國 立 交 通 大 學 電子工程學系電子研究所

碩士論文

應用於正交分頻多工技術為基礎之

無石英無線近身網路同步器

Synchronization Method for

Crystal-less OFDM-based

Wireless Body Area Network Applications

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中華民國九十八年七月

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A Thesis

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摘要

在本篇論文裡,介紹一個正交分頻多工系統的同步方法,應用於無石英震盪器之無 線近身網路,來增加整個系統收發端的頻率誤差容忍度。

無線近身網路為主的健康照護的系統越來越受人們的重視,尤其是針對人體生醫訊 號的偵測,可降低醫療成本以及提高醫療成效。應用情境如配戴在身上的無線感測器對 人體訊號做長時間的偵測,並以無線的方式將資料傳送給整合在手機或個人數位助理的 接收端。基於這樣的一個應用,極低的功率消耗跟高度整合的面積會是系統不可或缺的 需求,因此我們使用了互補式金屬氧化層半導體震盪器取代傳統產生系統時脈的石英震 盪器,以降低系統功率消耗以及提升整合度。

無石英震盪器現階段技術尚未成熟,使用此系統會造成收發段頻率誤差大的問題, 造成整個系統收發資料損失。於是本篇論文提出了一種套用於正交分頻多工的基頻同步 演算法配合一個可以調整的數位控制震盪器已達到減少收發端頻率誤差的效果。

將晶體振盪器整合進單一晶片中,可以降低系統的製造成本、面積及功率消耗。在 本篇論文我們對整個正交分頻多工無線近身網路系統的行為做一個詳盡的闡述,並分析 頻率校準的基頻演算法,最後建立了一個正交分頻多工的基頻原型來驗證這樣的行為。 這個方法套用在此論文之應用系統可使整個系統的頻率誤差容忍度拓展為140倍,進而 達到小面積,低功率,高整合度的基頻系統晶片設計。

Synchronization Method for Crystal-less OFDM-based Wireless Body Area Network Applications

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Abstract

In this thesis, we propose a synchronization method for crystal-less OFDM-based wireless body area network (WBAN) applications to enlarge the frequency error tolerance between the transmitter and receiver.

WBAN systems for ubiquitous health monitoring are gradually attracting many attentions. This can reduce the medical cost and improve medical treatment outcomes. The wireless sensor node (WSN) nodes are placed on the human body allowing long-term health monitoring. Those gathered signals from a multiple of WSNs are wirelessly transmitted to a remote central processing node (CPN), such as mobile phone or PDA. Based on these applications, low power and highly integration properties are indispensable. To meet these needs, the CMOS oscillator is applied instead of the conventional quartz crystal oscillator.

However, the crystal-less technology does not come to maturity. It causes large frequency error in the system using the crystal-less oscillator. We propose a synchronization method for OFDM-based WBAN systems. Applying the crystal-less oscillator in the system, the area and power can be reduced a lot. In this thesis, a complete WBAN system and the novel synchronization algorithm are described. An OFDM emulation system is also established. In our application system, the overall frequency error tolerance is expanded to 140x, enabling the tiny area and highly integration SOC design.

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在 Si2 實驗室的碩士班研究過程中,讓我學到了非常多的東西,過程相當充實。在 碩班的日子裡,幾乎每天待在實驗室的時數平均超過 14 小時,假日也還是在實驗室過, 但還是樂此不疲。

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-III-

摘要	I
Abstract	II
誌謝	III
CONTENTS	IV
LIST OF FIGURES	VIII
LIST OF TABLES	XI
Chapter 1	1
Introduction	1
1-1 Introduction to WBAN Systems	1
1-2 Introduction to Crystal-less Systems	2
1-3 Motivation	5
1-4 Design Target	7
1-5 Outline of the Thesis	
Chapter 2	9
Application System	9
2-1 Overview	9
2-2 System Behavior	
2-2-1 Downlink	
2-2-2 Uplink	
2-3 Packet Format	
2-3-1 Short Preamble	
2-3-2 Long Preamble	
2-3-3 Packet Format	
2-4 WiBoC System Block Diagram	
2-4-1 Wireless Sensor Node	
2-4-2 Central Processing Node	
2-5 Channel Model	

2-5-1 AWGN	
2-5-2 Carrier Frequency Offset	
2-5-3 Sampling Clock Offset	
2-5-4 Link Budget	
2-6 Frequency Allocation	
Chapter 3	
Synchronization PAFEE Method	
3-1 PAFEE Packet Detection Algorithm	
3-1-1 Conventional Algorithm	
3-1-2 Proposed Algorithm	
3-2 PAFEE Frequency Error Estimation Algorithm	
3-2-1 Conventional Algorithm	
3-2-2 Proposed Algorithm	
3-3 PAFEE Method Flow	
Chapter 4	
Simulation Results and Performance Analysis	
4.1 Simulation on DAFEE Deduct Detection	50
4-1 Simulation on PAPEE Packet Detection	
4-1-1 ROC Curves	
4-1-2 Detection Rate, False Alarm Rate versus SNR	
4-1-5 Detection Rate Versus Frequency Error Estimation	
4-2 Simulation on PAFEE Frequency Error Estimation	01
4-3 Simulation on System PER Performance	
Chapter 5	
Hardware Implementation	
5-1 Overall Architecture	
5-1-1 Packet Detector	
5-1-2 Phase Rotator	
5-1-3 Frequency Error Estimator	71
5-2 Simulation on Quantization Results	
5-2-1 Simulation on PAFEE Packet Detection	
5-2-2 Simulation on PAFEE Frequency Error Estimation	

5-2-3 Simulation on System PER Performance	
5-3 Hardware Overhead	
Chapter 6	
Emulation of Crystal-less Baseband System	
6-1 Building Block	
6-2 Evaluation System	
6-3 Emulation Results	
Chapter 7	
Conclusions and Future Work	
7-1 Conclusions	
7-2 Future Work	
References	
Appendix A	
Embedded Crystal Design	
A-1 Introduction 1896	
A-2 Proposed DCO	
A-2-1 DCO Architecture	
A-2-1 Coarse-tuned Stage	
A-2-2 Fine-tuned Stage	
A-3 Measurement Results	
A-3-1 Coarse-tuned Stage	
A-3-2 Fine-tuned Stage	
A-4 System Comparison	
A-5 Conclusion	
Appendix B	
IP Deliverable	
B-1 Overall Architecture	
B-2 Architecture of Receiver	

B-2-1 Components	
B-2-3 External Signal Descriptions	
B-2-3 FSM	
B-2-4 Area	
B-2-5 Power	
B-3 Architecture of Transmitter	
B-3-1 Components	
B-3-2 External Signal Descriptions	
B-3-3 FSM	
B-3-4 Area	
B-3-5 Power	



LIST OF FIGURES

Figure 1-1: Motivation, pros and cons	6
Figure 1-2: Motivation and PAFEE method	6
Figure 2-1: The target operation scenario of WBAN system	
Figure 2-2: WiBoC system behavior	
Figure 2-3: WiBoC system device connection behavior	11
Figure 2-4: Short preamble format	
Figure 2-5: Preamble format with 24-tone in frequency domain	14
Figure 2-6: Preamble format with 6-tone in frequency domain	15
Figure 2-7: Long preamble format in time domain	17
Figure 2-8: Downlink packet format	
Figure 2-9: Uplink packet format.	
Figure 2-10: WSN block diagram	
Figure 2-11: CPN block diagram	21
Figure 2-12: CFO effect	
Figure 2-13: mathematical CFO model	
Figure 2-14: MATLAB CFO model	
Figure 2-15: SCO effect	
Figure 3-1 (a): ROC curves from mathematics deduction	
Figure 3-1 (b): ROC curves from mathematics deduction (Zoom-in)	
Figure 3-2: ROC curves under different M	
Figure 3-3: Frequency error estimation block	
Figure 3-4: Synchronization PAFEE algorithm flow	
Figure 4-1(a): Frequency error estimation block	
Figure 4-1(b): Frequency error estimation block (Zoom-in)	
Figure 4-3: ROC curves in different L	
Figure 4-4: ROC curves in conventional one and proposed one	

LIST OF FIGURES

Figure 4-5: Detection rate in conventional one and proposed one	58
Figure 4-6: False alarm rate in conventional one and proposed one	58
Figure 4-7: Detection rate under different CFO and SCO conditions, SNR=1 dB	59
Figure 4-8: Detection rate under different CFO and SCO conditions, SNR=2 dB	60
Figure 4-9: Detection rate under different FO and SNR conditions	61
Figure 4-10: Estimation corrent rate versus frequency error	
Figure 4-11 (a): Maximum remaining error versus frequency error	
Figure 4-11 (b): Maximum remaining error versus frequency error (Zoom-in)	
Figure 4-12: Packet error rate versus SNR, N=3	
Figure 4-13: Packet error rate versus SNR, N=1	
Figure 5-1: Overall architecture of WSN system	
Figure 5-2: Hardware architecture of packet detector	68
Figure 5-3: Hardware architecture of moving average	69
Figure 5-4: Hardware architecture of phase rotator in packet detection state	69
Figure 5-5: Hardware architecture of phase rotator after detecting the packet	71
Figure 5-6: Hardware architecture of frequency error estimator	
Figure 5-7: Real part of the Ri, i is from 1 to 16	72
Figure 5-8: Imaginary part of the Ri, i is from 1 to 16	73
Figure 5-9: Fixed point ROC curves	74
Figure 5-10: Fixed point detection rate under different frequency error condition	75
Figure 5-11: Fixed point estimation correct rate versus frequency error	76
Figure 5-12: Fixed point maximum remaining error versus frequency error	77
Figure 5-13: Fixed point packet error rate versus SNR	
Figure 6-1: Hardware emulation building blocks	
Figure 6-2: Evaluation system	82
Figure 6-3: Received signal shown in spectrum analyzer	84
Figure 6-4: Estimation results with frequency error 0, 400, 800, 1200 ppm	
Figure 6-5: Estimation results with frequency error 1600, 2000, 2400, 2800 ppm	87
Figure A-1: DCO Architecture	97

LIST OF FIGURES

Figure A-2: Coarse-tuned stage	
Figure A-3: Schmitt trigger cell	
Figure A-4: Fine-tuned stage	
Figure A-5: The period of DCO in coarse-tuned stage	
Figure A-6: The RMS jitter of DCO in coarse-tuned stage	
Figure A-7: The period of DCO in fine-tuned stage	
Figure A-8: The RMS jitter of DCO in fine-tuned stage	
Figure B-1: Overall architecture of WSN system	
Figure B-2: FSM of WSN_RX	
Figure B-3: P&R view of WSN_RX	
Figure B-4: FSM of WSN_TX	
Figure B-5: P&R view of WSN_TX	



LIST OF TABLES

LIST OF TABLES	PAGE
Table 1-1: The power consumption, area, and cost of the quartz crystal [11]	3
Table 1-2: Existing solutions for crystal-less communications systems	4
Table 1-3: Candidate clock source in CMOS technology	4
Table 1-4: WBAN system with their allowable frequency errors	5
Table 1-5: Design target	7
Table 2-1: Link Budget	
Table 5-1: Area overhead	79
Table 5-2: Power overhead	
Table 6-1: Baseband components	
Table 6-2: The relationship between frequency error and clock period	
Table 7-1: System comparison summary	
Table 7-2: WiBoC OFDM system summary	
Table A-1: Delay element in coarse-tuned stage	
Table A-2: Delay element in fine-tuned stage	
Table A-3: DCO in coarse-tuned stage.	
Table A-4: DCO in fine-tuned stage	
Table A-5: DCO power consumption under different supply voltage	
Table A-6: DCO performance comparison	
Table B-1: The component in WSN_RX	110
Table B-2: Mode of operation in WSN_RX	111
Table B-3: External signal description in WSN_RX	
Table B-4: State description in WSN_RX	
Table B-5: Area reports in WSN_RX	
Table B-6: Power classification and definition	
Table B-7: Power report in WSN_RX	
Table B-8: The component in WSN_TX	
Table B-9: Mode of operation in WSN_TX	

LIST OF TABLES

Table B-10: External signal description in WSN_TX	118
Table B-11: State description in WSN_TX	119
Table B-12: Area report in WSN_TX	120
Table B-13: Power report in WSN_TX	121



Chapter 1 Introduction

1-1 Introduction to WBAN Systems

With the progress of the medical technology, there are more and more accurate and higher-level instruments invented in the hospitals. These devices help human to observe their disease in early time. The doctor will prevent and cure the disease efficiently.

In recently years, the ubiquitous healthcare devices are presented to the public and explode to be popular. Ubiquitous healthcare monitoring plays a crucial role in body signal tracking and recording. The patients want comfortable and portable devices to examine their physical status. This device is not only portable and convenient, but extends medical services from an indoor room to any open roaming spaces.

The wireless body area network (WBAN) is designed for the applications of body signal gathering and monitoring to provide reliable physical information. It is composed by a multiple of wireless sensor nodes (WSN), and a central processing node (CPN). The WSN is capable of sampling, processing, and communicating the body information to the CPN. These nodes are placed on the human body as tiny patches. They are comfortable and convenient for human to observe their physical status in any time from the CPN. The CPN is built in some portable devices, such as PDA, cell phones, or personal laptop. Existing solutions for the WBAN applications could be found in [1-5]. The well-defined systems, e.g. Bluetooth [1] and Zigbee [2], are designed for widespread applications, including entertainment, positioning, factory product management, and healthcare. With the increasing demands in wireless body area applications, however, these two candidate systems have difficulties to meet the consumer electronic devices functions and the healthcare at the same time.

There are also some customized systems, MIThrils [3], CodeBlue [4], and Human++ [5], are explored for WBAN system constructions in body-oriented applications.

It is our intention to design WBAN systems to be tiny and low power. To achieve the target, the crystal replacement method is used. It is called crystal-less system if the system does not have a crystal oscillator as its clock source.

1896

1-2 Introduction to Crystal-less Systems

With the progress of the system on chip (SoC) technology, the most of the circuits in a system can be integrated in one chip. Applying the SoC technology in communications system is very attractive. Nowadays the baseband circuits are integrated in one chip except the clock source, a crystal oscillator.

Though the crystal oscillator plays an important role for system clock, it boosts the effort in system integration. The quartz crystal consumes a lot of power and occupies large area in the chip, as shown in Table 1-1 [11].

Ch1. Introduction

Power consumption	In-crystal	1µW~200µW	
	Oscillator	1mW~50mW (active)	
		10μW~50μW (standby)	
Aroo	SMD	3.2mm x 2.5mm x 0.5mm	
Area	DIP	11.5mm x 4.7mm x 3.5mm	
Cost		US\$0.15~2	

Table 1-1: The power consumption, area, and cost of the quartz crystal [11]

Wireless sensor nodes require transceivers that are small, cheap, and power efficient. To achieve better integration and less power, more cost-effective baseband chip applications, the crystal-less system is explored. One solution of the crystal-less system, which has a self-calibrated embedded crystal (eCrystal), is proposed by NCTU [6]. The eCrystal system uses its embedded clock generator instead of a crystal oscillator.

There are some existing customized solutions for crystal-less communications systems [7-10]. The CMOS circuits are used as a system reference clock in the chip, e.g. ring oscillator, digital controlled oscillator, and voltage controlled oscillator. The CMOS circuits are sensitive to the process, voltage, and temperature (PVT) variations. The customized solutions use some frequency-insensitive modulation to overcome the inaccuracy of system clock. The following table shows the modulation and oscillator design of the existing solutions for crystal-less communications systems. The initial error of the oscillator is large, i.e, above 1%.

Systems	modulation	oscillator design	initial error
[7] ISCAS 2008	IR + PPM	CMOS clock generator	1.1 %
[8] ISSCC 2008	OOK	CMOS Ring Oscillator	2.5 %
[9] PIMRC 2006	BFSK	voltage controlled oscillator	1 %
[10] ISSCC 2009	ASK	Ring Oscillator	N/A

Table 1-2: Existing solutions for crystal-less communications systems

In the proposed eCrystal system, the clock source is designed. Table 1-3 shows some candidates clock source made in CMOS technology. The LC tank oscillator is not suitable in our design due to its large frequency drift and large power. Though the MEMS oscillator has good properties about the frequency drift and power, it is not taken into consideration due to its non-standard process and long processing period.

