

國立交通大學
光電工程研究所
碩士學位論文

熔拉參數和色散機制對波長可調短通光纖
濾波器之影響研究



**The Effects of Taper Parameters and
Dispersion Mechanism on Tunable Short
Wavelength Pass Fiber Filters**

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中華民國九十八年六月

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Tunable Short Wavelength Pass Fiber Filters**

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摘要

論文名稱：熔拉參數和色散機制對波長可調短通光纖濾波器之影響研究

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關鍵詞：光纖濾波器、熔拉光纖元件、波長可調、光纖色散

在本論文中我們利用熔拉技術來製作光纖濾波元件，透過將熔拉的區域浸於折射率匹配油(色散材料)內來完成波長可調短通光纖濾波器的實驗製作。利用溫度控制器控溫，可觀察到此濾波器對溫度的調變率為 $50\text{nm}/^{\circ}\text{C}$ ，濾波效率 $-1.2\text{dB}/\text{nm}$ ，拒波效率達 50dB 。我們也使用模擬軟體模擬出各種熔拉參數對濾波器的影響，包括熔拉直徑、熔拉均勻長度、熔拉漸變長度等。根據實驗和模擬的對照，我們歸納了一組最佳的熔拉參數範圍。最後，我們將原先的單模光纖換為雙被覆層光纖來製作出新的光纖濾波器。由於雙被覆層光纖的外被覆層具有較低的折射率，根據色散機制可得知此濾波器可以有更佳的濾波效率，而我們在實驗和模擬上都一致地證實這個效應的存在。

ABSTRACT

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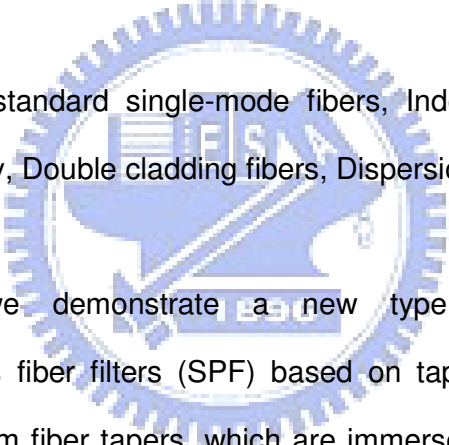
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Keywords: Tapering standard single-mode fibers, Index matching liquids, Cut-off efficiency, Double cladding fibers, Dispersion mechanism



In the thesis, we demonstrate a new type of thermo-optic tunable short-wavelength-pass fiber filters (SPF) based on tapering standard single-mode fibers (SMF-28) to form fiber tapers, which are immersed in index matching liquids. Some of the significant results are the tuning efficiency can be $50\text{nm}/^{\circ}\text{C}$, the cut-off efficiency can be $-1.2\text{dB}/\text{nm}$ and the rejection efficiency can be 55 dB . The effects of various taper parameters on SPF have also been investigated by simulation to determine the optimum parameter range. We have also demonstrated a new structure of widely tunable $\text{LP}_{01-\text{C}}$ tapered fiber filters with an even higher cutoff slope based on the tapered depressed-index outer ring fiber made from the double cladding fibers (DCLFs). The observed experimental results are explained by the dispersion mechanism and confirmed by theoretical simulation.

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Chapter 1

Introduction

1.1 Review of evanescent wave fiber taper components

Optical fiber components are essential for fiber-optic communication and sensing applications. Especially, since fiber-optic communication systems such as the local area networks (LANs) and metropolitan area networks (MANs) have been developed rapidly in recent years, optical fiber components have played very important roles in today's networking systems. Optical fiber filters, for example, are important devices in wavelength division multiplexed (WDM) optical communication systems, in wavelength encoded or multiplexed fiber sensor systems, and also in fiber amplifier modules. [1.1] They can be made by chemical-etching[1.2-1.4], fused-tapering [1.5-1.9], side-polishing [1-10-1-13], and laser ablation [1-14] techniques to expose their evanescent field. In this way, to interact with the guiding light in the fiber core, we can gain access through the exposed evanescent field. In more details, a straightforward method is to remove a portion of the fiber cladding by chemical-etching, side-polishing or laser ablation until the evanescent field is accessed. Another method is to taper the fiber so as to expand the mode field distribution by using flame or laser heating [1-15]. Among these methods, the fusion-tapering technique is most widely adopted due to the easy, fast, and cost-effective fabrication process. However, the guided mode may be transferred into high-order modes through the tapered transition if it is not well tapered. [1-16].

When the fiber core is tapered to a dimension of a few tens of micrometers, the mode field is expanded to the tapered fiber cladding which now serves as a new guiding core. One can then use dispersive liquids surrounded around the taper fiber to serve as the new cladding. The device formed by this way can be a short wavelength pass fiber filter (SPF) if the dispersion relations of the tapered fiber and the dispersive

liquids are properly designed. One can also tune the temperature of the dispersive liquids to change their dispersive curves for obtaining different cutoff wavelengths. The SPF can be used to achieve S-band Er⁺ fiber amplifiers and fiber lasers by using the conventional silica-based erbium-doped fibers. It also has the advantages of low insertion loss and wide tunability.

1.2 Dispersion mechanism of fiber taper components

The dispersion property of an evanescent wave fiber filter component is important for determining its spectral characteristics. The causes of dispersion can be divided into two categories, material and waveguide dispersion. In general, the material dispersion comes from the material dispersion properties of the fiber material and the external medium while the waveguide dispersion results from the waveguiding fiber structure. For fiber filter devices studied here, the relative refractive index difference of the fiber waveguide changes with the variation of wavelength through the material and waveguide dispersion. Therefore, the spectral responses will also vary accordingly. These influences are important when a wide range of wavelengths are considered.

1.2-1 Material Dispersion

When the refractive index varies with the wavelength of light, we call it material dispersion. The material dispersion of glass can be expressed by Sellmeier equation. The formula is valid at frequencies far from material resonance:

$$n^2 - 1 = \sum_{j=1}^p \frac{A_j \lambda^2}{\lambda^2 - \lambda_j^2} \quad (1.2.1)$$

Have the summation is taken over all the resonances. For silica, a three-term Sellmeier equation is typically used, accounting for the resonances in the ultraviolet

and infrared:

$$n^2 - 1 = \frac{A_1 \lambda^2}{\lambda^2 - \lambda_1^2} + \frac{A_2 \lambda^2}{\lambda^2 - \lambda_2^2} + \frac{A_3 \lambda^2}{\lambda^2 - \lambda_3^2} \quad (1.2.2)$$

Eq(1.2.2) is plotted in Fig1-1 for pure silica and for 4.1% germania-doped silica, using the empirically determined Sellmeier coefficients given in Table 1.1[1.17-1.18].

Table 1.1 Sellmeier parameters used in Fig1-1

Material	A1	$\lambda_1(\mu\text{m})$	A2	$\lambda_2(\mu\text{m})$	A3	$\lambda_3(\mu\text{m})$
SiO₂ [1.17]	0.6961663	0.0684043	0.4079426	0.1162414	0.8974794	9.896161
GeO₂: SiO₂ [1.18]	0.68671749	0.072675189	0.43481505	0.11514351	0.89656582	10.002398



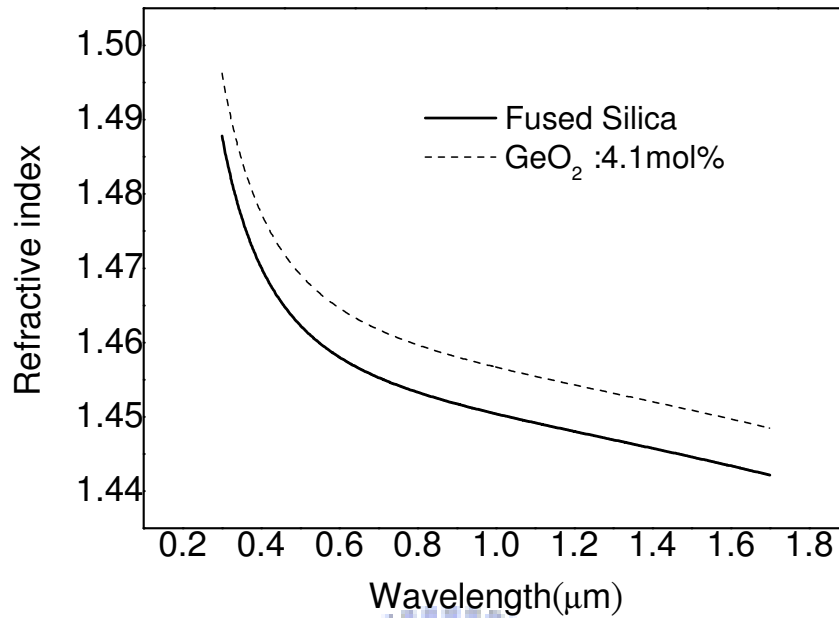


Fig1-1 Sellmeier and Cauchy's refractive index dispersion curves.

When the material dispersion is un-matched between core and cladding, like in some special dispersive fiber [1.19-1.21], a fundamental-mode cutoff phenomenon will occur. Generally speaking, the index difference between the core and the cladding is usually almost wavelength independent. Therefore, all wavelengths longer than the second-mode cutoff wavelength can be well-confined to propagate in core with very low optical losses. However, the refractive index dispersion curves of the core and the cladding in a dispersive fiber can have an intersection point to induce the above mentioned fundamental-mode cutoff phenomenon [1.22], since the material dispersion is un-matched between the core and the cladding [1.19]. Consequently, the wavelengths longer than the cutoff wavelength will suffer a huge amount of optical losses and the guidance is prohibited. Consequently, we can use the dispersive fiber to design a short wavelength-pass fiber filter. In general, the refractive index dispersion of the wavelength in proximity to the absorption bands of substances is

highly dispersive. The energy bandgap ($\sim 9\text{eV}$) [1.23] and the phonon energy ($\sim 1100\text{ cm}^{-1}$) of the Si-O bond in fused silica are higher than most of the covalently bonded optical polymers which makes the fused silica have flatter and steeper dispersion slope than the polymers at visible and near-infrared regions, respectively. Some polymers with intermolecular hydrogen bonds [1.24] have higher phonon energy and steeper dispersion slope than fused silica in the inner-infrared region. In ultraviolet regions, materials with stronger ionic bonds (Li-F or Mg-F) or a polar covalent bond (Si-F), i.e., a large value of electro-negativity difference will make the absorption blue-shifted to produce higher bandgap energy [1.25] and flatter dispersion slope than fused silica. Therefore, dispersive materials with different phonon energies can be applied on evanescent-wave fibers to realize tunable fundamental-mode cutoff based on the discrepancy of material dispersion.

1.2-2 Waveguide Dispersion

In contrast to material dispersion, the waveguide dispersion due to the waveguiding fiber structure is not so effective to affect the spectral characteristics. In fused-tapered fibers, the length, diameter, strain, bending, and dopant diffusion at the tapered region are the key issues for waveguide dispersion. In general, the variation of these parameters will mainly vary the dispersion slope of the guiding mode. Usually, people discussed the influences of waveguide dispersion on fiber devices based on special fibers [1.26-1.29]. However, the waveguide structure can also be locally changed to alter the waveguide dispersion for light propagation and the spectral responses of the fiber devices by using standard fibers [1.30-1.31]. The electromagnetic field distribution is locally modified to vary the dispersion characteristics or to excite the higher-order modes [1.31]. Therefore, novel fiber devices can be achieved based on the variation of waveguide structure of the standard fiber in a small

local area. In this dissertation, since the dispersion measurement instruments are not available in these cases, the influences of the variation of the waveguide structure on the spectral characteristics are studied instead.



1.3 Structure and Material Constituents of Double Cladding fibers (DCLFs)

Recently high power fiber lasers have played more and more important roles in micromachining, remote sensing, laser surgery, space communication, laser ignition, and so forth. With the advent of double-cladding fibers (DCLFs) and large mode area photonic crystal fibers, the laser output power under single transverse mode operation can be easily elevated to the Watt level with a length of a few meters [1.32]. The ultra-high gain efficiency comes from the long interaction length between the high power pump and the highly doped gain medium. In fact, the DCLF has a small rare-earth-doped core for single-mode signals and a larger fused silica core for multi-mode pump lights. The pump core can deliver very high pump power up to tens of Watts from multi-mode lasers and reflect the pump lights to intersect the signal core for many times so as to excite the doped ions efficiently for generating optical gain. Usually, the high power fiber lasers are very expensive due to the inclusion of highly doped DCLFs and the multi-mode diode lasers and thus high power fiber lasers with wide tuning range definitely have the economic advantages for many applications.

In our experiment, the DCLF of our work is SMM900 that is bought from Fibercore. The structure of the DCLFs is shown in Fig1-2. The signal wave travels in the core and the pump wave travels in the inner cladding (pump region) for cladding pump fiber lasers. The material constituents of the DCLFs are given in Table1.2. The refractive index distribution of the DCLFs is shown in Fig1-3. The material constituents of the core and the inner cladding are the same as convention single mode fibers. However, the material constituent of the outer cladding is Fu-doped silica. The refractive index of the outer cladding is much lower than the inner one because Fu is doped.

