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聯氨與四氧化二氮自燃反應機制的研究 Ab Initio Study of the Mechanism for the Hypergolic Reaction of Hydrazine with Dinitrogen Tetroxide **THUM**

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聯氨與四氧化二氮自燃反應機制的研究

Ab Initio Study of the Mechanism for

the Hypergolic Reaction of

Hydrazine with Dinitrogen Tetroxide

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Abstract

 Hydrazine and dinitrogen tetroxide reaction is a spontaneously ignited combustion reaction, and the propellants are practically used in the space shuttle of NASA. However, the mechanism of this hypergolic combustion system is still unknown theoretically and experimentally. In the practical system, the reactants are not only composed of $N_2H_4(C_2)$ and $N_2O_4(D_{2h})$ molecules, and they also contain trans-ONONO₂(C_s), cis-ONONO₂(C_s) and NO₂(C_{2v}) molecules which can react with hydrazine when the liquid N_2O_4 oxidizer is ejected into reaction chamber with high velocity. We consider these four bimolecular reactions by using ab-initio calculations with the Gaussian03 code. The geometries of all stationary points on the potential energy surfaces (PESs) are optimized by B3LYP/6-311++G(3df,2p). Moreover, the single-point calculations, including G3B3, CCSD(T), and G2M methods, correct the relative energies to give better values for the kinetic calculations. The G2M method provides the good prediction as $CCSD(T)/6-311++G(3df,2p)$, and it also has smaller differences comparing with experimental data. The G2M(CC1) and G2M(CC3) schemes are chosen for the smaller and larger reaction system, respectively.

The geometries of cis- and trans-ONONO₂ molecules are unknown experimentally. The PES of N_2O_4 isomerization has been studied; the energy barrier between the cis-isomer and $N_2O_4(D_{2h})$ is lower than that between the trans-isomer and $N_2O_4(D_{2h})$ by 20.15 kcal/mol. The energy of transition state (TS) between cis- and trans-ONONO₂ is only 1.71 kcal/mol; thus cis-trans isomerization can occur rapidly.

In the bimolecular reactions, the major and lower-energy channels are the hydrogen abstraction reactions, and the mechanism for breaking the N-O bond of $NO₂$ or N_2O_4 molecule needs much higher energies. In the $N_2H_4 + NO_2$ reaction, the lowest-energy channel produces the N_2H_3 and cis-HONO via the TS with a 7.57

kcal/mol barrier. The rate constant predicted by transition state theory is 3.20×10^{-25} T $^{3.74}$ exp(-1662.5/T) cm³/(molecule · sec) at 100K - 4000K. In the N₂H₄ + N₂O₄ reaction, the hydrogen transfer reaction accompanies with bonds breaking and forming via a ring-like TS. The energy barriers of transition state in most of the reaction channels are higher than 10 kcal/mo; however, the N_2H_4 + trans-ONONO₂ reaction occurs by hydrogen transfer via a six-member ring TS without an intrinsic barrier. In this lowest-energy channel, the energy of transition state is predicted to be lower than intermediate by 2.66 kcal/mol at the G2M(CC3) level. However the difference is only 0.16 kcal/mol at the B3LYP/6-311++G(3df,2p) level, which is confirmed by IRC calculation; therefore, it may be caused by the zero-point energy correction and computational errors. This lowest-energy channel produces $HONO₂ + H₂NN(H)NO$ with 15.57 kcal/mol exothermicity. Moreover, another lower-energy channel of N_2H_4 + $N_2O_4(D_{2h})$ reaction is also exothermic, and the products are trans-HONO and $H_2NN(H)NO_2$ Furthermore, the decomposition reactions of $H_2NN(H)NO$ and H2NN(H)NO2 molecules provide another possibility producing the active species. The direct dissociation reaction to form N_2H_3 and NO radicals is the most possible path for H2NN(H)NO molecule, where it needs to overcome a small rotation TS with 6.28 kcal/mol barrier height and undergoes the dissociation reaction with 27.83 kcal/mol energy. On the other hand, the $H_2NN(H)NO_2$ can overcome a five-member ring TS, with a barrier is 26.6 kcal/mol barrier, and decompose to trans- N_2H_2 and trans-HONO. Besides, it is also possible to directly dissociate to N_2H_3 and NO_2 with 38.23 kcal/mol energy.

The hypergolic reaction of N_2O_4 with N_2H_4 is therefore believed to be initiated by the reaction of trans-ONONO₂ with N_2H_4 which is shown to occur barrierlessly.

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I. Introduction

RNHNH₂ and N₂O₄ (R = H, CH₃, (CH₂-CH₃)) reaction systems have been continuously used as propellants for rocket propulsions into space by NASA nowadays. ⁽¹⁾ The hydrazine (N₂H₄) and dinitrogen tetroxide (N₂O₄) reaction has an extremely hypergolic property, which ignites spontaneously upon mixing without a source of ignition. A great many reports discussed this important reaction in early NASA research $(2-6)$, and most of them highlighted the combustion process of the rocket, whose fuel and oxidizer are hydrazine and dinitrogen tetroxide, respectively. This reaction contains many complex and rapid reactions, which make up a kind of huge chemical soup of reactions, and the spectra of these reactions make it very difficult to separate the signals originating from many species. To our best knowledge, there is no recent paper which discusses the mechanism or kinetics of this reaction computationally or experimentally.

The hydrazine and dinitrogen tetroxide have critical chemical properties as a combustion fuel and oxidizer, respectively, and some of their basic physical properties are presented in table1-1.

1.1 Chemical properties of hydrazine and dinitrogen tetroxide

Hydrazine (N_2H_4) is a toxic, flammable caustic liquid and strong reducing agent. Its odor is similar to that of ammonia, but less strong. It is soluble in water, methanol, ethanol, UDMH (Unsymmetrical Dimethyl hydrazine $((CH_3)_2)$ NNH₂)), and ethylenediamine, and therefore, it can be used with UDMH in the bi-fuel system. Hydrazine is found early and used as a storable liquid fuel, and it is replaced gradually by UDMH and MMA (Monomethyl hydrazine (CH_3NHNH_2)). Currently, it is used as a monopropellant for satellite motors. Hydrazine can be made by different methods, and these are briefly described below.

Raschig Process:

NH₃ + OCl⁻
$$
\rightarrow
$$
 NH₂Cl+OH⁻ \rightarrow N₂H₄ + Cl⁻ + H₂O
\nBayer Process:
\n2NH₃ + OCl⁻ + 2Me₂C=O \rightarrow Me₂C=N- N=CMe₂ + 3H₂O+Cl⁻
\nMe₂C=N- N=CMe₂ + 2H₂O \rightarrow N₂H₄ + 2Me₂C=O
\nProducts Chimiques Uginie Kuhlmann Process (PCUK)
\n2NH₃ + H₂O₂ + 2R₂C=O \rightarrow R₂C=N- N=CR₂ + 4H₂O
\nR₂C=N- N=CR₂ + 2H₂O \rightarrow N₂H₄ + 2R₂C=O
\n(1.3)

The MMA and UDMA originate from hydrazine in which one and two hydrogen atoms are replaced by one or two methyl groups, respectively. These two species are also easy to manufacture as N_2H_4 , and are applied as common rocket fuels nowadays.

On the other hand, dinitrogen tetroxide (N_2O_4) is a powerful oxidizer, highly toxic and corrosive, and it is manufactured by the catalytic oxidation of ammonia, in which steam is used as a diluting agent in order to reduce the reaction temperature. Next, the gases are cooled, and most of the water is condensed and removed. Furthermore, the nitric oxide (NO) is oxidized into nitrogen dioxide $(NO₂)$, and the remainder of the

water is removed as nitric acid. The above process is represented by eq. (1.4). This almost pure nitrogen dioxide gas is cooled to a low temperature and condensed into liquid, which keeps the equilibrium towards dinitrogen tetroxide (N_2O_4) as the temperature decreased. The last cooling step is called a dimerization reaction, which is the eq. (1.5).

$$
4NH3+5O2 \xrightarrow{Pt catalyst} 4NO+6H2O
$$

2NO+O₂ \rightarrow 2NO₂ (1.4)

Therefore, the $NO₂$ exists in equilibrium with $N₂O₄$.

$$
2NO_2 \xleftrightarrow{\longrightarrow} N_2O_4 \tag{1.5}
$$

This equilibrium is famous, and is often used as a good example in many text books. Verhoek and Daniels⁽⁷⁾ studied this effect in 1931, and the following equation is the representation of the dissociation constant, $\mathbf{K}_{N_2O_4}$. Fig1-1 and Table1-2 represent the equilibrium constant in this study.

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$$
K_{N_2O_4} = \frac{4\alpha^2 P}{1 - \alpha^2}
$$

where the P is the measured pressure in atmosphere and α is the degree of dissociation.

$$
\alpha = \frac{P - P_{N_2O_4}^{\circ}}{P_{N_2O_4}^{\circ}}; \quad P_{N_2O_4}^{\circ} = \frac{g}{M} \frac{RT}{V}
$$
\n(1.6)

in which g is the weight of nitrogen tetroxide, M is the molecular weight and R, T, and V have their usual meanings.

