between two cameras. Choose the stereo reference frame at  $O_s$ , which divides the tilt angle, roll angle, and baseline equally, with  $Z$ -axis pointing towards the fixating point  $F$ . For the left camera coordinate frame  $L$ , it is related to the stereo reference frame by a translation vector  $\mathbf{d}_L = (-d, 0, 0)$  and a rotation matrix  $\mathbf{\Omega}_L = \mathbf{\Omega}(\alpha_L, \beta_L, \phi_L)$ , where

$\alpha_L$ ,  $\beta_L=\beta_0$  and  $\phi_L=\phi_0$  are respectively the Euler angles of pan, tilt and roll of frame  $L$  and  $\mathbf{\Omega}(\alpha, \beta, \phi)$  is the general rotation matrix expressed as

$$\mathbf{\Omega}(\alpha, \beta, \phi) = \begin{bmatrix} \omega_{11}(\alpha, \beta, \phi) & \omega_{12}(\alpha, \beta, \phi) & \omega_{13}(\alpha, \beta, \phi) \\ \omega_{21}(\alpha, \beta, \phi) & \omega_{22}(\alpha, \beta, \phi) & \omega_{23}(\alpha, \beta, \phi) \\ \omega_{31}(\alpha, \beta, \phi) & \omega_{32}(\alpha, \beta, \phi) & \omega_{33}(\alpha, \beta, \phi) \end{bmatrix} \quad (3.1-3)$$

with

$$\omega_{11}(\alpha, \beta, \phi) = \cos \alpha \cos \phi$$

$$\omega_{12}(\alpha, \beta, \phi) = \sin \alpha \sin \beta \cos \phi - \cos \beta \sin \phi$$

$$\omega_{13}(\alpha, \beta, \phi) = \sin \alpha \cos \beta \cos \phi + \sin \beta \sin \phi$$

$$\omega_{21}(\alpha, \beta, \phi) = \cos \alpha \sin \phi$$

$$\omega_{22}(\alpha, \beta, \phi) = \sin \alpha \sin \beta \sin \phi + \cos \beta \cos \phi$$

$$\omega_{23}(\alpha, \beta, \phi) = \sin \alpha \cos \beta \sin \phi - \sin \beta \cos \phi$$

$$\omega_{31}(\alpha, \beta, \phi) = -\sin \alpha$$

$$\omega_{32}(\alpha, \beta, \phi) = \cos \alpha \sin \beta$$

$$\omega_{33}(\alpha, \beta, \phi) = \cos \alpha \cos \beta$$



The transformation equation of the object point  $B$  from frame  $L$  to the reference frame is described as

$$\mathbf{p}_L = \mathbf{\Omega}_L(\mathbf{p}_s - \mathbf{d}_L) \quad (3.1-4)$$

where  $\mathbf{p}_L = [X_L \ Y_L \ Z_L]^T$  is the position vector of  $B$  in frame  $L$  and  $\mathbf{p}_s = [X_s \ Y_s \ Z_s]^T$  is the position vector of  $B$  in the reference frame. From (3.1-1) and (3.1-4), we have

$$\begin{bmatrix} x_L \\ y_L \end{bmatrix} = \frac{f_L}{Z_L} \begin{bmatrix} X_L \\ Y_L \end{bmatrix} \quad (3.1-5)$$

where

$$x_L = (X_s + d) \omega_{11}(\alpha_L, \beta_0, \phi_0) + Y_s \omega_{12}(\alpha_L, \beta_0, \phi_0) + Z_s \omega_{13}(\alpha_L, \beta_0, \phi_0)$$

$$y_L = (X_s + d) \omega_{21}(\alpha_L, \beta_0, \phi_0) + Y_s \omega_{22}(\alpha_L, \beta_0, \phi_0) + Z_s \omega_{23}(\alpha_L, \beta_0, \phi_0)$$



$$Z_L = (X_s + d)\omega_{31}(\alpha_L, \beta_0, \phi_0) + Y_s\omega_{32}(\alpha_L, \beta_0, \phi_0) + Z_s\omega_{33}(\alpha_L, \beta_0, \phi_0)$$

Therefore, the relation between image coordinate of frame  $L$  and world coordinates are

$$\begin{cases} u_L = \text{round}(k_u x_L) + u_0 \\ v_L = \text{round}(k_v y_L) + v_0 \end{cases} \quad (3.1-6)$$

Similarly, for the right camera coordinate frame  $R$ , the transformation equation of  $B$  is described as

$$\mathbf{p}_R = \mathbf{\Omega}_R(\mathbf{p}_s - \mathbf{d}_R) \quad (3.1-7)$$

where  $\mathbf{p}_R = [X_R \ Y_R \ Z_R]^T$  is the position vector of  $B$  in frame  $R$ ,  $\mathbf{d}_R = (d, 0, 0)$  is the translation vector, and the rotation matrix  $\mathbf{\Omega}_R = \mathbf{\Omega}(\alpha_R, \beta_R, \phi_R)$  with  $\alpha_R, \beta_R = -\beta_0$  and  $\phi_R = -\phi_0$  being the Euler angles of pan, tilt and roll of frame  $R$ , respectively. Using (3.1-1) and (3.1-7), the relation between the right camera coordinates and the world coordinates are given by

$$\begin{bmatrix} x_R \\ y_R \end{bmatrix} = \frac{f_R}{Z_R} \begin{bmatrix} X_R \\ Y_R \end{bmatrix} \quad (3.1-8)$$

where

$$\begin{aligned} x_R &= (X_s - d)\omega_{11}(\alpha_R, -\beta_0, -\phi_0) + Y_s\omega_{12}(\alpha_R, -\beta_0, -\phi_0) + Z_s\omega_{13}(\alpha_R, -\beta_0, -\phi_0) \\ y_R &= (X_s - d)\omega_{21}(\alpha_R, -\beta_0, -\phi_0) + Y_s\omega_{22}(\alpha_R, -\beta_0, -\phi_0) + Z_s\omega_{23}(\alpha_R, -\beta_0, -\phi_0) \\ Z_R &= (X_s - d)\omega_{31}(\alpha_R, -\beta_0, -\phi_0) + Y_s\omega_{32}(\alpha_R, -\beta_0, -\phi_0) + Z_s\omega_{33}(\alpha_R, -\beta_0, -\phi_0) \end{aligned}$$

Accordingly, the relation between image coordinate of frame  $R$  and world coordinates can be express as

$$\begin{cases} u_L = \text{round}(k_u x_L) + u_0 \\ v_L = \text{round}(k_v y_L) + v_0 \end{cases} \quad (3.1-9)$$

Since the angles  $\beta_0$  and  $\phi_0$  are small, the absolute value of the terms  $\omega_{12}, \omega_{21}, \omega_{23}, \omega_{32}$  for both the left and the right frames are usually much smaller compared to the other terms. Further define stereo disparity,  $u_{sd}$ , as the disparity of  $B$  between the left image

frame and right image frame, expressed as

$$u_{sd} = u_L - u_R \quad (3.1-10)$$

which will be applied to the determination of the depth of  $B$ .

In the HVS, if two cameras are placed precisely in parallel, then the pan, tilt, and roll angles between these two cameras are zeros, i.e.,  $\alpha_L = \alpha_R = 0$ ,  $\beta_L = \beta_R = \beta_0 = 0$ , and  $\phi_L = \phi_R = \phi_0 = 0$ . From (3.1-4) and (3.1-7), the position vector of  $B$  in the left and right camera frames are respectively obtained as

$$p_L = p_s - d_L \quad (3.1-11)$$

$$p_R = p_s - d_R \quad (3.1-12)$$

with  $\Omega_L = \Omega_R = I$ . Based on the same process from (3.1-5) to (3.1-9), the disparity is found as

$$u_{sd} = u_L - u_R = \text{round}(k_u x_L) - \text{round}(k_u x_R) \quad (3.1-13)$$

Since the term on the right can be approximated as

$$\begin{aligned} & \text{round}(k_u x_L) - \text{round}(k_u x_R) \\ & \approx k_{uL} \frac{f_L X_L}{Z_L} - k_{uR} \frac{f_R X_R}{Z_R} \end{aligned} \quad (3.1-14)$$

where  $Z_L = Z_R = Z$ , the disparity can be written as

$$u_{sd} = u_L - u_R \approx \frac{k_{uL} f_L X_L - k_{uR} f_R X_R}{Z} \quad (3.1-15)$$

Rearranging it leads to

$$Z \approx \frac{k_{uL} f_L X_L - k_{uR} f_R X_R}{u_{sd}} \quad (3.1-16)$$

which gives the depth of  $B$  after  $u_{sd}$ ,  $X_L$ ,  $X_R$ ,  $f_L$ ,  $f_R$ ,  $k_{uL}$  and  $k_{uR}$  are obtained. In general case, for arbitrary object point, it is hard to obtain the  $X_L$  and  $X_R$  values. Therefore, the traditional depth computation is usually used under the assumption that both cameras have the same focal length, i.e.,  $k_{uL} f_L = k_{uR} f_R = k_u f$ , and then (3.1-16) can be simplified as

$$Z \approx \frac{k_{uL}f_L X_L - k_{uR}f_R X_R}{u_{sd}} = \frac{k_u f (X_L - X_R)}{u_{sd}} = \frac{k_u f (2d)}{u_{sd}} \quad (3.1-17)$$

where  $X_L - X_R = 2d$  is the separation of two cameras. Clearly, with (3.1-17), only  $k_u f$ ,  $d$  and  $u_{sd}$  are required to find the depth  $Z$ .