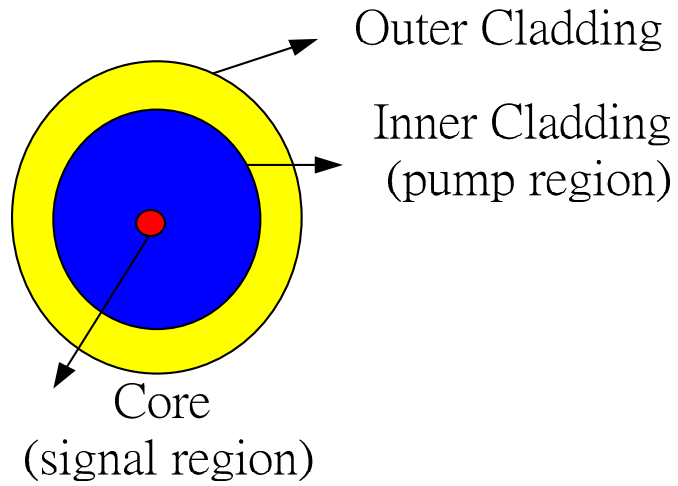


Fig1-2 Structure of DCLFs

Table 1.2 The material constituents of the DCLFs

	Material	Range
Core	Ge-SiO₂	8~9(μm)
Inner cladding	SiO₂	9~90(μm)
Outer cladding	Fu-SiO₂	90~125(μm)

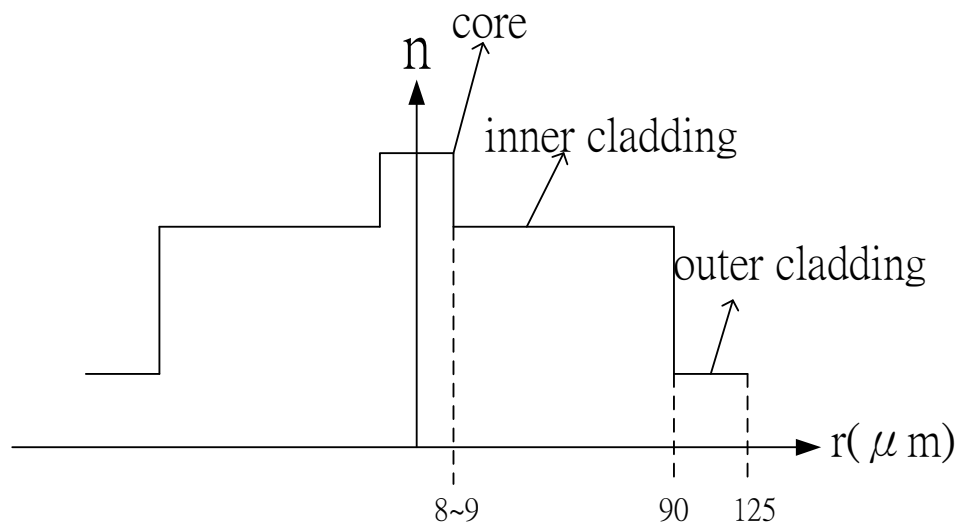
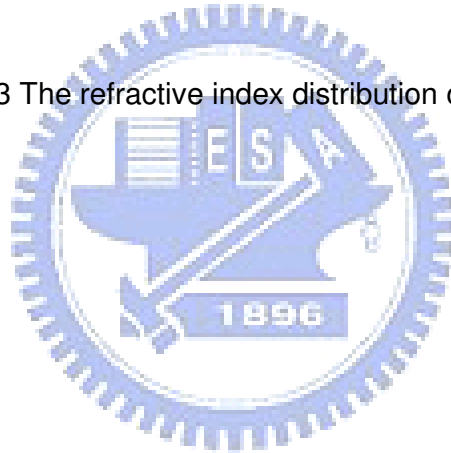


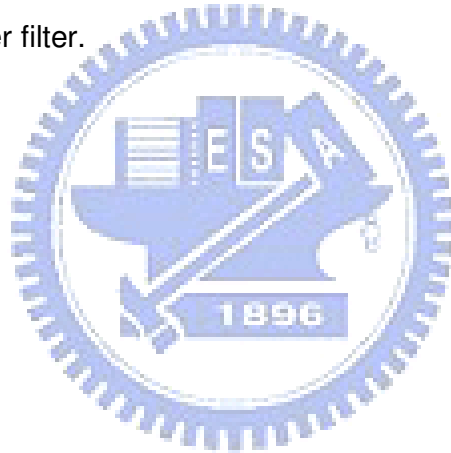
Fig1-3 The refractive index distribution of the DCLFs



1.4 Motivation of This Work

This work presents new theoretical and experimental results on the thermo-optic tunable filters by using the tapered single mode fiber (SMF-28) immersed in dispersive liquids. We use simulation to predict the device cut-off wavelength and the tuning curve with respect to temperature changes. The optimal uniform taper diameter, taper length and transition length are also investigated by simulation.

Besides, we discuss the influence of the depressed-index outer ring on the fundamental-mode leakage loss in tapered double-cladding fibers. Accordingly, we can understand the effects of material dispersion on the characteristics of fundamental mode cutoff and expect the cutoff slope that is steeper than the previous single mode fiber taper filter.



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Chapter 2

Theory

2.1 Wave propagation in tapered single mode fibers

Tapering of a single-mode optical fiber leads to a loss of power from the fundamental core mode because of the departure from the translational invariance of the uniform fiber. As it propagates along the taper, the field is unable to change its distribution rapidly enough to keep up with the variation of the fundamental local mode which shape is determined by the local taper cross section. The power loss from the core mode is associated with bending of the phase front owing to coupling of the fundamental mode with higher order modes. This power couples to cladding modes in a finite-clad fiber.

Intuitively, one would expect loss to decrease with decreasing taper angle, so that, in principle, loss could be kept arbitrarily small by using a sufficiently small taper angle. However, for practical devices, such as fiber tapers and fused taper couplers, there is a practical limit to the smallest taper angle that can be achieved over a significant length. Furthermore, extremely long devices are difficult to package, as well as being more susceptible to environmental effects.

2.1-1 Local modes [2.1]

Fabrication of tapered fibers and devices using the fused taper technique entails stripping the protective coating or jacket. Accordingly, the cross-sectional profile anywhere along the taper consists of a core embedded in a finite cladding, which is surrounded by air. Because of the relatively large index difference between the cladding and air, power loss from the fundamental mode can be described accurately through coupling to the finite set of discrete bound modes propagating in the cladding, i.e. the cladding modes [2.2]. Each cladding mode is characterized by an effective index which lies between the cladding index and the index of air, and is guided by the

complete core-finite cladding-air waveguide.

A taper is approximately adiabatic if the taper angle is small enough everywhere to ensure that there is negligible loss of power from the fundamental mode as it propagates along the length of the transition. The fields and propagation constant within an approximately adiabatic taper of a single-mode fiber can be described accurately by those of the local fundamental mode, which conserves power as it propagates and is the solution to the wave equation with the geometry of the local cross-section. If $\mathbf{E}(x, y, z)$ denotes the modal electric field, where z is the distance along the taper and x, y are the transverse co-ordinates, then [2.4, Chap. 19]

$$E(x, y, z) = a(z) \hat{e}(x, y, \beta(z)) \exp\left\{ i \int_0^z \beta(z') dz' \right\} \quad (2.1.1)$$

where $a(z)$ and $\beta(z)$ are, respectively, the modal amplitude and propagation constant at position z , and \hat{e} contains the transverse dependence. At each position z along the taper, the fundamental local-mode propagation constant and fields are evaluated by solving the boundary-value problem for the fundamental mode on an infinitely-long cylindrically symmetric fiber whose cross-sectional geometry and refractive-index profile match those of the taper, as illustrated in Fig2-1(a),(b).[2.4] This prescription also applies to all the higher order local cladding modes of the finite-cladding taper.

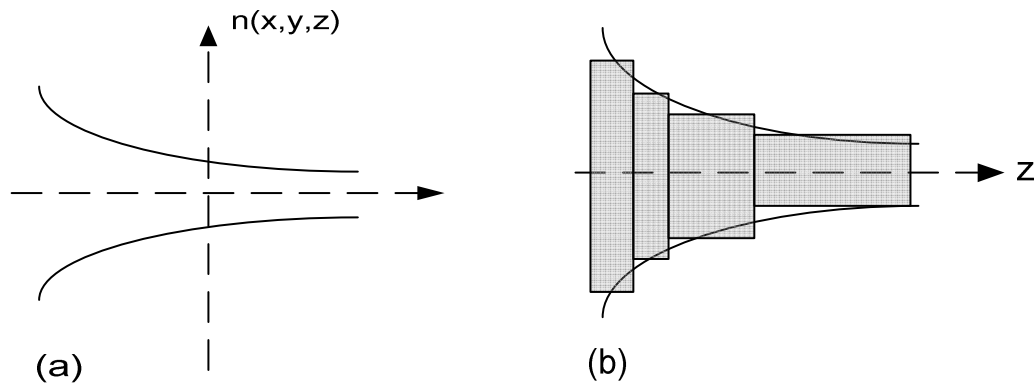


Fig2-1 (a) A non-uniform fiber varies along its length and has refractive-index profile $n(x,y,z)$ (b) the approximate model of its series section that matched taper shape.[2.4]

If the fiber core diameter varies with tapering, the local V defined by

$$V(z) = \frac{2\pi\rho(z)}{\lambda} \sqrt{(n_{co}^2 - n_{cl}^2)} \quad (2.1.2)$$

and decreases linearly with fiber core. As shown in Fig2-2[2.1], the abscissa $V(z)$ is the local V -value along the taper, and the ordinate gives the values of the effective index n_{eff} for the first five LP_{0m} modes by solving eigenvalue equation. The horizontal dashed lines correspond to the core and cladding index values. As would be expected, the values of n_{eff} for the high order LP_{0m} modes all lie below the cladding index when $V(z)$ is below 0.84. We call these modes cladding modes because the finite cladding produces air-cladding waveguide. However, the n_{eff} of Lp_{01} for $V(z)$ behind 0.84 lies between the core index and cladding index, so it is called core mode since the core still has effect on the waveguide.

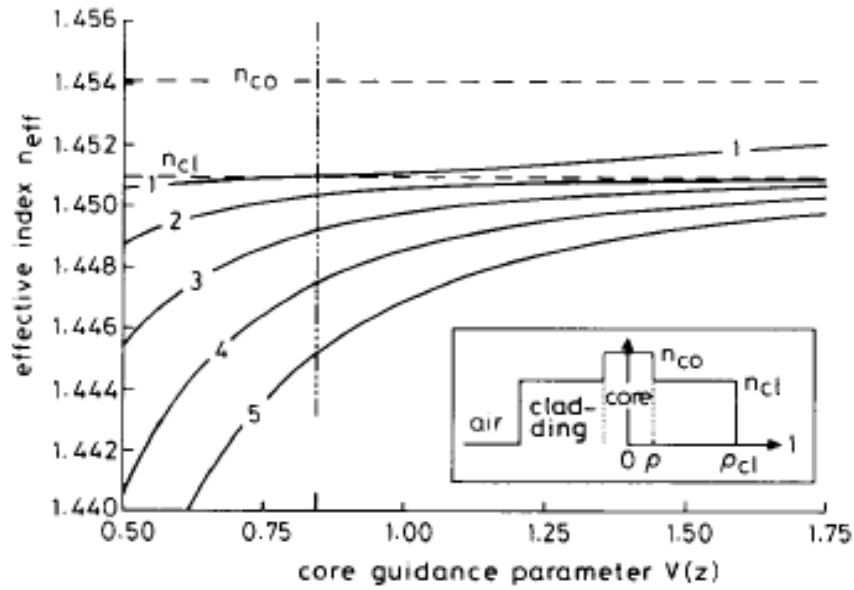
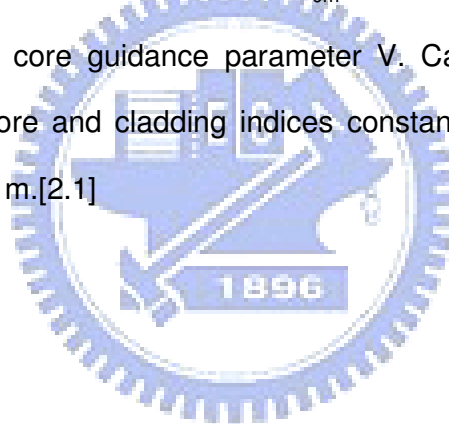


Fig2-2 Effective index values for first five LP_{0m} modes of finite cladding, step-profile taper as functions of core guidance parameter V . Calculations are performed by varying ρ . Keeping core and cladding indices constant and equal to their value at wavelength $\lambda = 1.2 \mu\text{m}$. [2.1]



2.1-2 Adiabaticity [2.1]