Table1-2: The equilibrium constant of ${}^{2}N_2 \leftrightarrow {}^{2}N_2O_4$ at three temperatures. ⁽⁷⁾

Fig1-1: Measured data for equilibrium constant $2NO_2 \rightleftarrows N_2O_4$ of at 25, 35, and WWW 7 45°C. $^{(7)}$

Many papers discuss the N_2O_4 single molecule or the unimolecular dissociation reaction. The most stable N_2O_4 geometry is D_{2h} , and the N-N bond distance varies between 1.772 and 1.776, which is much longer than the N-N bond distance of hydrazine (1.434-1.449). $(8,9)$ The weak N-N bond is also evidenced by the low values of the enthalpies of the dissociation reaction, which are $12.7-12.9$ kcal/mol at $0K^{(10,11)}$ and $13.1-13.7$ kcal/mol at $298K$. $(10-12)$ The activation energy barrier is also low. The dissociation energy, the reaction is very fast, and the experimental rate constants for the limiting low-concentration (k₀) and high-concentration (k∞) regions are 4.5×10^6 cm³/mol⁻¹ sec⁻¹ and 1.7×10^5 1/sec at 298K, respectively.⁽¹³⁾ The reason for the high rate constant is that the weak N-N bond undergoes an internal rotation (torsion) with a barrier height of about 3 kcal/mol. $(14,15)$

This dissociation reaction have been also calculated by an ab-initio calculation method (CCSD(T)/cc-PVTZ) to determine the rate constants, which are 0.62×10^{1} , $1.90 \times$ $10³$, and $1.66\times10⁵$ 1/sec at 250, 298.15, and 350K. ⁽¹⁶⁾ The following tables are the

geometries of NO₂, N₂O₄, and the energetic properties of the reaction $N_2O_4 \rightarrow 2NO_2$.

Table1-3: Equilibrium distance (in Å), bond angle (in deg), harmonic frequencies (in cm⁻¹)and zero-point vibrational energies (kcal/mol) for $NO₂$. ⁽¹⁶⁾

Method	$r_e(\text{NO})$	∠ONO	ω_1	ω_2	ω_3	ZPVE
CASSCF/cc-pVDZ	1.209	133.8	1640	1328	751	5.32
CASSCF/cc-pVTZ	1.205	133.9	1626	1319	757	5.29
$CCSD(T)/cc-pVDZ$	1.207	134.1	1759	1370	735	5.53
$CCSD(T)/aug-cc-pVDZ$	1.210	134.0	1751	1367	693	5.45
$CCSD(T)/cc-pVTZ$	1.199	134.2	1668	1348	658	6.91
Experimental	$1.1939^{\rm a}$	133.5°	16555 ^b	13578^{b}	756.8^{b}	

Table1-4: Bond distance (in Å), bond angle (deg), harmonic frequencies (cm⁻¹),

zero-point vibraional energies (kcal/mol) for the N_2O_4 dimer. ⁽¹⁶⁾

Method	ΔE^a	ΔH_0^{0b}	ΔH_{298}^0	ΔG_{298}^0	BSSE
$CCSD(T)/cc-pVDZi$	12.16(6.74)	8.70(3.28)	9.64(4.22)	$-3.08(-8.50)$	5.42
$CCSD(T)/aug-cc-pVDZ$	14.61(10.25)	11.39(7.03)	12.29(7.93)	$-0.30(-4.66)$	4.36
$CCSD(T)/cc-pVTZi$	15.36(12.65)	14.61(11.90)	14.47(12.76)	$+2.81(0.10)$	2.71
CCSD(T)/TZ2P ^c	15.0	9.9			
$CCSD(T)/TZ2P+f/TZ2Pc$	16.0	10.9(7.2)			3.70
CASPT2/QT ^d	13.2	9.6			
$CASSCF/cc-pVDZi$					
CASSCF/cc-pVTZ ⁱ					
CASSCF-CI/cc-pVTZ ^{e,i}	15.4	10.8			
Expt.		12.7 ^f 12.9 ^g	$13.6f$ 13.7 ^g 13.1 ^h	1.1 ^j	

Table1-5: Energetics (in kcal/mol) of the reaction $N_2O_4 \rightarrow 2NO_2$. Values in parentheses include the BSSE correction (basis set superposition error) in kcal/mol. (16)

1.2 Review of NASA reports

Weiss⁽²⁾ studied the dinitrogen tetroxide and hydrazine reaction with an infrared spectrum at a low temperature, and he found some important elements of note, the first of which was, that the NO₂ exists in pure N₂O₄ liquid at -196°C, which is shown in Fig1-2. Although this situation is normal due to the equilibrium, it suggested that $NO₂$ is also one of the important liquid oxidants for this combustion reaction.

Fig1-2: the infrared spectrum of N₂O₄ (high concentration) at -196[°]C ⁽²⁾

By means of the experiment at low temperature, this reaction could occur under control. The experiment was started at -196℃ and slowly warmed up, and the infrared spectra began to change at around -78℃. After continuously increasing the temperature, the concentration of $NO₂$ increased more than the quantity in the equilibrium state, and the spectra was more complex than it was at a lower temperature. However, the heat of the system did not increase to the same temperature until at -54° C. Therefore, comparing the results of the infrared spectrum and the calorimeter; Weiss suggests that (1) the initial formation of adducts in the lower temperature made the spectrum change, (2) increasing the concentration of $NO₂$ may be the result of adduct formation,

(3) the decomposition of adducts made the free-radical reaction occur and a large amount of heat and gas was released. Table1-6 presents the summary of the species in the spectrum at different temperatures. However, Weiss also indicates that there are contradictions between the results and the assumptions of the reaction mechanism. Furthermore, there were some species in the spectra which could be not identified.

Table1-6: Gas evolution from the low temperature reaction of $N_2H_4 + N_2O_4$ ⁽²⁾

 In the end, the simple miscibility experiments had been done, and there were some principle factors when the $N_2H_4-N_2O_4$ impinging jets were diverted by the interaction between the two propellants. The factors causing this phenomenon were:

(1) Immiscibility of two reactants,

(2) Rapid reaction rate between N_2O_4 and N_2H_4 ,

(3) The high heat evolution and large gas volume generated by the reaction, and the heat can make the product gases expand and the propellants vaporize.

Therefore, the way to resolve the immiscibility problem is to increase the ratio of the contact surface and the volume of the two reactants as much as possible, since this would be very important for achieving better performance of the combustion system. This part is a different topic from the reaction kinetic, and another NASA reports (3-6) tried to solve it. Although these reports did not focus on the reaction mechanism, they could still offer the experimental conditions to make a better computational assumption. In the real rocket system, the N_2O_4 and N_2H_4 are in the liquid phase, which stays with the cooler system, and are ejected into the combustion chamber with a high flow velocity. In order to achieve the best performance by means of a good mix of two propellants, the ratio of N_2O_4/N_2H_4 should be optimized, and the type of the injector, including the arrangement of the injector positions of the two propellants and the impingement angles of the injecting direction for every injector.^{$(3-5)$} Furthermore, the injecting velocity and temperature of the propellants, the size of the nozzle, and the pressure of the combustion chamber are also very important elements which affect the performance.⁽⁶⁾ Therefore, it can be understood that the combustion reaction occurs as the N_2O_4 and N_2H_4 collide with each other at very high momentum, and it also combines with the phased transformation of propellants from a liquid to gas phase. The temperature of the chamber is over 3000℃ after continuous reaction. The following figures are the photographs of the combustion reaction.

Fig1-4: Parallel injector spray pattern in the combustion reaction. (3)

(b)

Fig1-5: Typical spray photographs for (a) stream mixing for high pressure, (b) stream separation for high pressure. ⁽⁶⁾

1.3 Isomers of N_2O_4

In the gas phase, the association of $NO₂$ produces the $N₂O₄$ dimer, which is a stable molecule. Infrared and Raman spectral techniques were used to record the vibrational frequencies of the molecules. The existence of unstable forms of the dinitrogen tetroxide was proposed by Fateley, Bent, and Crawfold⁽¹⁷⁾, and they studied $NO₂$ at helium temperature in six types of matrices. Apart from bands belonging to $NO₂$ and stable N_2O_4 (D_{2h}), other bands were assigned to an unstable isomer of N_2O_4 . Baldeschwieler⁽¹⁸⁾ repeated Fateley's work, which was a similar work at liquid-hydrogen temperature. Furthermore, Hisatune, Devlin, and Wada⁽¹⁹⁾ reported that unstable molecules appeared to be formed when pure $NO₂$ gas was deposited at liquid-nitrogen temperature.

1.3.1 Isomerization of N_2O_4

St. Louis and Crawford⁽²⁰⁾ used infrared spectra to study $NO₂$ suspended in oxygen and argon matrices at helium temperature, and assign the absorption spectra of NO_2 , N_2O_4 (D_{2h}), and three unstable forms of N_2O_4 , including N_2O_4 (D_{2d}) and another two $ONO-NO₂$ isomers based on the relative optical density measurements and the temperature dependence of the bands. They called the two conformers of $ONO-NO₂$ as D and D', where D and D' are notations for cis-ONO-NO₂ and trans-ONO-NO₂. However, it is actually difficult to identify which one is cis- or trans- ONONO₂. Subsequent papers have applied the same notation, but sometimes the meanings of the notation would change from each other. They assumed that the $ONO₂$ molecule is planar as in similar cases of stable N_2O_4 and stable N_2O_2 , and they calculated the vibrational symmetry species for the molecule in terms of the symmetry group Cs. They

also assumed the bonding structures, as Fig1-6, and most subsequent researchers followed this assumption. After warming up from the temperature of existence D, they also found another isomer D', and the bands of D' were near to D. It appeared that D was isomerized to D , a molecule with a structure close to D. The following tables are the absorption spectra of D and \overrightarrow{D} .

Fig1-6: The D structure can undergo a cis-trans isomerization to form D'.

\mathbf{A}	WW	Table1-7: The correspondence between D and D.	
$D(\text{ONONO}_2)$		TY	
1829 cm ⁻¹		$1889 - 1899$ cm ⁻¹	
1645		1584	
1291		1290	
905		916	
783		794	
644		660	
488		524	

Table1-8: Frequency and vibrational assignment of infrared bands of $ONONO₂$ (D) in an oxygen matrix. (NO₂ refers to the nitro group, and O=N-O- to the nitrite group of D).