### 3.2.2 ANN depth detection algorithm

Stereo pair obtained from two cameras can be utilized to compute the depth of a point by using the traditional depth computation introduced in previous section. However, to apply the computation, parameters of each camera need to be experimentally obtained in advance. Therefore, ANN can be used to train the system for eliminating the complicate computation process.

It is well known that multilayer neural networks can approximate any arbitrary continuous function to any desired degree of accuracy [14]. A number of investigators have it for different proposes in stereo vision. For example they have been used for camera calibration [15], establishing correspondence between stereo pair based on features [16] and generating depth map in stereo vision [12][15]. In this thesis, a feed forward neural network was used for depth estimation. The ANN computation system doesn't need to calibrate the cameras in HVS. This can be very helpful in rapid prototyping application. The proposed thesis employs a Multi-Layer Perceptron (MLP) network trained by BP training algorithm, which is the most commonly adopted for MLP network.

In the problem, the thesis proposed a multilayer ANN model because camera calibration problem is a nonlinear problem and cannot be solved with a single network [17]. Further, according to the neural network literature [18] more than one hidden layer is rarely needed. The more layers that a neural network have, the more parameter values need to be set because the number of neurons in each layer must be

determined. Therefore, to reduce the number of permutations, a network with one hidden layer was selected.

The network model had been used in Fig. 3.4 for simulation consists of four input neurons, five hidden neurons and three output neurons. The input neurons' corresponding to the image coordinates of matched points found in the stereo images  $(u_l, v_l)$  and  $(u_r, v_r)$ . These points are generated by the same world point on both images and formed the input data for the neural network. The output neurons corresponding to the world coordinates of a point which are mapped as  $(u_l, v_l)$  and  $(u_r, v_r)$  on the two images. The network is trained in an interesting range of actual depth, after training; give the world coordinates for any matched pair of points.

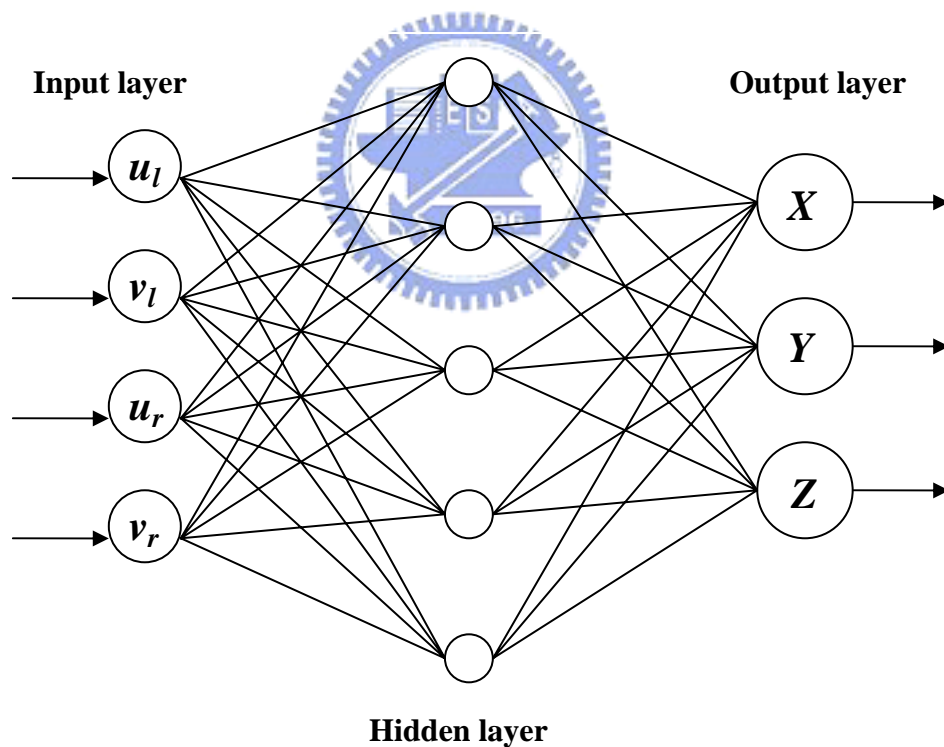


Fig. 3.4 ANN model used for this thesis

The algorithm requires training a set of matched image points whose corresponding world point is known. The set of matched points and the world

coordinates thus obtained and formed the training data set for the ANN. Once the network is trained, we present it with arbitrary matched points and it directly gives us the depth corresponding to the matched pair.

The main problem to using the MLP network is how to choose optimum parameters. Presently, there is no standard technique for automatically setting the parameters of MLP network. That is to say, the best architecture and algorithm for the problem can only be evaluated by experimentation and there are no fixed rules to determine the ideal network model for a problem. Therefore, experiments were performed on the neural network to determine the parameter according to its performance. Parameters with the number of neurons in the hidden layer (one hidden layer is employed in this thesis) will be issued in next Chapter for getting more precise detection result.



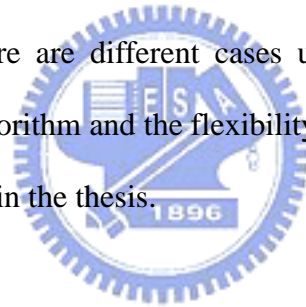
# Chapter 4

## Experimental Results and Discussion

### 4.1 Experimental Settings

The board consisting of a set of grid points is placed in front of the HVS for depth detection as shown in Fig.4.1 and Fig.4.2, one for the left camera and the other for the right. With the use of these two cameras, the HVS captures images of a specified cross at various distances, ranging from 65 to 165 cm. To verify the usefulness of the proposed ANN depth detection algorithm, the experiment is implemented by changing the distance  $Z$  between the HVS and the board, where  $Z$  starts from 65 cm to 165 cm at an increment of 10 cm.

In the next section, there are different cases used to show the restriction of traditional depth detection algorithm and the flexibility and features of the ANN depth detection algorithm proposed in the thesis.



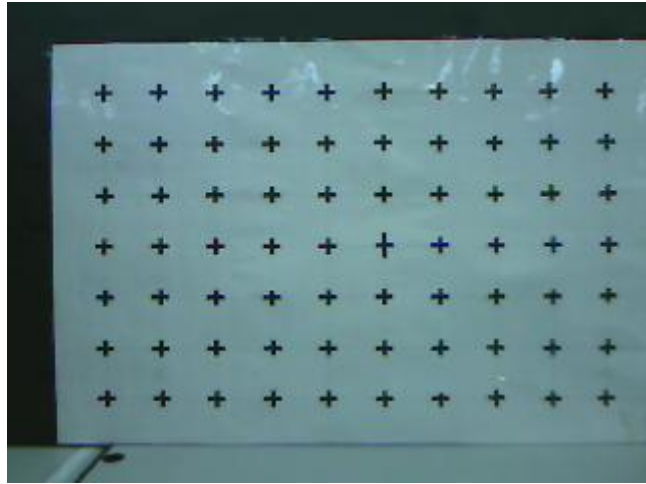


Fig. 4.1 The board at  $Z=105\text{cm}$  captured from left camera

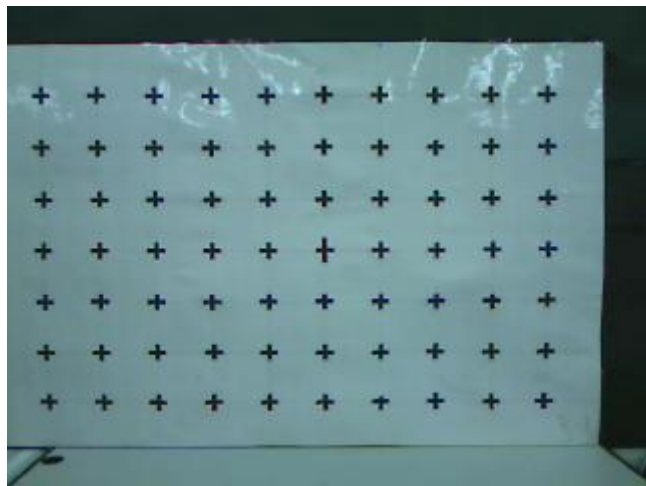


Fig. 4.2 The board at  $Z=105\text{cm}$  captured from right camera

## 4.2 Experimental Results

### 4.2.1 Restrictions on Traditional depth detection

#### algorithm

It is known that the traditional depth detection algorithm (3.1-17) is only suitable for the case that both cameras have the same focal length and their optic axes are parallel. However, in practical situation, the two cameras of an HVS generally have a little difference in their focal length or a little deflection between their optic axes. As a result, (3.1-17) is inappropriately used to detect the depth of a scene. To show these restrictions on an HVS, experiments will be set for demonstration.