The eCrystal method in NCTU has been proposed in self-defined system specification with generation frequency 5MHz and frequency drift 0.28%.

	LC [31]	MEMS [32]	RO [33]	eCrystal
Process	CMOS	CMOS/ MEMS	CMOS	CMOS
Fgen	Carrier freq.	Wide	7MHz	5MHz
	0.1~10GHz	1.5~4GHz		
Frequency	10~15%	±0.03%	±2.65%	±0.28%
Power	6~20mW	0.1mW	1.5mW	0.25mW
Freq.	Yes	N/A	N/A	Yes

Table 1-3: Candidate clock source in CMOS technology

4

1-3 Motivation

To achieve the low-power and highly integrated ubiquitous healthcare monitoring applications, we apply the crystal-less technology in the WBAN system.

The communications systems need accurate clock generator, or the data won't be correctly recovered in the receiver side. Table 1-4 shows the existing WBAN system and their allowable frequency error tolerance.

Systems	modulation	Frequency Error Tolerance
[1] Bluetooth	FHSS	±20ppm
[2] Zigbee	DSSS	±40ppm
[3] MIThril	FHSS 1	396 ±30ppm
[4] CodeBlue	DSSS	±25ppm
[5] Human++	UWB	N/A

Table 1-4: WBAN system with their allowable frequency errors

The allowable frequency error tolerance is very small, i.e, below 40ppm. The clock generator is designed with limited initial frequency offset, say 0.28%, under process, voltage, and temperature variations.

The target is to establish a standard compatible system with crystal replacement. The OFDM-based system is selected. Due to the low precision of the eCrystal oscillator, our motivation is to design a baseband calibration algorithm to detect the clock error and compensate the frequency mismatch between the transmitter and the receiver as shown in Figure 1-1.



Figure 1-1: Motivation, pros and cons

For the large clock error, the first problem encountered is that packet is undetectable. The algorithm of detecting the packet under large frequency error is proposed. After the packet detection, the frequency error is estimated and feedback to the clock generator. The algorithm is called packet detection and frequency error estimation (PAFEE) method, as shown in Figure 1-2.



Figure 1-2: Motivation and PAFEE method

A system defined as wireless body on the chip (WiBoC), based on the OFDM scheme is used as the evaluation platform in this thesis. The crystal-less system behavior and hardware design will be discussed and analyzed. The prototype platform is also established to verify the behavior of the overall system.

1-4 Design Target

In the self-defined crystal-less system, there is frequency drift 0.28% in our eCrystal clock generator. To solve the large frequency error and have the performance remain the same, we have to reach the design target as shown in Table 1-5.

		Conventional [12]	Proposed PAFEE
Target	Frequency error tolerance range	100 ppm 1 896	2800 ppm
	Final accuracy	20 ppm	20 ppm
	Detection rate	99.95% @ SNR ≥ 2dB	99.95% @ SNR ≥ 2dB
	False alarm rate	< 0.05 %	< 0.05 %
	Estimation correct rate	> 0.9999 @ SNR ≥ 2dB	> 0.9999 @ SNR ≥ 2dB
	Short preamble	2.5	12
Spec.	Short preamble	2.5	(Downlink only/ Once)
Requirement	Estimation time	32 ms	153.6 ms
	Packet format	the same	modified (strengthen)

Table 1-5: Design target

We apply the 802.11a specification [12] in our WiBoC system as the conventional approach. The frequency tolerance range is 100 ppm. We have to meet the constraints of the detection rate, false alarm rate and estimation correct rate in our system with 2800 ppm frequency error condition. However, there are some requirements in the specification. The short preamble is designed strengthen.

In the following simulation, the SNR condition is set 2 dB for the packet error rate (PER) performance is 1 at SNR = 2dB. If we can guarantee the synchronization performance is stable in SNR=2 dB, the PER performance will remain the same.

1-5 Outline of the Thesis

The thesis is organized as follows. Chapter 2 introduces the application system, WiBoC, which is an OFDM-based WBAN system, including the overall system behavior and system specification. In Chapter 3, the proposed synchronization algorithm is presented. Chapter 4 shows the system simulation results of the proposed algorithm. The hardware implementation details are described in Chapter 5. Then the overall system emulation results are shown in Chapter 6. Finally, chapter 7 gives the conclusions and future work.

8

Chapter 2

Application System

2-1 Overview

In this chapter, the WiBoC system is introduced, which is the OFDM-based WBAN system. It is the evaluation platform in the thesis. The target operation scenario is shown in Figure 2-1.

The WBAN system contains one central processing node (CPN) and a multiple of wireless sensor nodes (WSN). The WSN gathers the physical information from the human body, such as EEG wave, ECG wave, glucose, blood pressure, and so on. It is capable of sampling, processing, and communicating, and presents as a tiny patch in human body. The gathered signals from a multiple of WSNs are wirelessly transmitted to a remote CPN, which is integrated in a portable device, such as mobile phone or PDA. Both the CPN and WSN have transmitter and receiver. They transmit and receive data to each other through downlink and uplink path.

For simplicity, the evaluation WiBoC system has one central processing node and one wireless sensor node in the thesis.



Figure 2-1: The target operation scenario of WBAN system

2-2 System Behavior

The WiBoC system behavior is shown in Figure 2-2. A successful transmission is divided into two parts, downlink and uplink. Here the downlink is defined as that CPN transmits preamble to WSN. The uplink is defined as both the preamble and data transmit from WSN to CPN. The downlink process will help WSN to detect the packet and estimate the frequency error by the packet information.



Figure 2-2: WiBoC system behavior

Figure 2-3 shows the system behavior in terms of time axis and system device connection. The body signals are gathered and transmitted from the WSNs. The CPN receives the human body signals from WSNs for ubiquitous monitoring. When the WSNs and CPN are activated, they are initially in a reset state. In the beginning of network establishment, the CPN waits for sign-in signals from possible WSNs. After all WSNs join this network, the CPN broadcasts packets to every WSN (downlink process) for timing and frequency synchronizations. After the network synchronization in the downlink process, each WSN starts to gather body signals and transmits to the CPN (uplink process). Finally, the CPN receives the body information from WSNs.



Figure 2-3: WiBoC system device connection behavior

2-2-1 Downlink

In the downlink process, the CPN transmits the downlink preamble to the WSN. The preamble is the known sequence transmitted from the CPN. The WSN is activated all the time after the reset. It detects the data from the downlink channel. The preamble is transmitted through the channel and is distorted under a variation of channel conditions. Once the packet is detected, the WSN uses the remaining distorted received data to estimate the frequency error.

2-2-2 Uplink

After the downlink process, the clock source in WSN is tuned correctly. The frequency mismatch from the CPN to the WSN is eliminated. The WSN starts to gather the body signal and transmits to the CPN. In the uplink process, not only the data is transmitted, but the preamble is also added in front of the data and transmitted. Then the CPN receives the complete uplink data for the further inspections.

2-3 Packet Format

2-3-1 Short Preamble

The short preamble format is from the IEEE 802.11a [12] specification. It takes advantage of the properties of short preamble to do the synchronization and frequency error estimation. The short preamble format in frequency domain S(f) is shown in the Equation 2-1,

where AS is a scaling factor that is dependent on the front-end device. In the receiver side, AS varies by the auto gain control (AGC) of the analog to digital converter (ADC). From the Equation 2-1, the short preamble format can be regard as 12 tones in frequency domain. It is also observed that the short preamble s(t) in time

domain as expressed in Equation 2-2. The 16 of the 64 time domain data are shown, because the time domain of the short preamble is repeated sequence, i.e., s(1:16)=s(17:32)=s(33:48)=s(49:64). And *as* is also a scaling factor similar to the *AS* in Equation 2-1.

$$\begin{split} s(t) &= ifft(S(f), 64) \\ s(1:16) &= as \times [0.0313 + 0.0313i - 0.0900 + 0.0016i - 0.0092 - 0.0533i 0.0970 - 0.0086i \\ 0.0625 & 0.0970 - 0.0086i - 0.0092 - 0.0533i - 0.0900 + 0.0016i \\ 0.0313 + 0.0313i & 0.0016 - 0.0900i - 0.0533 - 0.0092i - 0.0086 + 0.0970i \\ 0 + 0.0625i - 0.0086 + 0.0970i - 0.0533 - 0.0092i & 0.0016 - 0.0900i], \end{split}$$

The short preamble in frequency domain and time domain are plot in Figure 2-4.

The real part and imaginary part are shown respectively.



Figure 2-4: Short preamble format

The frequency domain properties are good for us to estimate the frequency error. It has 12 tones in frequency domain. It repeated 4 times every 16 data in time domain. The repeated preamble is used to do the packet detection, and the remaining preamble is for the frequency error estimation. The preamble format is suitable in this algorithm. If the preamble that has 24 tones in frequency domain is used, the time domain data will be repeated 2 times every 32 data, as shown in Figure 2-5. If the preamble that has 6 tones in frequency domain, the time domain data will be repeated 8 times every 8 data, as shown in Figure 2-6.



Figure 2-5: Preamble format with 24-tone in frequency domain



Figure 2-6: Preamble format with 6-tone in frequency domain

If the 6-tone preamble format is selected as the short preamble, the repeated 8 data are used for packet detection. For the frequency domain information is not enough to estimate the frequency error, this short preamble is not applied in our system. If the 24-tone preamble format is selected as the short preamble, the repeated 32 data are used for packet detection. The 32 data is needed for packet detection, this will increase the preamble length and hardware overhead is raised. This is not appropriate in our system.

2-3-2 Long Preamble

The long preamble format is from the IEEE 802.11a [12] specification. It takes advantage of the properties of long preamble to perform the boundary detection and fine CFO estimation. The long preamble format in frequency domain L(f) can be expressed as Equation 2-3, where AL is a scaling factor that is depend on the front-end device.

The long preamble format in time domain l(t) is expressed as Equation 2-4, where *al* is also a scaling factor similar to the *AL* in Equation 2-3.

l(t) = ifft(L(f))-0.0082 - 0.1322i 0.0704 - 0.0899i 0.1059 + 0.0564i $= al \times [0.1250]$ -0.0078 + 0.0544i 0.0451 - 0.1098i -0.0891 - 0.0405i -0.0185 - 0.1127i 0.0754 - 0.0259i 0.0292 + 0.0073i 0.0184 - 0.1175i -0.1092 - 0.0490i 0.0125 - 0.0512i 0.0288 - 0.0270i -0.0164 + 0.1741i 0.1503 - 0.0137i 0.0625 - 0.0625i 0.0058 + 0.1126i -0.0633 + 0.0086i -0.1014 + 0.1109i0.0942 + 0.0372i 0.0420 + 0.0702i -0.0777 + 0.0346i -0.0323 + 0.0053i-0.0129 - 0.1509i -0.1417 - 0.0470i -0.1533 + 0.0383i 0.0898 - 0.1538i 0.0261 + 0.1428i - 0.1010 + 0.0310i 0.0611 + 0.1713i 0.0153 + 0.0618i0.0153 - 0.0618i 0.0611 - 0.1713i -0.1010 - 0.0310i -0.12500.0261 - 0.1428i 0.0898 + 0.1538i -0.1533 - 0.0383i -0.1417 + 0.0470i -0.0129 + 0.1509i -0.0323 - 0.0053i -0.0777 - 0.0346i 0.0420 - 0.0702i 0.0942 - 0.0372i -0.1014 - 0.1109i -0.0633 - 0.0086i 0.0058 - 0.1126i 0.0625 + 0.0625i 0.1503 + 0.0137i -0.0164 - 0.1741i 0.0288 + 0.0270i0.0125 + 0.0512i - 0.1092 + 0.0490i - 0.0184 + 0.1175i - 0.0292 - 0.0073i0.0754 + 0.0259i -0.0185 + 0.1127i -0.0891 + 0.0405i 0.0451 + 0.1098i -0.0078 - 0.0544i 0.1059 - 0.0564i 0.0704 + 0.0899i -0.0082 + 0.1322i], (2-4)

Figure 2-7 shows the long preamble format in time domain and frequency domain.



Figure 2-7: Long preamble format in time domain

2-3-3 Packet Format

The packet comprises of short preamble, long preamble and the data. The preamble is in the head of the packet. The data is followed behind the preamble. Figure 2-8 shows the downlink broadcast packet. The first N repeated short preambles are used for the synchronization algorithm. The N depends on the simulation and the recursive times of the synchronization, and N is 3 in our approach. The following SGI is the half of the short preamble, which is regarded as GI of the short preamble. The LGI from the long preamble are for the boundary detection, which is the half of long preamble. The subsequent two long preambles are used to perform channel estimation and further fine frequency error estimation.



Figure 2-8: Downlink packet format

Uplink packet structure is shown in Figure 2-9. The preambles and the data are scrambled into a packet. The preamble is the same as the downlink one. It is used to perform symbol timing synchronization and symbol boundary detection. The following two long preambles are used for channel estimation. The final part of the packet is the payload data.



Figure 2-9: Uplink packet format

2-4 WiBoC System Block Diagram

The WiBoC system block diagram is introduced in this section. The WiBoC system consists of one WSN and one CPN. The operation of the CPN just sets for simulation. We put more emphasis on the WSN behavior and its hardware implementation in this thesis.

2-4-1 Wireless Sensor Node

Figure 2-10 shows the block diagram of the WSN. In the downlink process, the WSN receives the downlink preamble from the CPN in the beginning. The packet detector detects the packet all the time after the reset state. Once the packet have detected, the phase rotator calculates the signal phase between two carriers and rotates the received signal. After the processing of the phase rotator, the frequency error estimator performs the frequency error detection during the time that receiving the short preamble.

The overall frequency error is the summation of the amount estimated by the phase rotator, the frequency error estimator, and fine CFO estimator. This estimation error amount is feedback to the eCrystal, which is the tunable clock generator. The clock generator will generate the accurate clock in a short period, and the data after the short preamble (i.e long preamble) will not be lost. Then the boundary detection and fine CFO estimation is operated.

After the clock is tuned accurately, WSN starts to gather the body signal to the uplink packet and transmits to the CPN. The body signal is encoded in FEC bitstream. The FEC encoder is convolutional encoder, which is designed with coding rate R=1/2, K=7, and generator polynomials g0=133₈ and g1=171₈. The FEC bitstream is modulated in QPSK and then passed through IFFT block. After the IFFT and GI insertion, the packet is transmitted to the uplink channel.

The WSN is composed of one transmitter (WSN_TX) and one receiver (WSN_RX). The yellow part in Figure 2-10 is the block diagram of synchronization algorithm, PAFEE method.





2-4-2 Central Processing Node

In the CPN, the received data from the WSN have been pre-calibrated. The synchronizer detects the symbol timing with symbol correlation results. The synchronized data are then sent into the FFT block. After transformation, the phase recovery is performed to calibrate the data. Then the recovered data are demapped for later FEC decoding. The CPN clock diagram is shown in Figure 2-11.



Figure 2-11: CPN block diagram

2-5 Channel Model

The channel condition is important for the wireless communications systems. The system design depends on the channel conditions. In WBAN applications, the channel is assumed simple because its communication distance is short, i.e., smaller than 3 meter. We can ignore the multipath channel effect. In this section, three kinds of channel conditions are focused, additive white Gaussian noise (AWGN) channel, carrier frequency offset (CFO) and sampling clock offset (SCO).

2-5-1 AWGN

In the wireless channel, due to the thermal vibrations of atoms in antennas, shot noise, black body radiation, etc, the receiver can not receive identical signal from the transmitter. The phenomenon is called additive white Gaussian noise, say, AWGN. When the original signal pass through the AWGN channel, the linear addition noise is added to the signal. The additive noise is modeled as a Gaussian distribution. The AWGN generated by MATLAB can be expressed as Equation 2-5,

$$w(t) = randn(1, L) \times rms + j \times randn(1, L) \times rms$$

where $rms = \frac{1}{\sqrt{2}} \times 10^{(P_{data} - SNR)/20}$ (2-5)

The randn(1, L) returns an 1-by-L matrix containing random values from a normal distribution with mean zero and standard deviation one. The rms represents the normalized root mean square power of the coming L data. The P_{data} is the power of the data with unit dB.