1.3.2 Temperature induced autoionization

Parts and Miller $^{(21)}$ first observed that the heterolytic dissociation of ONO-NO₂ produced the nitrosonium-nitrate $NO⁺NO₃⁻$ complex in a solid state form by the infrared spectra. Bouduan, Jodi, and Loewenschuss^{(22)} also observed this complex by the Raman spectra, and $NO⁺NO₃$ complex could produce as spontaneously as $N₂O₄$ trapping in an Ne matrix. They suggested that autoionization is an intermolecular rather than intramolecular process. The results indicate that, when a solid matrix is warmed to about 180K, an almost complete conversion occurs to the ionic $NO⁺NO₃⁻$ which remains stable over the full temperature range of 15-180K. There was no evidence that the unsymmetrical forms, D and D' of $\overline{ONO-NO_2}$, are observed prior to the transformation to the ionic form. Even though the unsymmetrical isomers exist in the matrix, all unsymmetrical and symmetrical N_2O_4 still undergo the temperature induced ionization in the mean time.

However, Jones, Swanson, and Agnew ⁽²³⁾ also reported a similar experiment with the infrared spectra, but they indicated the mechanism of the temperature induced autoionzation was intramolecular, contrary to that of Bolduan *et al.* (22) The experiment used the gas which was an equilibrium mixture of NO_2 and N_2O_4 at room temperature to make the low pressure deposition at various temperatures onto a CsBr window. The spectra were observed as the matrix samples were heated to different temperatures. The results showed that temperature induced that autoionization only occurred with the two less stable isomers of $ONO-NO₂, D$ and D' existing. The frequencies of these isomers were shifted towards those $NO⁺NO₃⁻$ relative to the more stable nitrite form. In addition, the bulk of N_2O_4 did not undergo autoionization at low pressure and at temperatures below 200K.

In fact, the band assignments for the solid N_2O_4 isomers in the matrix are far less conclusive than N_2O_4 (D_{2h}) gas. In earlier researches, there is no systematic correlation between the different conditions as the solid sample is formed, such as its composition and the effect of the temperature cycling on such solid samples. Therefore, A. Givan and A. Loewenschuss^{$(24-27)$} have also tried to solve this open question, and the results appear to clarify some of the conflicting points. In their work, the Raman and Fourier transform infrared spectra had been used to detect the matrices which included different preparation processes, such as controlling deposition rates, substrate material, deposition temperatures, and temperature cycling as parameters. They found similar results as Jones *et al*⁽²³⁾ that there was no evidence of the conversion to the ionic form of either an ordered or disordered $N_2O_4(D_{2h})$ layer, and the existence in the solid of the D' isomer was directly related to the formation of ionic nitrosonium nitrate $(NO⁺NO₃)$ and nitrogen dioxide (NO₂). With temperature cycling, up to $150K$, the NO₃ bands increased in intensity while the D' features decreased. On the other hand, the summary of the relationship between the deposition rate and temperature for the species appearing in the solid matrix was that lowering the deposition temperature increased the relative amount of the monomer, and increasing the deposition temperature favored the D' formation in the solid. Givan and Loewenschuss also suggested a mechanism of the formation of D and D' , $(24,25)$ and proposed that the formation of temperature induced autoionization is an intermolecular process. Although these experimental results offered different mechanisms of autoionization, it is still open to question, because of the uncertain assignments for the results of the Raman or infrared spectra. The existence of D and D' isomers (cis- and trans- $ONONO₂$) and the $NO⁺NO₃⁻$ complex appearing from temperature induced autionization could stand up by the above observations.

1.3.3 Ab-initio studies of N_2O_4 isomers

Stirling (28) , McKee (29) and many other researchers $(30-33)$ have calculated the conformations and characterizations of N₂O₄ isomers, which include O₂N-NO₂(D_{2h}), cis-ONO-NO₂(C_s), trans-ONO-NO₂(C_s), cis-perp-cis ONO-ONO(C_2), cis-perp-trans $ONO-ONO(C_s)$, and trans-perp-trans $ONO-ONO(C₂)$, and the geometries are shown in Fig1-7. McKee ⁽²⁹⁾ also calculated the N₂O₄ Potential Energy Surface (PES) as Fig.1-8, and the estimated activation energy in Table1-9.

cis-perp-trans ONOONO trans-perp-trans ONOONO

 Ω^4

Fig1-7: Structures of N_2O_4 isomers ⁽³³⁾

Fig1-7: Potential energy surface for the formation of ONO-ONO and N_2O_4 from $2NO+O₂$ at the QCI level theory. $^{(29)}$

Table1-9: Estimated activation barrier (kcal/mol) at the QCI and DFT (in parentheses) level of theories. $a^{(29)}$ 1896

reactant \rightarrow TS	radicals at //reactant ^b	TS^c	radicals at $\ell T S^d$
$ONOONO \rightarrow ON - OO - NO$ $ONOONO \rightarrow ONO-ONO$ $O_2NNO_2 \rightarrow O_2N$ - -NO ₂	32.1(27.7) 53.7(50.1) $-0.1(0.1)$	17.4 28.0(30.4) 1.7	10.1 10.9(2.7)

^a The first energy is at QCI = [QCISD(T)/6-31+G(2df)]//MP2/6- $31G(d) + ZPC$. The value in parentheses is DFT = Becke3LYP/6-31G(d)//Becke3LYP/6-31G(d)+ZPC. $\frac{b}{c}$ The energy of the transition structure is assumed to be equal to radicals frozen in the geometry of the reactant. The zero-point energies are taken from optimized NO. O_2 , and NO_2 . The energy of the transition structure is evaluated at the optimized transition structure. ^d The energy of the transition structure is assumed to be equal to radicals frozen in the geometry of the transition structure. The zero-point energies are taken from optimized NO , O_2 , and NO_2 .

These isomers are only the stationary points from computation, and only $N_2O_4(D_{2h})$, trans-ONONO₂, and cis-ONONO₂ have been observed in experiments. However, there is no direct measurement for the geometries of isomers in experiments, except for the most stable state N_2O_4 (D_{2h}). Therefore, the computational work can only be compared with the results of the vibrational frequencies in the Raman or infrared spectra for $cis-ONONO₂$ and trans-ONONO₂ molecules. The geometries of cis-ONONO₂ and trans-ONONO₂ molecules are assumed to be planar and C_s symmetry, as discussed in section 1.3.1 (20) . No other papers discuss this important assumption further, and thus, it may be still an open question needing to be resolved in experiments.

Since there is a possibility of the existence of $NO₂$, trans-ONON $O₂$, and cis-ONONO₂ with the N₂O₄ (D_{2h}) as oxidizers, the N₂H₄+NO₂, N₂H₄+cis-ONONO₂, N_2H_4 +trans-ONONO₂, and $N_2H_4 + N_2O_4(D_{2h})$ reactions should be considered for this combustion system. After all, in order to account for the hypergolic phenomenon in the reactions, the products of these reactions have to be produced as reactive radicals fast and exothermically to make the reactions occur violently.

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II. Computation Methods

2.1 Ab-initio Calculations

 The equilibrium geometries, including reactants, complexes, transition states (TS), and products, have been optimized at the B3LYP/6-311++G(3df,2p) level in both $NO₂+N₂H₄$ and $N₂O₄+N₂H₄$ reactions. The zero-point energies and the harmonic vibrational frequencies have been also determined by the B3LYP method, which is the Becke's three-parameter nonlocal exchange functional (1) with the nonlocal correlation functional of Lee, Yang, and Parr^{(2)}. All the stationary points have been positively identified for local minima (number of imaginary frequencies NIMAG=0), transition states (NIMAG=1), and higher order top (NIMAG>1). In order to confirm that the transition states have connected between the correct complexes (intermediates), we use the intrinsic reaction coordinate $^{(3)}$ (IRC) calculations at the B3LYP/6-311++G(3df,2p) level. 1896

 In order to obtain the more reliable energies, we have used the higher level computational methods to calculate the single-point energies with structures optimized by B3LYP/6-311++G(3df,2p). In the NO₂+N₂H₄ reaction, the CCSD(T)/6-311+G(d,p), CCSD(T)/6-311G(3df,2p), the CC1 scheme of modified G2 (G2M)⁽⁴⁾, and G3B3^(5,6) have been employed to achieve more reliable evaluation of energies. In the $N_2O_4 + N_2H_4$ reaction, there are four nitrogen atoms, four oxygen atoms, and four hydrogen atoms; hence, the higher-level ab-initio calculations could only be done by a large amount of computational resources. Due to the limitation of the resource, we have only calculated the single-point energies by $CCSD(T)/6-311+G(d,p)$ and the CC3 scheme of modified G2 (G2M) method. In the Potential Energy Surface (PES), the total energy of each equilibrium geometry is composed of the zero-point energy determined by

B3LYP/6-311++G(3df,2p) and the single-point energy calculated by high-level ab-initio calculations. All of the ab-initio calculations have been performed by the Gaussian03 program, and the calculation theories are summarized in Appendix II.