The tradition depth detection algorithm (3.1-17) is derived from (3.1-16) under the assumption that  $k_{uL}f_L = k_{uR}f_R$  and  $2d = X_L - X_R$ . Here, let's find the real values of  $k_{uL}f_L$  and  $k_{uR}f_R$  to see whether they are the same or not. For simplicity, define  $\Phi_L = k_{uL}f_L$  and  $\Phi_R = k_{uR}f_R$  and let  $2d = X_L - X_R$ , i.e., the two optic axes are in parallel. Then, (3.1-16) becomes

$$\begin{aligned} u_{sd}Z &\approx k_{uL}f_L X_L - k_{uR}f_R X_R \\ &= \Phi_L X_L - \Phi_R X_R \\ &= \Phi_L (X_L - X_R) + (\Phi_L - \Phi_R) X_R \\ &= 2d\Phi_L + (\Phi_L - \Phi_R) X_R \end{aligned} \quad (4.1-1)$$

which can be further rearranged as

$$\Phi_L = \frac{u_{sd}Z - X_R(\Phi_L - \Phi_R)}{2d} \quad (4.1-2)$$

where the baseline  $2d$  is fixed. Next, let's show the way to calculate  $\Phi_L$  for the left camera in the HVS. By setting the shortest focal length for each camera, which is fixed but not exactly known, two images are obtained in Fig. 4.5 for  $Z=95$  cm and  $2d=10.5$  cm. To calculate  $\Phi_L$ , the term  $X_R(\Phi_L - \Phi_R)$  in (4.1-2) has to be eliminated.

By choosing the same 12 points in both images Fig. 4.5 (a) and (b), enclosed in the



dashed square, the addition of  $X_R(\Phi_L - \Phi_R)$  of these twelve points will vanish when they are vertically symmetric to the center line  $l_R$  in the right image. Hence,

$$\Phi_L = \frac{1}{12} \sum_{i=1}^{12} \frac{(u_{sd})_i Z}{2d} \quad (4.1-3)$$

where  $(u_{sd})_i$  is the disparity of the  $i$ -th point. Fig. 4.3 shows the result of  $\Phi_L$  for different distance  $Z$  from 45 cm to 105 cm to verify that  $\Phi_L$  is around the average value  $\bar{\Phi}_L = 142.918$  with 0.24116% variation. In a similar way, the value of  $\Phi_R$  corresponding to the case of the shortest focal length,  $Z=85$  cm and  $2d=10.5$  cm, can be obtained as

$$\Phi_R = \frac{1}{12} \sum_{i=1}^{12} \frac{(u_{sd})_i Z}{2d} \quad (4.1-4)$$

where the 12 points are chosen from the images shown in Fig. 4.6, vertically symmetric to the center line  $l_L$  in the left image. Fig. 4.4 shows the result of  $\Phi_R$  for different distance  $Z$ . It is obvious that  $\bar{\Phi}_L$  is approximate to  $\bar{\Phi}_R$  with 0.27821% variation. Since  $\bar{\Phi}_L$  is indeed near to  $\bar{\Phi}_R$ , the traditional depth detection algorithm (3.1-17) is applicable and adopts the average of  $\bar{\Phi}_L$  and  $\bar{\Phi}_R$  as  $k_{if}$ .

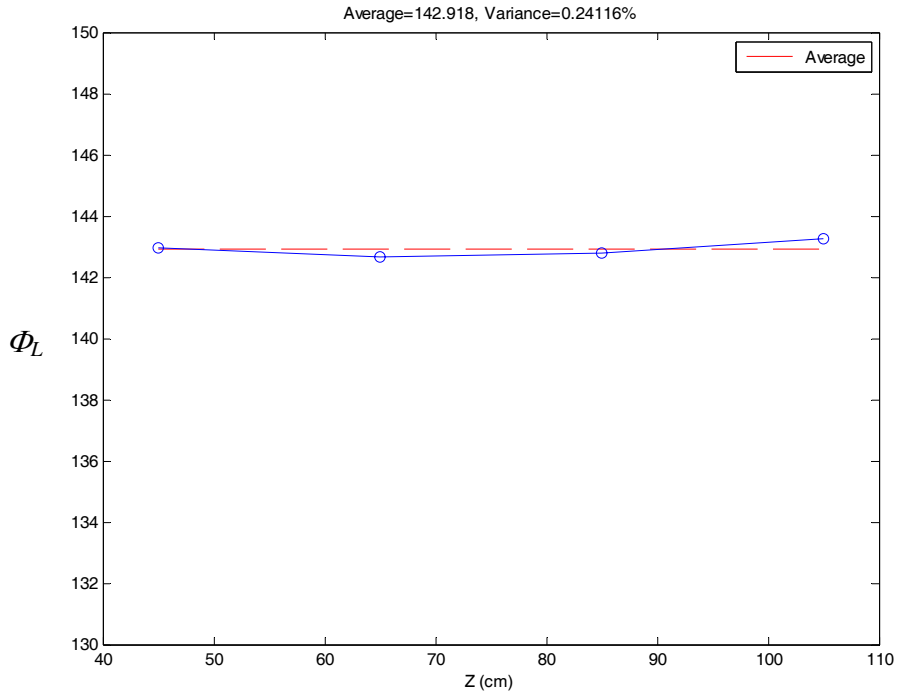


Fig. 4.3  $\Phi_L$  for different distance Z from 45 cm to 105 cm

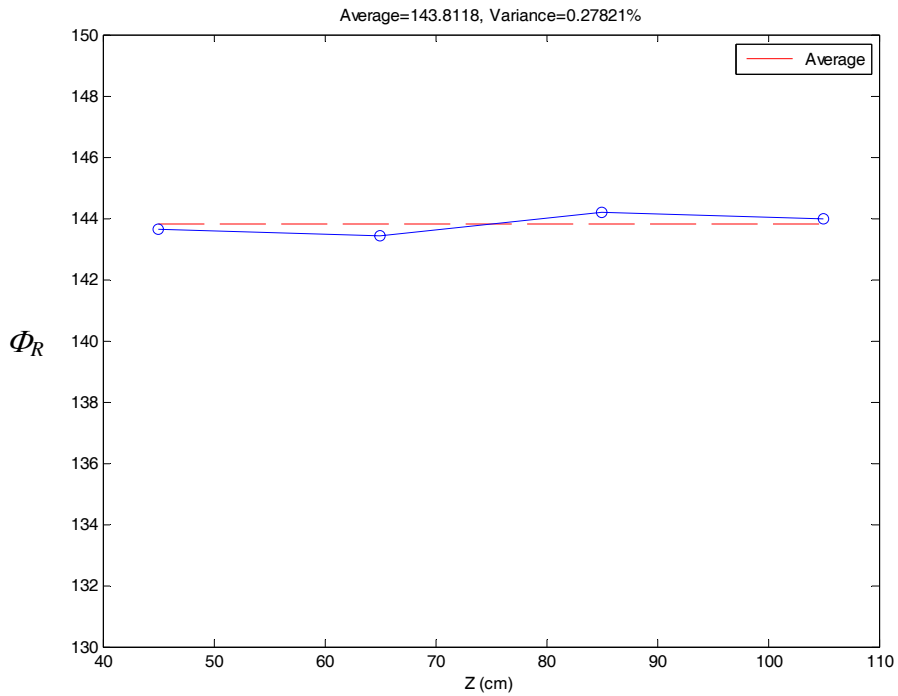
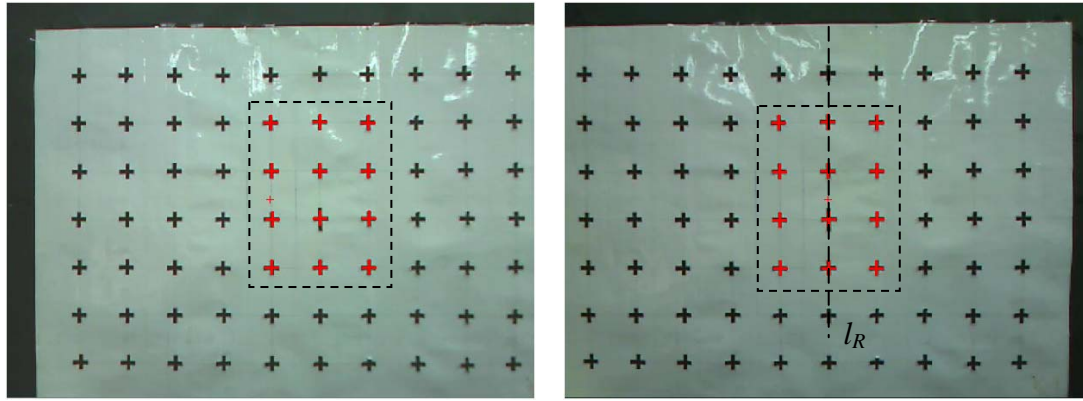
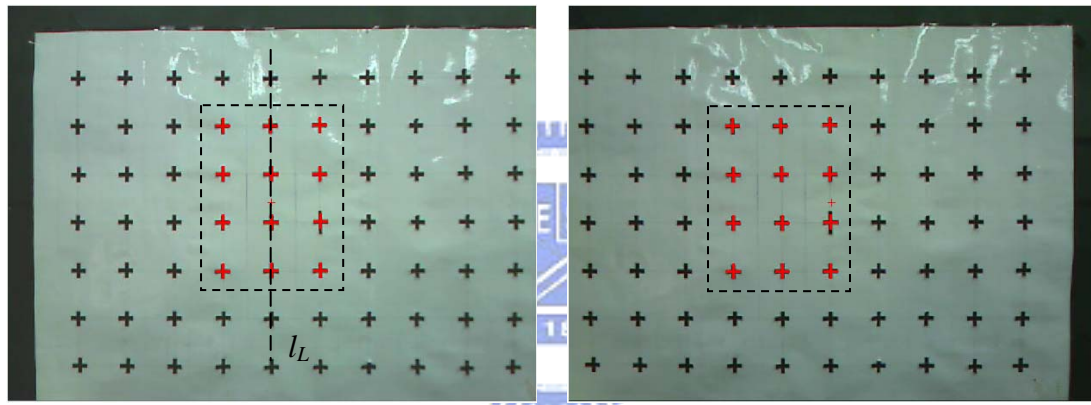