The first criterion for adiabaticity is length scale that must be much larger than the coupling length between the fundamental mode and the dominant coupling mode for power loss to be small [2.5-6]. Accordingly, we define the local taper length-scale z_t as the height of a right circular cone with base coincident with the local core cross-section and apex angle equal to the local taper angle $\Omega(z) = \tan^{-1} \left| \frac{d\rho}{dz} \right|$, as illustrated in Fig2-3, where z is the distance along the taper, and $\rho = \rho(z)$ is the local core radius. Because in practice $\Omega(z) \ll 1$, then

$$z_t \approx \frac{\rho}{\Omega} \quad (2.1.3)$$

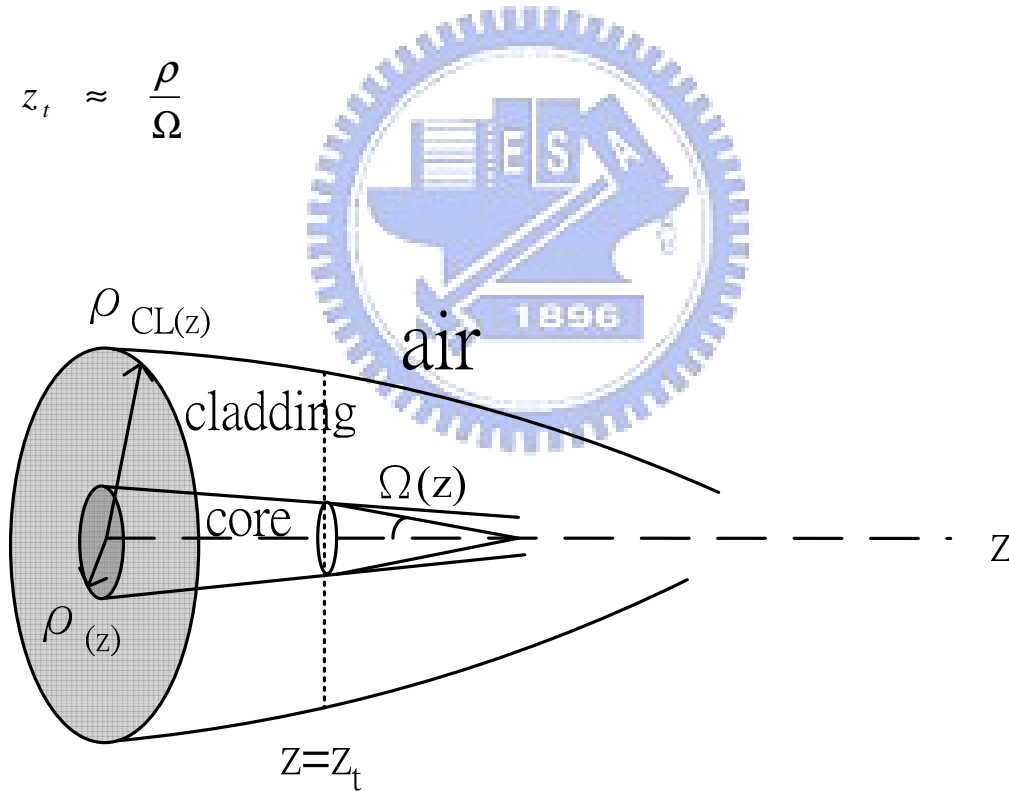


Fig2-3 Tapered single-mode fiber showing finite cladding and air as surrounding medium

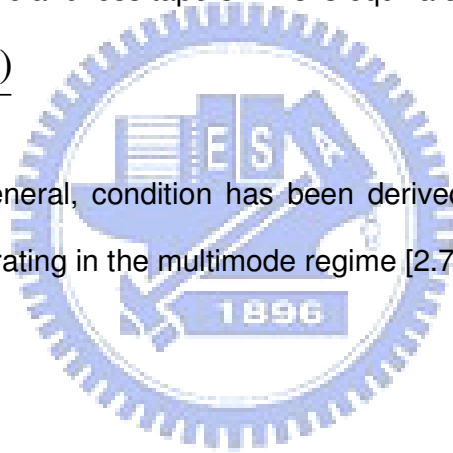
The local coupling length between the two modes is taken to be the beat length $z_b = z_b(z)$, between the fundamental and second local modes, where

$$z_b = \frac{2\pi}{\beta_1 - \beta_2} \quad (2.1.4)$$

and $\beta_1 = \beta_1(z)$ and $\beta_2 = \beta_2(z)$ are respective propagation constants. It is intuitive that if $z_t \gg z_b$ everywhere along the taper, then negligible coupling will occur and the fundamental mode will propagate approximately adiabatically with negligible loss. Conversely, if $z_t \ll z_b$ there will be significant coupling to the second mode. Accordingly, the condition $z_t = z_b$ provides an approximate delineation between approximately adiabatic and loss tapers. This is equivalent to [2.5]

$$\Omega = \frac{\rho(\beta_1 - \beta_2)}{2\pi} \quad (2.1.5)$$

A similar, but less general, condition has been derived to minimum loss in optical waveguide horns operating in the multimode regime [2.7].



2.2 The minimum diameter of tapered fiber that can guide light [2.3]

Decreasing the taper fiber diameter d to values significantly smaller than the radiation wavelength, λ , causes a dramatic growth of the transversal dimensions of the fundamental mode, which propagates primarily outside the microfiber.[2.4] However, for $d/\lambda \ll 1$, a negligibly small nonuniformity of the microfiber can completely kill the propagating mode. For a fixed wavelength, quite general physical assumptions determine the threshold for the diameter of the microfiber, below which the propagation of evanescent light along the taper fiber is impossible. Consider two modes having propagation constants $\beta_1(z)$ and $\beta_2(z)$. The coupling between these modes is defined by the coupling coefficient $R_{12}(z)$ [2.4]. Usually, for optical waveguides, the transmission amplitudes between modes at the input and output of the fiber taper are expressed within the first-order perturbation theory as an integral,

$$A_{12} = \int_{-\infty}^{\infty} dz R_{12}(z) \exp \left\{ i \int^z dz' [\beta_1(z') - \beta_2(z')] \right\} \quad (2.2.1)$$

which is calculated numerically.[2.4,2.8]

However, the solution of a similar problem yielding an extremely simple result for A_{12} in the adiabatic approximation was obtained in quantum mechanics in the early 1960s by Dykhne[2.9] and Landau.[2.10] Crucially, the Landau–Dykhne formula, which corrects the mentioned first-order approximation for A_{12} in the case of finite nonuniformities, does not depend on the coupling coefficient $R_{12}(z)$ at all.

$$A_{12} = \exp \left[i \int_{z_r}^{z_r^*} dz [\beta_1(z) - \beta_2(z)] \right], \quad P_{12} = |A_{12}|^2 \quad (2.2.2)$$

Here z_r is an arbitrary point at the real z axis, whose position does not change the value of the transmission power.

Consider the taper of the shape $d(z)=d_{\infty}-(d_{\infty}-d_0)\{1-[(z-z_0)/L]^2\}^{-1}$, where d_{∞} and d_0 are the taper's diameters at its ends and at the center. For a silica microtaper (with a refractive index of 1.45) with a small waist diameter $d \ll \lambda$, one can find from Ref. [2.4] that

$$\beta_1(z) - \beta_2(z) = \Delta\beta_{12}(z) \approx 0.57 [\lambda/d^2(z)] \exp[-0.27\lambda^2/d^2(z)] \quad (2.2.3)$$

where $\Delta\beta_{12}(z)$ now represents the difference between the propagation constant of the HE_{11} mode, $\beta_1(z)$, and the radiation threshold, $\beta_2(z) = 2\pi/\lambda$. Then the transmission loss P found from Eqs. (2.2.4) depends on the taper waist diameter d_0 double exponentially:

$$P \sim \exp \left[\frac{0.687 L}{d_0^{1/2} (d_{\infty} - d_0)^{1/2}} \exp \left(\frac{0.27\lambda^2}{d_0^2} \right) \right] \quad (2.2.4)$$

where L represents the transition length. The fundamental mode propagates along the microfiber only if $P \ll 1$, while the condition $P \sim 1$ corresponds to the threshold when it disappears. Figure 2-4 shows the transmission loss P as a function of the taper fiber waist diameter d_0 for radiation wavelength $\lambda = 1.55 \mu\text{m}$. [2.3] It demonstrates the dramatic threshold behavior of the transmission loss predicted by Eq. (2.2.4) (curves 1, 2, and 3) and shows no significant difference between the threshold values of the taper waist diameter for a typical $L = 10 \text{ mm}$ and for a gigantic $L = 10 \text{ km}$. Note that the loss P is in the strongest double-exponent dependence only on the minimum taper waist diameter, d_0 . The dependence of P on the parameter $d_{\infty} - d_0$, which determines the shape of the microfiber's taper, is much weaker. Therefore it is reasonable to conclude that the specific shape of the taper as well as its characteristic length L does not significantly affect the value of the threshold diameter. For this reason smoothly deformed optical fiber tapers can have very small losses. However, losses dramatically increase with a thinning of the taper fiber down to a diameter much

smaller than the radiation wavelength.

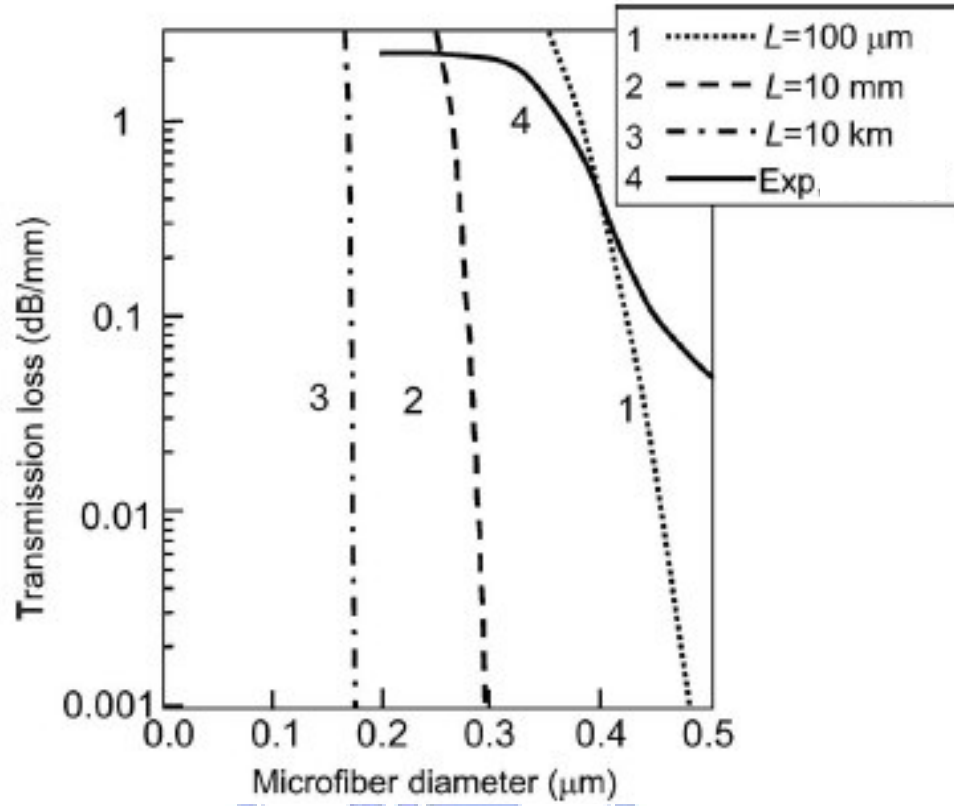


Fig2-4 Transmission loss as a function of the taper fiber waist diameter d_0 calculated with Eq. (2.2.4) for different characteristic lengths of the transition length L (curves 1, 2, and 3) and $d_\infty=1\mu\text{m}$, and experimentally measured in $L=10\text{mm}$ (curve 4) [2.3].

2.3 Working principle of optical tunable short pass filter (SPF) based on fiber tapering

Tunable short-pass fiber filters (SPF) are advantageous for the S-band EDFAs [2.11] and for the high isolation WDM (de)multiplexers in triple-play (1310/1490/1550-nm) fiber-optic systems. A tunable short-pass fiber filter can be achieved by utilizing the fundamental-mode cutoff mechanism in which the lights with the wavelength longer than the cutoff wavelength λ_c can be highly attenuated to obtain efficient filtering with sharp filter skirt. If we taper the single mode fiber adiabatically and let taper region immersed in a dispersive liquid such as Cargille index-matching liquid with the index $n_D = 1.456$ and dn_D/dT of $-3.74 \times 10^{-4} / ^\circ\text{C}$. The core effect vanishes because the taper fiber diameter is in a few tens of micro-order. Hence, the effective core is the original fiber cladding and the effective cladding is the outer surrounding. The effective index of waveguide is between fibers those of the original cladding and the outer surrounding, say dispersive liquids. For material dispersion, the effective index curve will cross the dispersive curve of the outer liquid, and the crossed point is referred as the cut-off wavelength (LP_{01-c}). The field which wavelength is longer than cut-off will experience high loss and the field which wavelength is shorter than cut-off will pass. The achieved cutoff efficiency is dependent on the material dispersion of the surrounding dispersive material and the waveguide dispersion of the tapered fiber device but typically the former dominates the cutoff efficiency more strongly than the latter when optical fields are mainly distributed over the guiding core. In the refractive index dispersion (RID) plot shown in Fig2-5, high cutoff efficiency is possible when the cross angle between the refractive index dispersion (RID) curves of the tapered fiber and the surrounding dispersive liquid is large [2.12]. A larger cross angle can give rise to a steeper cutoff with higher rejection efficiency for the wavelengths longer than the cutoff wavelength.