2.1.1 Modified GAUSSIAN-2 (G2M)

This method is developed by Mebel and coworkers; it improves the G2 method in many places. First, for the open shell species, G2 uses the unprojected MPn energies, but spin-projected MPn energies are expected to be more reliable than UMPn ones, especially for the systems with large spin contamination. However, the spin contamination problems occur not only on UMPn methods but also on the (unprojected) QCISD(T) method. On the other hand, the zero-point energy (ZPE) of the G2 method is from HF/6-31G* method, and it is better to include the electron correlations. Therefore, G2M method improves the G2 method by using PUMPn, CCSD(T) methods, and the ZPE at B3LYP levels. The following eq. is the G2M(CC1) and G2M(CC3) methods. 1896

 $E(G2M(CC1))=E_{bas} + \Delta E(+) + \Delta E(2df) + \Delta E(CC) + \Delta + \Delta E(HLC, CC1) + ZPE$ $E_{bas} = E[PMP4/6 - 311G(d, p)]$ $\Delta E(+) = E[PMP4/6 - 311 + G(d, p)] - E_{bas}$ $\Delta E(2df) = E[PMP4/6 - 311G(2df, p)] - E_{bas}$ $\Delta E(CC) = E[CCSD(T)/6 - 311G(d, p)] - E_{bas}$ $\Delta = E[PMP2/6 - 311 + G(2df, p)] - E[PMP2/6 - 311G(2df, p)]$ $-E[PMP2/6-311+G(d, p)]+E[PMP2/6-311G(d, p)]$ $\Delta E(HLC, CC1) = -xn_{\beta} - 0.00019n_{\alpha}$

where the PMPn stands for the spin-projected PUMPn energies for open shells and restricted RMPn energies for closed shell. The ∆E(HLC,CC1), the higher level correction, is defined by the number of α and β valence electrons, with $n_{\alpha} \ge n_{\beta}$. Furthermore, the x value for ∆E(HLC,CC1) is optimized for each of modified G2

schemes, minimizing the average absolute deviation of calculated atomization energies from experiment values for the G2 sample set of molecules. The ZPE is determined at the B3LYP level, which is the same method as geometry optimization. The G2M(CC3) is similar with G2M(CC1) but with some simplification.

$$
E(G2M(CC3))=E_{bas} + \Delta E(+) + \Delta E(2df) + \Delta E(CC) + \Delta + \Delta E(HLC, CC3) + ZPE
$$

\n
$$
E_{bas} = E[PMP4/6 - 311G(d, p)]
$$

\n
$$
\Delta E(+) = E[PMP4/6 - 311 + G(d, p)] - E_{bas}
$$

\n
$$
\Delta E(2df) = E[PMP2/6 - 311G(2df, p)] - E[PMP2/6 - 311G(d, p)]
$$

\n
$$
\Delta E(CC) = E[CCSD(T)/6 - 311G(d, p)] - E_{bas}
$$

\n
$$
\Delta' = E[UMP2/6 - 311 + G(2df, p)] - E[UMP2/6 - 311G(2df, p)]
$$

\n
$$
- E[UMP2/6 - 311 + G(d, p)] + E[UMP2/6 - 311G(d, p)]
$$

\n
$$
\Delta E(HLC, CC3) = -xn_\beta - 0.19n_\alpha
$$

The following tables are the summary of the other branch methods in G2M, including

the parameters.

Table2-1: Formulas for the recommended G2M methods.

Method	Optim. $E(HLC)$, (mhartree)	AAD ^a (kcal/mol)	$E_{\rm calc} - E_{\rm exp}$ ^b (kcal/mol)	Largest calculation	Number of heavy atoms ^c	Number of basis functions ^d
G2M(RCC1)	$-5.68n_{\beta}-0.19n_{\alpha}$	0.878	Li_2 : +2.55 C_2H_2 : -2.36 O_2 : -2.40	MP4(SDQ)/6-311 $+G(3df,2p)$	$\overline{4}$	$168 + 9n_{\rm H}$
G ₂ M(CC _I)	$-5.77nB - 0.19na$	0.891	Li_2 :+2.59 C_2H_2 : -2.34 O_2 : -2.26	MP4(SDQ)/6-311 $+G(3df,2p)$	4	$168 + 9n_{\rm H}$
$G2M(RCC2)$ or G2M(RCC)	$-5.71n_{\beta}-0.19n_{\alpha}$	0.883	Li_2 : +2.57 C_2H_2 : -2.36 O_2 : -2.37	MP4(SDTQ)/6-311 G(2df, p)	4	$128 + 6n_H$
$G2M(CC2)$ or G2M(CC)	$-5.78n_{\beta}-0.19n_{\alpha}$	0.890	Li_2 : +2.59 C_2H_2 : -2.38 O_2 : -2.25	MP4(SDTO)/6-311 G(2df,p)	$\overline{4}$	$128 + 6n_H$
G2M(RCC3)	$-5.45n_{\beta}-0.19n_{\alpha}$	1.054	$BeH: -2.42$ $CH_2(^3B_1) = 2.24$ Li_2 : +2.88	MP4(SDQ)/6-311 G(2df,p)	5	$160 + 6n_H$
G2M(CC3)	$-5.63n\beta - 0.19n\alpha$	1.042	C_2H_2 : -3.47 C_2H_4 : -2.13 $BeH: -2.40$ $CH_2(^{3}B_1) - 2.03$ Li_2 : +2.97	RCCSD(T)/ 6-311G (d,p) $MP4(SDQ)/6-311$ G(2df,p)	5	$95 + 6n_H$ $160 + 6n_H$
G2M(RCC4)	$-5.33n_{B} - 0.19n_{\alpha}$	1,082	$C_2H_2: -3.28$ $BeH: -2.42$ $CH2(3B1) - 2.19$ Li_2 : +2.80 C_2H_2 : -3.38 C_2H_4 : -2.12	$CCSD(T)/6-311G(d,p)$ $RCCSD(T)/6-311$ G(d,p)	6	$95 + 6n_{\rm H}$ $160 + 6n_H$
G2M(CC4)	$-5.37n_{B} - 0.19n_{\alpha}$	1.067	$BeH: -2.40$ $CH_2(^{3}B_1) = 2.06$ Li_2 : +2.80 C_2H_2 : -3.46 C_2H_4 : -2.18	$CCSD(T)/6-311$ G(d,p)	6	$160 + 6n_H$
$G2R(RCC5)$ or G2M(RCC,MP2)	$-5.25n_{\beta}-0.19n_{\alpha}$	1.149	$BeH: -2.45$ $CH_2(^{3}B_1)$: -2.16 Li_2 : +2.76 C_2H_2 : -3.27 C_2H_4 : -2.03 $CO: +2.17$	$RCCSD(T)/6-311$ G(d,p)	6	$160 + 6n_H$
$G2M(CC5)$ or G2M(CC,MP2)	$-5.30n\beta - 0.19n\alpha$	1.134	$BeH: -2.43$ $CH_2(^{3}B_1): -2.02$ Li_2 : +2.76 C_2H_2 : -3.33 C_2H_4 : -2.06 $CO: +2.02$	$CCSD(T)/6-311$ G(d,p)	6	$160 + 6n_{\rm H}$
$G2M(RCC6)$ or G2M(rcc, MP2)	$-4.93ng-0.19nu$	1.277	$BeH: -2.67$ $CH2(3B1)$: -2.44 CH_3 : -2.24	$RCCSD(T)/6-31$ G(d,p)	7	$105 + 5n_H$
			Li_2 : +2.99 C_2H_2 : -3.54 C_2H_4 : -2.64 C_2H_6 : -3.00	MP4(SDTQ)/ 6-311 $G(d,p)$		$133 + 6n_{\rm H}$
			$CO: +2.32$ CO_2 : +2.05	$MP2/6-311+G$ (3df,2p)		$294 + 9n_H$
$G2M(CC6)$ or $G2M$ (cc, $MP2$)	$-5.05n_{B} - 0.19n_{\alpha}$	1.246	$BeH: -2.65$ $CH_2(^3B_1)$: -2.27 CH_3 : -2.06	$CCSD(T)/6-31$ G(d,p)	7	$105 + 5n_H$
			Li_2 : +2.54 C_2H_2 : -3.45 C_2H_4 : -2.49 C_2H_6 : -2.77	MP4(SDTQ)/ 6-311G (d,p)		$133 + 6n_H$
			$CO: +2.30$ CO_2 :+2.01	$MP2/6-311+G$ (3df,2p)		$294+9n_{\rm II}$

Table2-2: Comparison of the accuracy and the range of applicability for various modified Gaussian-2 (G2M) methods. (4)

The strategy absolute deviation from experimental atomization energies.

^BFor the worst cases where deviation of calculated atomization energy from experiment exceeds 2 kcal/mol.

^eMaximum number of heavy atoms for whi with $6d$ functions. n_H is the number of hydrogen atoms in the species.

2.1.2 Gaussian-3 theory using DFT geometries and zero-point energies (G3B3)

The G3B3 method (5) is based on the Gaussian-3 theory (G3) and used the geometries and zero-point energies by B3LYP calculations. The G3 method uses geometries by MP2(FC)/6-31G(d) and scaled zero-point energies by HF/6-31G(d) followed by a series of single-point energy calculations at the MP2, MP4, and QCISD(T) levels. The detail of the G3 method is presented in the Table2-3. It includes a spin-orbit correction and a higher-level correction; therefore, the average absolute derivation between experimental data and G3 theory for 299 energies is 1.01 kcal/mol. It performs much more accurate and requires less computation time than the G2 theory. In the modified version of the G2 method, such as G2M $^{(4)}$, G2(MP2) $^{(7)}$, G2(MP2,SVP) $^{(8)}$ methods, they use different methods to determine the geometries and zero-point energies for getting better computation results. They suggested that using B3LYP methods has many advantages. First, the frequencies and zero-point energies obtained at the B3LYP level have improved much more than those obtained at the HF level, and B3LYP geometries may be easier and cheaper to obtain than MP2 geometries for larger systems. The accuracy of density functional theory for calculation of geometries has been examined in several studies. $(9,10)$ For the above reasons, Redfern's group presents variations of G3 and G3(MP2) theories that use the B3LYP density functional method for geometries and zero-point energies in place of the MP2/6-31G(d) geometries and scaled HF/6-31G(d) zero-point energies. These two variations were referred to as G3//B3LYP (G3B3) and G3(MP2)//B3LYP. On the other hand, there is another variation for zero-point energy calculations; that is introducing the new scaling factor. As the scaling factor is optimized (along with the high-level correction parameters), it gives a smallest average absolute derivation. The scaling factor in G3B3 is 0.925.

However, such a low scaling factor for B3LYP is clearly nonphysical and may compensate for other deficiencies. In the end, the new scaling factor for the zero-point energy was recommended to be 0.96. In the table2-3, we can realize clearly what the difference between G3 and G3B3 is.