Fig. 4.4  $\Phi_R$  for different distance Z from 45 cm to 105 cm



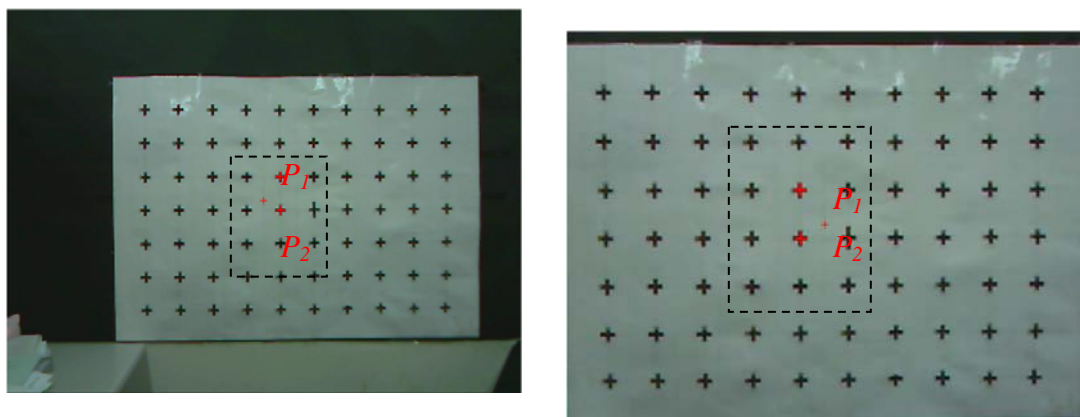
(a)

(b)

Fig. 4.5 The same 12 points using to calculate  $\Phi_L$  for  $Z=95\text{cm}$ 

(a)

(b)

Fig. 4.6 The same 12 points using to calculate  $\Phi_R$  for  $Z=95\text{cm}$ 

(a)

(b)

Fig. 4.7 Two adjacent points  $P_1$  and  $P_2$  in the center line of the training area for  $Z=135$

Human eyes always focus on the center of entire eyeshot. Based on this characteristic, two adjacent points  $P_1$  and  $P_2$  in the center line of the training area, within eyeshot center of HVS, on the experimental board was shown in Fig. 4.7 are chosen as the testing points.  $P_1$  and  $P_2$  used to acquire test the error between depth detection result and actual depth.

The average error is computed by mean absolute error that can be written as

$$e_{ma} = \text{mean} \left[ \left| Z - \hat{Z} \right| \right] \quad (4.1-5)$$

where  $e_{ma}$  is the mean absolute error of the network.  $Z$  and  $\hat{Z}$  denote the depth that is actually measured and the corresponding depth given by the network respectively. Therefore, to represent distinct situation of  $e_{ma}$ , four different conditions are schemed as shown in the Fig. 4.8 to Fig. 4.11. The first case represent two cameras of HVS are placed in parallel with the same focal length. The second case is respect to distinct focal length. The third case is respect to insignificant deflection between optic axes of two cameras. And for the last case distinct focal length and insignificant deflection are included.

Case I

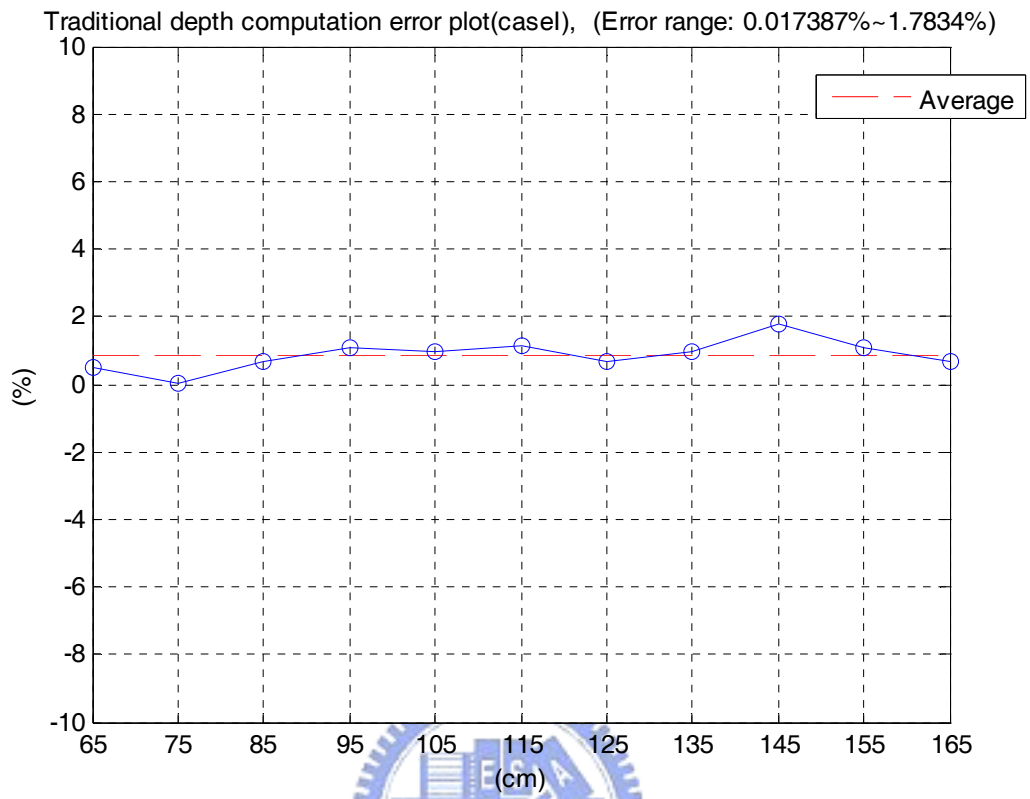


Fig. 4.8  $e_{ave}$  of two cameras placed in parallel with the same focal length