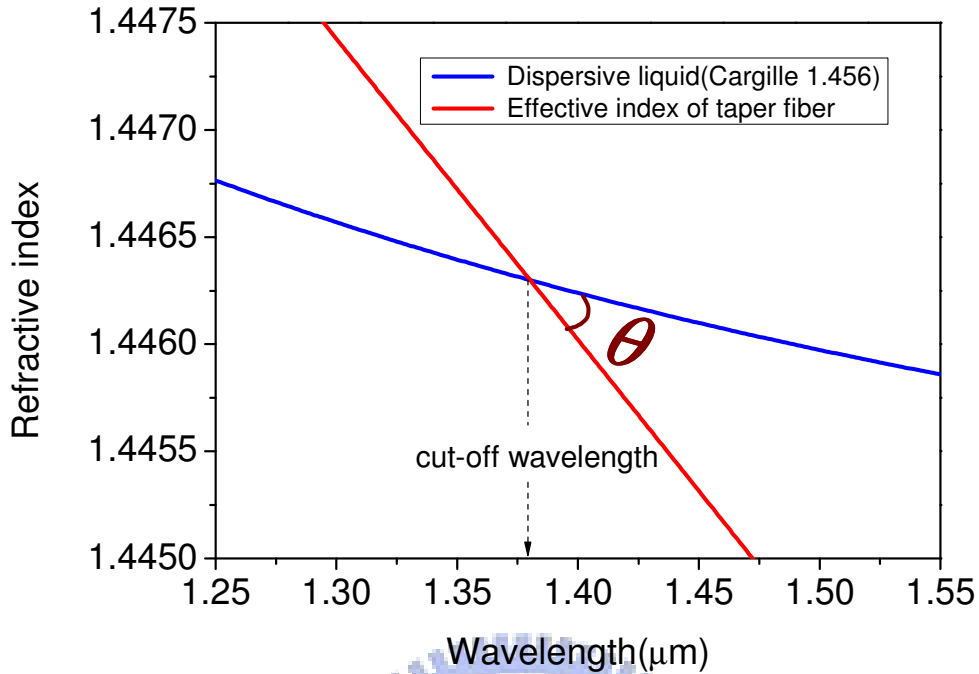


Fig2-5 The refractive index dispersion curves. θ is the parameter that determines the cut-off efficiency.

Since the absorption phonon energy of the used dispersive liquid (Cargille index matching liquids) is so different from the high absorption phonon energy ($\sim 1100 \text{ cm}^{-1}$) of the silica fiber glass, the spectral response will be short-pass and the cutoff wavelength can be moved upward or downward, depending on the thermo-optic coefficients (dn/dT) of the dispersive material and the applied heating temperature [2.11]. The dn/dT of the index liquid is $-3.74 \times 10^{-4}/^{\circ}\text{C}$, which is high enough to give rise to high efficient temperature-tuning. Fig2-6 shows the refractive index dispersion curves for the index matching liquid and the effective index of the tapered fiber at different temperatures. However, if the taper diameter is much smaller than wavelength, the waveguide dispersion effect will play an important role and the dispersions are more sensitive to wavelength. In addition, the cutoff efficiency is also

influenced by the interaction length, the shape of the fused-tapered region [2.13] and the bending curvature of the tapered fiber.

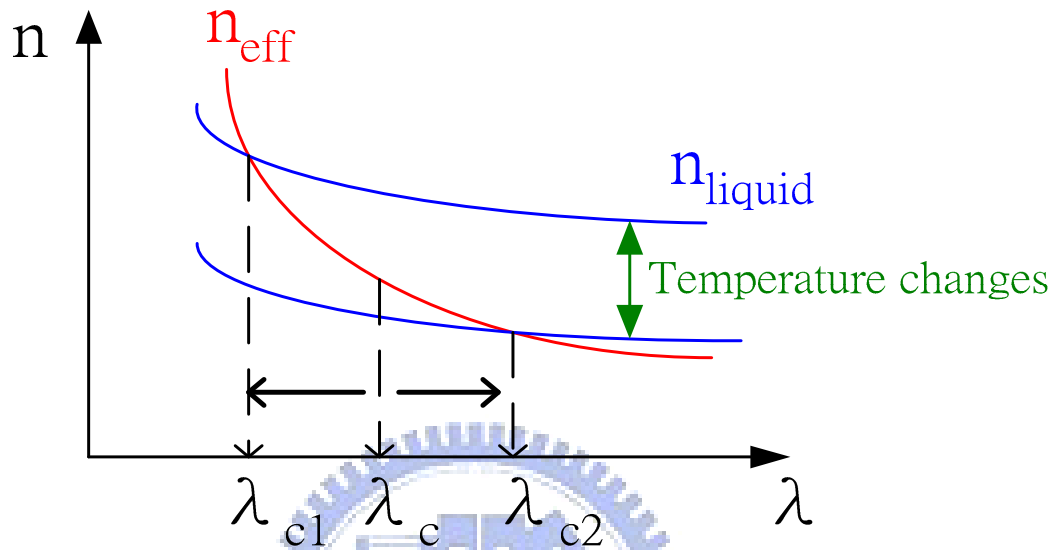


Fig 2-6 Refractive index dispersion curves for the index matching liquid and the effective index of the tapered fiber at different temperatures.

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Chapter 3

Wideband tunable short-pass single mode fiber filter

3.1 Introduction

In this section, we will discuss the effects of taper parameters on temperature tunable short-pass single mode fiber filter (SPF) in the experiment and simulation. Parameters like the taper waist diameter, taper waist length, and transition length may change the cut-off efficiency since they will cause variation of the dispersion and mode field spreading in the taper waist. In other words, these parameter changes may affect the confinement of shorter wavelengths and the loss of longer wavelengths. Hence, we calculate the cut-off slope to evaluate the cut-off efficiency and get a proper parameter set to fabricate wideband tunable short-pass single mode fiber filters that can have best performance.

3.2 Experimental setup

One can taper an optical fiber of initial diameter d_0 to a final diameter d by stretching a uniformly heated fiber section of length L_0 . The taper waist is predicted to vary with the elongation distance z as [3.1]

$$d = d_0 \exp\left(\frac{z}{2L_0}\right) \quad (3.2.1)$$

and the taper waist of length L_0 . The taper transitions are exponential in shape [3.2].

The homemade tapering station depicted in Fig. 3-1 was implemented to fabricate the tapered fiber. d is denoted as uniform taper diameter, and L_0 is taper length and τ is transition length. Fig 3-2 shows the real pictures of the taper station. A small flame produced by controllable hydrogen was used to heat a section of the optical fiber. The flame diameter was approximately 15 mm with a temperature of approximately 1300 °C. The flame torch was mounted on a three-axis translation stage, which in turn

rested on a sliding stand driven by a stepper motor. This process ensures that the flame identically heats each section of the fiber being tapered in each cycle of oscillation. Distance L_0 can be exactly controlled. Therefore, the length of the uniform waist of the tapered fiber is controllable. In our experiments the speed of the flame was set to approximately 0.2 mm/s, and L_0 was in the range 10-20 mm range. At the same moment when the flame starts to heat the fiber, the fiber is gently stretched in opposite directions. The pulling mechanism involves two sliding stands driven by stepper motors. The speed of the stand was approximately 0.055 mm/s. Total elongation distance z is the sum of the distances traveled by each stand, which can also be controlled precisely.

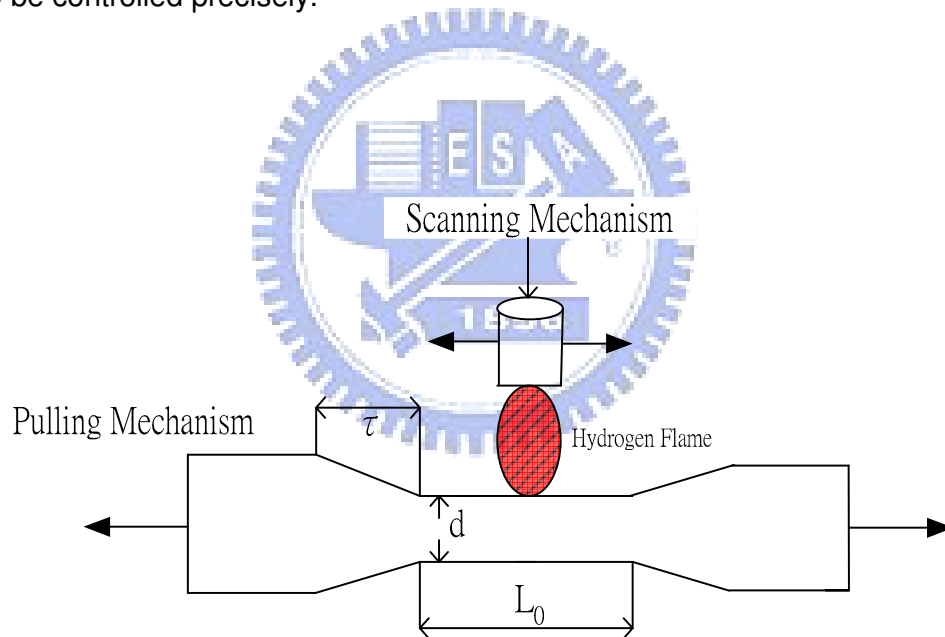


Fig3-1 Diagram of taper mechanism. d is donated as uniform taper diameter, and L_0 is taper length and τ is transition length.

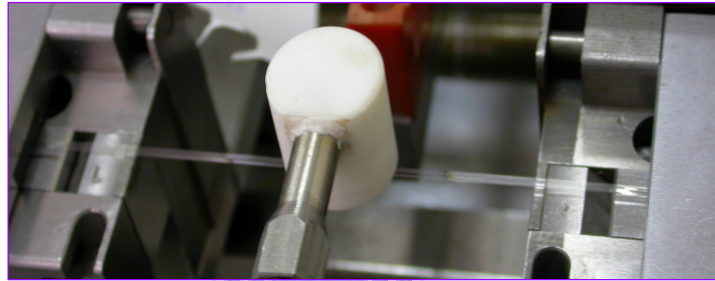
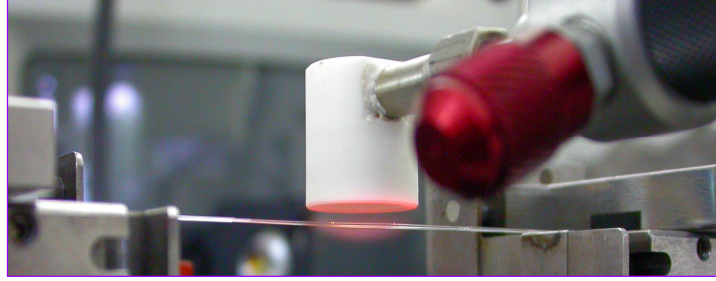


Fig3-2 Real picture of the taper station

Standard telecommunication single-mode step-index fiber (SMF-28: Corning) was used to fabricate our samples. The fiber cladding-core diameters were 125/8.2 μm with a 0.13 numerical aperture, It is important to mention that this fiber is inexpensive and readily available. Before the pulling process began, the jacket was removed from the fiber over a section larger than L_0 . The fiber was cleaned with ethanol. By above fabrication, we can make a low loss($<0.3\text{dB}$) taper fiber and consider that the taper transition is adiabatically varying .Finally, we place the taper fiber in the V groove of glass substrate and inject the dispersive liquid (Cargille index matching liquids) with the index $n_D = 1.456$ and dn_D/dT of $-3.74 \times 10^{-4} / ^\circ\text{C}$. We finish the fabrication of short-pass fiber filter (SPF).