2-5-2 Carrier Frequency Offset

Carrier frequency offset is caused by the frequency mismatch between the transmitter and receiver in the front-end device, i.e., synthesizer, modulator, and demodulator.

Take the short preamble in our system as the example, the following Figure 2-12 shows the frequency offset effect in frequency domain. The system operates in 1.4GHz radio band, and occupies 5MHz bandwidth. The frequency domain is comprehended in terms of 64-point FFT results. The x-axis represents the index from 1 to 64. The y-axis is the magnitude of the subcarrier. Consider the frequency allocation in RF band as the fixed window which is occupied from fc-BW/2 to fc + BW/2 in the frequency domain. The fc and BW represent the center frequency and the bandwidth respectively. The frequency offset effect is regarded as the data shift out of the window in the frequency domain. This phenomenon results in large amount data loss. From the Figure 2-12, the carriers are shifted left with the frequency that is proportional to the frequency offset amount. When the CFO = 3000 ppm, the carriers are shifted about 1.4GHz x 3000ppm = 4.2 MHz, which is close to the bandwidth 5MHz. There is no data in this window under such large frequency offset.


Figure 2-12: CFO effect

The effects of the frequency offset can be defined in two types, integral frequency offset (IFO) and fractional frequency offset (FFO). IFO is the effect that the received frequency domain data are in the wrong frequency position. FFO means loss of mutual subcarrier orthogonality. Figure 2-12 (2), (3), and (6) shows the joint influence of IFO and FFO in the subcarrier. Figure 2-12 (4) and (5) shows that IFO impact dominates a lot.

Consider the short preamble format in our system, because of the FFT sizes and frequency allocation, the IFO can be calculated as Equation 2-6,

$$IFO = \frac{BW}{RF} \times \frac{1}{Minimum \ Carrier \ Spacing} \times N$$
$$= \frac{5MHz}{1.4GHz} \times \frac{1}{16} \times N = 223.19 \times N \text{ ppm}$$
$$(2-6)$$

where N is an integer. Because the FFT size is 64, and the subcarrier locates every 4 points, the minimum carrier spacing is defined as 64/4 = 16.

The mathematical model of the CFO effect can be expressed as the following Equations, from 2-7 to 2-16. To operate in the coordination, please reference to the Figure 2-13.

When the baseband signal is ready, first it will pass through the DAC.

$$a(t) = \sum_{k=1}^{\infty} a_k p(t - kT_s), \quad b(t) = \sum_{k=1}^{\infty} b_k p(t - kT_s)$$
(2-7~8)

The modulator combines a(t) and b(t) to s(t) and transmits to the channel.

$$s(t) = a(t)\cos(2\pi f_c t) - b(t)\sin(2\pi f_c t)$$

$$r(t) = s(t) + n(t)$$
(2-9~10)

Let $\Delta f = f_c - f_e$, and $\Delta f_1 = f_c + f_e$. The receiver demodulates r(t) to be c(t) and d(t).

$$c(t) = r(t) \times (2\cos(2\pi f_e t)) + n_1(t)$$

= $a(t) \{\cos(2\pi\Delta f_1 t) + \cos(2\pi\Delta f t)\} - b(t) \{\sin(2\pi\Delta f_1 t) + \sin(2\pi\Delta f t)\} + n_1(t)$
 $d(t) = r(t) \times (2\sin(2\pi f_e t)) + n_2(t)$
= $a(t) \{\sin(2\pi\Delta f_1 t) - \sin(2\pi\Delta f t)\} + b(t) \{\cos(2\pi\Delta f_1 t) - \cos(2\pi\Delta f t)\} + n_2(t)$

(2-11~12)

After the low pass filter, the terms with f_1 are filtered out. The e(t) and f(t) are obtained.

$$e(t) = a(t)\cos(2\pi\Delta ft) - b(t)\sin(2\pi\Delta ft)$$

$$f(t) = a(t)\sin(2\pi\Delta ft) + b(t)\cos(2\pi\Delta ft)$$
(2-13~14)
Consider the CFO effect only, let Te = Ts.
$$Let \ x(t) = a(t) + jb(t)$$
1896
$$c_n = \int_{nTe}^{(n+1)Te} e(t)dt = \int_{nTs}^{(n+1)Ts} \{a(t)\cos(2\pi\Delta ft) - b(t)\sin(2\pi\Delta ft)\}dt$$

$$= \int_{nTs}^{(n+1)Te} \Re\{x(t)\exp(j2\pi\Delta ft)\}dt = \Re\{x_n\exp(j2\pi\Delta fnT_s)\}$$

$$d_n = \int_{nTe}^{(n+1)Te} f(t)dt = \int_{nTs}^{(n+1)Ts} \{a(t)\sin(2\pi\Delta ft) + b(t)\cos(2\pi\Delta ft)\}dt$$

$$= \int_{nTs}^{(n+1)Te} \Im\{x(t)\exp(j2\pi\Delta ft)\}dt = \Im\{x_n\exp(j2\pi\Delta fnT_s)\}$$

(2-15~16)

 $c_n \mbox{ and } d_n \mbox{ are the received signal in the baseband}.$



Figure 2-13: mathematical CFO model

From the mathematical model, the CFO model in the MATLAB platform as shown in Figure 2-14 is established. To model the analog signal, we upsample the signal by a factor M and use a low pass filter (LPF) to eliminate the redundant shadow signal. Then the subcarriers are multiplied by the exponential terms, which are caused by Equations 2-15 and 2-16. The MATLAB equation is expressed from Equations 2-17 to 2-19.

$$f=1.4 \times 10^{9} \times (CFO_ppm/M) \times 10^{-6}$$

t=1/(5×10⁶)
data_cfo(k)=data(k) × exp(j × 2π × f × t × k) (2-17~19)

where the CFO_ppm is the frequency offset value in unit ppm. The data_cfo represents the data that distorted by CFO effect. The k represents the index of the subcarriers. After the multiplying, the LPF and down-sampling filter in Figure 2-14 works like the front-end LPF before ADC.



Figure 2-14: MATLAB CFO model

2-5-3 Sampling Clock Offset

Sampling clock offset (SCO) is caused by the ADC and DAC sampling clock mismatch between the transmitter and the receiver. The effect is modeled in the Equation 2-20 at the receiver side. The $R_{preADC}(t)$ and R(t) represents the signal before and after the ADC respectively. The $\triangle P_n$ is the sampling error amount. ℓ is the index of the sampling point.

$$R(nT_{s}) = R_{preADC}(nT_{s}) * \sin c(\frac{nT_{s} - \Delta P_{n}}{T_{s}})$$

$$= \sum_{k=-\ell}^{\ell} R_{preADC}(nT_{s} - kT_{s}) \times \sin c(k - \frac{\Delta P_{n}}{T_{s}})$$
(2-20)

Take the short preamble as an example, Figure 2-15 shows the distortion of the SCO effect on the real part of the preamble in time domain. The imaginary part of the preamble will be distorted in the same way, for simplicity, the imaginary part is not plotted. In general, the SCO effect does not distort the signal severely. From the Figure 2-15, the SCO added in the signal is from 100 to 3000 ppm. It doesn't influence the data a lot.

The major problem of the SCO effect is the sample data may loss. For example, if the SCO is 200 ppm, that means the sampling clock is 5.001 MHz and the period is 199.96 ns. In other words, there is 0.04 ns mismatch each sample. Our system clock frequency is 5MHz, and the period is 200 ns. That means after 200/0.04 = 5000

samples, one data may be loss.



Figure 2-15: SCO effect

2-5-4 Link Budget

In the wireless communications system, the transmitted signal may lose energy

during propagation from the transmitter to the receiver. The transmitted information will loss due to the distance propagation loss, diffraction loss, penetration loss, or others loss. For the WBAN system, the T-R separation distance is not very long, but the path loss will still affect our system. The key factor that affects the path loss is channel model of the system. However, few attempts have been made to characterize electromagnetic propagation around human body. It is difficult to develop the simple mathematic channel model of the human body. EM waves can propagate around the body via two path. One is the penetration inside the body and the second path is creeping wave that follows the surface of the body. Reference [13] uses the simulators with an anatomically accurate model of the human body, derived from the Visual Human project of the National Library of Medicine. They projected that penetrating loss is even higher than the propagation loss, so the contribution of the penetrating wave can be neglected. Reference [14] shows that the overall peak to peak variation of path loss between the belt and shoulders in an anechoic chamber with changes in posture is 16dB at 2.45GHz, and the S21 is from -68~-86dB. Statistics [15] shows that the channel exhibits great variability due to body movements with path loss data behaving in different manors depending mainly on the freedom of communication link between transmitting and receiving antenna.

For the lack of information about the channel model and path loss mathematics model in the 1.4GHz, our issue is to discuss the path loss in the channel that encounter and set the restriction and specification of the parameters such as required SNR and sensitivity in the receiver by link budget. The parameter about the link budget is listed in the Table 2-1 below.

Parameter	value (dBm)
Transmitted Power (Pt)	10 dBm
Transmitter Antenna Gain (Gt)	0 dBm
Transimitter Cable Loss (Lt)	3 dBm
Receiver Antenna Gain (Gr)	0 dBm
Receiver Cable Loss (Lr)	3 dBm
Receiver Sensitivity (Rs)	-80 dBm
Free space T-R separation path loss (PL1)	45.5 dB
PL1 = $20\log(4\pi f_c/c) + 20\log(d), d=3m$	
Path loss from the human body (PL2)	35 dB
Remaining margin (Prm) ⁸⁹⁶	3.5 dB

Table 2-1: Link Budget

A radio Link consists of three basic elements: effective transmitting power (Pte), propagation loss (PL), and effective receiving sensibility (Prs). The effective transmitting power is transmitter power minus cable loss plus antenna gain, which is shown as Equation 2-21.

$$Pte = Pt + Gt - Lt \tag{2-21}$$

In the WBAN channel, the path loss is divided into two kinds, one is due to free space T-R separation, the other is the loss from the human body. The path loss is the summation of them, as shown in Equation 2-22.

$$PL = PL1 + PL2 \tag{2-22}$$

The receiver sensitivity (Rs) is the combination of the noise power and noise figure in the receiver. It is depending on manufacturer between -78 to -85 dBm. The overall effective receiving sensitivity is shown in Equation 2-23.

$$Prs = Gr - Lr - Rs$$
 (2-23)

For the overall link, the remaining margin (Prm) is the summation of these three components, as shown in Equation 2-24.

In our WBAN system, the wireless medical telemetry service (WMTS) radio bands are used in our applications. Wireless medical telemetry is generally used to monitor patient physiological parameters (i.e., ECG, EEG signal) over a distance via radio-frequency (RF) communications between a transmitter worn by the patient (i.e., WSN) and a central monitoring station (i.e., CPN). It provides 3 bands for the services, 608-614 MHz, 1395-1400 MHz, and 1427-1432 MHz. Our WiBoC system is designed targeting at 1395 – 1400 MHz WMTS band. The bandwidth is 5MHz.

Chapter 3 Synchronization PAFEE Method

In this chapter, the synchronization algorithm in the receiver side will be described. The synchronization algorithm is called PAFEE method, which is the abbreviation of packet detection and frequency error estimation method. This operation works all the time after the reset state. The transmitter sends the known preamble for receiver synchronization. Once the packet has been detected, the remaining data are used for frequency error estimation. The estimation value is sent to embedded crystal (eCrystal), and the system clock can be tuned accurately. The overall synchronization procedure has been done.

3-1 PAFEE -- Packet Detection Algorithm

In our channel condition (i.e., large frequency error), the conventional packet detection algorithm may be failed due to the large loss of the data. In our proposed algorithm, the packet detection algorithm development is based on the conventional one. The receiver operating characteristic (ROC) curves are shown to prove the packet detection algorithm is successful under large frequency error.

3-1-1 Conventional Algorithm

There are some conventional approaches for symbol timing synchronization and packet detection. The Van de Beek's [16] work presents the joint maximum likelihood symbol timing and carrier frequency offset estimator in OFDM systems. He describes a method using a correlation with the cyclic prefix to find the symbol. The symbol timing can be found in Equation 3-1.

$$\hat{\theta} = \arg \max_{\theta} \left\{ \left| \sum_{k=\theta}^{\theta+L+1} r(k) r^{*}(k+N) \right| - \frac{\rho}{2} \sum_{k=\theta}^{\theta+L+1} (|r(k)|^{2} + |r(k+N)|^{2}) \right\}$$
where $\rho = \left| \frac{E\{r(k)r^{*}(k+N)\}}{\sqrt{E\{|r(k)|^{2}\}E\{|r(k+N)|^{2}\}}} \right|$
(3-1)

The r(k) represents the baseband receive signal. The detector decides a maximum argument to be the packet arrival.

Schmidl and Cox [17] present the auto-correlation method for packet detection. This algorithm operates near the Cramer-Rao lower bound for the variance of the frequency offset. This method is very usual for packet detection in OFDM system. The timing metric is defined as Equation 3-2.

$$V(d) = \frac{\left|\sum_{m=0}^{L-1} r_{d+m}^* r_{d+m+L}\right|^2}{\left(\sum_{m=0}^{L-1} \left|r_{d+m+L}\right|^2\right)^2}$$
(3-2)

where d is a time index corresponding to the first sample in a window of 2L samples. The window slides along in time as the receiver searches the first training symbol.

To improve the timing metric, Minn [18] presents another synchronization scheme applicable to OFDM systems. In Minn's approach, the preamble symbol is designed to have a sharp timing metric trajectory. He uses the minimum Euclidean distance to define the timing metric, the Equation 3-3 shows the normalized metric.

$$V_{n}(d) = \frac{E(d) - 2|P(d)|}{E(d)} = 1 - \frac{2|P(d)|}{E(d)}$$

where $E(d) = \sum_{i=0}^{M-1} (|r(i+d+M)|^{2} + |r(i+d)|^{2}),$ (3-3)
and $P(d) = \sum_{i=0}^{M-1} r(i+d+M)r^{*}(i+d)$

where d is a time index, and M is the data length for auto-correlation. Finding the minimum of Euclidean distance $V_n(d)$ is equivalent to finding the maximum of $\frac{|P(d)|}{E(d)}$. The method is similar to the approach of Schmidl and Cox. On the other hand, Minn's approach uses different preamble format. The time domain of the short preamble from the Chapter 2 is repeated 4 times. Consider the repeated part to be A. The original preamble is $s(t) = [A \ A \ A]$. In Minn's approach, the preamble becomes $[-A \ A - A \ -A]$.

From the three famous approaches about the packet detection in OFDM systems, they all use the similarities between two repeated data. However, the methods are for the OFDM systems which have small frequency error, i.e., FFO only. Our system encounters the large frequency error problems, i.e., joint FFO and IFO. The new approach has to be derived.