Case II

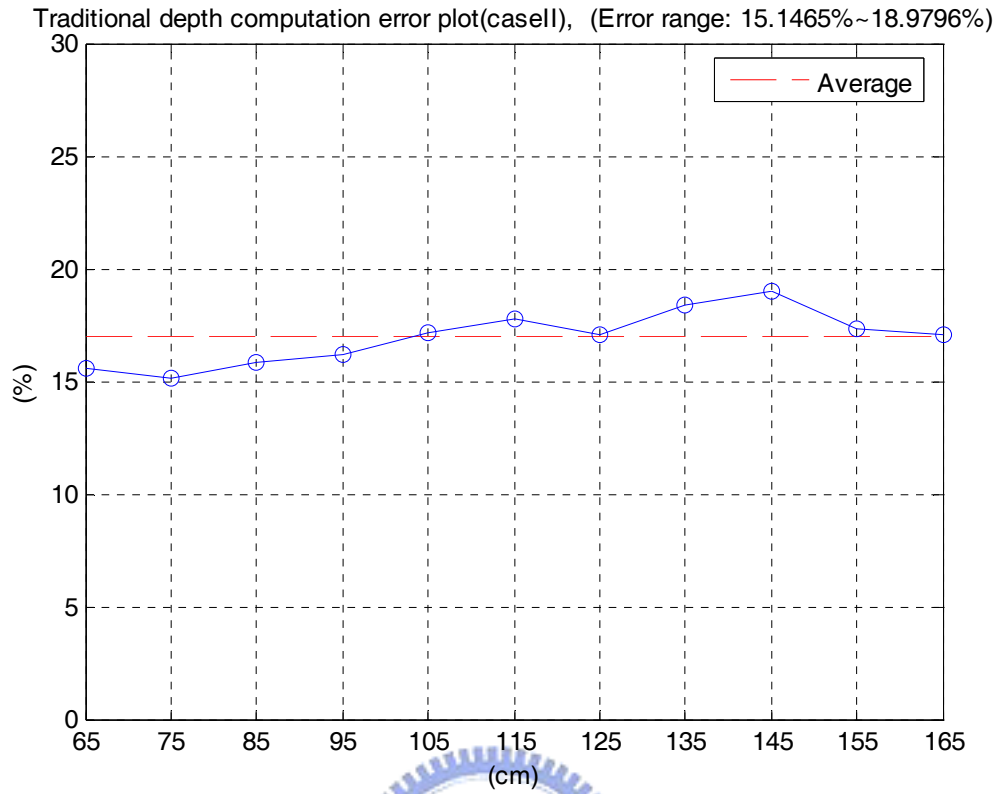


Fig. 4.9  $e_{ave}$  of two cameras with distinct focal length

Case III

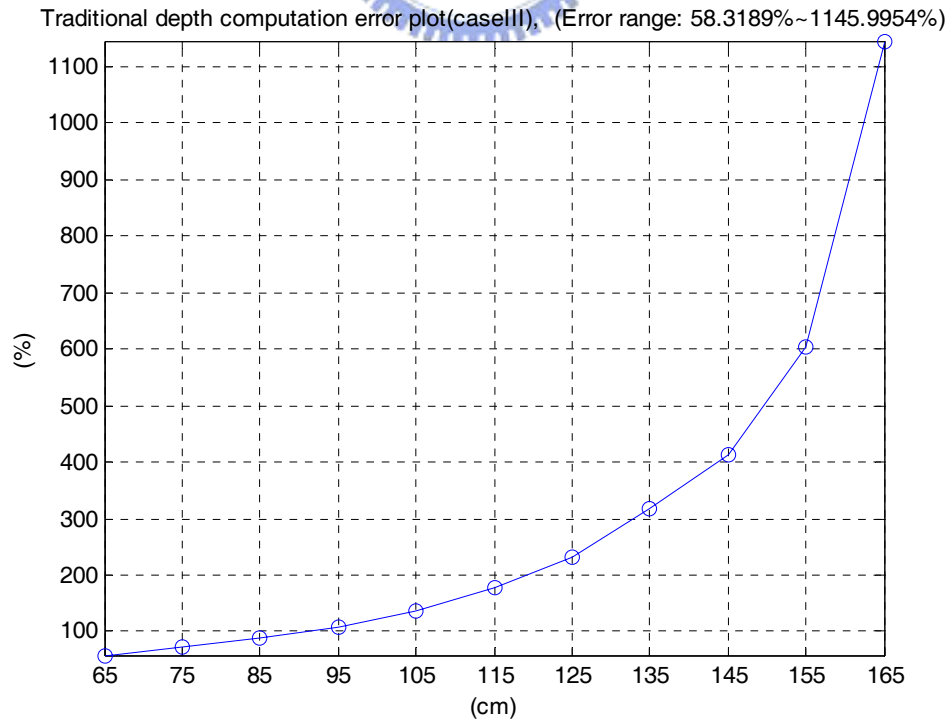


Fig. 4.10  $e_{ave}$  of two cameras with insignificant deflection between optic axes

## Case IV

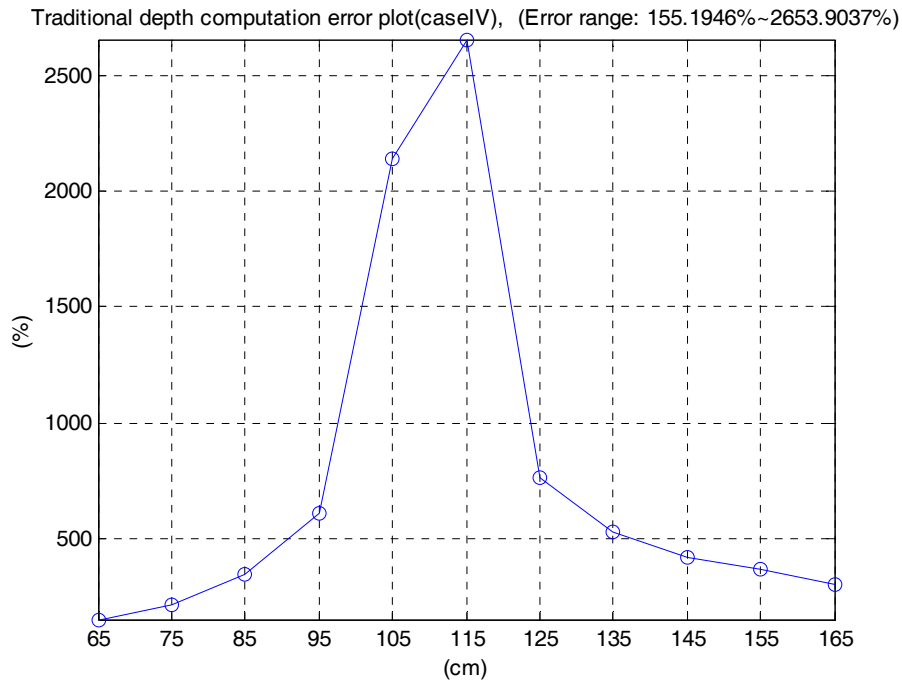


Fig. 4.11  $e_{ave}$  of two cameras with distinct focal length and insignificant deflection

These figures show that the  $e_{ma}$  of the actual depth range in 65 to 165 cm of case I is between 0.017387% and 1.7834%, case II is between 15.1465% and 18.9796%, case III is between 58.3189% and 1145.9954% and case IV is between 155.1946% and 2653.9037%. The maximum of percentage error results of these case are greater than 15% except case I. This is mean that the algorithm only is used in the situation similar to case I, or else need to rewrite the formula with more parameter to fit all situation able to appear.

## 4.2.2 Flexibility of ANN Depth Detection Algorithm

The existence of restrictions on Traditional depth detection algorithm is already confirmed and shown in previous subsection. In order to unrestricted, the ANN depth detection algorithm proposed in this thesis.

The ANN architecture for depth detection will evaluate by experimentation. Here, the number of neuron in the output layer need to be decides first. One case is three neurons which respectively corresponding to the world coordinates ( $X$ ,  $Y$ ,  $Z$ ) of the world object point in the output layer and another one is just one neuron for depth  $Z$ . The case IV in the previous subsection is used to treat as the general case in the problem. The training data of the neural network is the same 12 points in left and right of each image, with different distance  $Z$  from 65cm to 165cm at an increment of 20cm. To check the accuracy of the trained network, we presented the network with stereo-pair points that were not completely included in the training set but were from within our range of interest of distance. The testing data is the two same points; they are adjacent, as introduced in the previous subsection in the left and right image with different distance  $Z$  from 65cm to 165cm at an increment of 10cm. After the training process had finished, each neural network is tested with the training and testing data sets.

Fig. 4.12 shown the  $e_{ma}$  in each depth simulated from the net that consists of four input neurons, five hidden neurons and three output neurons. As the diagram indicates, the  $e_{ma}$  ranges from 0.48455% to 2.4771%. The maximum  $e_{ma}$ , 2.4771%, represents the error of its corresponding net. Each different number of neuron creates ten distinct nets and the  $e_{ma}$  of ten nets shown in Fig. 4.13 with five hidden neurons. The average of  $e_{ma}$  from ten nets with the same number of neurons  $H_n$  in hidden layer,  $e_{ma_{H_n}}$ , represent the error of  $H_n$  neurons where  $H_n$  starts form 1 to 10. Fig. 4.14 and Fig. 4.15



show each  $e_{ma_{Hn}}$  with one and three output neurons respectively. It is clearly to find that the error range of one output neuron is always greater than three output neurons. For accuracy, the three output neuron is chosen in the proposed architecture.