3.3 Simulation parameter

In our simulation, we use Beam Propagation Method (BPM)[3.3-3.4] to simulate the performance of SPF by commercial software and discuss more details about the wave propagating in tapered fiber including transverse mode profile, the effective index of refraction and power monitored during wave propagation. BPM refers to a computational technique in electromagnetics, used to solve the Helmholtz equation under conditions of a time-harmonic wave. BPM works under the slowly varying envelope approximation, for linear and nonlinear equations. The Helmholtz equation is following as:

$$(\nabla^2 + k_0^2 n^2) \psi = 0 \quad (3.3.1)$$

With field written as:

$$E(x, y, z, t) = \psi(x, y, z) \exp(-i\omega t) \quad (3.3.2)$$

Now the spatial dependence of this field is written according to any one TE or TM polarizations:

$$\psi(x, y, z) = A(x, y, z) \exp(ik_z z) \quad (3.3.3)$$

.with the envelop $A(x,y)$ following a slowly varying approximation,

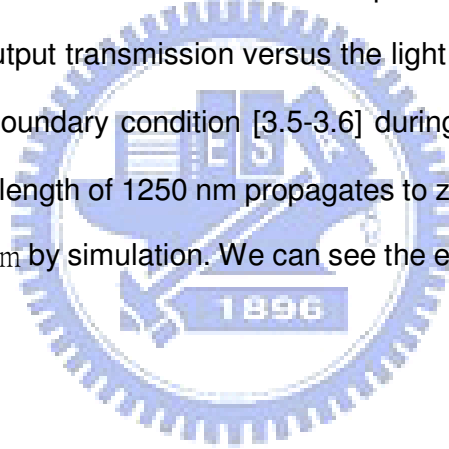
$$\frac{\partial^2 A}{\partial z^2} \ll k^2 A \quad (3.3.4)$$

$$\frac{\partial A}{\partial z} \ll kA \quad (3.3.5)$$

Now when the solution ansatz is inserted into the Helmholtz equation for simplification, one obtains the following equation:

$$\left[\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + (k_0^2 n^2 - k_z^2) \right] A(x,y,z) = \pm 2i k_z \frac{\partial A(x,y,z)}{\partial z} \quad (3.3.6)$$

With the aim to calculate the field at all points of space for all times, we only need to compute the function $A(x,y,z)$ for all space, and then we are able to reconstruct $\psi(x,y,z)$. Since the solution is for the time-harmonic Helmholtz equation, we only need to calculate it over one time period. We can visualize the fields along the propagation direction, or the cross section waveguide modes. The master equation is discretized (using various centralized difference, crank nicholson scheme etc) and rearranged in a causal fashion. Through iteration the field evolution is computed, along the propagation direction. We set the taper transition to be exponential varying and get the output transmission versus the light wavelength. In addition, we use the transparent boundary condition [3.5-3.6] during simulation. Fig 3-3 shows the field with the wavelength of 1250 nm propagates to z axis in a taper fiber with the taper diameter of 30 μm by simulation. We can see the evanescent field arises in the taper waist.



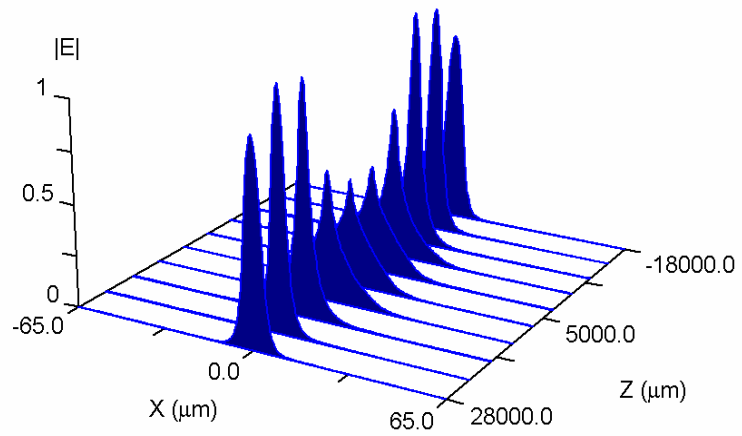


Fig3-3 The field which wavelength is 1250 nm propagates to z axis in a taper fiber with the taper diameter of 30 μm by simulation.



3.4 Results & discussion

3.4-1 Experiment

In our measurement, a broadband white light source containing super-luminescent diodes spanning from 1250 to 1650 nm was launched into the measured fiber for performing measurement. The tapered fiber was heated by a TE-cooler to stabilize the temperature within 0.1°C. The refractive index of the surrounding index liquid decreases with the increasing temperature and in this way the temperature tuning can make the whole wavelength band from 1250 to 1650 nm become all-rejection or all-pass. Therefore, we use an optical spectrum analyzer to get the transmission data. Fig3-4 demonstrates the spectral transmission of a SPF with tuning temperature (24°C~27°C) and compare to the results of simulation. The taper diameter d is 26 μm , and the taper length L_0 is 18 mm, and the transition length τ is 6 mm. We can see that the experimental results agree well with the simulation ones. The significant results are the tuning efficiency can be 50nm/°C, and cut-off efficiency can be -1.2dB/nm and rejection efficiency can be 55 dB. For the last case, if we change d to 40 μm , and L_0 to 20 mm and τ to 10 mm, the tuning efficiency can improve to 58 nm/ °C and the cut-off efficiency can improve to -2dB/nm in our experiment.

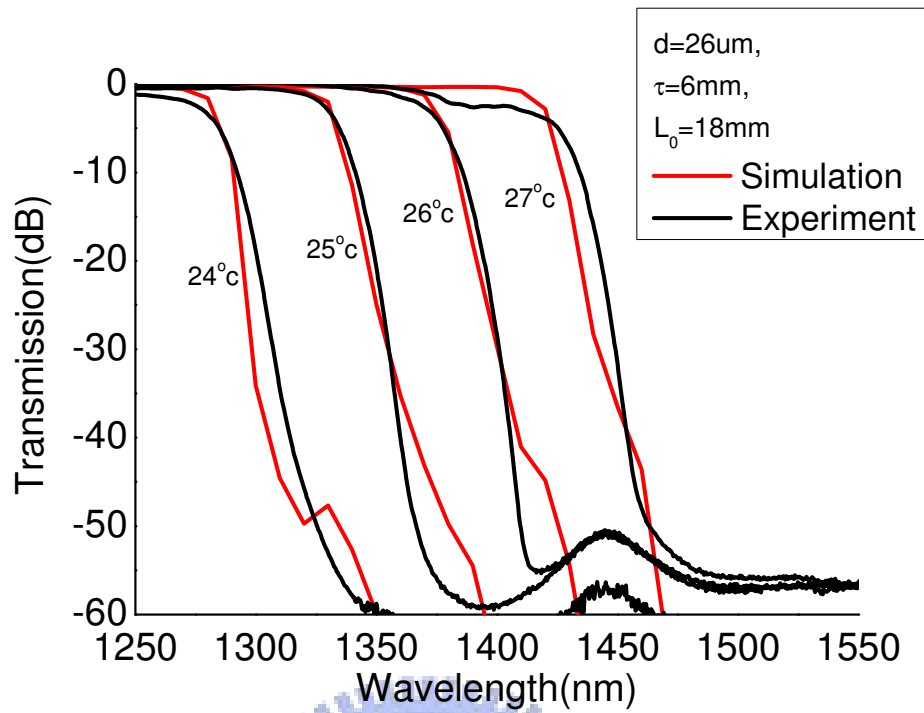


Fig3-4 Spectra transmission of SPF with tuning temperature (24°C~27°C)

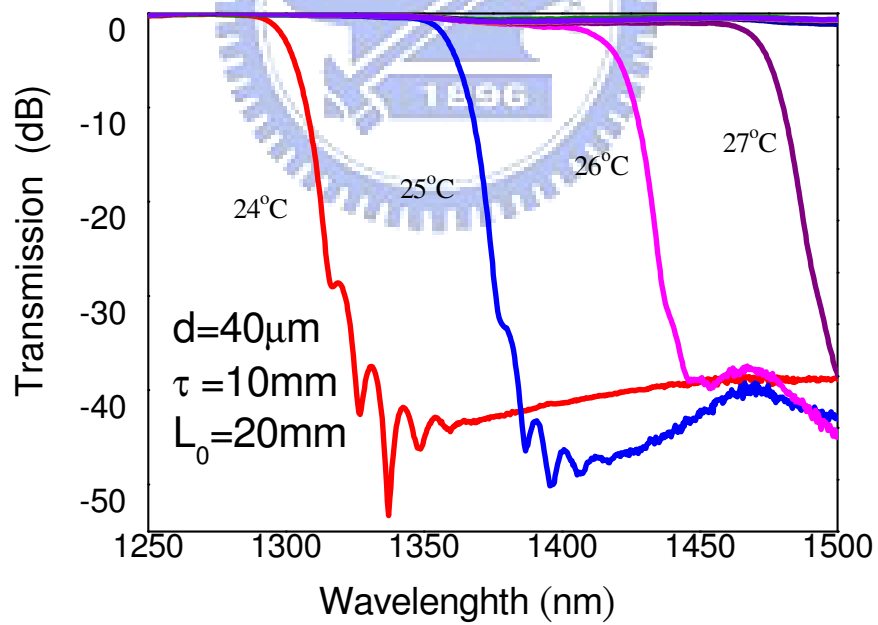


Fig3-5 Spectral transmission of a SPF with tuning temperature (24°C~27°C)

Here, we will compare the effect of different taper diameter d on SPF in experiment. The result shows in Fig3-6. We can find the cut-off efficiency of shorter taper diameter is lower because the guidance of shorter wavelength becomes worse. However the rejection efficiency of larger taper diameter also becomes worse because the better confinement affects the longer wavelength loss.

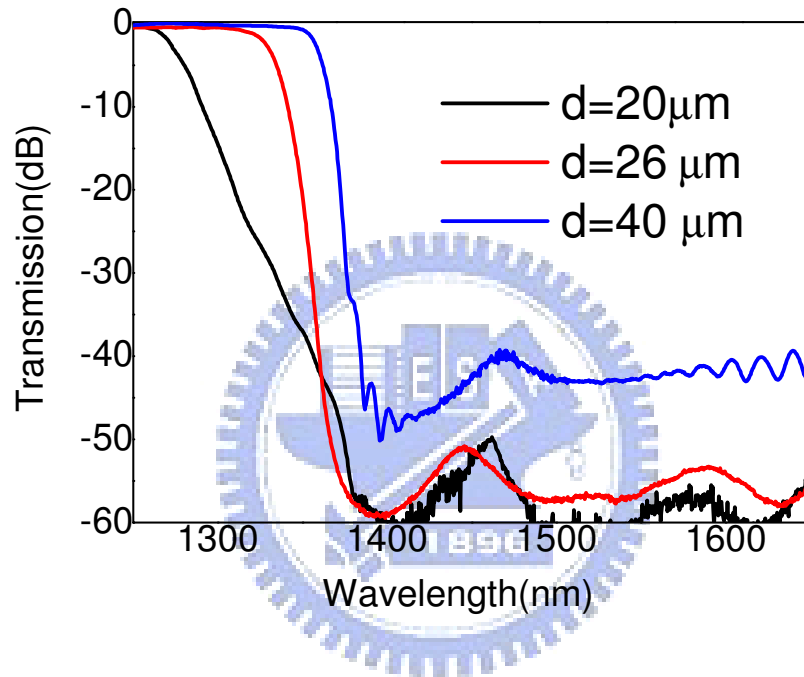
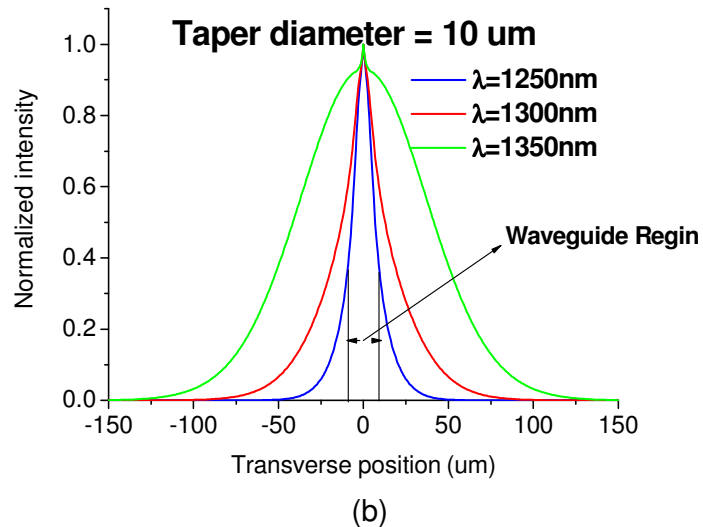
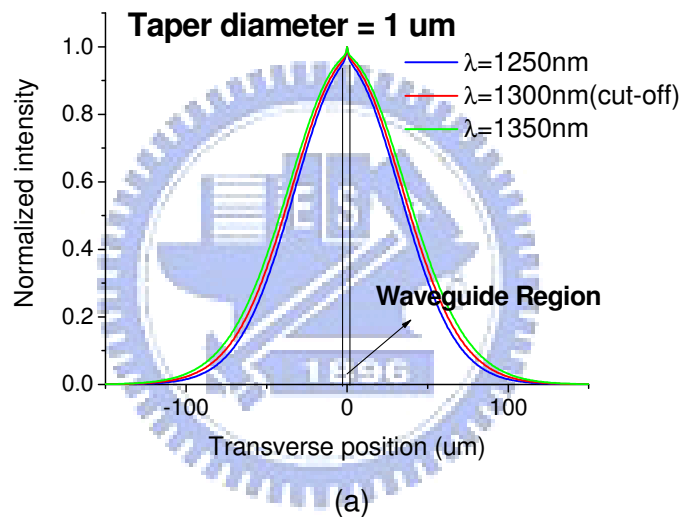
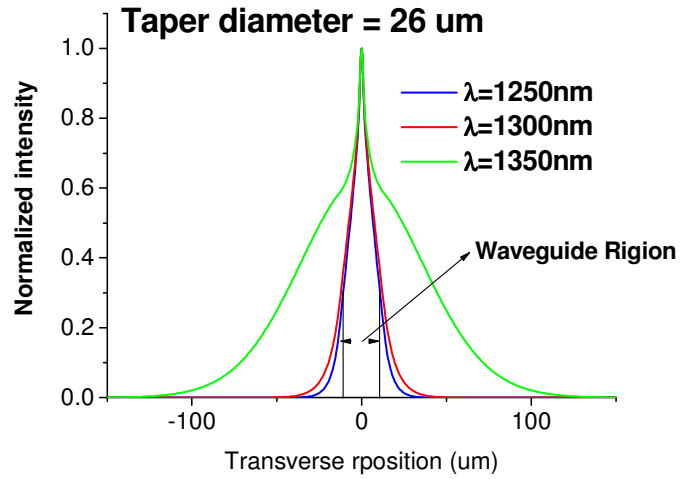