3-1-2 Proposed Algorithm

In our channel conditions, the data will be distorted severely. Though the violent data loss, the likelihood between the repeated data is existed. Consider the minimum Euclidean and maximum likelihood issues, the timing metric is defined in Equation 3-4.

$$V(n) = \frac{|C(n)|^2}{P(n)}$$
where $C(n) = \sum_{i=0}^{M-1} r_{i+n} r_{i+n+M}^*$, and $P(n) = \sum_{i=0}^{M-1} |r_{i+n+M}^*|^2$
(3-4)

where d is a time index, and M is the data length for auto-correlation. The Equation 3-4 can be expressed as Equation 3-5.

$$V(n) = \frac{|C(n)|^{2}}{P(n)} = \frac{\left|\sum_{i=0}^{M-1} r_{i+n}r^{*}_{i+n+M}\right|^{2}}{\sum_{i=0}^{M-1} |r_{i+n+M}|^{2}}$$

$$= \frac{(R_{l}^{i+n}R_{l}^{i+n+M} + R_{Q}^{i+n}R_{Q}^{i+n+M})^{2} + (R_{Q}^{i+n}R_{l}^{i+n+M} - R_{l}^{i+n}R_{Q}^{i+n+M})^{2}}{\sum_{i=0}^{M-1} (r_{i+n+M}^{i})^{2} + (r_{i+n+M}^{Q})^{2}} = \frac{u_{1}^{2} + u_{2}^{2}}{\sum_{i=0}^{M-1} (u_{4i})^{2} + (u_{5i})^{2}}$$
where $u_{1} = R_{l}^{i+n}R_{l}^{i+n+M} + R_{Q}^{i+n}R_{Q}^{i+n+M} = \sum_{i=0}^{M-1} r_{i+n}^{i}r_{i+n+M}^{i} + r_{i+n}^{Q}r_{i+n+M}^{Q}$,
and $u_{2} = R_{Q}^{i+n}R_{l}^{i+n+M} - R_{l}^{i+n}R_{Q}^{i+n+M} = \sum_{i=0}^{M-1} r_{i+n}^{Q}r_{i+n+M}^{i} + r_{i+n}^{i}r_{i+n+M}^{Q}$
(3-5)

Let H_0 be the null hypothesis, that is, there is no OFDM preamble transmission present. Let H_1 be the alternate hypothesis, i.e., the OFDM preambles are present, as shown in Equation 3-6.

$$H_0: r_i = \omega_i H_1: r_i = s_i + \omega_i$$
, where $\omega_i \sim N(0, \sigma_n^2)$ (3-6)

The noise is assumed to be white, with mean 0 and variance σ_n^2 . Let the energy of s_i is σ_s^2 , and the real part and the imaginary part of the energy are $\sigma_s^2/2$ and $\sigma_s^2/2$ respectively. For H₀, by the central limit theorem (CLT), the u₁ and u₂ can be

regarded as Gaussian distribution. The u_{4i} and u_{5i} are Gaussian, too. The probability distribution of V(n) can be approximate to the F-distribution [19], with the degree 2 in nominator, and degree 2M in the denominator. To obtain the probability density function of the F-distribution, the mean and variance of u_1 , u_2 , u_{4i} and u_{5i} have to be deduced. The white noise is statistically uncorrelated, so the mean of u_1 , u_2 , u_{4i} and u_{5i} are all zero, as shown in Equations 3-7 to 3-10.

$$E[u_{1} | H_{0}] = E\left[\sum_{i=0}^{M-1} r_{i+n}^{l} r_{i+n+M}^{l} + r_{i+n}^{Q} r_{i+n+M}^{Q}\right] = E\left[\sum_{i=0}^{M-1} \omega_{i+n}^{l} \omega_{i+n+M}^{l} + \omega_{i+n}^{Q} \omega_{i+n+M}^{Q}\right] = 0$$

$$E[u_{2} | H_{0}] = E\left[\sum_{i=0}^{M-1} r_{i+n}^{Q} r_{i+n+M}^{l} - r_{i+n}^{l} r_{i+n+M}^{Q}\right] = E\left[\sum_{i=0}^{M-1} \omega_{i+n}^{Q} \omega_{i+n+M}^{l} - \omega_{i+n}^{l} \omega_{i+n+M}^{Q}\right] = 0$$

$$E[u_{4i} | H_{0}] = E\left[r_{i+n+M}^{l}\right] = E\left[\omega_{i+n+M}^{l}\right] = 0$$

$$E[u_{5i} | H_{0}] = E\left[r_{i+n+M}^{Q}\right] = E\left[\omega_{i+n+M}^{Q}\right] = 0$$
(3-7~10)

To obtain the variance, the calculation of the second moment of u_1 is shown as Equation 3-11.

$$E\left[u_{1}^{2} \mid H_{0}\right] = E\left[\left(\sum_{i=0}^{M-1} r_{i+n}^{\prime} r_{i+n+M}^{\prime} + r_{i+n}^{Q} r_{i+n+M}^{Q}\right)^{2}\right] = E\left[\left(\sum_{i=0}^{M-1} \omega_{i+n}^{\prime} \omega_{i+n+M}^{\prime} + \omega_{i+n}^{Q} \omega_{i+n+M}^{Q}\right)^{2}\right]$$
(3-11)

Let $a_i = r_{i+n}^{\prime} r_{i+n+M}^{\prime}$, and $b_i = r_{i+n}^{Q} r_{i+n+M}^{Q}$. They can be regarded as uncorrelated noise.

The Equation 3-11 can be written as

$$\begin{split} E\left[u_{1}^{2} \mid H_{0}\right] &= E\left[\left(\sum_{i=0}^{M-1} (a_{i} + b_{i})\right)^{2}\right] \\ &= E\left[\sum_{i=0}^{M-1} a_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1} b_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1} (2a_{i}b_{j} + (2a_{i}a_{j}) \mid_{i \neq j} + (2b_{i}b_{j}) \mid_{i \neq j})\right] \\ &= E\left[\sum_{i=0}^{M-1} (a_{i}^{2} + b_{i}^{2})\right] = E\left[\sum_{i=0}^{M-1} ((\omega_{i+n}^{l} \omega_{i+n+M}^{l})^{2} + (\omega_{i+n}^{Q} \omega_{i+n+M}^{Q})^{2})\right] \\ &= \sum_{i=0}^{M-1} (E((\omega_{i+n}^{l})^{2})E((\omega_{i+n+M}^{l})^{2}) + E((\omega_{i+n}^{Q})^{2})E((\omega_{i+n+M}^{Q})^{2})) \\ &= M\left[\left(\frac{\sigma_{n}^{2}}{2}\right)\left(\frac{\sigma_{n}^{2}}{2}\right) + \left(\frac{\sigma_{n}^{2}}{2}\right)\left(\frac{\sigma_{n}^{2}}{2}\right)\right] \\ &= M\left(\frac{\sigma_{n}^{4}}{2}\right) \end{split}$$

In the same manner, the second moment of u_2 is obtained

$$E\left[u_{2}^{2} \mid H_{0}\right] = M\left(\frac{\sigma_{n}^{4}}{2}\right)$$
(3-12)
The second moment of u_{4i} and u_{5i} and is shown in Equation 3-13.
$$E\left[u_{4i}^{2} \mid H_{0}\right] = E\left[u_{5i}^{2} \mid H_{0}\right] = E\left[\omega_{i}^{2}\right] = \frac{\sigma_{n}^{2}}{2}$$
(3-13)

From Equations 3-11 to 3-13, the variance is achieved in Equations 3-14 to 3-17.

$$Var\left[u_{1}^{2} \mid H_{0}\right] = E\left[u_{1}^{2} \mid H_{0}\right] - \left(E\left[u_{1} \mid H_{0}\right]\right)^{2} = M\left(\frac{\sigma_{n}^{4}}{2}\right)$$

$$Var\left[u_{2}^{2} \mid H_{0}\right] = E\left[u_{2}^{2} \mid H_{0}\right] - \left(E\left[u_{2} \mid H_{0}\right]\right)^{2} = M\left(\frac{\sigma_{n}^{4}}{2}\right)$$

$$Var\left[u_{4i}^{2} \mid H_{0}\right] = E\left[u_{4i}^{2} \mid H_{0}\right] - \left(E\left[u_{4i} \mid H_{0}\right]\right)^{2} = \left(\frac{\sigma_{n}^{2}}{2}\right)$$

$$Var\left[u_{5i}^{2} \mid H_{0}\right] = E\left[u_{5i}^{2} \mid H_{0}\right] - \left(E\left[u_{5i} \mid H_{0}\right]\right)^{2} = \left(\frac{\sigma_{n}^{2}}{2}\right)$$

$$Var\left[u_{5i}^{2} \mid H_{0}\right] = E\left[u_{5i}^{2} \mid H_{0}\right] - \left(E\left[u_{5i} \mid H_{0}\right]\right)^{2} = \left(\frac{\sigma_{n}^{2}}{2}\right)$$

By the same way for H_1 , the mean and variance of the u_1 , u_2 , u_{4i} and u_{5i} can be

figured out. First, the mean of u_1 and u_2 are calculated in Equations 3-18 and 3-19.

$$E[u_{1} | H_{1}] = E\left[\sum_{i=0}^{M-1} r_{i+n}^{i} r_{i+n+M}^{i} + r_{i+n}^{Q} r_{i+n+M}^{Q}\right]$$

$$\therefore E\left[\sum_{i=0}^{M-1} r_{i+n}^{i} r_{i+n+M}^{i}\right] = E\left[\sum_{i=0}^{M-1} (s_{i+n}^{i} + \omega_{i+n}^{i})(s_{i+n+M}^{i} + \omega_{i+n+M}^{i})\right]$$

$$= E\left[\sum_{i=0}^{M-1} (s_{i+n}^{i} s_{i+n+M}^{i} + s_{i+n}^{i} \omega_{i+n+M}^{i} + \omega_{i+n}^{i}(s_{i+n+M}^{i} + \omega_{i+n+M}^{i}))\right]$$

$$= \sum_{i=0}^{M-1} \left[E(s_{i+n}^{i} s_{i+n+M}^{i}) + E(s_{i+n}^{i})E(\omega_{i+n+M}^{i}) + E(\omega_{i+n}^{i})E(s_{i+n+M}^{i} + \omega_{i+n+M}^{i})\right]$$

$$= M \times E(s_{i+n}^{i} s_{i+n+M}^{i}) = M \frac{\sigma_{s}^{2}}{2}$$

and
$$E\left[\sum_{i=0}^{M-1} r_{i+n}^{Q} r_{i+n+M}^{Q}\right] = M \frac{\sigma_{s}^{2}}{2}$$

$$\therefore E[u_{1} | H_{1}] = M \sigma_{s}^{2}$$

the same manner, the mean of the us is obtained.

In the same manner, the mean of the u_2 is obtained.

$$E[u_2 | H_1] = E\left[\sum_{i=0}^{M-1} r_{i+n}^Q r_{i+n+M}^i - r_{i+n}^I r_{i+n+M}^Q\right] = 0$$
(3-19)

The u_{4i} and u_{5i} are easily obtained by Equations 3-20 and 3-21.

$$E[u_{4i} | H_1] = E[r'_{i+n+M}] = E[s'_{i+n+M} + \omega'_{i+n+M}] = 0$$

$$E[u_{5i} | H_1] = E[r^Q_{i+n+M}] = E[s^Q_{i+n+M} + \omega^Q_{i+n+M}] = 0$$
(3-20~21)

To obtain the variance, the calculation of the second moment of u_1 is shown as Equation 3-22.

$$E\left[u_{1}^{2} \mid H_{1}\right] = E\left[\left(\sum_{i=0}^{M-1} \left(r_{i+n}^{I} r_{i+n+M}^{I} + r_{i+n}^{Q} r_{i+n+M}^{Q}\right)\right)^{2}\right]$$

$$= E\left[\sum_{i=0}^{M-1} a_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1} b_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1} \sum_{j=0}^{M-1} \left(2a_{i}b_{j} + \left(2a_{i}a_{j}\right)\right)_{i\neq j} + \left(2b_{i}b_{j}\right)\right]_{i\neq j}\right]$$
(3-22)

To be simplified, each term is analyzed individually,

$$E\left[\sum_{i=0}^{M-1} a_{i}^{2}\right] = E\left[\sum_{i=0}^{M-1} \left(r_{i+n}^{\prime} r_{i+n+M}^{\prime}\right)^{2}\right] = E\left[\sum_{i=0}^{M-1} \left(\left(s_{i+n}^{\prime} + \omega_{i+n}^{\prime}\right)\left(s_{i+n+M}^{\prime} + \omega_{i+n+M}^{\prime}\right)\right)^{2}\right]$$
$$= E\left[\sum_{i_{1}=0}^{M-1} \sum_{i_{2}=0}^{M-1} \left(s_{i_{1}+n}^{\prime} + \omega_{i_{1}+n}^{\prime}\right)\left(s_{i_{1}+n+M}^{\prime} + \omega_{i_{1}+n+M}^{\prime}\right)\left(s_{i_{2}+n}^{\prime} + \omega_{i_{2}+n}^{\prime}\right)\left(s_{i_{2}+n+M}^{\prime} + \omega_{i_{2}+n+M}^{\prime}\right)\right] \quad (3-23)$$
$$= \sum_{i_{1}=0}^{M-1} \sum_{i_{2}=0}^{M-1} E\left[\left(s_{i_{1}+n}^{\prime} + \omega_{i_{1}+n}^{\prime}\right)\left(s_{i_{1}+n+M}^{\prime} + \omega_{i_{1}+n+M}^{\prime}\right)\left(s_{i_{2}+n}^{\prime} + \omega_{i_{2}+n}^{\prime}\right)\left(s_{i_{2}+n+M}^{\prime} + \omega_{i_{2}+n+M}^{\prime}\right)\right]$$

If a, b, c, and d are jointly Gaussian random variables, then from [20], we have

$$E[abcd] = E[ab]E[cd] + E[ac]E[bd] + E[ad]E[bc]$$
(3-24)

$$-2E[a]E[b]E[c]E[d]$$
Apply the Equations 3-24 to 3-23,

$$E[(s'_{i_{i}+n} + \omega'_{i_{i}+n})(s'_{i_{i}+n+M} + \omega'_{i_{i}+n+M})(s'_{i_{2}+n} + \omega'_{i_{2}+n})(s'_{i_{2}+n+M} + \omega'_{i_{2}+n+M})]$$

$$= E[(s'_{i_{i}+n} + \omega'_{i_{i}+n})(s'_{i_{2}+n} + \omega'_{i_{2}+n})]E[(s'_{i_{2}+n} + \omega'_{i_{2}+n})(s'_{i_{2}+n+M} + \omega'_{i_{2}+n+M})]$$

$$+ E[(s'_{i_{i}+n} + \omega'_{i_{i}+n})(s'_{i_{2}+n+M} + \omega'_{i_{2}+n})]E[(s'_{i_{1}+n+M} + \omega'_{i_{1}+n+M})(s'_{i_{2}+n+M} + \omega'_{i_{2}+n+M})]$$

$$+ E[(s'_{i_{i}+n} + \omega'_{i_{i}+n})(s'_{i_{2}+n+M} + \omega'_{i_{2}+n+M})]E[(s'_{i_{1}+n+M} + \omega'_{i_{1}+n+M})(s'_{i_{2}+n} + \omega'_{i_{2}+n+M})]$$

$$= \left(\frac{\sigma_{s}^{2}}{2}\right)^{2} + \left(\frac{\sigma_{s}^{2} + \sigma_{n}^{2}}{2}\right)^{2} + \left(\frac{\sigma_{s}^{2}}{2}\right)^{2} - 0$$

$$= \left(\frac{\sigma_{s}^{2} + \sigma_{n}^{2}}{2}\right)^{2} + 2\left(\frac{\sigma_{s}^{2}}{2}\right)^{2}$$

$$E[\sum_{i=0}^{M-1} a_{i}^{2}] = \frac{M^{2}}{4} \left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} + 2\left(\sigma_{s}^{2}\right)^{2}\right]$$
(3-25)

In the same way, Equation 3-26 is followed,

Ch3. Synchronization PAFEE Method

$$E\left[\sum_{i=0}^{M-1} b_i^2\right] = \frac{M^2}{4} \left[\left(\sigma_s^2 + \sigma_n^2\right)^2 + 2\left(\sigma_s^2\right)^2 \right]$$
(3-26)

As to the third term in Equation 3-22, it is derived in Equation 3-27.