 ${}^{\text{p}}$ FC=frozen core approximation for the correlation calculation, FU=all electrons included in the correlation calculation. Further details of G3 and G3(MP2) theories are in Refs. 1 and 5, respectively.

theories are in Rets. 1 and 5, respectively.
 ${}^{b}E_o(G3) = E[MP4(FC)/6-31] + \Delta(2df, p) + \Delta(QCI) + \Delta + \Delta SO + \Delta HLC + ZPE$ where
 $\Delta(+) = E[MP4(FC)/6-31 + G(d) - MP4(FC)/6-31G(d)],$
 $\Delta(2df, p) = E[MP4(FC)/6-31G(2df, p) - MP4(FC)/6-31G(d)],$
 $\Delta(QCI) = E[QCISD(T, FC)/6-31G(d) - MP4(FC)/6-$

^dThe IILC is $-An_B-B(n_\alpha-n_B)$ for molecules and $-Cn_B-D(n_\alpha-n_B)$ for atoms (including atomic ions). The n_B and n_α are the number of β and α valence electrons, respectively, with $n_{\alpha} \ge n_{\beta}$. The A, B, C, D are in mhartrees.

IN

^eScale factor of 0.8929 used for HF/6-31G(d) and 0.96 for B3LYP/6-31G(d). **TOUGH** \mathbf{L}

By the comparing with the experimental energies of 299 species, the average results for

these four methods are given in the following table.

2.2Kinetic Calculation

 The canonical Transition State Theory (cTST) is employed to calculate the rate constants for the biomolecular and unimolecular reactions. In addition, the quantum tunneling effects are included in the rate constant calculations with the Eckart tunneling model. With the transition state theory, the thermal rate constant of a reaction can be expressed as

$$
k(T) = \kappa(T)\sigma \frac{k_B T}{h} \frac{Q_{TS}(T)}{Q_r(T)} Exp[\frac{-\Delta E_{TS}}{k_B T}]
$$

Where $\kappa(T)$ is the transmission coefficient accounting for the quantum tunneling effect; σ is the reaction symmetry number; $Q_{TS}(T)$ and $Q_r(T)$ are the total partition functions of the transition state and reactants, respectively; ΔE_{TS} is the classical energy barrier for the transition state at \overline{OK} . The conventional T, k_B , and h are temperature, Boltzmann constant and Planck constant, respectively. The details of partition functions are shown in Appendix $F11$. The kinetics of a reaction was computed by the Rate Program at the platform of Computational Science and Engineering Online $(CSE\text{-online})^{(11)}$.

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III. Results and Discussions

3.1 $N_2H_4 + NO_2$ reaction

In the first section, we focus on N_2H_4 and NO_2 reaction, which is one of the possible reactions in the hydrazine and dinitrogen tetroxide combustion system, since the NO₂ always co-exists with N_2O_4 in the equilibrium state. The characteristic bond lengths and angles of optimized geometries in this reaction are discussed, including reactants, complexes, transitions states (TS), and products at the B3LYP / 6-311++G(3df,2p) calculation level, showed in Fig3-1. Next, we describe the reaction channels in the full potential surface energy surface (PES) of the $N_2H_4+NO_2$ reaction, whose energies obtained by G2M(CC1) calculation shown in Fig.3-2. Furthermore, the moments of inertia and vibrational frequencies are represented in Table3-1. Table3-2 displays the details of relative energies computed by various computational methods. Finally, we predict the rate constants for the reaction channels by mean of the Transition **THEFT** State Theory (TST).

3.1.1 Molecular Geometries of hydrazine and nitrogen dioxide

 Reactants, hydrazine and nitrogen dioxide, are well-studied molecules, and we compare the geometries and vibrational frequencies with the computational and experimental data, as shown in Tables 3-3 to 3-5. In Table3-3, comparing with the experimental data, the N-N bond of N_2H_4 predicted by B3LYP is smaller by 0.015Å; at the CCSD(T) level the agreement between theory and experiment is very good. In the case of the bond angles, both B3LYP and CCSD(T) methods have good predictions.

Therefore, the geometry by B3LYP calculation is still reliable as CCSD(T) does. Furthermore, in Table3-4, the vibrational frequencies are over-predicted by the B3LYP, MP2, and CCSD(T) methods; the most serious difference results from the MP2 method. In the high frequency region, B3LYP and CCSD(T) give similar values. The B3LYP method has a much serious over-prediction problem in the low frequency region, which is higher than 40 cm⁻¹ on average. On the other hand, for the N-O bond of the NO₂ molecule, the B3LYP method performs slightly better than the CCSD(T) and CASSCF methods. The errors of bond length between calculations and the experimental data are less than 0.01Å, and they have similar values in the bond angle. Moreover, the average error of vibrational frequencies predicted the B3LYP method is about 20 cm^{-1} , which is a reliable prediction. Comparing with DFT calculation, the CCSD(T) and CASSCF methods need much computational resources, and the MP2 method suffers from spin contamination in many cases. Therefore, according to comparison between the DFT method (B3LYP) and the MP2, CCSD(T), CASSCF methods for prediction of geometries and vibrational frequencies of N_2H_4 and NO_2 molecules, the former can not only save computational resources for larger molecular systems, it can also have a reliable prediction.

3.1.2 PES of the $N_2H_4 + NO_2$ reaction

There are four product channels in the $N_2H_4 + NO_2$ reaction, are presented in Fig3-2. Three of them are hydrogen-abstraction reactions, and the other is the oxygen transfer reaction. In the hydrogen-abstraction channels, the products are similar, including cis-HONO+N₂H₃, trans-HONO+N₂H₃, and HNO₂+N₂H₃ for channel-1, channel-2, and channel-3 respectively. Nitrous acid (HONO) is a key reactive intermediate in the combustion of many nitramine propellants, and hydrazinyl radical (N_2H_3) is very reactive with other species due to one unpaired electron in the open shell configuration. Therefore, the N_2H_3 radical and HNO_2 isomers can play an important role in the hypergolic combustion reaction. In the $N_2H_4+NO_2$ reaction, every channel starts to react from complex1, which originates from the physical attraction of the two reactants. This intermediate is lower in energy by 2.50 kcal/mol relative to the reactants at the G2M(CC1) level, and the closest distance of the two molecules is 2.494 Å. The hydrogen bond between O and H may be the reason for the decrease in the energy of complex1, and this makes the N-O bond of $NO₂$ and the N-N bond of $N₂H₄$ slightly longer. Moreover, the $NO₂$ and $N₂H₄$ in complex1 still maintain their symmetries.

In channel-1, in the beginning, complex1 is transformed to complex2 through TS1, the relative energy of which is 2.56 kcal/mol and is lower than complex2 by 0.81 kcal/mol. TS1 is a transition state to change the symmetry of N_2H_4 , and the imaginary frequency is only 114 cm-1, corresponding to a rotation motion. According to Table3-2, the energy difference between complex2 and TS1 is -0.7 to -0.8kcal/mol by single-point calculations. Therefore, we believe the small negative value should originate from a calculation error (less than 1 kcal/mol in normal situations). On the other hand, the increase in the energy of complex2 result from the structural change of N_2H_4 in complex2, from C_2 symmetry to its anti-form $(C_{2h}$ symmetry)⁽²¹⁾, the energy of C_{2h} form is much higher than that of C_2 symmetry. Therefore, the energy of complex2 is the balance between creating hydrogen bonds and the high energy conformation of N_2H_4 . Since complex1 and complex2 are the physical attraction of the two reactant molecules, the bond lengths (N-H, N-N, and N-O) and bond angles (H-N-H) have only a small difference comparing with the separate single molecules, except that the bond angle of O-N-O decreases by 5 degrees due to the formation hydrogen bonds. To produce the

cis-HONO and N_2H_3 , complex2 needs to cross over TS2, whose energy barrier is 4.2 and 7.6 kcal/mol at the G2M(CC1) level with respect to complex2 and the reactants, respectively. The intrinsic reaction coordinate (IRC) calculation of TS2 in the direction of the products indicates the formation of the O-H bond and the breaking N-H bond, resulting in the production of the cis-HONO and N_2H_3 radical. This hydrogen transfer breaks the symmetry of complex2 and elongates the N-O bond to connect with the hydrogen into an N-O-H form, but the change in the other N-O bond is less significant. In the mean time, the N-N bond shortens by 0.9 Å to balance the loss of one electron. At the next step, complex3, the association complex of cis-HONO and the N_2H_3 radical, dissociates to two independent molecules; with 8.4 and 9.5 kcal/mol energies predicted at G2M(CC1) and CCSD(T)/6-311G(3df,2p) levels of theory.

 Comparing complex1 with complex2, the hydrogen is in a different position relating to $NO₂$. For complex2, the two hydrogen atoms are in the inner side of the N-O-N angle, whereas the hydrogen is in the outer side of O-N-O angle of complex1, as presented in Fig3-1. Therefore, the products are cis-HONO+N₂H₃ and trans-HONO+N₂H₃ in channel-1 and channel-2, respectively. In channel-2, complex1 directly goes through TS3, whose energy barrier is 15.5 and 13.0 kcal/mol with respect to complex1 and the reactants at the G2M(CC1) level, producing complex4 (trans-HONO and N_2H_3). TS2 and TS3 have similar hydrogen transfers, but the position of the hydrogen atom between the oxygen atom of $NO₂$ and nitrogen atom of $N₂H₄$ is different. The distances between the hydrogen and nitrogen of N_2H_4 are 1.144 Å and 1.083Å, and those between hydrogen and oxygen of $NO₂$ are 1.395Å and 1.528Å for TS2 and TS3, respectively. This means that the energy for hydrogen transfer will be higher as the hydrogen atom is closer to the nitrogen. On the other hand, TS2 and TS3 have the same tendencies in bond lengths and the bond angle of N_2H_3 and NO_2 , as

discussed above. The last step is also a dissociation of complex4 into N_2H_3 and trans-HONO, whose energy is 10.5 and 12.2 kcal/mol predicted at the G2M(CC1) and CCSD(T)/6-311G(3df,2p) levels. Furthermore, the arrangement of the two molecules in complex3 and complex4 may mean that the hydrogen bonding in complex3 is weaker than in complex4. Therefore, the dissociate energy of complex4 is higher than that of complex3.