Fig3-6 Different taper diameter d for SPF

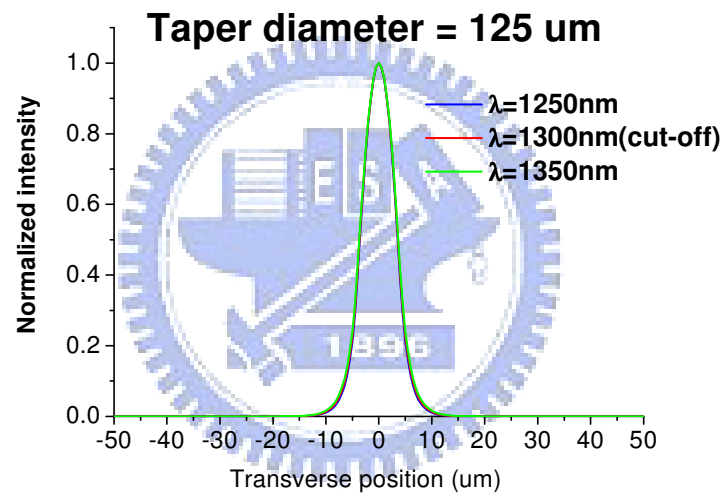
3.4-2 Simulation

First, we discuss how mode field diameter (MFD) in the uniform taper waist of SPF varies with the taper diameter and wavelength. Fig3-7(a),(b),(c),(d) show the MFD of 1250,1300(cut-off),1350nm for different taper diameters. From fig3-7(a), all wavelengths spread out of fiber to the outer surrounding since the taper fiber is too thin to confine the short wavelength. From Fig3-7(b),(c), when increasing taper diameter, the short wavelength begin to shrink into the fiber, and the wavelengths longer than cut-off still spread out. If we don't taper the fiber, all wavelengths confine in the fiber, like Fig3-7(d).





(c)



(d)

Fig3-7 MFD of 1250,1300(cut-off),1350nm for different taper diameters.(a) 1 μm ,(b)10 μm ,(c)26 μm ,(d)125 μm .

We use simulation to discuss the effect of taper parameter on SPF Fig 3-8 shows the effect of different uniform taper diameter d on SPF in simulation. Taper length L_0 is 18 mm and transition length τ is 6 mm. The tendency behaves like experimental results. The diameter of taper fiber can not be too thin or thick because both would affect cut-off efficiency and rejection efficiency. Besides, if the taper diameter is larger than $60\ \mu\text{m}$, all wavelengths will pass and the filter will fail.

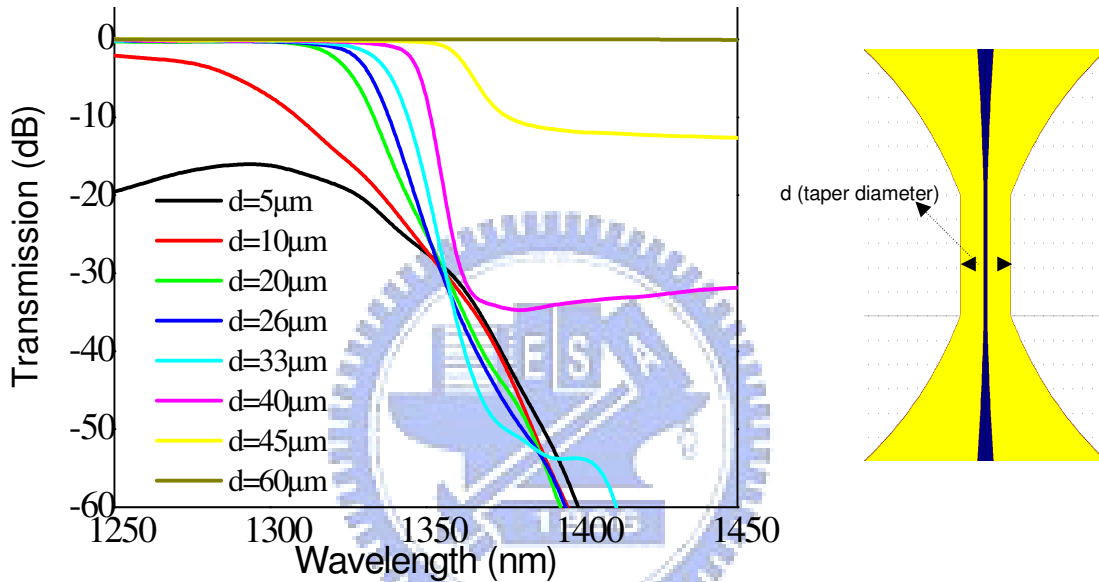


Fig3-8 The effect of different uniform taper diameter d on SPF in simulation. L_0 is 18 mm and τ is 6 mm.

Then, we try changing the taper length to simulate what effect it will cause. Fig3-9 shows the effect of different taper length L_0 on SPF when d is $40\ \mu\text{m}$ and τ is 10 mm in simulation. We can find the longer taper length would cause much better rejection efficiency and improve cut-off efficiency and if L_0 is smaller than 2 mm, the device almost doesn't have the effect of filtering.

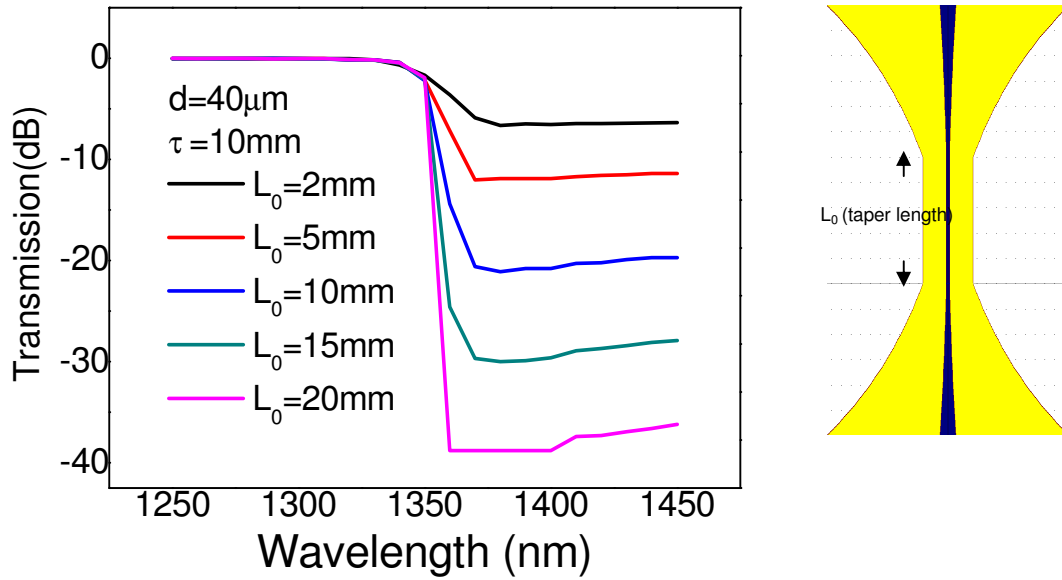


Fig3-9 The effect of different taper length L_0 on SPF when d is $40 \mu\text{m}$ and τ is 10mm in simulation.

Finally, we discuss the effect of transition length on SPF Fig 3-10 shows the effect of different transition length τ on SPF when d is $40 \mu\text{m}$ and L_0 is 15mm in simulation. From the fig 3-10, too shorter transition length causes insertion loss in guided region. However, the cut-off and rejection efficiency do not change obviously.

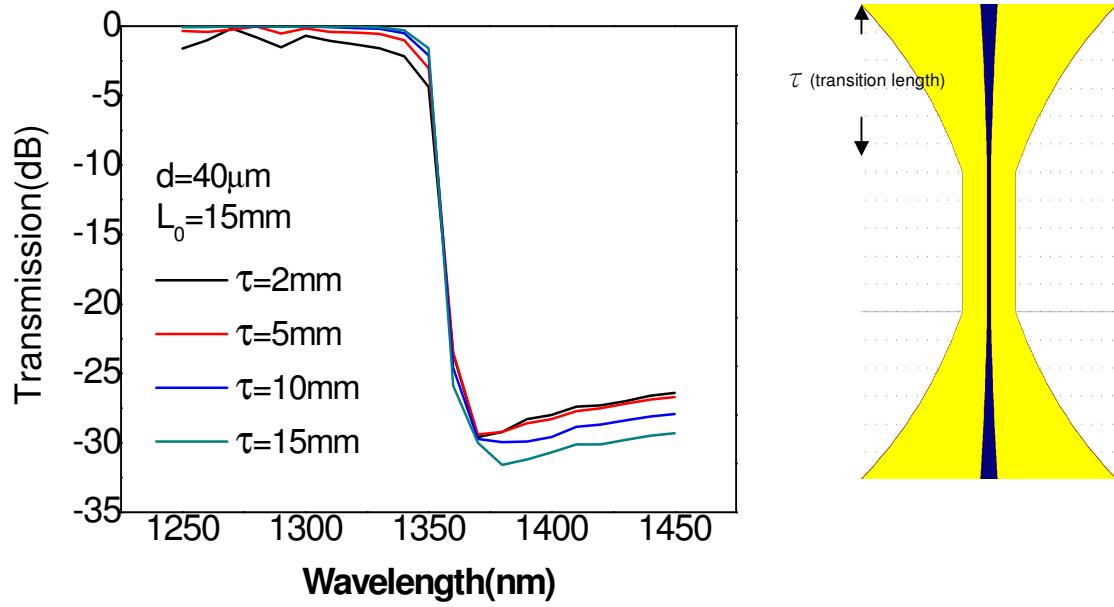


Fig3-10 Effect of different transition length τ on SPF when d is 40 μm and L_0 is 15 mm in simulation.



3.5 Summary

Table 3.1 The cutoff slopes and dispersion slopes for different waist diameters of taper filters immersed in Cargille index matching liquid.

Taper diameter	Dispersion slope $\Delta n_{\text{eff}} / \text{nm} (\times 10^{-5})$	Cutoff slope dB / nm
10 μm	-0.55	-0.38(simulation)
20 μm	-0.87	-0.79(simulation), -0.54(experimental)
26 μm	-0.94	-1.14(simulation), -1.38(experimental)
33 μm	-1.07	-1.68(simulation)
40 μm	-1.14	-2.01(simulation), -2.00(experimental)

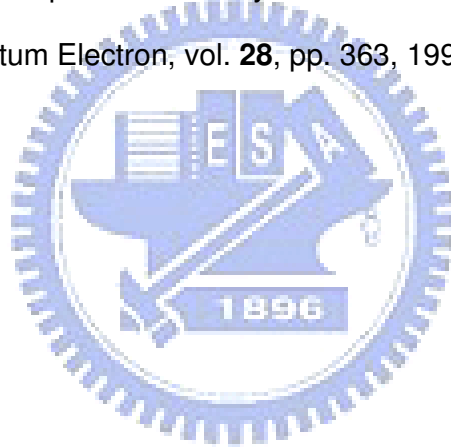
From the table 3.1, the optimal taper diameter is 40 μm for getting a high cut-off efficiency device. Therefore, we use experiments and simulation to investigate the optimal taper condition for SPF that has good performance. We summarize each effect of taper parameters and present suggestive range of taper parameters in table 3.2.

Table 3.2 Summary of each taper parameter

Fiber: SMF-28	Effects	Suggestive Range
Taper Diameter	Cut-off wavelength and Cut-off efficiency	35~40μm
Taper Length	Spectral contrast and Cut-off efficiency	30~50mm
Transition Length	Insertion loss of shorter wavelength	10~15mm

3.6 Reference

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Chapter 4

Wideband tunable short-pass double-cladding fiber filter

4.1 Introduction

Since the variation of propagation constant $\beta(\omega)$ can also substantially affect the propagation losses of lights through the mode cutoff effects, the dispersion engineering on $\beta(\omega)$ has been employed to achieve fundamental-mode cutoff LP_{01-C} SPF [4.1-4.6]. However, The cutoff slope can be increased by modifying waveguide dispersion [4.2-4.4] or by modifying the material dispersion [4.1,4.5-4.6] for silica-based S-band erbium-doped fiber amplifiers and lasers [4.1,4.3,4.7].