$$\begin{split} E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} \left(2a_{j}b_{j}\right)\right] &= E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} \left(2r_{i+n}^{\prime}r_{i+n+M}^{\prime}r_{i+n}^{Q}r_{i+n}^{Q}\right)\right] \\ &= 2\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} E\left(r_{i+n}^{\prime}r_{i+n+M}^{\prime}r_{i+n}^{Q}r_{i+n}^{Q}\right) \\ &\because E\left(r_{i+n}^{\prime}r_{i+n+M}^{\prime}\right) E\left(r_{i+n}^{Q}r_{i+n+M}^{Q}\right) + E\left(r_{i+n}^{\prime}r_{i+n}^{Q}\right) E\left(r_{i+n+M}^{\prime}r_{i+n+M}^{Q}\right) + E\left(r_{i+n}^{\prime}r_{i+n+M}^{Q}\right) + E\left(r_{i+n}^{\prime}r_{i+n+M}^{Q}\right) + E\left(r_{i+n}^{\prime}r_{i+n+M}^{Q}\right) \\ &= \left(\frac{\sigma_{s}^{2}}{2}\right)\left(\frac{\sigma_{s}^{2}}{2}\right) + 0 + 0 = \left(\frac{\sigma_{s}^{4}}{4}\right) \end{split}$$

$$E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} (2a_{j}a_{j})\Big|_{i\neq j}\right] = E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} (2r_{i+n}^{I}r_{i+n+M}^{I}r_{j+n}^{I}r_{j+n+M}^{I})\Big|_{i\neq j}\right]$$

$$= 2\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} E\left(r_{i+n}^{I}r_{i+n+M}^{I}r_{j+n}^{I}r_{j+n+M}^{I}\right)\Big|_{i\neq j}$$

$$E\left(r_{i+n}^{I}r_{i+n+M}^{I}r_{j+n}^{I}r_{j+n+M}^{I}\right) = E\left(r_{i+n}^{I}r_{i+n+M}^{I}\right) = E\left(r_{i+n}^{I}r_{i+n+M}^{I}\right) = E\left(r_{i+n}^{I}r_{i+n+M}^{I}\right) = E\left(r_{i+n}^{I}r_{i+n+M}^{I}\right) = E\left(\frac{\sigma_{s}^{4}}{2}\right) = 0$$

$$\begin{split} & E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} \left(2b_{j}b_{j}\right)\right|_{i\neq j}\right] = E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} \left(2r_{i+n}^{Q}r_{i+n+M}^{Q}r_{j+n}^{Q}r_{j+n+M}^{Q}\right)\right|_{i\neq j}\right] \\ &= 2\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} E\left(r_{i+n}^{Q}r_{i+n+M}^{Q}r_{j+n}^{Q}r_{j+n+M}^{Q}\right)\right|_{i\neq j} \\ &\simeq E\left(r_{i+n}^{Q}r_{i+n+M}^{Q}r_{j+n}^{Q}r_{j+n+M}^{Q}\right) + E\left(r_{i+n}^{Q}r_{j+n}^{Q}\right) E\left(r_{i+n+M}^{Q}r_{j+n+M}^{Q}\right) + E\left(r_{i+n}^{Q}r_{j+n+M}^{Q}\right) + E\left(r_{i+n+M}^{Q}r_{j+n+M}^{Q}\right) + E\left($$

$$\therefore E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1} \left(2a_ib_j\right) + \left(2a_ia_j\right)\Big|_{i\neq j} + \left(2b_ib_j\right)\Big|_{i\neq j}\right] = 3M^2\left(\frac{\sigma_s^4}{2}\right)$$
(3-27)

So the Equation 3-22 is rewritten to Equation 3-28,

$$E\left[u_{1}^{2} \mid H_{1}\right] = E\left[\sum_{i=0}^{M-1} \left(\left(r_{i+n}^{I} r_{i+n+M}^{I}\right) + \left(r_{i+n}^{Q} r_{i+n+M}^{Q}\right)\right)^{2}\right]$$

$$= E\left[\sum_{i=0}^{M-1} a_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1} b_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1} \sum_{j=0}^{M-1} \left(2a_{j}b_{j} + \left(2a_{j}a_{j}\right)\right)_{i\neq j} + \left(2b_{i}b_{j}\right)\right)_{i\neq j}\right)\right]$$

$$= \frac{M^{2}}{2}\left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} + 2\left(\sigma_{s}^{2}\right)^{2}\right] + 3M^{2}\left(\frac{\sigma_{s}^{4}}{2}\right)$$

$$= \frac{M^{2}}{2}\left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} + 5\left(\sigma_{s}^{2}\right)^{2}\right]$$
(3-28)

In the same way, the second moment of the u_2 can be derived, as shown in Equation 3-29.

$$E\left[u_{2}^{2} \mid H_{1}\right] = E\left[\sum_{i=0}^{M-1} \left(r_{i+n}^{Q}r_{i+n+M}^{I} - r_{i+n}^{I}r_{i+n+M}^{Q}\right)^{2}\right]$$

$$= E\left[\sum_{i=0}^{M-1}a_{i}^{2}\right] + E\left[\sum_{i=0}^{M-1}b_{i}^{2}\right] - E\left[\sum_{i=0}^{M-1}\sum_{j=0}^{M-1}\left(2a_{j}b_{j} - (2a_{j}a_{j})\mid_{i\neq j} - (2b_{j}b_{j})\mid_{i\neq j}\right)\right]$$

$$= \frac{M^{2}}{2}\left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} + 2\left(\sigma_{s}^{2}\right)^{2}\right] - M^{2}\left(\frac{\sigma_{s}^{4}}{2}\right)$$

$$= \frac{M^{2}}{2}\left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} + \left(\sigma_{s}^{2}\right)^{2}\right]$$

(3-29)

The second moment of u_{4i} and u_{5i} and is shown in Equation 3-30.

$$E\left[u_{4i}^{2} \mid H_{1}\right] = E\left[u_{5i}^{2} \mid H_{1}\right] = E\left[(s_{i} + \omega_{i})^{2}\right] = \frac{\sigma_{s}^{2} + \sigma_{n}^{2}}{2}$$
(3-30)

From Equations 3-18 to 3-30, the variance is achieved in Equations 3-31 to 3-34.

Ch3. Synchronization PAFEE Method

$$Var\left[u_{1}^{2} \mid H_{1}\right] = E\left[u_{1}^{2} \mid H_{1}\right] - \left(E\left[u_{1} \mid H_{1}\right]\right)^{2} = \frac{M^{2}}{2}\left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} + 3\left(\sigma_{s}^{2}\right)^{2}\right]$$
$$Var\left[u_{2}^{2} \mid H_{1}\right] = E\left[u_{2}^{2} \mid H_{1}\right] - \left(E\left[u_{2} \mid H_{1}\right]\right)^{2} = \frac{M^{2}}{2}\left[\left(\sigma_{s}^{2} + \sigma_{n}^{2}\right)^{2} - \left(\sigma_{s}^{2}\right)^{2}\right]$$
$$Var\left[u_{4i}^{2} \mid H_{1}\right] = E\left[u_{4i}^{2} \mid H_{1}\right] - \left(E\left[u_{4i} \mid H_{1}\right]\right)^{2} = \left(\frac{\sigma_{s}^{2} + \sigma_{n}^{2}}{2}\right)$$
$$Var\left[u_{5i}^{2} \mid H_{1}\right] = E\left[u_{5i}^{2} \mid H_{1}\right] - \left(E\left[u_{5i} \mid H_{1}\right]\right)^{2} = \left(\frac{\sigma_{s}^{2} + \sigma_{n}^{2}}{2}\right)$$

 $(3-31 \sim 34)$

From these equations, the V(n) is approximate to non-central F-distribution with degree 2 and 2M under H₁ hypothesis. The non-central parameter λ is derived in Equation 3-35.

$$\lambda = \sum_{i=0}^{1} \left(\frac{\mu_{i}^{2}}{\sigma_{i}^{2}} \right)$$

$$= \frac{(M\sigma_{s}^{2})^{2}}{\left(\frac{M^{2}}{2} \left[\left(\sigma_{s}^{2} + \sigma_{n}^{2} \right)^{2} + 3 \left(\sigma_{s}^{2} \right)^{2} \right] \right] \times \left(\frac{2}{2M} \right)^{2}} = \frac{2M^{2}}{\left(1 + \frac{1}{SNR} \right)^{2} + 3}$$
(3-35)

The signal to noise ratio, SNR, is defined as $SNR = \sigma_s^2 / \sigma_n^2$. To analysis the performance, we summarizes the probability distribution of V(n) under the H₀ and H₁ conditions.

H0: F-distribution with degree 2 and 2M.

H1: Non-central F-distribution with degree 2 and 2M, non-central parameter λ .

The frequency offset effect can be modeled into SNR loss. Equation 3-36 shows the degradation of SNR due to frequency error.

$$D = 10\log_{10}\left(1 - \frac{IFO}{BW/RF} - \frac{4}{64}\right)$$

+20 × M × log₁₀ $\left|real\left(exp\left(\frac{FFO}{BW/RF}\right)\right) - lm ag\left(1 - exp\left(\frac{FFO}{BW/RF}\right)\right)\right|$ (3-36)
+20 × M × log₁₀ $\left|real\left(exp\left(\frac{FFO}{BW/RF}\right)\right) + lm ag\left(1 - exp\left(\frac{FFO}{BW/RF}\right)\right)\right|$

where BW is bandwidth, RF is radio frequency, and IFO and FFO represents the integral frequency offset and fractional frequency offset respectively. For example, the BW is 5MHz and the RF is 1.4 GHz in our system. If the FO = 3000 ppm, the IFO and FFO are shown in Equations 3-37 and 3-38 respectively.

$$IFO = floor \left(\frac{3000 \times 10^{-6}}{BW/RF/16} \right) \times (BW/RF/16) = 2899 \text{ ppm}$$
(3-37~38)

$$FFO = 3000 - 2899 = 101 \text{ ppm}$$

The SNR degradation is -9.24 dB as shown in Equation 3-39.

$$D = 10\log_{10}(1 - \frac{2899}{BW/RF} - \frac{4}{64})$$

$$+ 20 \times M \times \log_{10} \left| \text{real} \left(\exp(\frac{101}{BW/RF}) \right) - \text{Im} ag \left(1 - \exp(\frac{101}{BW/RF}) \right) \right|$$
(3-39)

$$+ 20 \times M \times \log_{10} \left| \text{real} \left(\exp(\frac{101}{BW/RF}) \right) + \text{Im} ag \left(1 - \exp(\frac{101}{BW/RF}) \right) \right|$$
(3-39)

$$= -9.24 \text{ dB}$$

By using the MATLAB function, ncfpdf (Probability Density Function of non-central F-distribution) and ncfcdf (Cumulative Distribution Function of non-central F-distribution), the ROC curves is plotted under different SNR conditions in terms of frequency error conditions as shown in Figure 3-1. The Pd represents detection rate and Pfa represents false alarm rate. The deduction results are similar to the simulation results, and the comparison will be shown in Chapter 4.



Figure 3-1 (b): ROC curves from mathematics deduction (Zoom-in)

From the mathematics deduction, it shows that if the M increases, the ROC performance will be improved a lot. Figure 3-2 shows the different M value under different SNR conditions. In our design, the M=32 is chosen for auto-correlation length.



Figure 3-2: ROC curves under different M

3-2 PAFEE -- Frequency Error Estimation Algorithm

To overcome the frequency mismatch problem, there are many approaches. In hardware approaches, the famous ones are phase lock loop (PLL) and frequency lock loop (FLL). It is an electronic control system to generate a clock that is locked to a reference frequency.

In the baseband digital signal processing approaches, there are some frequency

offset estimation or tracking algorithms in OFDM systems. They use some baseband processing to achieve frequency error estimation and calibration. In our system, our approach is to estimate the frequency error by some baseband processing.

3-2-1 Conventional Algorithm

The popular conventional approach about the frequency error estimation is Moose's work [21]. The Moose's work applies the repeated training sequence to estimate the frequency error. The estimation equation is derived by the maximum likelihood estimation (MLE) algorithm, as shown in Equation 3-40.



where $\hat{\varepsilon}$ is the estimation value of frequency error. The Y_{2k} and Y_{1k} are the repeated part received from the transmitter side.

Sliskovic's approach [22] enables joint carrier and sampling frequency-offset estimation from the repeated pilot symbols. He use the MLE estimation to do the estimation. The sampling frequency offset can be derived by the difference of phase shifts on two neighboring subcarriers, where R_{1i} and R_{2i} are the received signal.

$$\hat{\varepsilon}_{s,i} = (\varepsilon_s i + \varepsilon_c) - (\varepsilon_s (i-1) + \varepsilon_c) = \frac{1}{2\pi} \left[\angle \left(\frac{R_{1i}}{R_{2i}} \right) - \angle \left(\frac{R_{1i-1}}{R_{2i-1}} \right) \right]$$
(3-41)

Because of the noise, the estimates can obtain by some weighting factors

$$\hat{\varepsilon}_{s} = \sum_{i=1}^{M-1} \omega_{i} \cdot \hat{\varepsilon}_{s,i}$$
(3-42)

The carrier frequency offset can also be derived by using the same weighting factor.

$$\hat{\varepsilon}_{c,i} = \frac{1}{2\pi} \left[\angle \left(\frac{R_{1i}}{R_{2i}} \right) - i \cdot \hat{\varepsilon}_s \right]$$

$$\hat{\varepsilon}_c = \sum_{i=1}^{M-1} \omega_i \cdot \hat{\varepsilon}_{c,i}$$
(3-43)

From these equations, they take advantage of the characteristic of time domain phase shift to estimate the frequency offset by inner product. This method is popular for frequency error estimation in OFDM system. However, this approach is suitable only for the FFO effect. If there is IFO effect in the system, this approach will be failed.

1896

3-2-2 Proposed Algorithm

In order to solve the IFO effect, the correlator bank method to detect the frequency error is introduced. To introduce the correlator bank, the attempt is to grab the frequency domain information by the correlation results. Assume the frequency domain signal is s[n], H0 is the null hypothesis, and H1 is the alternative hypothesis as shown in Equation 3-44. Consider the w[n] as the white Gaussian noise, the probability that H1 and H0 happen can be represented as Equation 3-45 and Equation 3-46 respectively.

$$H_0: x[n] = w[n]$$
, n=0, 1, ..., N
 $H_1: x[n] = s[n] + w[n]$, n=0, 1, ..., N where $\underline{x} = [x[0], x[1], ..., x[N-1]]^T$

$$p(\underline{x}; H_1) = \frac{1}{(2\pi\sigma^2)^{N/2}} \exp\{-\frac{1}{2\sigma^2} \sum_{n=0}^{N-1} (x[n] - s[n])^2\}$$
(3-45)

$$p(\underline{x}; H_0) = \frac{1}{(2\pi\sigma^2)^{N/2}} \exp\{-\frac{1}{2\sigma^2} \sum_{n=0}^{N-1} (x[n])^2\}$$
(3-46)

By Neyman-Pearson Theorem [23], the detection probability can be maximized for a given false alarm to decide H1.

$$L(x) = \frac{p(\underline{x}; H_1)}{p(\underline{x}; H_0)} > \gamma$$

$$L(x) = \exp\{-\frac{1}{2\sigma^2} (\sum_{n=0}^{N-1} (x[n] - s[n])^2 - \sum_{n=0}^{N-1} (x[n])^2)\} > \gamma \quad (3-47\sim50)$$

$$\ln L(x) = -\frac{1}{2\sigma^2} (\sum_{n=0}^{N-1} (x[n] - s[n])^2 - \sum_{n=0}^{N-1} (x[n])^2) > \ln \gamma$$

$$\frac{1}{\sigma^2} \sum_{n=0}^{N-1} x[n] s[n] - \frac{1}{2\sigma^2} \sum_{n=0}^{N-1} s^2[n]) > \ln \gamma$$

From the previous equations, the test statistic T(x) and threshold can be decided as Equation 3-51,

$$T(x) = \sum_{n=0}^{N-1} x[n] s[n] > \sigma^2 \ln \gamma + \frac{1}{2} \sum_{n=0}^{N-1} s^2[n]$$
(3-51)

Assume the signal in different position of the frequency domain are $s_1[n]$, $s_2[n]$, ..., $s_N[n]$, the hypothesis test can be expressed as follows. The test statistic are $T_1(x), T_2(x), ..., T_N(x)$, corresponding to $s_1[n], s_2[n], ..., s_N[n]$.

$$T_{k}(x) = \sum_{n=0}^{N-1} x[n]s[n] > \sigma^{2} \ln \gamma + \frac{1}{2} \sum_{n=0}^{N-1} s_{k}^{2}[n]$$
Let

$$H_{0}: x[n] = w[n] , n=0, 1, ..., N$$

$$H_{1}: x[n] = s_{1}[n] + w[n] , n=0, 1, ..., N$$

$$H_{2}: x[n] = s_{2}[n] + w[n] , n=0, 1, ..., N$$

$$\vdots$$

$$H_{N}: x[n] = s_{N}[n] + w[n] , n=0, 1, ..., N$$

$$T_{1}(x) = \sigma^{2} \ln \gamma + \frac{1}{2} \sum_{n=0}^{N-1} s_{1}^{2}[n]$$

$$\vdots$$

$$T_{N}(x) = \sigma^{2} \ln \gamma + \frac{1}{2} \sum_{n=0}^{N-1} s_{N}^{2}[n]$$

Figure 3-2 shows the frequency error estimator block with phase rotator and correlator bank. After the packet detection, the FFO, ɛ1 is estimated by the symbol inner product. The FFO of the data has been calibrated after all. The pilot tracer detects signal properties in frequency domain (i.e., The number and position of tones in frequency domain). Each branch in the correlator bank calculates the signal correlation result by the constant sequence, Ri. The Ri is the form expressed in Equation 3-52.