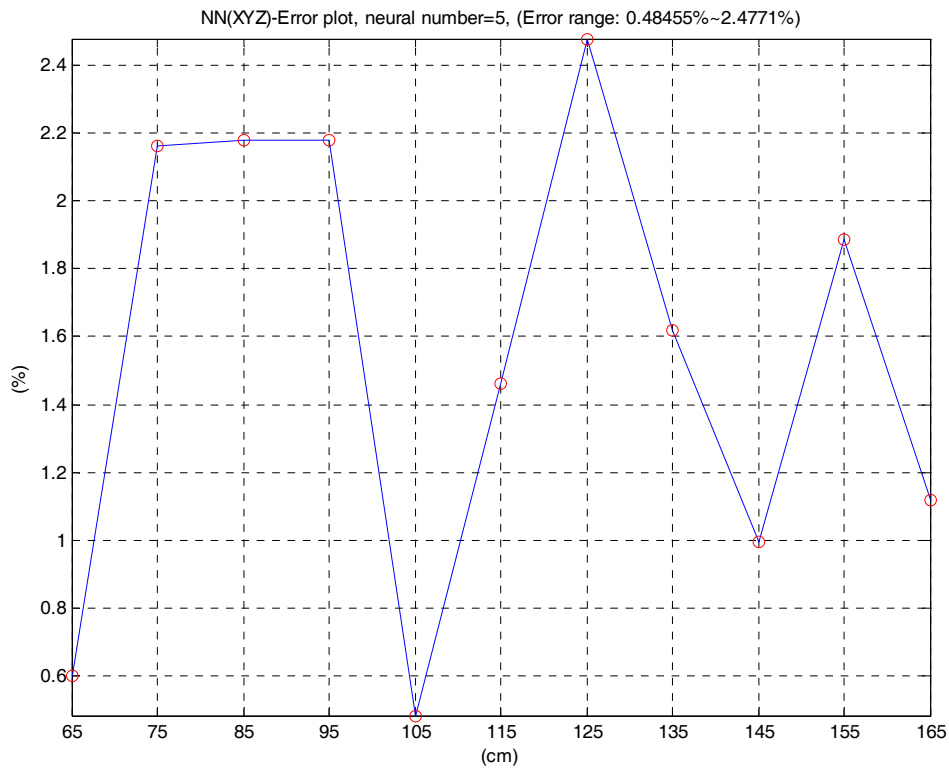


Fig. 4.12  $e_{ma}$  in each depth simulated from the net

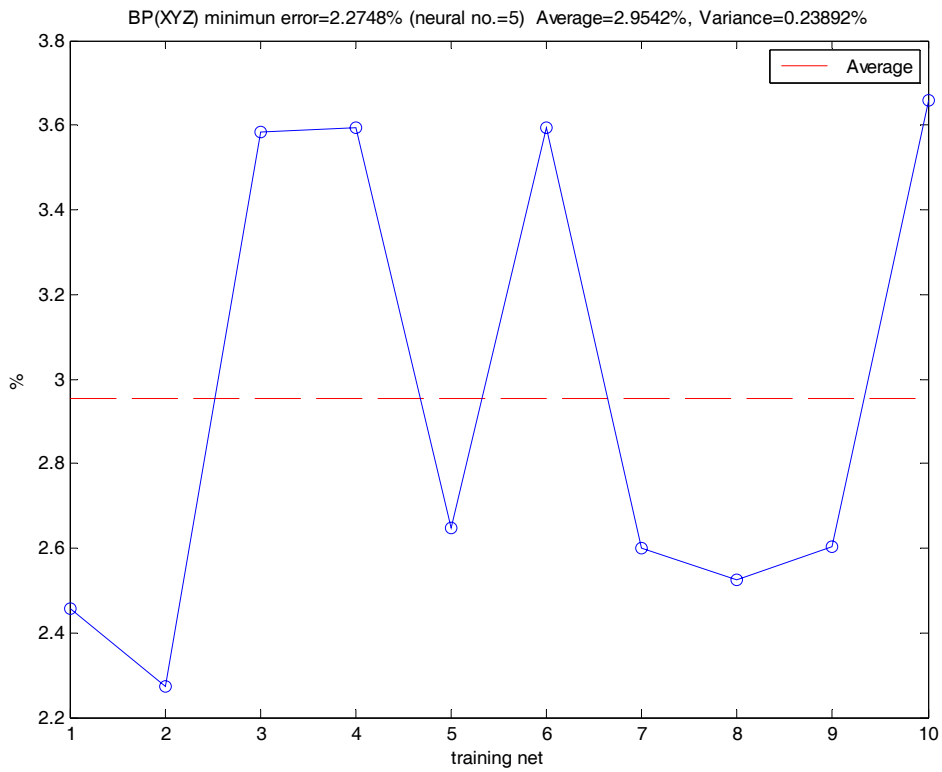


Fig. 4.13  $e_{ma}$  of ten nets with five hidden neurons

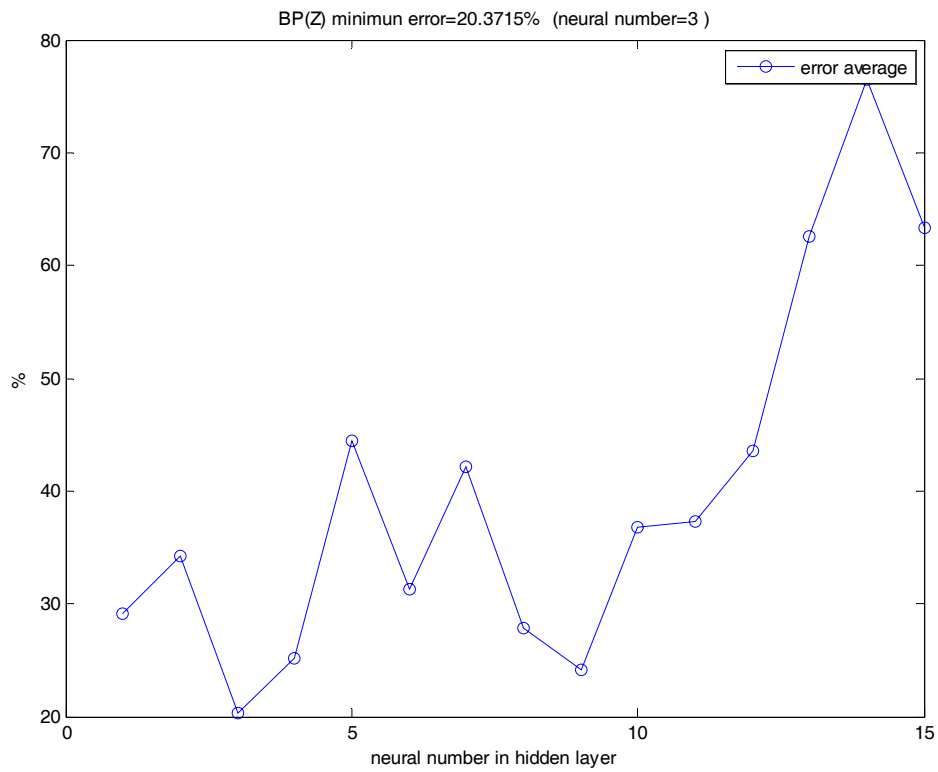


Fig. 4.14 Each  $e_{ma_{Hn}}$  with one output neuron

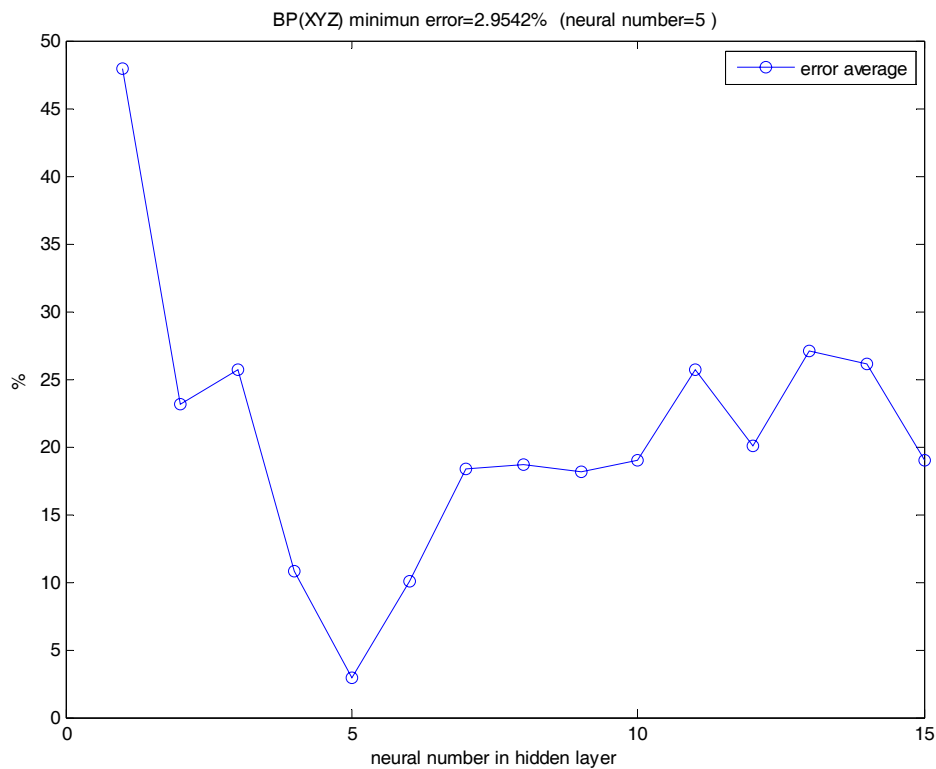


Fig. 4.15 Each  $e_{ma\_Hn}$  with three output neurons

After decide the number of output neuron, the number in the hidden layer is proceeded to be resolved. From Fig. 4.15 also tells us that the best choice for neuron number in the hidden layer in the problem is five. Therefore, we may reasonably conclude that the better MLP network architecture for detecting depth should be consists of four input neurons, five hidden neurons and three output neurons.

In order to eliminate the net that doesn't train the training data successfully, a threshold value T of  $e_{ma}$  from training data need to be set. If the  $e_{ma}$  form training data of the net is large than T, the net will not be enrolled. The setting value H must be large than the  $e_{ma}$  from training data such that the network could.

The error results can be seen for different case introduced in subsection from proposed net is shown from Fig. 4.16 to Fig. 4.19. They can be noted that even in the worst case, the error in depth computation was still well below 4%.