In this section, we propose a new structure of tapered fibers with a depressed-index outer ring that is made by double cladding fibers (DCLFs) surrounded by optical index matching liquids to achieve the sharpest LP_{01-C} than ever reported. The material of DCLFs(Fibercore:SMM900) has been introduced in section 1.3 that the depressed-index outer ring is Fu. The refractive index dispersion (RID) curves $n(\lambda)$ of tapered DCLFs would be steeper and more λ -dependent than of tapered SMF-28 because of material dispersion characteristics. Therefore, we expect the depressed-index outer ring in tapered DCLF, usually F-doped with the thickness in the wavelength scale, can confine the shorter wavelengths more tightly than the longer wavelengths to produce a higher cutoff slope,

4.2 Experimental & simulation setup

The detailed fabrication procedure of tapered DCLFs SMM900 and measurement setup of filters that we apply Cargille index matching liquid as the new effective cladding for generating tunable LP_{01-c} are the same as those of tapered fused SMF-28. Fig4-1 shows the cross-sectional structures of the tapered SMM900 with diameter d equal to (a) 125, (b) 70, and (c) $22\ \mu\text{m}$, respectively, examined under a $1000\times$ CCD microscope. Through the tapering process, the F-doped outer cladding starts to affect RID $n(\lambda)$ of DCLFs when the thickness of F-doped ring reduces down to the wavelength scale.

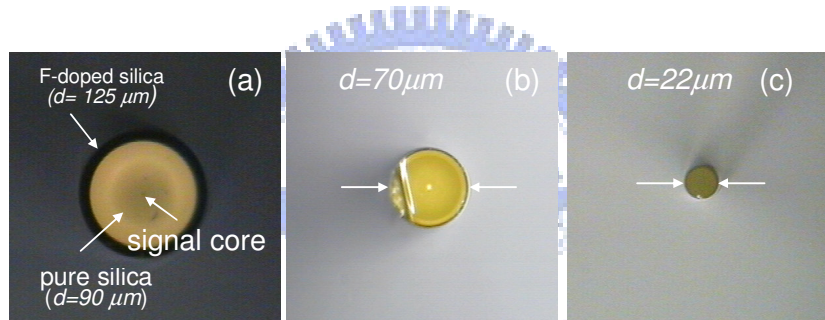


Fig 4-1 (Color online) Cross-sectional views of the SMM900 at different tapered diameters.

In our simulation, we design a double cladding structure as Fig4-2 and the other details are the same as the simulation for SMF-28. Since the Sellmeier coefficients of F-doped silica for SMM900 are not available, we consider approximately 1 mol% F-doped silica as the outer ring of SMM900.

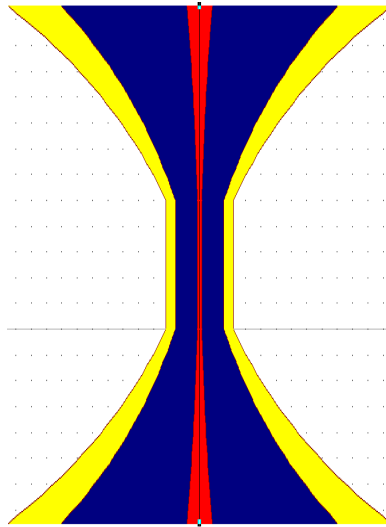
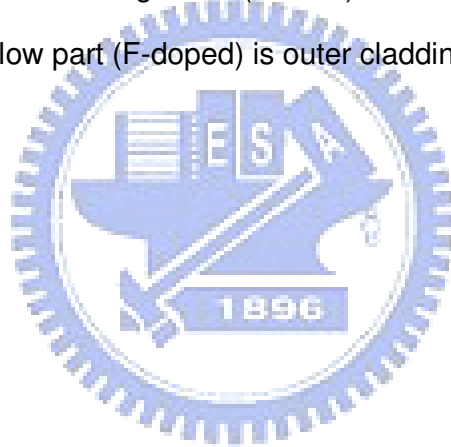


Fig4-2 Sketch for double cladding fibers (DCLFs). The red part is core and blue part is inner cladding and yellow part (F-doped) is outer cladding.



4.3 Result & discussion

4.3-1 Experiment

Fig4-3 shows the transmission spectra of the tapered SMM900 SPF at different temperature and the taper diameter is 22 μm . It is obvious that the SPF can also be available for tapering DCLFs and the tuning range would cover all band (1250nm~1650nm). Fig 4.4 shows the transmission spectra of the tapered SMM900 SPF at different taper diameter d with taper length L_0 is about 5 μm . When d goes down to 10 μm , the cutoff slopes are getting flat since the waveguide has lost the confinement ability of short wavelengths, which is similar to the tapered SMF-28 SPF as stated before. However, when d is larger than 30 μm , the F-doped silica ring would confine the longer wavelength field such that the evanescent field is not accessible. Therefore the maxima taper diameter of SMM900 is much smaller than of SMF-28 because of F-doped silica and it will be shown in the simulation section later.

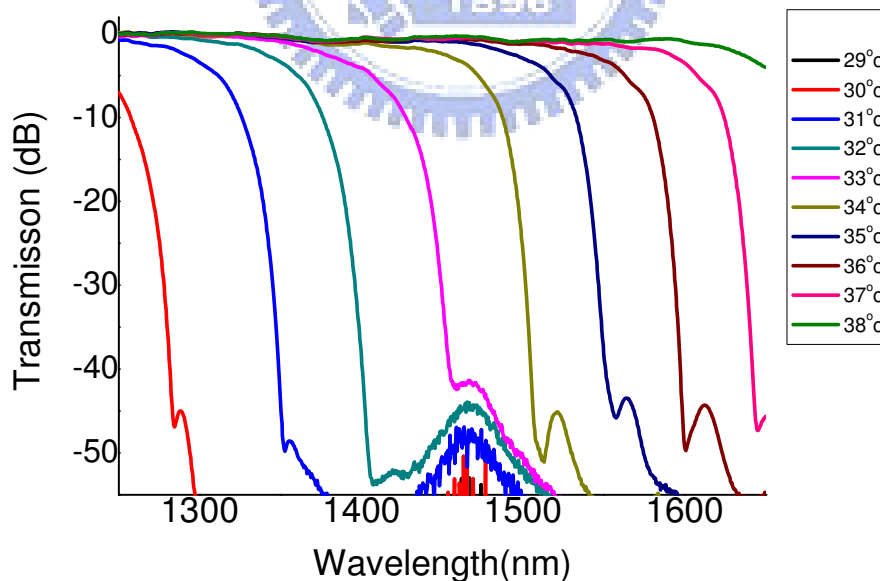


Fig4-3 Transmission spectra of the tapered SMM900 SPF at different temperature and the taper diameter is 22 μm .

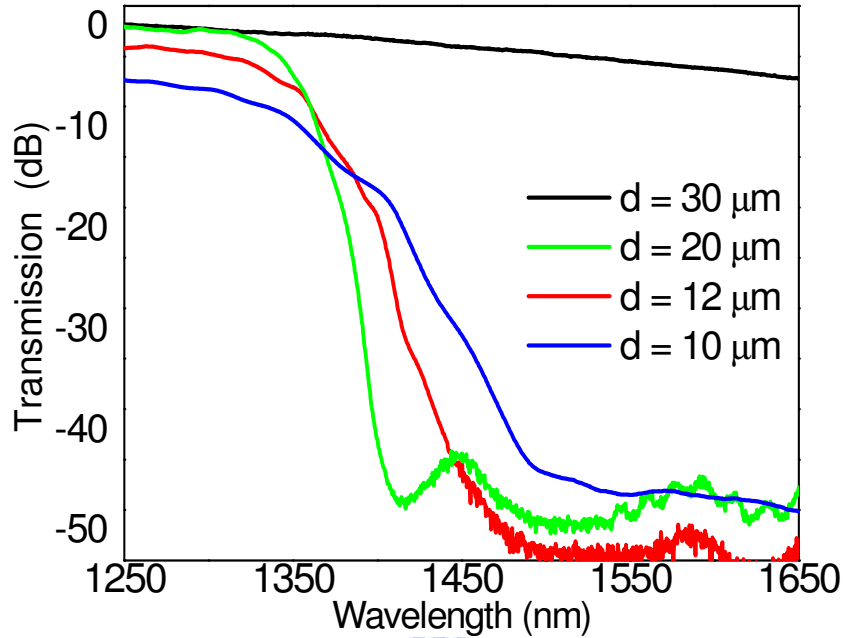


Fig4-4 Transmission spectra of the tapered SMM900 SPF at different taper diameter d with taper length L_0 is about 5 mm.

The following parts are that we will compare the tapered SMM900 SPF with the tapered SMF-28 SPF by immersing them in both A optical liquid ($n_D=1.454$) and B optical liquid ($n_D=1.456$). The results are shown in Fig 4-5 and the taper diameters are both 14 μm and taper length are both 10 mm. It would be demonstrated that the slope of SMM900 (-0.88dB/nm) is steeper than of SMF-28 (-0.49dB/nm) because of F-doped ring. However, the cut-off wavelength of SMM900 would be shorter than of SMF-28 since the F-doped ring has much lower RID $n(\lambda)$ and can degrade the effective index of tapered SMM900. In addition, the cut-off wavelength also can be tuned by using the index matching liquids which have different refractive index. Fig4-6 shows the tapered SMM900 SPF with the tapered SMF-28 SPF that taper diameter d is 22 μm and immerse them B optical liquid ($n_D=1.456$). The results are the same as when the taper diameter is 14 μm .

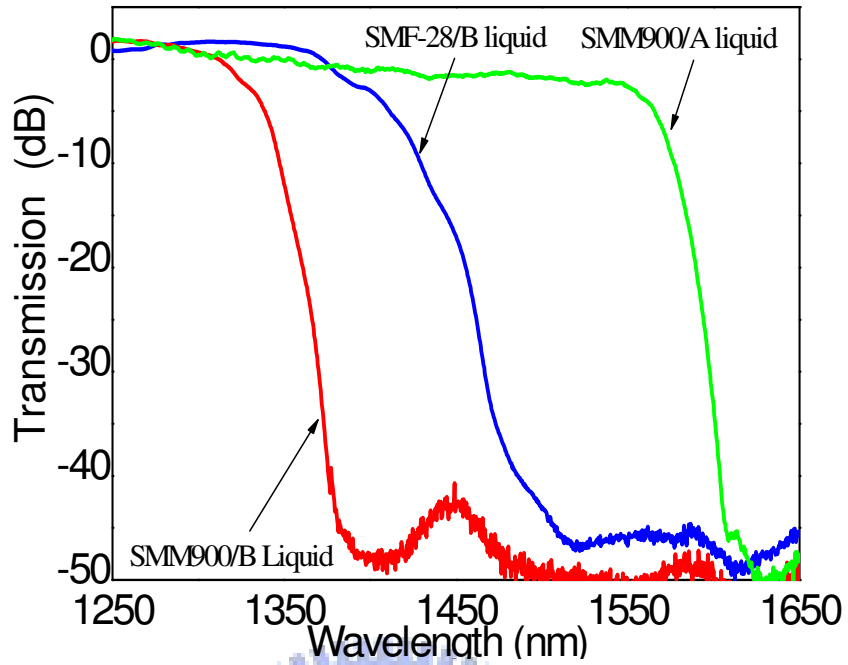


Fig4-5 Measured spectral responses of tapered SMF-28 and tapered SMM900 using *A* and *B* liquids with $d=14 \mu\text{m}$.

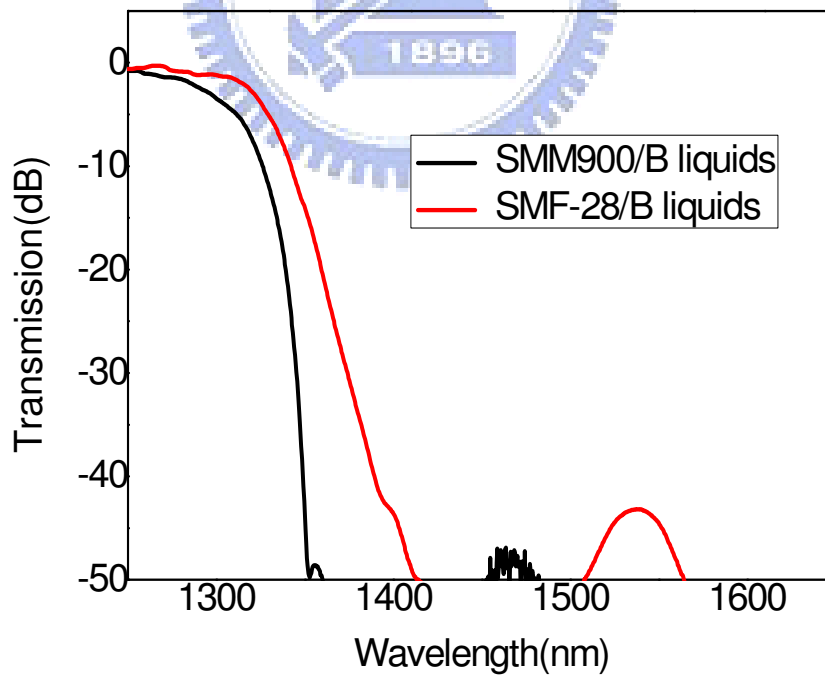


Fig4-6 Measured spectral responses of tapered SMF-28 and tapered SMM900 using *B* liquids with $d=22 \mu\text{m}$.