Ri = ifft (
$$[zeros(1, i*4) -1-j zeros(1,63-i*4)]$$
), where i =1 to 15.
(3-52)

There are 16 branches in the correlator bank. The frequency shifted amount $\epsilon 2$ can be decided by the pilot tracer. The overall frequency offset can be detected by

$$\varepsilon = \varepsilon 1 + \varepsilon 2. \tag{3-53}$$



The estimation value is sent to the tunable clock generator, the WSN clock can be tuned accurately.

3-3 PAFEE Method Flow

The overall PAFEE method flow is shown in Figure 3-3. In the beginning, the system is in the initial state. Then the packet detector starts to detect the packet all the time. Once the packet has been detected, the first FFO, is estimated by the inner product. The phase rotator compensates the received data and reduces the FFO for the next procedure. After the packet detection, the correlation bank search for the pilot tone in the frequency domain by the cross-correlation results. Then the IFO is estimated. The summation of the FFO and IFO are sent to the eCrystal and calibrate the frequency mismatch from the CPN side.

This procedure is iterative N times. The 4 short preambles are used in each iteration. N depends on the required performance, and N=3 in our system. After that, the eCrystal is supposed to be tuned accurately in one clock cycle (200 ns) and the

coming data will be distorted by the adjusted clock. By the N iteration time, the eCrystal is accurate at 5MHz. The boundary detector performs the boundary detection. The further fine FFO estimation value has been estimated.



Figure 3-4: Synchronization PAFEE algorithm flow

Chapter 4 Simulation Results and Performance Analysis

The proposed PAFEE method is evaluated in the WiBoC OFDM-based system under AWGN, CFO, and SCO channel conditions. To elaborate the CFO and SCO pre-calibration efforts, the system performance is illustrated in this chapter. In our system, the target SNR at FER = 1% is about 5.4 dB. So it mainly focus on the SNR = 2dB in our synchronization algorithm and make a comparison with the conventional one.

Our target system tolerance frequency error is 2800 ppm. The bandwidth in our system is 5MHz, and the RF frequency is 1.4GHz. The number of preamble pilots in the frequency domain is 12. So the maximum system tolerance is about

$$\max FO = \frac{12}{64/4} \times \frac{5MHz}{1.4GHz} = 2678.6\,ppm \tag{4-1}$$

The "FO" is the abbreviation of "frequency offset". So the target system tolerance frequency error is defined 2800 ppm.

4-1 Simulation on PAFEE -- Packet Detection

4-1-1 ROC Curves

To depict the performance in packet detection, the ROC curves is discussed under different conditions, i.e., different M, L, SNR, frequency error. The characteristic curve of popular conventional approach is shown in Figure 4-1. Each point is simulated by 2000 packets. The ROC curves have a right angle. In other words, there is a threshold value that make the Pd =1 and Pfa =0. However, when the frequency error exists 3000 ppm, the curve is not ideal. We want to find an ROC curve under the large frequency error condition that meets our requirement.

Figure 4-2 shows the comparison between simulation results and theorem deduction from Chapter 3. Take the M=16 and L=1 as the example, the curves are very close under the frequency error 2000 ppm and 3000 ppm. In other words, the deduction model is similar to the real one.



Figure 4-1(a): Frequency error estimation block



Figure 4-2 (a): Comparison between simulation and theorem deduction



To improve the ROC curves to an ideal one, the M value can be increased from the theorem deduction in Chapter 3. The other way is to increase the depth L. Here we introduce the parameter, L. The packet detection procedure is shown in Equation 4-2.

$$V(n) = \frac{|C(n)|^{2}}{P(n)}$$
where $C(n) = \sum_{i=0}^{M-1} r_{i+n}r_{i+n+M}^{*}$, and $P(n) = \sum_{i=0}^{M-1} |r_{i+n+M}^{*}|^{2}$
(4-2)

Summation of the V(n) during L time is shown in Equation 4-3.

$$V_{\rm L}(n) = \frac{1}{L} \sum_{i=0}^{L-1} V({\sf n+i})$$
(4-3)

Then the $V_{L}(n)$ is defined as the new timing metric. The operation can flatten the noise effect and achieve performance improvement. The Figure 4-3 shows the simulation results under different L conditions.

In our system, the M is chosen to be 32, and L is 32. This can make the ROC curves to the ideal one under FO = 2800 ppm as shown in Figure 4-4.



Figure 4-3: ROC curves in different L



Figure 4-4: ROC curves in conventional one and proposed one

4-1-2 Detection Rate, False Alarm Rate Versus SNR

Though the detection rate is guaranteed to be 1 under SNR = 2 dB by the proposed algorithm, the low-SNR condition is also simulated, i.e., SNR < 1 dB. The proposed algorithm has bad performance under low SNR conditions. If we want the performance remain the same under some SNR conditions we expect, the M and L have to be redefined. This effect can be described by algorithm in Chapter 3-2. If it is under low SNR condition, the alternative hypothesis is approximate to central F-distribution. The ROC curve is close to a straight line. The detection rate and false alarm rate versus SNR are shown in Figure 4-5 and Figure 4-6. The threshold is chosen to be 0.29 for conventional one, and 0.19 for proposed one. The false alarm rate is lower than the conventional one due to the noise is white in the overall spectrum. In the Figures 4-5 and 4-6, 2000 packets are simulated.



Figure 4-6: False alarm rate in conventional one and proposed one
Figure 4-6 shows the false alarm rate of the proposed algorithm compared to the conventional algorithm. For the data are all noise, the plot are randomly distributed.

4-1-3 Detection Rate Versus Frequency Error

The detection rate under different frequency error conditions are simulated, i.e., SCO is from -2800 ppm to 2800 ppm, and CFO is from -2800 ppm to 2800 ppm with threshold, 0.19. Figure 4-7 and Figure 4-8 shows the detection rate versus different frequency error under SNR 1 dB and 2 dB respectively. Each condition is simulated in 2000 packets. The detection rate is guaranteed to be 1 in any frequency error under SNR 2 dB.



Figure 4-7: Detection rate under different CFO and SCO conditions, SNR=1 dB



Figure 4-8: Detection rate under different CFO and SCO conditions, SNR=2 dB

1896

Here we simulate different frequency offset conditions, i.e. CFO and SCO. For the baseband and the synthesizer clock source are from eCrystal, in our system, the value of the CFO and SCO are the same. We use the frequency offset, FO, to show the CFO and SCO effect at the same time. Figure 4-9 shows the Detection rate under different FO and SNR conditions. The worst case of the detection rate is under 2800 ppm condition.



4-2 Simulation on PAFEE -- Frequency Error Estimation

To depict the performance of frequency error estimation, the estimation correct rate versus different frequency error is shown in Figure 4-10. The estimation correct rate is 1 when the estimation error is smaller than 50 ppm. The maximum value of remaining error after estimation is smaller than 2800 ppm. In other word, this procedure won't make the system divergent, i.e., frequency error > 2800 ppm. The maximum remaining error versus frequency error under different SNR condition is shown in Figure 4-11. Each condition is simulated by 5000 packets.





Figure 4-11 (b): Maximum remaining error versus frequency error (Zoom-in)

In order to let frequency error estimation be stable under 2 dB, we increase the short preamble length and recursive the estimation procedure. Let the estimation correct rate is Pec, and the estimation error rate is Pee, which is 1-Pec. The recursive times is N. The new estimation correct rate and estimation error rate are shown as Equations 4-4 and 4-5 respectively.

$$P_{ee}' = P_{ee}^{N} = (1 - P_{ec})^{N}$$
(4-4)

$$P_{ec}' = 1 - P_{ee}^{N} = 1 - (1 - P_{ec})^{N}$$
(4-5)

The N=3 is selected, the estimation correct rate will be approximate to 1, i.e., 0.999973, under SNR=1dB and FO=2800 ppm conditions. That is, 12 short preambles are transmitted for synchronization.

4-3 Simulation on System PER Performance

The overall system performance is illustrated in Figure 4-12. The performance target is packet error rate (PER) 1%., i.e., PER = 1% @ SNR = 5.4dB. Apply the conventional method, the system only tolerate frequency error below 100 ppm. The system performance can not coverage under large frequency error conditions, i.e. PER = 100 %. With the proposed technique, the system tolerates larger frequency error and the performance remains the same. Each condition is simulated in 5000 packets.



If iteration time N=1 is simulated, the performance curves are shown in Figure 4-13. The performance is loss due to the estimation correct rate is slightly declined. Four short preambles are used in a iteration. If the iteration time is 3, that means 12 preambles are used. The clock is tuned after one synchronization procedure, that is, the clock will be tuned 3 times when the N is 3.



Chapter 5

Hardware Implementation

5-1 Overall Architecture

In this chapter, the hardware implementation for synchronization algorithm is introduced in wireless sensor node receiver part. For the detailed information of the overall WSN system tapeout chip, please reference to the appendix B. Figure 5-1 shows the receiver part in WSN, our algorithms are composed by gray blocks.



Figure 5-1: Overall architecture of WSN system

5-1-1 Packet Detector

Equation 5-1 shows the operation of the packet detector.

$$V(n) = \frac{\left|\sum_{i=0}^{M-1} r_{i+n} r^{*}_{i+n+M}\right|^{2}}{\sum_{i=0}^{M-1} \left|r_{i+n+M}\right|^{2}}, \text{ where } M=32.$$
(5-1)

There is one input FIFO with 192 registers in the receiver, 96 for I channel data and 96 for Q channel data. To implement Equation 5-1, the following components are required: one FIFO with 96 registers, 4 multipliers, 4 square multipliers, 7 adders, 3 substracters, and one divider. Figure 5-2 shows the hardware architecture of the packet detector.

Equation 5-2 shows the moving average operation.

$$V_{\rm L}(n) = \frac{1}{L} \sum_{i=0}^{\rm L-1} V({\rm n+i})$$
(5-2)

The moving average is a simple architecture as shown in Figure 5-3. In our application, L = 32, so there are 33 registers, 1 adder, and 1 substracter are used.



Figure 5-2: Hardware architecture of packet detector



Figure 5-3: Hardware architecture of moving average

5-1-2 Phase Rotator

The phase rotator is implemented in order to solve the FFO problems. First the phase error is calculated by Equation 5-3.



Figure 5-4: Hardware architecture of phase rotator in packet detection state

The hardware architecture of the phase rotator is shown in Figure 5-4. Once the packet detector detects the data, the phase rotator estimate the FFO $\hat{\varepsilon_{r_1}}$. After the packet detection, the system waits 32 cycles to calibrate the data as shown in Equation

5-4.

$$r'_{i+n+M} = r_{i+n+M} \times (\cos(M\widehat{\varepsilon_{f1}}) + j\sin(M\widehat{\varepsilon_{f1}})), \quad \text{M is from 0 to 31}$$
(5-4)

The calibrated data is stored after FIFO 32.

After 32 cycles, the other fine FFO estimation is shown in Figure 5-5. The FFO $\widehat{\varepsilon_{r_2}}$ is estimated from the calibrated data to achieve the more accurate phase value. The data calibration after that is shown in the Equation 5-5. N represents Nth cycle after the 32 cycles.

$$r'_{i+n+N+32} = r_{i+n+N+32} \times (\cos((32+N)\widehat{\varepsilon_{f1}} + \sum_{i=0}^{N} \widehat{\varepsilon_{f2}}) + j\sin((32+N)\widehat{\varepsilon_{f1}} + \sum_{i=0}^{N} \widehat{\varepsilon_{f2}}))$$
(5-5)

The two operations happen in different time, so the hardware can be shared by using a multiplexer. The total hardware are composed by 6 multipliers, 4 adders, 2 subtracters, 1 arc tangent table, 1 cosine table, 1 sine table, and 1 phase accumulator. The phase accumulator is composed by one multiplier and one adder.



5-1-3 Frequency Error Estimator

The hardware architecture of the frequency error estimator is shown in Figure 5-6. From the chapter 3, the correlation coefficient is shown in Equation 5-6.

$$Ri = ifft ([zeros(1, i*4) -1-j zeros(1,63-i*4)]), where i is from 1 to 15.$$
 (5-6)

The 64-point cross-correlation is used in our system, so the the length of Ri is 64. It is easily find that 64 points is repeated every 16 points, the hardware is simplified a lot. The 16 points real and imaginary part of Ri are shown as Figure 5-7 and 5-8. The calibrated data store in the input FIFO from 32 to 95 is used for the cross-correlation. The pilot tracer decides the correlation coefficient from the correlation bank, then the correlation results tell the pilot is detected or not. After 15 position of the pilot is finished detect, the pilot tracer checks the mapping table to determine the frequency error.



Figure 5-6: Hardware architecture of frequency error estimator



Figure 5-7: Real part of the Ri, i is from 1 to 16



The baseband processor has been implemented in fixed point hardware. In this section, the simulation results after the quantization are illustrated.

5-2-1 Simulation on PAFEE -- Packet Detection

To show the performance of packet detection, the ROC curve after the quantization is shown. Figure 5-9 shows the ROC curve under the frequency error 2800 ppm and SNR 2 dB. Each point is simulated in 2000 packets. There is one point with the characteristic, Pd=1 and Pf =0. The threshold 0.19 is chosen in the timing metric for detecting the packet, which is the same as floating point one. Figure 5-10 shows the detection rate under different frequency error conditions. Each condition is

simulated in 2000 packets. The detection rate is 1 under different frequency error conditions. In other words, the quantization procedure will not affect the performance of packet detection.



Figure 5-9: Fixed point ROC curves



5-2-2 Simulation on PAFEE -- Frequency Error Estimation

After quantization, the estimation correct rate is decreased from 0.97 to 0.957. Figure 5-11 shows the estimation correct rate versus frequency error. The threshold of the correlation output is 0.0024. The worst condition of the estimation correct rate is 0.957. The maximum remaining error versus frequency error is shown in Figure 5-12. The worst case of the maximum remaining error is smaller than 2800 ppm. In other words, the system will be convergent after N iterations. The N has to be decided here.

The estimation correct rate is Pec, and the estimation error rate is Pee. N is the iteration times. Equation 5-7 and Equation 5-8 show the new estimation correct rate and estimation error rate after N iterations.

$$P_{ee}' = P_{ee}^{N} = (1 - P_{ec})^{N}$$
 (5-7)

$$P_{ec}' = 1 - P_{ee}^{N} = 1 - (1 - P_{ec})^{N}$$
(5-8)

The worst case of Pec is 0.957. To achieve estimation correct rate larger than 0.9999 under SNR 2 dB, the N is chosen to be 3, which is the same as fixed point one.



Figure 5-11: Fixed point estimation correct rate versus frequency error



Figure 5-13 shows the packet error rate versus SNR. The iteration number is N=3. The fixed point curve is attached to floating one. In other words, the performance is almost remains the same after the quantization.



5-3 Hardware Overhead

Compared to the conventional synchronization method, to achieve the large frequency error tolerance, the hardware area overhead is shown in Table 5-1. The design hardware is evaluated in UMC 90 nm process. The conventional approach, the synchronization hardware is composed by packet detector and phase rotator. The conventional approach is able to overcome 100 ppm frequency error. To overcome the larger frequency error, the different packet detector and frequency error estimator are used. From the synthesis results, the overall hardware overhead is 60104 μ m² in 90nm technology. The synthesis tool is Synopsys Design Compiler.

The power overhead is shown in Table 5-2. The power analysis tool used is Synopsys PrimePower. 500 packets are simulated. The total power overhead of the proposed one is about 148.5 μ W. The packet detector is about 50 μ W more than the conventional one. And the frequency error estimator is about 100 μ W.