Case I

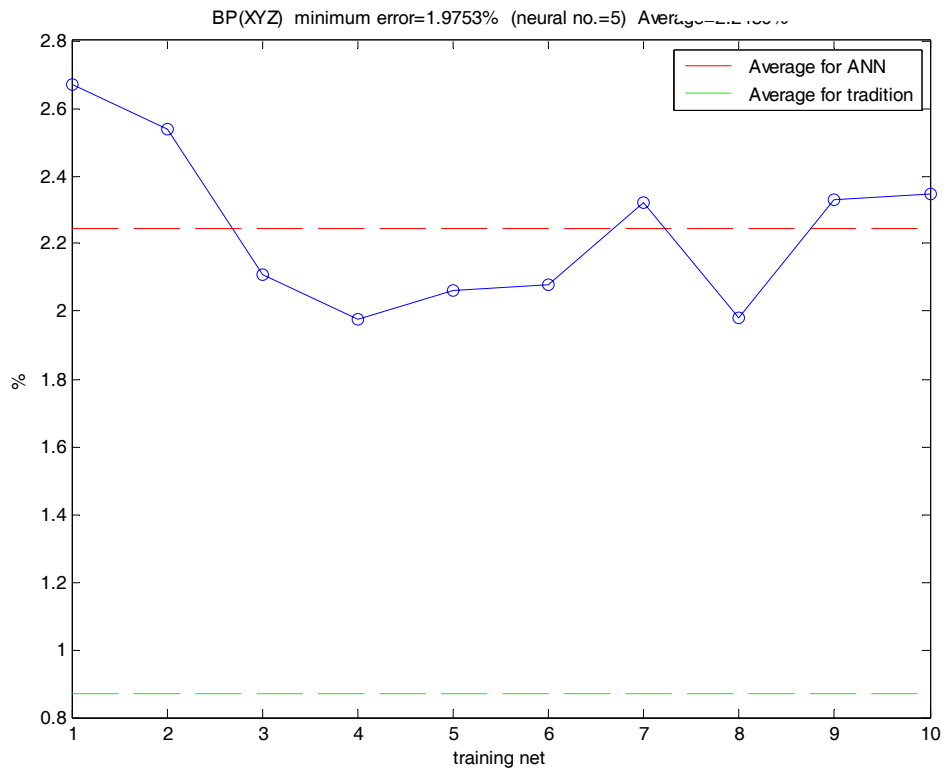


Fig. 4.16 Each  $e_{ma_{Hn}}$  from proposed net of Case I

Case II

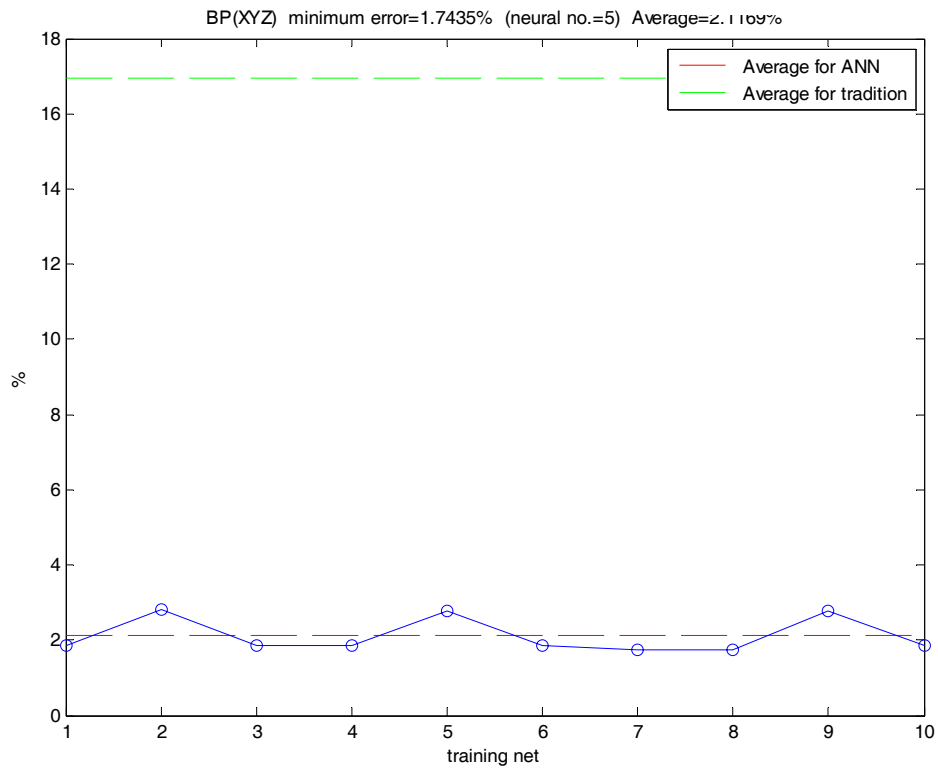


Fig. 4.17 Each  $e_{ma\_Hn}$  from proposed net of Case II

Case III

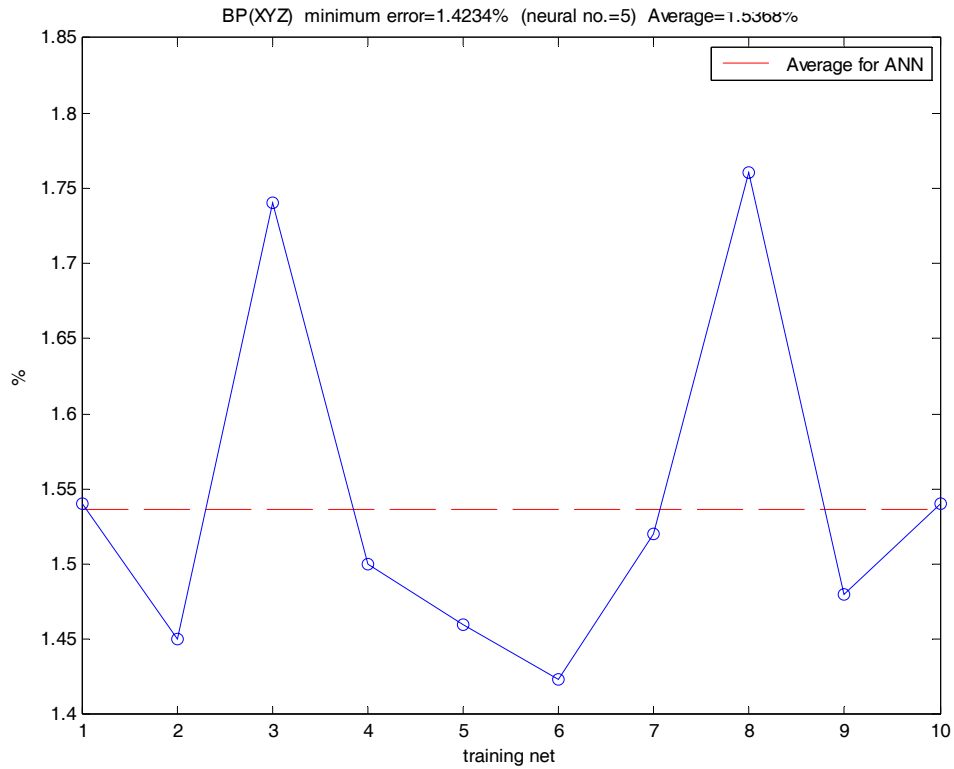


Fig. 4.18 Each  $e_{ma_{Hn}}$  from proposed net of Case III

Case IV

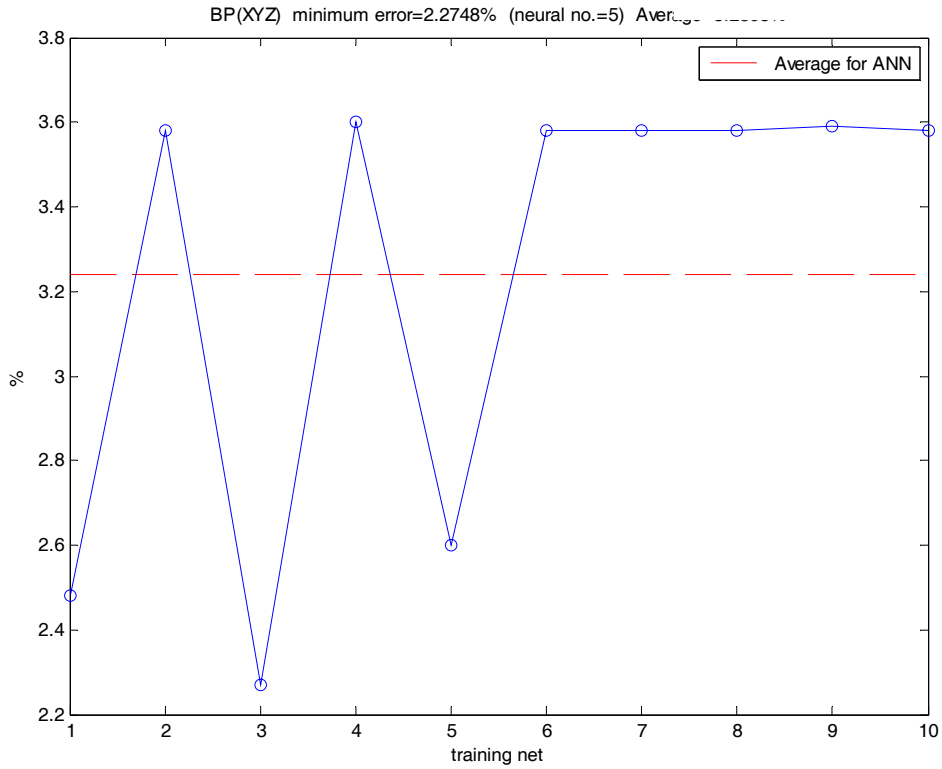


Fig. 4.19 Each  $e_{ma_{Hn}}$  from proposed net of Case IV

The training data is obtained from stereo pair manually. The reason for decreasing the number of inputs was to determine whether the desired depth values could still be achieved with acceptable accuracy. Therefore, if the training data is only obtained from  $Z=65$  and  $165\text{cm}$ , the testing error average is  $53.0081\%$  as shown in Fig. 4.20. Fig. 4.21 and Fig. 4.22 are shown the testing error of training data is obtained from  $Z=65, 115, 165\text{cm}$  and  $Z=65, 95, 135, 165\text{cm}$  respectively. The Fig. 4.22 indicates that the training data with four distinct depths can get the result with error around  $5\%$ .