4.3-2 Simulation

F-doped silica as the outer ring of SMM900, and the material dispersion characteristics of its RID curve together with those of fused silica and Cargille liquids at 25°C are shown in Fig 4-7. The effective fundamental mode index n_{eff} of tapered SMF-28 and SMM900 surrounded by Cargille liquids at different taper diameter d are shown in Fig4-7 as well. From Fig 4-7, we can find the slope of tapered SMM900 is steeper than that of tapered SMF-28 because of F-doped outer ring. If we observe the cross point for two RID $n(\lambda)$ curves of different fibers and liquids, we can see the cut-off wavelength of tapered SMM900 is shorter than of tapered SMF-28. The simulation results agree with the experimental ones shown previously.

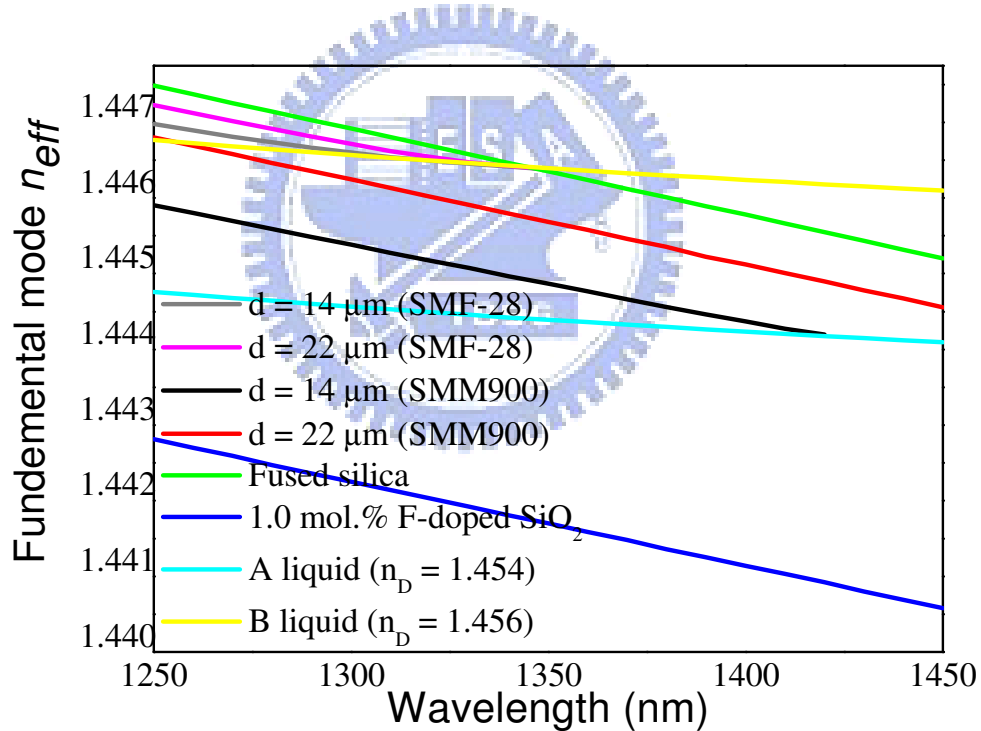


Fig4-7 Estimated RID of the fused silica, 1 mol. % F-doped silica, and Cargille liquids as well as the effective index of tapered SMF-28 in B liquid and tapered SMM900 in A liquid at different d .

Fig 4-8 shows mode field and refractive indices distribution in the taper waist of SMM900 at guided λ of 1300nm and taper diameter of 22 μm . We can infer that the layer between the fused silica and F-doped silica forms another waveguide to confine shorter wavelength. Fig 4-9(a), (b) demonstrate the comparison of mode field distribution between SMM900 and SMF-28 at the same taper diameter and different light wavelengths. Obviously, we find the confinement of SMM900 is better than of SMF-28 in guided wavelength reign.

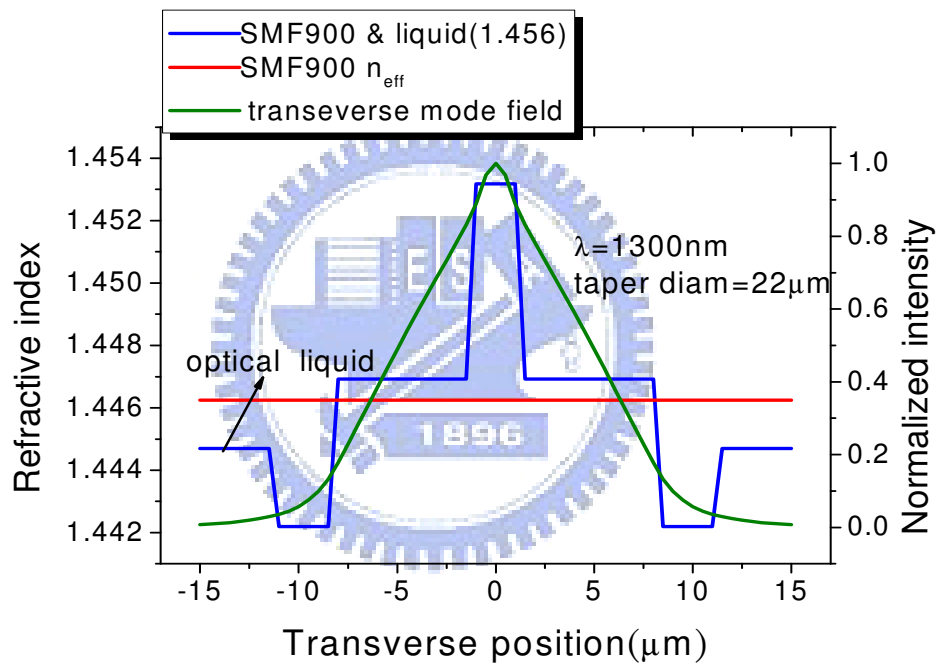


Fig4-8 Mode field and refractive indices distribution in the taper waist of SMM900 at guided λ 1300 nm and taper diameter is 22 μm .

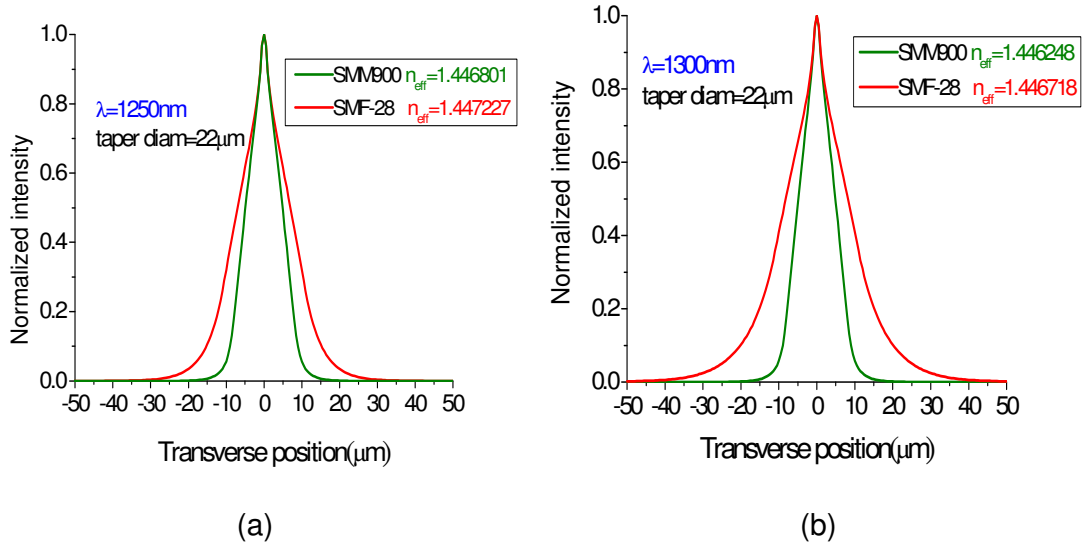


Fig4-9 Mode field distribution for SMM900 and SMF-28 at the taper diameter 22 μm and different wavelength (a)1250, (b)1300 nm.

The simulated spectral response for the tapered SMM900 immersed in A liquids and SMF-28 immersed in B liquids, with $d=14\ \mu\text{m}$ and $22\ \mu\text{m}$ are shown in Fig4-10. The waveguide dispersion dominates more over the cutoff wavelength in DCLF structures since the variation of d produces a wavelength shift of $\text{LP}_{01-\text{C}}$, but the higher cutoff slope is obtained.

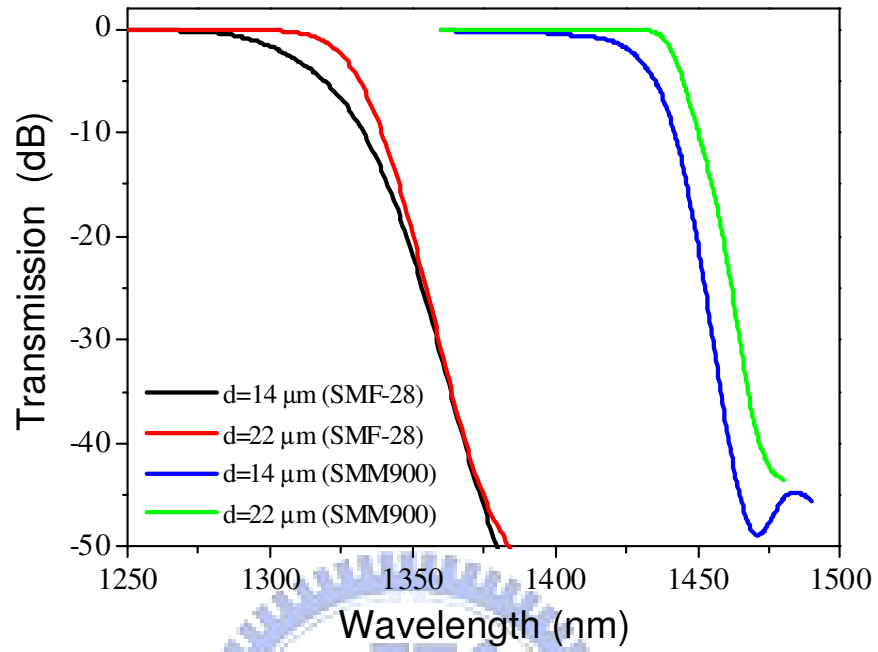


Fig 4-10 Simulated spectral response for the tapered SMM900 immersed in A liquids and SMF-28 immersed in B liquids, with $d=14 \mu\text{m}$ and $22 \mu\text{m}$.

4.4 Summary

Table 4.1 shows the cut-off slopes of SMM900 and SMF-28 with taper diameter 14 μm , 22 μm in experiment and simulation. Because the effective refractive index dispersion slopes of SMM900 are steeper than of SMF-28 for filter application, we can get higher cut-off efficiency for DCLF filter.

Table 4.1 Cut-off slopes of SMM900 and SMF-28 with taper diameter 14 μm , 22 μm in experiment and simulation.

Fiber	Cutoff slope	Cutoff slope
	dB / nm (d=14μm)	dB / nm (d=22μm)
SMF-28	-0.49(exp)	-0.54(exp)
	-0.64(sim)	-0.80(sim)
SMM900	-0.88(exp)	-1.28(exp)
	-1.04(sim)	-1.38(sim)

4.5 Reference

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Chapter 5

Conclusion

A new type of thermo-optic tunable short-wavelength-pass fiber filters (SPF) based on tapering standard single-mode fibers (SMF-28) to form fiber tapers which are then immersed in index matching liquids has been demonstrated experimentally and analyzed theoretically. The significant results are the tuning efficiency can be $50\text{nm}/^\circ\text{C}$, the cut-off efficiency can be $-1.2\text{dB}/\text{nm}$ and the rejection efficiency can be 55 dB . The effects of taper parameters on SPF have been investigated so that we can propose suggestive parameter ranges for achieving better performance of SPF.

In addition, we have demonstrated a new structure of widely tunable $\text{LP}_{01-\text{C}}$ tapered fiber filters with a high cutoff slope over $1250\text{--}1650\text{ nm}$ based on the depressed-index outer ring over a tapered fiber. The fiber with a depressed-index outer ring comes from double cladding fibers (DCLFs) named SMM900. We have compared the cut-off slopes of SMM900 with those of SMF-28 by both experiments and simulation. We have also used the material dispersion mechanism to explain why the cut-off efficiency of SMM900 is better than SMF-28.

Based on those experimental and simulated results, we can understand more about the mechanism of the SPF. The knowledge can be applied to the studies of more novel tapered device and may help develop practical products of fiber communication in the future.

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