Hardware		Conventional one	Proposed one
		(μm * μm)	(μm * μm)
Packet detector		20762	39535
F	Phase rotator:	24765	24765
	FFO estimator	E S ¹¹⁰⁹³	11093
	cosine table	53250	5325
	sine table	4857	4857
	arc tangent table	3490	3490
Frequency error estimator		0	41331
Total		45527	105631
Hardware overhead		0	60104
Gate count overhead		0	21298
(Area / 2.822) for 90nm process			21200

Table 5-1: Area overh	iead
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	Conventional one	Proposed one		
Hardware				
	(μW)	(μW)		
Packet detector	52.21	106.6		
Cosine table	2.053	2.090		
Sine table	1.900	1.939		
Arc tangent table	0.932	0.918		
Frequency error estimator	0	94.97		
Others (FIFO + FSM)	117.0 IF S	117.0		
Total	174.6	323.1		
Hardware overhead	1890	148.5		

Table 5-2: Power overhead

Chapter 6 Emulation of Crystal-less Baseband System

6-1 Building Block

In this chapter the hardware emulation is implemented for crystal-less WiBoC baseband system downlink procedure. The overall system building block is shown in Figure 6-1. In the downlink procedure, the CPN is regarded as the transmitter and the WSN is regarded as the receiver. The CPN transmit some preambles to the downlink channel, and the WSN detects the preambles and performs the synchronization in FPGA. The CLK source in the CPN used is an accurate crystal clock source. In the WSN, the crystal-less tunable clock source is used. After the downlink procedure, the clock in WSN will be tuned accurately. The clock mismatch from the CPN side will be reduced.



Figure 6-1: Hardware emulation building blocks

6-2 Evaluation System

The baseband and ADDA system are integrated in WPI board. The received signal from the AD is stored in the FPGA and then send to the PC. The RF system is composed by several commercial products, one modulator, one demodulator and two synthesizers. The modulator has 2 differential inputs for I channel data and 2 for Q channel data. The demodulator has 2 differential outputs for I channel data and 2 for Q channel data. To demonstrate the frequency error channel, two synthesizers are used. One is for modulator and the other is for demodulator. The synthesizer is programmed by MCU to achieve 280x from 5MHz, i.e., 1.4 GHz.



Figure 6-2: Evaluation system

	Component	Type Specification
А	FPGA	Xc2v4000 4bf957
В	FPGA	Xc2v6000 4bf957
С	DAC	MAX5888 16-bit 500Msps DAC
D	ADC	AD6644 14-bit 40Msps ADC
Е	Modulator	AD8346 0.8 to 2.5GHz Modulator
F	Demodulator	AD8347 0.8 to 2.7GHz Demodulator
G	Synthesizer	AD4360-5 1.2 to 1.4GHz Synthesizer
Н	CPN clock	Crystal oscillator clock generator
Ι	WSN clock	Clock source from function generator
J	RF antenna	N/A (RF cable now), lack of BPF
K	MCU	MCU integration board

Table 6-1: Baseband components

The clock source in CPN side is from an accurate crystal oscillator. And the clock source in WSN side is from the function generator, which plays a role of large error and tunable clock source.

If it is desired to demonstrate the frequency error 1000 ppm, the clock frequency can be set in 5MHz and 5.005MHz. The synthesizer will produce 1.4 GHz and 1.4014 GHz respectively. The components in the overall evaluation systems are shown in Table 6-1.

6-3 Emulation Results

The received signal (I channel) is shown in Figure 6-3 from the spectrum analyzer. The part (A) represents the preamble signal without any frequency error. The part (B), (C), and (D) represent the preamble with frequency error 1000, 2000, and 2800 ppm respectively. For there is no bandpass filter in the RF band, the pilot tones that shifted out of the bandwidth are preserved.



Figure 6-3: Received signal shown in spectrum analyzer

Table 6-2 shows the relationship between frequency error and clock period. The crystal oscillator clock source is used in CPN, it has 5MHz frequency and RMS jitter 210 ps. The clock source in WSN is from the function generator.

	CPN clock period (Crystal)		WSN clock period (Crystal-less)	
FO	frequency (MHz)	RMS jitter (ps)	frequency (MHz)	RMS jitter (ps)
0 ppm	5.0000	210	5.0000	126.6
400 ppm	5.0000	210	5.0020	142.6
800 ppm	5.0000	210	5.0040	177.4
1200 ppm	5.0000	210	5.0060	221.4
1600 ppm	5.0000	210	5.0080	269.4
2000 ppm	5.0000	E 210 M	5.0101	320.8
2400 ppm	5.0000	210	5.0120	368.8
2800 ppm	5.0000	210	5.0140	415.6

Table 6-2: The relationship between frequency error and clock period

Figure 6-4 and 6-5 shows the processed received signal and its estimation results by the MATLAB. The FFO in the preamble has been calibrated, and then the frequency estimator finds the pilot position by the frequency estimator and estimates the frequency error by this information. The FFT of the signal is also shown compared to the frequency estimator results.



Figure 6-4: Estimation results with frequency error 0, 400, 800, 1200 ppm



Figure 6-5: Estimation results with frequency error 1600, 2000, 2400, 2800 ppm

Chapter 7

Conclusions and Future Work

7-1 Conclusions

The system performance in crystal WiBoC system and crystal-less WiBoC system is shown in Table 7-1. In the crystal platform, the main components for clock generation are the external crystal and crystal oscillator pad. The external crystal oscillator occupies large area and makes it difficult to implement system on chip (SoC) design. The oscillator pad consumes a lot of power in the crystal system. Compared to the components in the crystal-less system, the area of synchronization hardware, and DCO occupies only 0.46mm², which have 98.4% area reduction from crystal system.

The power consumption to the overhead component in crystal-less platform is only 10.7 % of crystal system. The eCrystal system has 89.3 % power reduction and 98.4% area reduction.

The synchronization method for OFDM-based WBAN applications is proposed. With this proposal, the communications system can be integrated into the crystal-less system and is enabled with larger frequency errors, i.e. 2800 ppm. This work can be implemented in others OFDM systems. Apply this method to the others systems, the CPN has to transmit the downlink preamble to WSN for symbol timing synchronization and frequency error estimation. The tolerated frequency range is up to bandwidth over RF frequency.

	WiBoC on crystal platform	WiBoC on crystal-less platform	
Hardware overhead	 (1) Crystal oscillator [11] (2) Oscillator pad 	 Proposed algorithm eCrystal [24] 	
Area overhead	 (1) 8 mm² [11] (2) 0.0147 mm² 8.01 mm² (total) 	(1) 0.06 mm^2 (2) 0.40 mm^2 [24] 0.46 mm^2 (total)	
Power overhead	 (1) 1.8 μW (crystal) [11] (2) 3625 μW (osc pad) 3626.8 μW (total) 	 (1) 149 μW (2) 237 μW [24] 386 μW (total) 	

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Table /-1:	System	comparison	summarv
	·		····)

The overall design characteristics are summarized in Table 7-2 in terms of hardware and system specifications. The designed hardware is evaluated in UMC 90nm process. In the data processing, the overhead power consumption is 148.5 μ W. In the system design features, the WiBoC follows the constraints defined in WMTS with the provided maximum data rate 4.85Mbps.

Parameter	Feature	
Technology	Std. 90nm CMOS	
Area overhead	$60104 \ \mu m^2$	
Gate count overhead	21298	
Power overhead	148.5 μW	
RF band	1395-1400MHz	
Spectrum Bandwidth	5MHz	
Constellation Mapper	QPSK	
IFFT/FFT Block Size E S	64	
Maximum Data Throughput	4.85 Mbps	
Guard Interval Duration	0.4µs	
Data Bit per OFDM symbols	48	

Table 7-2: WiBoC OFDM system summary

7-2 Future Work

In the future, the preamble packet can be designed to improve the baseband processing, i.e., reduce the iteration times and enlarge the frequency error tolerance.

The prototype platform will be upgraded and replaced the RF cable by the RF antenna and low noise amplifier. The mechanism of auto gain control (AGC) will be added in the prototype platform. The integration communication PCB board is under

development.

However, the algorithm is limited by the bandwidth and RF specification, the initial error of the crystal-less clock generator needs to be improved. If the initial error of the eCrystal is reduced, it will ease the design effort in algorithm part.

Based on the following progress, the WSN can be re-designed and improved to become a low power, low cost, stabilization and miniaturized single chip.



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Appendix A Embedded Crystal Design

A-1 Introduction

The wireless body area network (WBAN) plays a crucial role in human body health monitoring for medical services. For the low cost, low power and tiny area WBAN applications, the embedded crystal (eCrystal) method is proposed in [6] by NCTU. In the wireless communications system, the system clock generates by a crystal oscillator. The oscillator occupies large area and consumes large power. By the eCrystal technique, it is tend to replace the crystal oscillator by other low power, standard CMOS process oscillator circuits.

One solution of the fine resolution DCO is LC tank DCO [25] by 0.13 μ m CMOS process. However, the LC tank DCO is not the standard CMOS process and needs extra lithography technology. The LC tank occupies large area and consumes a lot of power. This is not suitable for WBAN applications.

Another solution of the accurate DCO is MEMS [26] oscillator. The MEMS has smaller frequency error and better accuracy than the other oscillator in standard CMOS process. But the drawbacks of the MEMS are the long design cycle and the tunable mechanism is not digital.

The standard CMOS oscillator design depicts the flexibility of design CMOS circuits, and it is easy to integrate with other CMOS circuits. The well-known CMOS oscillator directly uses an inverter chain to create the oscillator behavior. But

it consumes much power in transition current. To save the power, the hysteresis delay cell (HDC) is used in [27]. Based on the segmental delay line and hysteresis delay cell architecture, the power consumption can be saved up to 70%.

In our design, we proposed another hysteresis delay cell to save the power. However, the hysteresis cell does not have good resolution, so we used a fine-tuned stage to cover the coarse-tuned range and increase the resolution.

The DCO is realized on a 1p9m 90nm CMOS process. The target frequency is from 10MHz to 35MHz, which is the frequency for baseband clock applications in WBAN system. This design have been simulated in three PVT conditions, (FF, 1.1v, 0oC), (TT, 1.0v, 25oC), and (SS, 0.9v, 100oC). The operating frequency range at typical case is from 3MHz to 350MHz from the HSPICE simulation results. The measurement results of the test chip are followed in section A-3. We measure the chip in several supply voltage condition to observe the voltage variation in this DCO test circuit.

This appendix A is arranged as followed. In section A-2, proposed DCO architecture are presented, and section A-3 shows the test chip measurement results. The test chip is measured under different supply voltage conditions. The results are present in terms of the frequency range and RMS jitter performance. Then the comparison of existing solutions of DCO is provided in section A-4. The conclusion is followed in section A-5.

A-2 Proposed DCO

A-2-1 DCO Architecture

Figure A-1 illustrates the proposed DCO architecture. This design is composed of one coarse-tuned stage and one fine-tuned stage. The SEL signal is the codeword to control the DCO frequency. The coarse-tuned stage provides longer delay and spends less power. The fine-tuned stage provides smaller resolution. In each stage, the delay time of the codeword is proportional to the output period.



A-2-1 Coarse-tuned Stage

To reduce the power and area of the DCO, we use the Schmitt trigger cell providing large delay to reduce the area and the power. The architecture of coarse-tuned stage is shown in Figure A-2. The bit number of tuning codeword is 7, and there are 128 codewords. We create the delay cell in each element and make the delay time 2x in each element compared to the previous element. In other words, the delay time in (N+1)th element is twice of the Nth element, N is from 1 to 6. The delay cell in each element, ST1D, ST2D, and ST3D as shown in Figure A-2 are one Schmitt trigger cell with some umc 90nm standard cell as its output loading. The delay cell in ST4D, ST5D, ST6D and ST7D are composed by the three elements of ST1D, ST2D, amd ST3D. They are designed to create different delay. The

transistor-level structure of Schmitt trigger delay cell is shown in Figure A-3. And the cell in each stage is shown in the Table A-1.

The delay time of the coarse-tuned stage can be illustrated as the following equation,

$$T_{coarse} = \sum_{N=0}^{6} T_{STND} \times SEL[N] + T_{cons \tan t}$$
(A-1)

Where T_{STND} represents the delay in each delay element of Schmitt trigger stage, i.e, N=3 means ST3D. Each bit of the select signal can be 1 or 0. If the delay time of the element follows the rule that the delay time in the N+1 element is twice of the N element, then the T_{coarse} can be expressed as

$$T_{coarse} = \sum_{N=0}^{6} 2^{N} \times SEL[N] + T_{eonstant}$$
(A-2)

This structure can reduce one decoder and save the area of the large input of multiplexers compared to the traditional DCO structure.



Figure A-2: Coarse-tuned stage



Figure A-3: Schmitt trigger cell

	ST cell (W/L)	Cload
ST1D	0.2/0.08	1 BUFM16H
ST2D	0.2/0.08	1 BUFM16H + 2 BUFM14H
ST3D	0.2/0.08	5 BUFM20H + 1 BUFM8H
ST4D	0.2/0.08	2 ST3D
ST5D	0.2/0.08	3 ST3D + 1 ST2D
ST6D	0.2/0.08	7 ST3D + 1 ST1D
ST7D	0.2/0.08	13 ST3D + 2 ST2D

Table A-1: Delay element in coarse-tuned stage

A-2-2 Fine-tuned Stage

Figure A-4 shows the fine-tuned stage. The delay element in this stage is

INVMON, which is the standard cell in UMC 90nm CMOS process. The structure in this stage is the same as the coarse-tuned stage. The delay time in N+1 elements is twice of the N elements, N is from 1 to 6. The fine-tuned stage have 7 delay elements, INV1D, INV2D, INV3D, INV4D, INV5D, INV6D, INV7D. The number of the delay cell in N+1 elements is designed to the twice of the N elements, N is from 1 to 6, too. This can achieve linearity in fine-tuned stage. There are 128 codewords in this stage, too. This stage provides small resolution and the delay range can cover the LSB resolution in coarse-tuned stage. The delay time is proportional to the number of the delay inverter cell. The cell in each stage is shown in the Table A-2.

In the same way, the period of the DCO in fine-tuned stage also can be expressed as followed, $T_{\text{fine}} = \sum_{N=0}^{6} T_{\text{INVND}} \times \text{SEL}[N+7] + T_{\text{constant}}$ $= \sum_{N=0}^{6} 2^{N} \times \text{SEL}[N+7] + T_{\text{constant}}$ (A-3)

The overall period of the DCO output clock can be expressed as the following equation,

$$T_{\text{period}} = T_{\text{coarse}} + T_{\text{fine}} + T_{\text{constant}}$$
(A-4)

where the T_{coarse} denotes the delay time in the coarse-tuned stage resulting in coarse-tuned codeword as Equation A-2. The T_{fine} represents the delay time in the fine-tuned stage as Equation A-3.



Figure A-4: Fine-tuned stage

	INV cell (W/L)	C _{load}
INV1D	0.36/0.08	2 INVM0N
INV2D	0.36/0.08	4 INVM0N
INV3D	0.36/0.08 E S	8 INVM0N
INV4D	0.36/0.08	16 INVMON
INV5D	0.36/0.08	32 INVMON
INV6D	0.36/0.08	64 INVMON
INV7D	0.36/0.08	128 INVM0N

Table A-2: Delay element in fine-tuned stage

A-3 Measurement Results

The test chip is fabricated using a standard 90nm 1p8m CMOS process. The DCO behavior is described in gate-level by Verilog-HDL. The DCO model is also built in HSPICE simulation and the delay time is accurately simulated. This design have been simulated in three PVT conditions, (FF, 1.1v, 0oC), (TT, 1.0v, 25oC), and (SS, 0.9v, 100oC). The Schmitt trigger cell is layouted by EDA tool in a format of

standard cell. An automatic placement and routing (APR) tool is used to complete the physical layout with the added hand-made Schmitt trigger cell. The post layout after APR is also simulated to ensure the codeword linearity of the DCO.

The proposed DCO occupies only 0.0063 mm^2 (210µm x 30µm). This DCO has been measured in 6 different voltage conditions to observe the linearity, resolution, power and RMS jitter in each condition.