 In channel-3, which also occurs by hydrogen transfer, it connects a hydrogen atom of N_2H_4 with the nitrogen atom of NO_2 . Complex1 twists its N-N bond of N_2H_4 to form TS4, bringing the hydrogen atom closer to the nitrogen atom of $NO₂$. The energy of TS4 is 11.86 and 9.36 kcal/mol above complex1 and the reactants, respectively, at the G2M (CC1) level. The characteristic of bond lengths and angles in TS4 has the same trend as in TS2 and TS3. The IRC calculation of TS4 confirms the hydrogen transfer to form complex5, which is composed of N_2H_3 and HNO_2 . The dissociation energy from complex5 to the two separated molecules is 11.8 and 13.7 kcal/mol predicted at the G2M(CC1) and CCSD(T)/6-311G(3df,2p) levels. Comparing the three products from channel-1 to channel-3, the dissociation energies are high and close. Therefore this infers that the physical attractions and the hydrogen bonding are similar and important in these three systems.

 Channel-4 is the pathway in which oxygen is transferred to produce NO, instead of hydrogen transfer reaction; this process has to pass through a very high energy barrier via TS5, in which one N-O bond breaks in NO_2 , creating another N-O bond with N_2H_4 . The N-N bond in N_2H_4 decreases by 0.4Å, which is less than that in TS2, and the N-O bond not involved in the oxygen transfer increases by 0.5Å at TS5. Furthermore, the oxygen is located in the middle of the nitrogen atoms of $NO₂$ and the nitrogen atom of N_2H_4 with 1.610 and 1.465Å distance, respectively. The angle of N-O-N at TS5 is

106.5°, and the O-N-O angle of $NO₂$ molecule is decreased from 134.5° to 109.8°. Since the NO double bond in $NO₂$ is originally short (1.190 $Å$), the elongation of this bond at TS5 by over 0.25Å makes the energy barrier (which is 48.47 and 45.97 kcal/mol relative to complex1 and reactants, respectively) very high comparing with the transition states for the hydrogen transfer. After passing through TS5, complex6 consisting of NO and $H_2NN(O)H_2$ molecule. The $H_2NN(O)H_2$ isomerizes to H2NN(H)OH via TS6, which is a more stable molecule obeying the Octet rule. The unimolecular reaction via TS6 involves hydrogen migration from the nitrogen to the oxygen with releasing of energy giving the more stable molecule, $H_2NN(H)OH$.

 In this computational work, we use G3B3, CCSD(T),and G2M methods to improve single-point energies based on the geometries at B3LYP/6-311++G(3df,2p). In Table3-2, the energies predicted by these methods are slightly different, but with the same trends. Based on few experimental data, we only compare the heats of the reaction for the cis-HONO+N₂H₃ and trans-HONO+N₂H₃ products. The experimental reference for $\Delta_f H^0$ of the N₂H₃ radical is the experimental study of Ruscic and Berkowitz⁽²²⁾. The heat of reaction in N₂H₄ \rightarrow N₂H₃+H is 3.50±0.01 eV (80.8±0.3 kcal/mol), and ΔH_f of N₂H₃ would be 55.3±0.3 kcal/mol after calculation with the values of $\Delta H_f(N_2H_4)$ and $\Delta H_f(H)$. Moreover, if we use the values of $\Delta H_f(N_2H_4)$ and $\Delta H_f(H)$ given in the NIST database^(23,24), the $\Delta H_f(N_2H_3)$ will be 55.333 kcal/mol, which is almost the same as the study of Ruscic. On the other hand, the $\Delta H_f(N_2H_3)$ is computed as 56.2 and 53.7 kcal/mol at 0K and 298K by Matus et al.^{(25)}, but they do not compare with the experimental data. After applying the ΔH_f (trans-HONO), ΔH_f (cis-HONO), and $\Delta H_f(N_2H_3)$, which are -17.36⁽²³⁾, -16.84⁽²³⁾, 55.333 kcal/mol, respectively, the heat of the reaction is 3.25 and 3.76 kcal/mol for the products trans-HONO+N₂H₃ and cis-HONO+N2H3, respectively. Comparing with the experimental data and

computational results, G3B3 and G2M(CC1) perform well, but the heat of reaction for trans-HONO+ N_2H_3 is higher than that for cis-HONO+ N_2H_3 at CCSD(T) /6-311G(3df,2p). However, since the difference of two CCSD(T) values are less with the trans product energy slightly higher than the cis-counterpart than 0.7 kcal/mol, which is within the accuracy of these methods. Comparing the experimental data, the errors of the computational result are -0.32, -0.33, and 0.66 kcal/mol for $\Delta H(cis-HONO+N₂H₃)$ and 0.68, -0.32, and 0.51 kcal/mol for $\Delta H(trans-HONO+N₂H₃)$ predicted at CCSD(T)/6-311G(3df,2p), G2M(CC1), and G3B3 methods, respectively.

3.1.3 Kinetic calculation

Based on the PES presented in the preceding section, we consider the N2H4+NO2 reaction to proceed through TS2-TS4 and calculate the rate constants by employing the transition-state theory.^{$(25,26)$} For these kinetic calculations, we use the barrier heights obtained at G2M(CC1) and molecular geometries of the reactants and transition states at B3LYP/6-311++G(3df,2p) presented in Table3-1. We use the conventional TST method with Eckart's tunneling corrections. The Arrhenius plots of various rate constants are shown in Fig3-3, and the three-parameters fitting expressions for the rate constants are presented in Table3-6.

The lowest-energy channel is channel-1,

 $N_2H_4 + NO_2 \rightarrow complex 1 \rightarrow TS1 \rightarrow complex 2$

$$
\rightarrow TS2 \rightarrow complex3 \rightarrow cis-HONO+N2H3 (channel-1)
$$

The rate constant k_1 , which is controlled mainly by TS2, is the highest at any temperature among the three channels. The activation energy is 7.6 kcal/mol, and channel-2 and channel-3 have similar reaction paths, namely

 $N_2H_4 + NO_2 \rightarrow complex 1 \rightarrow TS3 \rightarrow complex 4 \rightarrow trans-HONO + N_2H_3$ (channel-2)

$$
N_2H_4 + NO_2 \rightarrow complex 1 \rightarrow TS4 \rightarrow complex 5 \rightarrow HNO_2 + N_2H_3 \quad (channel-3)
$$

The activation energy of Channel-4 is too high and therefore, we do not calculate its rate constant. In Fig.3-3, the rate constants of channel-3 (k_3) is higher than that of channel-2 (k_2) at a low temperature, whereas the k_2 is slightly lower than k_3 at a high temperature. Although the activation energy of channel-2 is higher than that of channel-3 by 3.6 kcal/mol, the A factor, which is also called the pre-exponential factor, and temperature dependence are also more important as temperature increases. Unfortunately, as mentioned in the introduction, there is no experimental result for comparison with our predicted values.

Fig3-1: The geometries in the PES are determined by B3LYP/6-311++G(3df,2p).

Table3-1: Moments of inertia (I_A, I_B, I_C) and vibration frequencies of the species computed at the B3LYP/6-311++G(3df,2p) level.

Fig 3-2: Potential Energy Surface of the N₂H₄+NO₂ reaction, whose energies are calculated by G2M(CC1)//B3LYP/6-311++G(3df,2p).

	ZPE ^b			B3LYP/6-311++G(3df,2p) CCSD(T)/6-311G(d,p) ^c CCSD(T)/6-311G(3df,2p) ^c G2M(CC1) ^c		G3B3 \degree	ΔH_f
$N_2H_4 + NO_2$	38.93	-317.011335	-316.2485283	-316.4209306	-316.5287249	-316.7623438	
complex1	39.8	-1.21	-2.61	-3.6	-2.5	-1.64	
complex2	38.96	1.78	3.12	calculating	3.37	7.65	
complex3	38.67	-4.03	-4.88	-6.1	-4.94		
complex4	39.2	-6.18	-7.51	-8.26	-7.56	-6.95	
complex5	39.84	-0.24	WILLIP 1.16	-1.07	-0.51	0.05	
complex6	40.89	20.69	17.88	calculating	17.22	19.51	
$cis-HONO + N2H3$	37.4	3.96	3.63	3.44	3.43	4.42	3.76
trans-HONO+ N_2H_3	37.44	3.42	4.04	3.93	2.93	3.76	3.25
$HNO2+N2H3$	38.46	E 10.46	12.8	12.62	11.29	11.96	
$H_2NN(O)H_2 + NO$	39.59	$\overline{}$ 23.23	18.68	21.55	18.55	20.61	
$H_2NN(H)OH+NO$	39.04	3.61	-3.5 1896 ¹		-1.27	-0.30	
TS1	38.81	1.65	2.37	0.37 [°]	2.56	2.49	
TS ₂	36.99	2.38	8.81	7.72	7.57	7.33	
TS3	37.7	7.6	14.82	15.57	12.96	11.78	
TS4	36.86	4.75	11.06	10.36	9.36	9.89	
TS5	39.66	45.56	49.17	47.13	45.97	47.2	
TS6+NO	36.24	51.97	46.79	49.42	47.53	48.5	

Table3-2: Relative energies of species predicted at various theoretical levels.^a

a: The relative energy (kcal/mol) is taken the energy of $N_2H_4+NO_2$ as reference, whose energy unit is hartree/molecule.

b: The ZPE is determined by B3LYP/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every specie.

c: The energies are including single-point energies, based on geometries of B3LYP/6-311++G(3df,2p), and ZPE. The G3B3 is represented in Table2-3.