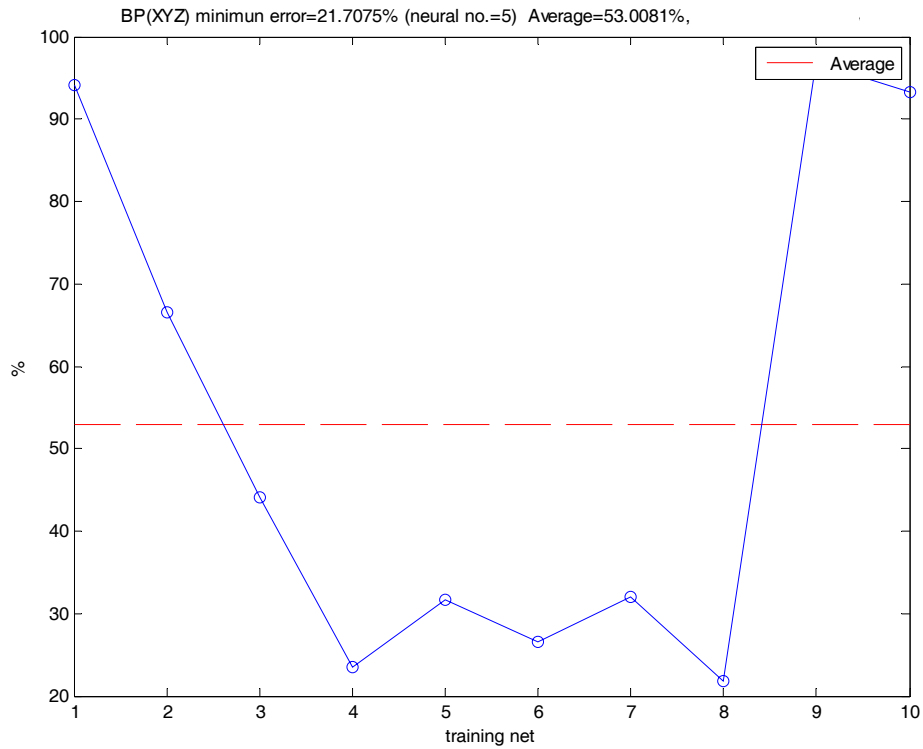


Fig. 4.20 The testing error of training data is obtained from Z=65 and 165cm

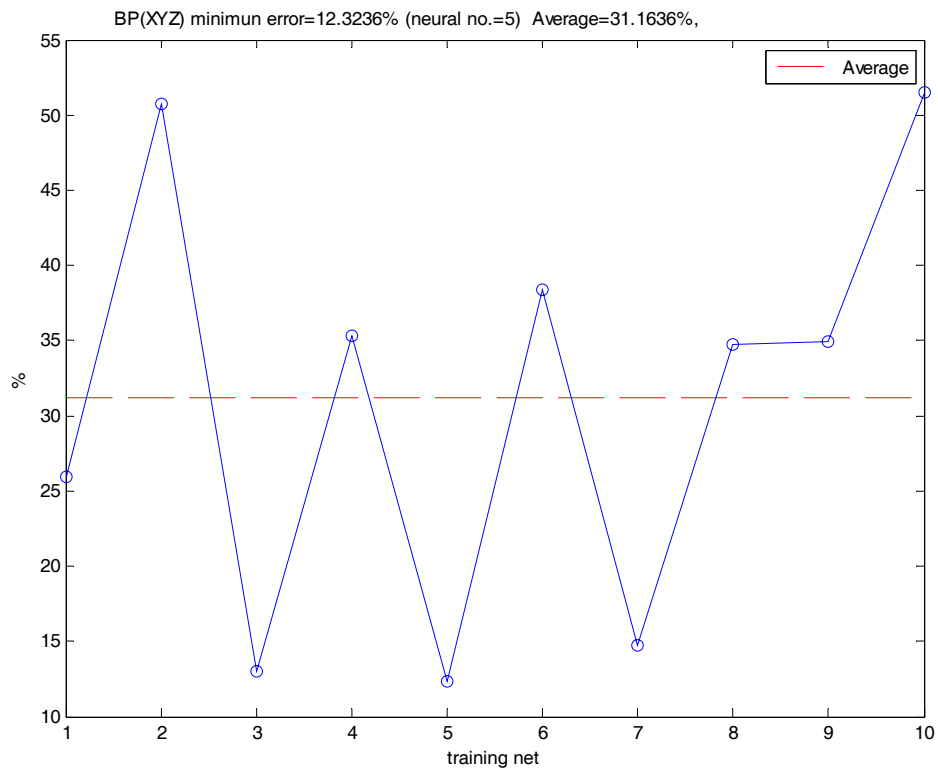


Fig. 4.21 The testing error of training data is obtained from Z=65, 115, 165cm

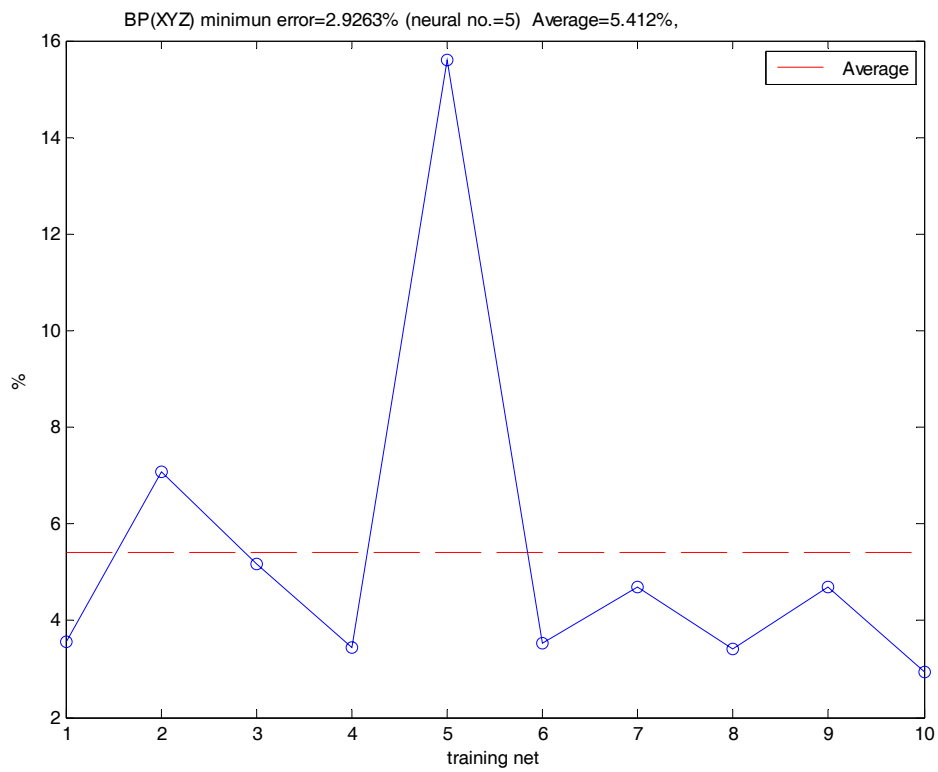


Fig. 4.22 The testing error of training data is obtained from Z=65, 95, 135, 165cm

The algorithm is different from traditional detection depth algorithm in the sense that no extrinsic or intrinsic camera parameters are found for any of the camera. The system is trained such that it learns to directly find the depth of objects.



# Chapter 5

## Conclusion

The proposed algorithm in this thesis has shown that it is possible to use a neural network to compute actual depth with good accuracy. The thesis used an ANN to train the system such that, when the system is presented with a matched pair of points, it automatically computes the depth of the corresponding object point. The algorithm differs from traditional depth detection algorithm to the problem. That is, there are restrictions for using Traditional depth detection algorithm and the network is trained to compute the correct depth of two matched points without any calibration. The algorithm that is used in this thesis is very simple in concept, independent of the camera model used and the quality of image obtained and yields very good results.

The experimental results in the thesis show that an acceptable accuracy can be obtained but it seems that is not very easy to reach high accuracy by using only neural networks. Neural networks have a good generalization capability in the range that they are trained.

If the depth of the world object can easy be obtain from the HVS, the HVS can be applied to an autonomous mobile robot using stereo vision for navigation, real time track nearest object in front region or locate the interesting object.

The future work for the learning algorithm is to simulate human learning behavior. Just like human learning structure, the learning network will learn in turn stroke by stroke, not in case of learn once for all.

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