A-3-1 Coarse-tuned Stage

Figure A-5 shows the period of the coarse-tuned stage DCO under different supply voltage condition. The operating frequency is from 3.5MHz to 153.25MHz when the supply voltage is 1.0v. The mean value of LSB resolution in the coarse-tuned stage is 2.15ns. Table A-3 shows frequency, LSB resolution, and RMS jitter of the DCO under every different supply voltage condition. The operating supply voltage is from 1.5v to 0.8v. We can observe the DCO frequency in terms of voltage variation. When the supply voltage is 1.1v, the period is about 0.7 times of the one with supply voltage 1.0v. When the supply voltage is 0.9v, the period is about 1.6 times of the one with supply voltage 1.0v. The small amount of voltage variation will cause large frequency change. The larger the supply voltage results in the high frequency, small resolution, small RMS jitter, and high linearity.

Figure A-6 shows the RMS jitter performance in different codeword under different supply voltage conditions. The jitter is large under low supply voltage condition. The variation of the jitter in different codeword is not so much.



The period of DCO in coarse-tuned stage

Figure A-6: The RMS jitter of DCO in coarse-tuned stage

Supply Operating		Resolut	ion (ns)	RMS jitter (ps)	
voltage	(MHz)	Max	Mean	Max	Mean
1.5 V	11.56 to 348.44	3.74	0.66	71.02	46.77
1.2 V	6.70 to 238.11	6.13	1.14	168.87	96.27
1.1 V	5.10 to 197.88	7.81	1.50	222.83	148.72
1.0 V	3.56 to 153.25	10.62	2.15	416.07	242.40
0.9 V	2.20 to 110.37	20.87	3.50	807.97	511.73
0.8 V	1.23 to 59.52	31.87	6.26	1503.2	968.03

Table A-3: DCO in coarse-tuned stage



A-3-2 Fine-tuned Stage

Figure A-7 shows the period of the fine-tuned stage DCO under different supply voltage condition. The mean of the resolution is 134.5 ps at the condition that supply voltage = 1.0 v. When the supply voltage is 1.1 v, the LSB resolution is about 0.84 times of the one with supply voltage 1.0 v. When the supply voltage is 0.9 v, the LSB resolution is about 1.28 times of the one with supply voltage 1.0 v. It shows that the effect of voltage variation is lighter than the coarse-tuned stage. The tuning range in the fine-tuned stage can cover the LSB resolution in coarse-tuned stage. When the supply voltage = 1.5 v, the mean and max RMS jitter in fine-tuned stage are close to the ones in the coarse-tuned stage, and can achieve LSB resolution 76 ps in overall DCO. Table A-4 shows the tuning range, LSB resolution, and RMS jitter of the DCO fine-tuned stage under every different supply voltage condition.

The following Table A-5 shows the power consumption under different supply voltage conditions. The higher the frequency, the larger the power consumes. The largest power consumption 190 μ W happens at frequency 160MHz when the supply voltage is 1.0v.



Figure A-7: The period of DCO in fine-tuned stage



Figure A-8: The RMS jitter of DCO in fine-tuned stage

Table A-4: DCO in fine-tuned stage

Supply	ply age Tuning Range (ns)	Resolut	Resolution (ns)		RMS jitter (p)	
voltage		Max	Mean	Max	Mean	
1.5 V	9.65	195.04	75.99	67.79	33.00	

1.2 V	12.53	421.44	98.67	119.49	39.08
1.1 V	14.47	283.65	113.29	94.46	40.36
1.0 V	17.08	669.32	134.50	90.84	42.34
0.9 V	21.88	1796.25	172.26	210.36	69.32
0.8 V	26.21	5275.42	198.26	2601.23	259.86

Table A-5: DCO power consumption under different supply voltage

Supply voltage	Working frequency (MHz)	Power consumption (µW)
1.5 V	10.09 to 348.87	832.5 to 4335
1.2 V	6.02 to 228.33	157.2 to 368.4
1.1 V	4.64 to 200.09	103.2 to 267.3
1.0 V	3.29 to 159.23	62.4 to 190.0
0.9 V	2.06 to 115.40	34.5 to 126.0
0.8 V	1.17 to 65.34	18.2 to 77.5

A-4 System Comparison

Table A-6 lists the chip measurement results compared with some conventional approaches [28], [29], [30]. The comparison results show in terms of resolution and power consumption. The proposed DCO also have the benefits of portability due to its tiny area and less power consumption.

Performance Index	Proposed DCO	TCAS2'05 [28]	JSSC'04 [29]	JSSC'03 [30]
Process	90nm CMOS	0.35mm CMOS	0.35mm CMOS	0.35mm CMOS
Supply	1.0	3.3	3.0	3.3
Wordlength	14	15	7	12
Operation Range(MHz)	3.3~159	18~214	152~366	45~510
LSB resolution	134ps	1.55ps	10~150ps	5ps
Lower freq. (<10 MHz) enabled	YES	NG A	NO	NO
Power Consumption	190µW @160MHz	18mW96 @200MHz	12mW @366MHz	50mW @500MHz

Table A-6: DCO performance comparison

A-5 Conclusion

In this section, an ultra small area, low power, and large delay DCO based on Schimitt trigger delay element is designed. The coarse-tuned stage provides large delay and saves much more area and power. The fine-tuned stage covers LSB resolution of the coarse tuned stage and provides good linearity. The test chip measurement results show the DCO can achieve 134 ps resolution and large frequency operation range under supply voltage = 1v. The DCO is enabled in lower frequency, which is suitable for baseband applications. The DCO is evaluated in standard CMOS process and implemented by APR tool.

Appendix B IP Deliverable

B-1 Overall Architecture

This wireless sensor node (WSN) is a baseband platform in communications system. It contains 2 major components, a transmitter (WSN_TX) and receiver (WSN_RX) module. The baseband receiver receives the downlink data from the downlink channel, and analyzes the data, feedback a frequency error value to tune the baseband clock. After the RX processing, the TX modulate the signal and transmit to the uplink channel. The overall architecture is shown in Figure B-1.



Figure B-1: Overall architecture of WSN system

B-2 Architecture of Receiver

B-2-1 Components

The baseband receiver is composed by phase rotator, downlink synchronizer, and the frequency error estimator. When the receiver receives the downlink data from the downlink channel, the baseband processor will analyze the data and feedback a frequency error value to the DCO-based clock generator. The baseband clock will be tuned accurately and reduce the clock mismatch from the central processing node side. The component in WSN_RX is list in Table B-1.

RTL code file name	Descriptions
WSN_RX.v	WSN RX top module
Sin13to10.v	Sin table for phase rotator
Cos13to10.v	Cos table for phase rotator
Arctan6to13.v	Arc tangent table for phase rotator
MULTI64.v	The multiplier shared by boundary detection and correlation part.
INNER_PRO.v	The autocorrelation part. The correlation length and the moving average of the correlation sum can be tuned.
INNER_PRO2.v	The phase rotator.

Table B-1: The component in WSN_RX

Table B-2 shows the mode of operation in WSN_RX. The M and L can be adjusted for different SNR conditions. The PARAM_RF_TH can be adjusted for different bandwidth and frequency allocation conditions.

Name	I/O	Width	Simple description	Default value
PARAM_AUTOM	Ι	1	Autocorrelation length. 0: M=16, 1: M=32	From 0~ 1
PARAM_AUTOL	Ι		Moving average. 0: L=1, 1: L=16, 2: L=32, 3: L=48	From 0~ 3
PARAM_AC_TH	Ι		Autocorrelation threshold	7'h 17
PARAM_BOOK_TH	Ι	19	Pattern book writing threshold	19'h 50
PARAM_BANK_TH	Ι	9	Correlation threshold	9'h 00e
PARAM_CC_TH	Ι	11	Boundary detection threshold	11'h 3d
PARAM_RF_TH	Ι	13	RF spec. (i.e: BW/RF/16 = 223)	13'd 223

Table B-2: Mode of operation in WSN_RX

B-2-3 External Signal Descriptions

The external signal description is shown in Table B-3. After the reset state, the baseband receiver will process the IN_I and IN_Q input signal. It performs the packet detection and frequency error estimation. The first output is FERR_COARSE, represents the coarse frequency error estimation value. After boundary detection, the second output FERR FINE is given. The overall receiver processing is over.

name	I/O	width	Simple description	
CLK	Ι	1	Clock signal. This design operates at positive edge clock	
RESET	Ι	1	Synchronous, active-high reset signal	
IN_I	Ι	6	I channel input signal	
IN_Q	Ι	6	Q channel input signal	
FUNC_EN	Ι	1	Function enable. 1: enabling the overall state diagram	
P_EN	Ι	1	Process enable. 1: enabling the initial state diagram	
FERR_COARSE	0	13	coarse frequency error estimation amount valid with OUT_VALID_COARSE	
FERR_FINE	0	13	fine frequency error estimation amount valid with OUT_VALID_FINE	
OUT_VALID_COARSE	0	1	valid signal for coarse frequency error estimation	
OUT_VALID_FINE	0	1	valid signal for fine frequency error estimation	
D_STATE	0	4	debug output (state diagram)	
PARAM_AUTOM	Ι	1	autocorrelation length. 0: M=16, 1: M=32	
PARAM_AUTOL	Ι	2	moving average. 0: L=1, 1: L=16, 2: L=32, 3: L=48	
PARAM_AC_TH	Ι	7	autocorrelation threshold	
PARAM_BOOK_TH	Ι	19	pattern book writing threshold	
PARAM_BANK_TH	Ι	9	correlation threshold	
PARAM_CC_TH	Ι	11	boundary detection threshold	
PARAM_RF_TH	Ι	13	RF spec. (i.e: BW/RF/16 = 223)	

Table B-3: External signal description in WSN_RX

B-2-3 FSM

The FSM in WSN_RX is shown in Figure B-2. The state description is list in Table B-4. The state is designed simple and easy to control. The hardware can be shared under different state conditions. When one state is active, the other states are inactive and consume less power.



Figure B-2: FSM of WSN_RX

state	state descriptions:
inist	initial state
autost	autocorrelation state for packet detection.
syncst	synchronization state for frequency tone detection
calist	calibration state: calibrate 64 data
cfoest	frequency error estimation state
bookst	(one cycle) pattern book match
bdetst	boundary detection state
finest	fine CFO estimation state
fishst	(one cycle) finish state

Table B-4: State description in WSN_RX

B-2-4 Area

Table B-5: Area reports in WSN_RX

module name		area (m ²)
WSN_RX		344239.967741
	cos13to10	5327.893139
	sin13to10	4857.282127
	arctan6to13	3491.967093
	MULTI64	222041.215886
	INNER_PRO	42006.091436
	INNER_PRO2	11236.061129

The area cost in terms of synthesis results and post-layout results are described. The hardware area from synthesis report is shown in Table B-5. The synthesis tool is Design Compiler. The post-layout results are shown as below. The place and route (P&R) tool is Cadence RTL Encounter. The P&R view of WSN_RX is shown in Figure B-3.



Core area: 770 * 800 μ m² Hardmacro area: 850 * 880 μ m² (Include Ring) Density: 86.513 %

Figure B-3: P&R view of WSN RX

B-2-5 Power

The power consumption in terms of gate-level simulation results and post-layout results are introduced. First, the power classification is introduced in Table B-6. The EDA tool used for power analysis is Prime Power. Table B-7 shows the power consumption in gate-level simulation and post-layout simulation.

Classification	Definition
Total Power	Dynamic + Leakage
Dynamic Power	Switching + Internal
Switching Power	load capacitance charge or discharge power
Internal Power	power dissipated within a cell
X-tran Power	component of dynamic power-dissipated into x-transitions
Glitch Power	component of dynamic power-dissipated into detectable
Leakage Power	reverse-biased junction leakage + subthreshold leakage

Table B-6: Power classification and definition

Table B-7: Power report in WSN_RX

Classification	Gate-level simulation results	Post-layout simulation results	
Total Power	5.056e-04 W (100%)	5.728e-04 W (100%)	
Dynamic Power	4.078e-04 W (80.65%)	4.639e-04 W (80.98%)	
Switching Power	6.709e-05 W (16.45%)	1.024e-04 W (22.07%)	
Internal Power	3.407e-04 W (83.55%)	3.615e-04 W (77.93%)	
X-tran Power	0.000e+00 W (0.00%)	3.323e-12 W (0.00%)	
Glitch Power	1.153e-06 W (0.28%)	5.391e-06 W (1.16%)	
Leakage Power	9.782e-05 W (19.35%)	1.089e-04 W (19.02%)	

B-3 Architecture of Transmitter

B-3-1 Components

The baseband transmitter is composed by a QPSK mapper, IFFT processor, and GI insertion FIFO. After the downlink process, the baseband clock has tuned accurately, the transmitter begins to gather the body signal and transmit to the uplink channel. The component in WSN_TX is list in Table B-8.

RTL code file name	Descriptions
WSN_TX.v	WSN TX top module
I_FFT_64p_8in_10out.v	IFFT module (provided by Chen-Fong Shao)
BITREV.v	Bit reversal part in IFFT module

Table B-8: The component in WSN_TX

The only signal in WSN TX for mode operation is PSDU signal. It represents the data length that modulated. Table B-9 shows the mode of operation in WSN_TX.

PSDU [1:0]	IN BITS number	Output IFFT symbol
2'b 00	128	321 + 128 * 8 / 2 / 24 * 66 = 1773
2'b 01	256	321 + 256 * 8 / 2 / 24 * 66 = 3159
2'b 10	512	321 + 512 * 8 / 2 / 24 * 66 = 5997
2'b 11	1024	321 + 1024 * 8 / 2 / 24 * 66 = 11607

Table B-9: Mode of operation in WSN_TX

B-3-2 External Signal Descriptions

The external signal description is shown in Table B-10. The transmitter sends the preamble and packets after the clock is tuned accurately by the receiver processing. The data is required from the sensor memory. The TX sends an IN_ACK signal to the memory, gets the data and transmit to the uplink channel.

name	I/O	width	Simple description	
CLK	I	1	Clock signal. This design operates at positive edge clock	
RESET	I	1	Synchronous, active-high reset signal	
IN_BIT	I	2	input data followed with IN_ACK, for qpsk modulation	
IN_ACK	0	1	input requirement signal, tell MCU that the IN_BIT is valid	
FUNC_EN	I	1	Function enable. 1: enabling the overall state diagram	
P_EN	I	1	Process enable. 1: enabling the initial state diagram	
PSDU	I	2	Indicate the data amount. 0: 128 bytes, 1: 256 bytes, 2: 512 bytes, 3: 1024 bytes	
OUT_I	0	7	I channel output signal (enabled with OUT_VALID)	
OUT_Q	0	7	Q channel output signal (enabled with OUT_VALID)	
OUT_VALID	0	1	indicate the output is valid now	

Table B-10: External signal description in WSN_TX

B-3-3 FSM

The FSM in WSN_TX is shown in Figure B-4.



Table B-11: State description in WSN_TX

state	state descriptions:
inist	initial state
pvast	transimit the preamble
inpst	valid for IN_BIT

B-3-4 Area

We show the area cost in terms of synthesis results and post-layout results. The hardware area from synthesis report is shown in Table B-12. The synthesis tool is Design Compiler.

module name		area (μm²)
WSN_TX		92983.287945
	IFFT	82628.369811
	GI insertion FIFO	8403.823131

Tabl	le B-	-12:	Area	report	in	WSN	ТΧ

The post-layout results are shown as below. The place and route (P&R) tool is

Cadence RTL Encounter. The P&R view of WSN_TX is shown in Figure B-5.



Figure B-5: P&R view of WSN_TX

B-3-5 Power

Here the power consumption in terms of gate-level simulation results and post-layout results are described. First, the power classification is introduced in Table B-6 in previous section. The EDA tool used for power analysis is Prime Power. Table B-13 shows the power consumption in gate-level simulation and post-layout simulation.

Classification	Gate-level simulation results	Post-layout simulation results	
Total Power	1.860e-04 W (100%)	2.329e-04 W (100%)	
Dynamic Power	1.547e-04 W (83.19%)	1.990e-04 W (85.46%)	
Switching Power	2.182e-05 W (14.10%)	4.689e-05 W (23.56%)	
Internal Power	1.329e-04 W (85.90%)	1.521e-04 W (76.44%)	
X-tran Power	9.944e-08 W (0.06%)	1.064e-07 W (0.05%)	
Glitch Power	4.669e-07 W (0.30%)	4.546e-06 W (2.28%)	
Leakage Power	3.126e-05 W (16.81%)	3.386e-05 W (14.54%)	

Table B-13: Power report in WSN_TX