Method	$r(N-N)$	$r(N-H_1)$	$R(N-H0)$			$\angle N-N-H_1 \angle N-N-H_0 \angle H_0-N-H_1$	$\angle H_1$ -N-N-H ₀
HF/cc-pVDZ ^a	1.412	1.007	1.004	112	107.8	107.3	88.3
$HF/cc-pVTZ^a$	1.411	0.999	0.996	112.4	108.4	108.6	89.4
$HF/cc-pVQZa$	1.408	0.998	0.995	112.6	108.7	108.8	89.7
B3LYP/cc-pVDZ ^a	1.436	1.027	1.022	111.6	106.7	105.8	87.9
B3LYP/cc-pVTZ ^a	1.436	1.015	1.011	112	107.4	108	90.2
B3LYP/cc-pVQZ ^a	1.433	1.014	1.01	112.2	107.7	108	90.2
B3LYP/cc-pV5Z ^a	1.432	1.014	1.01	112.3	107.9	108.2	90.2
B3LYP							
$/6 - 311 + + G(3df, 2p)$	1.432	1.015	1.012	112.4	107.9	108.1	90.2
$MP2/cc-pVDZa$	1.439	1.026	1.021	110.8	105.8	105.2	87.5
MP2/cc-pVTZ ^a	1.435	1.013	1.01	111.3	106.7	107	89.6
$MP2/cc-pVQZ^a$	1.43	1.011	1.008	111.7	107.1	107.5	89.9
$CCSD(T)/cc-pVDZa$	1.45	1.029	1.025	110.2	105.3	104.7	87.5
$CCSD(T)/cc-pVTZ^a$	1.445	1.015	1.012	110.8	106.2	106.6	89.9
$CCSD(T)/cc-pVQZ^a$	1.438	1.014	1.011	111.2	106.7	107.1	90
CCSD(T)/cc-pCVTZ ^a	1.445	1.015	1.012	110.8	106.2	106.6	89.9
$CCSD(T)/cc-pCVTZ$ ^{a,g}	1.441	1.014	1.0111 8910.9		106.3	106.7	89.6
$CCSD(T)/aVDZ^b$	1.4559	1.0252	1.0222	110.85	106.15	$ -$	90.13
$CCSD(T)/aVTZ^b$	1.4448	1.0162	1.013	111.13	106.63	$---$	89.73
Exp ^h (MW) ^c	1.447(5)	1.008(8)	1.008(8)	109.2(8)	109.2(8)	113(3)	88.9(15)
$Exph(\mathbb{R})^d$	1.446	1.016	1.016	108.85	108.85	106	88.05
Exp ^h (ED) ^e	1.449(4)	1.022(6)	1.022(6)	112(15)	112(15)	$---$	
$Exph$ (ED+MW) ^f	1.449(2)	1.021(3)	1.021(3)	112(2)	112(2)	106.6	91(2)

Table 3-3: Comparison of geometries (bond length in \AA and bond angle in deg) of N₂H₄ by different computational methods and experimental results.

^a: reference (1); ^b: reference (2); Microwave ^c: reference (3,4); Infrared ^d: reference (5); Electron diffraction e^{ϵ} : reference (6); Electron diffraction plus microwave f : reference (7)

^g: Correlating all electrons.

^h: Uncertainties attached to the last significant digits are given in parentheses.

Table 3-4: Calculated and Experimental Vibrational Frequencies (in cm⁻¹) of N_2H_4

Method	Vibrational Frequency				
	Symmetry $(a, a, b, a, b, a, b, a, b, a, a, b)$				
B3LYP/cc-pVDZ ^a	419, 828, 1027, 1125, 1302, 1340, 1661, 1675, 3382, 3399, 3499, 3508				
B3LYP/cc-pVTZ ^a	436, 810, 999, 1112, 1301, 1333, 1676, 1687, 3444, 3455, 3552, 3558				
B3LYP/cc-pVQZ ^a	438, 808, 989, 1113, 1299, 1329, 1675, 1686, 3452, 3461, 3554, 3559				
B3LYP/cc-pV5Z ^a	441, 803, 977, 1111, 1297, 1326, 1674, 1686, 3457, 3466, 3558, 3564				
B3LYP/6-311++G(3df,2p)	439, 801, 974, 1114, 1294, 1323, 1674, 1686, 3462, 3471, 3562, 3568				
$MP2/cc-pVDZa$	404, 885, 1077, 1154, 1326, 1370, 1677, 1690, 3469, 3479, 3591, 3597				
MP2/cc-pVTZ ^a	421, 852, 1033, 1142, 1315, 1350, 1680, 1693, 3510, 3517, 3625, 1629				
$MP2/cc-pVQZa$	431, 843, 1013, 1142, 1310, 1346, 1679, 1691, 3522, 3525, 3633, 3637				
$CCSD(T)/cc-pVDZa$	382, 878, 1086, 1134, 1323, 1366, 1670, 1684, 3412, 3430, 3530, 3537				
$CCSD(T)/cc-pVTZ^a$	398, 858, 1047, 1126, 1314, 1347, 1676, 1690, 3465, 3477, 3572, 3578				
$CCSD(T)/cc-pCVTZ^a$	404, 858, 1045, 1130, 1316, 1350, 1679, 1693, 3471, 3482, 3577, 3582				
$CCSD(T)/aVDZ^b$	404.1, 841.7, 1026.6, 1104.6, 1292.7, 1332.3, 1651.2, 1665.3, 3426.0,				
	3436.8, 3535.8, 3538.6				
$CCSD(T)/aVTZ^b$	406.0, 804.7, 1020.0, 1114.0, 1302.7, 1338.7, 1674.0, 1685.2, 1460.0,				
	3469.0, 3563.8, 3569.0				
	376.7°, 780 ^d , 966 ^e , 1076 ^d , 1275 ^e , 1275 ^d , 1628 ^e , 1642 ^d , 3314 ^e , 3329 ^d ,				
Exp. c,d,e	$3398d$, $3350e$				
$Exp.$ ^f	377, 780, 966, 875, 933, 1098, 1275, 1312, 3280, 3261, 3350, 3330				
Exp. ^g	377, 780, 937, 1098, 1283, 1324, 1587, 1628, 3297, ---, ---, 3390				
	(627), 871 (884), 1042 (1066), 1098 (1126), 1324 (1350), 1283 (1304),				
$Exp.$ ^h	1608 (1655), 1806 (1603), 3332 (3310), 3189(3200), 3332 (3310), 3332				
	(3310)				
	394, 832, 982, 1087, 1265, 1312, ---, ---, 3297 (3280), (3261), 3390 (3350),				
Exp. ¹	3356 (3330)				
	---, 780 (800), [966, 933] k (1038), (873), 1275 (1280), 1098, [1587, 1628],				
$Exp.$ ¹	1493, [3314, 3280] (3338), ---, 3325, 3350 (3338)				

^a: reference (1); ^b: reference (2); ^c: reference (8); ^d reference (9); ^e reference (10); ^f reference (11), which complied from different experimental source.; g reference (12), which complied</sup> from different experimental source.; h reference (13), which was infrared liquid and solid (in</sup> parentheses); $\frac{1}{1}$ reference (14), which was infrared and Raman (in parentheses); $\frac{1}{1}$ reference (15), which was infrared gas and liquid (in parentheses); k : double peaks [in square brackets].

Method	$r(N-O)$	\angle O-N-O	ω_1	ω	ω_3
MP2/6-31G(d) ^a	1.217	133.7	2271	1380	752
a $B3LYP/6-31G(d)$	1.203	133.8	1717	1402	749
B3LYP/6-311++G(3df,2p)	1.19	134.5	1703	1395	767
$CASSCF/cc-pVDZ$ ^b	1.209	133.8	1640	1328	751
CASSCF/cc-pVTZ	1.205	133.9	1626	1319	757
\mathbf{b} $CCSD(T)/cc-pVDZ$	1.207	134.1	1759	1370	725
$CCSD(T)/aug-cc-pVDZ^b$	1.21	134	1751	1367	693
$CCSD(T)/cc-pVTZ$	1.199	134.2	1668	1348	658
$\mathbf c$ Exp.	1.194	133.8	1671	1353	760
d,e Exp.	1.1939 ^d	$133.5^{\text{ d}}$	1655.5°	1357.8°	756.8°

Table3-5: Calculated and Experimental bond lengths (in Å), bond angles (in deg), and vibrational Frequencies (in $cm⁻¹$) of NO₂.

^a: reference (16); ^b: reference (17); ^c: reference (18); \sqrt{d} : reference (19); ^e: reference (20)

The Co

via TS4

Fig3-3: Arrhenius plots of the calculated rate constants for various channels of the $N_2H_4+NO_2$

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reaction.

$3.2 \qquad N_2O_4$ isomerization reaction

 The isomerization reaction of dinitrogen tetroxide is still unknown, since the isomers are mostly too unstable to study the properties in experiments, including structures, vibrational frequencies, dipole moments, and other physical parameters. Some computational works predict the geometries of isomers as discussed in section1.3, and we studied the geometries of trans-ONONO₂ and cis-ONONO₂. The geometries of the N_2O_4 isomers and the transition states between these isomers are determined at the B3LYP/6-311++G(3df,2p), PW91PW91/6-311++G(3df,2p), BHandHLYP/6-311++G(3df,2p), and CCSD/6-311+G(d,p) levels, as shown in Fig.3-4; the moments of inertia and vibrational frequencies are listed in Table3-7. The potential energy surface (PES) of the isomerization reaction is presented in Fig.3-5; the energies of species and TSs are determined by G2M(CC1) single-point calculations. Moreover, we use the notations of i-complexes and i-TSs in the PES for clarity.The energies from other calculations, such as the CCSD(T) method, and the heat of dissociation for $N_2O_4(D_{2h})$ to $2NO_2$ with different basis sets are listed in Table3-8 and Table.3-10, respectively.

3.2.1 The geometries of N_2O_4 isomers

The N_2O_4 (D_{2h}) molecule is the most stable structure of all isomers. The weak N-N bond, which is 1.756 Å, connects two $NO₂$ to form this well-studied molecule. Comparison of the computational and experimental results for the bond lengths, the bond angles, and the vibrational frequencies are presented in Table3-10 and Table3-11. The MP2, B3LYP, and CASSCF methods have larger errors than the CCSD(T) in the prediction of the N-N bond, which is overpredicted by 0.05Å on average, whereas B3LYP and CCSD(T) methods performs well in the prediction of the N-O bond and O-N-O angle. The PW91PW91 predicted a longer N-N bond, which is higher than experimental data by 0.1 Å , and the BHandHLYP has an inverse prediction, in which the N-N bond is shorter than experimental results by 0.07 Å. Moreover, the CCSD/6-311+G(d,p) also has underpredicted the N-N bond. Therefore, among the DFT methods in our calculations, the B3LYP provides the best prediction for the N-N bond of N_2O_4 . Furthermore, the errors of frequencies determined by the DFT and CCSD(T) are low, with 26 and 24 cm⁻¹ by B3LYP/6-311++G(3df,2p) and CCSD(T)/cc-pVTZ, respectively. Therefore, the DFT (we use B3LYP) calculation can predict the geometry and frequencies of the N_2O_4 to be as good as those by the CCSD(T) method; the B3LYP method has the advantage of saving computational resources.

The trans-ONONO₂ and cis-ONONO₂ molecules have been detected experimentally in several studies which employed infrared and Raman spectra. However, the geometries are still unknown in experiment. St. Louis and Crawford, (37) suggested that the two structures were planar with a C_s symmetry after calculating the relationship with the vibrational frequencies and molecule structures. In addition, St. Louis and Crawford noted that these two molecules can undergo cis-trans isomerization without specifying which is cis or trans. McKee⁽¹⁶⁾ firstly predicted the geometries of N_2O_4 isomers by ab-initio calculations, and Wang, Qin, and Fan⁽³⁶⁾ also calculated them later and obtained a different prediction for cis-ONONO₂ geometry. Moreover, Dyshlovoi's group⁽⁴⁰⁾ provided another cis-ONONO₂ structure. The geometries of cis-ONONO₂, cis-ONONO₂ 2, and cis-ONONO₂ 3 originate from Dyshlovoi⁽⁴⁰⁾, Wang⁽³⁶⁾, and McKee⁽¹⁶⁾, respectively; we optimize these three structures at the B3LYP/6-311++G(3df,2p), PW91PW91/6-311++G(3df,2p), BHandHLYP/ 6-311++G(3df,2p), and CCSD/6-311+G(d,p) levels as presented in Fig.3-4, respectively. First, cis-ONONO₂ calculated at B3LYP is a non-planar structure with C_s symmetry, and the $ONO-NO₂$ bond is the longest bond, 1.640Å. The cis- $ONONO₂$ optimized by BHandHLYP

and CCSD methods have similar structure, whereas the $ON-ONO₂$ bond is longer than ONO-NO₂ bond by 0.02 and 0.07 Å for BHandHLYP and CCSD method, respectively. Due to the small bond differences, we suggest the difference of cis- $ONONO₂$ optimized by B3LYP, BHandHLYP, and CCSD is simply due to the calculation methods, and these results point to the same stationary point. On the other hand, the longest bond in cis-ONONO₂ 2 and cis-ONONO₂ 3 computed at B3LYP is the ON-ONO₂ bond, which is 1.685 and 1.751Å, respectively. cis-ONONO₂ 2 is non-planar with C_1 symmetry, and the structure is just like the trans-ONONO₂ after rotating the ON group. The cis-ONONO₂ 2 predicted by PW91PW91 has the same prediction as B3LYP. The cis-ONONO₂ 3 optimized by B3LYP, PW91PW91, BHandHLYP, and CCSD are planar with C_s symmetry, which fits the suggestion of St. Louis and Crawford. However, as shown in Table3-12, cis-ONONO₂_3 computed by different methods have a small imaginary frequency, which means that it may be a saddle point on the PES. Compared with the experimental result, the errors in frequencies are 20.6 and 37.5 for cis-ONONO₂ and cis-ONONO₂ 2 geometries predicted at the B3LYP/6-311++G(3df,2p) level, respectively. In the experimental literature, Jones^{(41)} and Givan^{(42)} proposed that the autoionization, which is a formation of ionic nitrosonium nitrate $(NO⁺NO₃)$, originates from the D' isomer (Jones named it as II-ONONO₂ whose frequencies are 1961 and 1578 cm⁻¹ etc.)). The peaks of D isomer (otherwise known as $I-ONONO₂$ whose frequencies are 1840 and 1625 cm⁻¹ etc.)) were stable, whereas the peaks of D' are annihilated as the enhanced peaks of NO⁺NO₃⁻. Moreover, St. Louis and Crawford suggest that the D' form might be more stable in thermodynamic. According to this experimental evidence, we suggest that the D isomer is cis-ONONO₂. The longest bond of cis- $ONONO₂$ ₂ is $ON-ONO₂$, and this may provide a possibility for the occurrence of autoionization as the temperature increases. The $cis-ONONO₂$ 3 is thermodynamically unstable and is s saddle point, since every computation indicates that there is one small imaginary frequency. The existence of cis- $ONONO₂$ seems

less reasonable than cis-ONONO₂ and cis-ONONO₂ 2, even though cis-ONONO₂ is not a planar structure, its C_s symmetry provides the correct relationship in vibrational frequencies. Therefore, we conclude that the frequencies of D and D' in the research of St. Louis and Crawford belong to a cis- and a trans- $ONONO₂$ structure, respectively. This assignment of the vibrational frequencies is contrary to Wang's work^{(36)}. Fortunately the energies of these three cis-ONONO2 structures are very close, as shown in Table3-8, and the difference between them is smaller than 0.2 kcal/mol at the B3LYP/6-311++G(3df,2p) level of theory. The comparison of vibrational frequencies is listed in Table3-12, 3-13, and 3-14. The calculated results compare with those optimized by B3LYP/6-311++G(3df,2p) in Table3-12, and the frequencies of cis- $ONONO₂$ are much closer to the experimental result than those of cis-ONONO2_2. Precisely, the deviations comparing with experimental data are -20.6 and 37.5 cm^{-1} for cis-ONONO₂ and cis-ONONO₂ -2 computed at B3LYP, respectively. Moreover, the B3LYP method provides better predictions than the MP2 method does for cis- $ONONO₂$. The three types of cis-ONONO2 geometries optimized by B3LYP, PW91PW91, BHandHLYP, CCSD methods are compared in Table3-13 and Table3-14. It is worthy to note is that the error of cis-ONONO₂ 2 predicted by PW91PW91 is 21.4 cm⁻¹, which is close to the error of $cis-ONONO₂$. Therefore, the geometries of cis-ONONO₂ and cis-ONONO₂_2 are acceptable.

 Even though there is no complete experimental result to describe on these isomers, the geometries of trans-ONONO2 predicted in different computational works are similar. In Table 3-15, the ON-ONO₂ bond is the longest, 1.685, 1.634, 1.514, 1.550, 1.654, and 1.657 \AA computed at the B3LYP/6-311++G(3df,2p), PW91PW91/6-311++G(3df,2p), BHandHLYP/ 6-311++G(3df,2p), CCSD/6-311+G(d,p), MP2/6-31G(d)⁽¹⁶⁾, and MP2/6-311G^{*(36)} levels, respectively, for the trans- $ONONO₂$ molecule. All of the trans- $ONONO₂$ geometries are almost planar and C_s symmetry except that the one calculated by CCSD, and there is no other trans-isomer structure found in our calculations. These predictions of a long bond length may

help explain the appearance of the autoionization producing $NO⁺NO₃⁻$ complex. The vibrational frequencies are listed in Table3-15, and the errors in frequencies obtained by B3LYP, PW91PW91, and CCSD are 22.5, 13.1, 27.1 cm^{-1} on average, respectively. The trans-ONONO₂ BHandHLYP has a small imaginary frequency. Basically the trans-ONONO₂ structure has consistent results among different methods. These three N_2O_4 isomers determined here will be used as the reactants to react with N_2H_4 .

3.2.2 PES of N_2O_4 isomerization

Due to its low dissociation energy, at room temperature, the N_2O_4 (D_{2h}) molecule also contains a small amount of NO_2 monomers. The equilibrium concentration of the N_2O_4 increases as the temperature decreases. The N-N bond is 1.776 Å by experiment, and this weak bond is also evidenced by the low values of the enthalpies of reaction at 0K, 12.7-12.9 kcal/mol, and at 298K, 13.1-13.7 kcal/mol.^(27,28) The rate constant of the dissociation reaction is 4.5×10⁶ L mol⁻¹ sec⁻¹ and 1.7×10⁵ sec⁻¹ in the low-pressure (k₁) and the high-pressure (k∞) regions, respectively.⁽⁴³⁾ Shock waves measurements of the dissociation in the temperature range of 253-301K show activation energies varying from 11.0±0.6 kcal/mol (1 atm) to 13.0 kcal/mol (high pressure).⁽⁴⁴⁾ In Table3-9, the CCSD(T)/6-311++G(3df,2p) method shows a better prediction of the reaction enthalpy at 0K. However, other methods, even CCSD(T)/cc-pVTZ and G2M(CC1) methods, have poor performances. i-TS1 is a very high barrier from N_2O_4 (D_{2h}) to trans-ONONO₂, as shown in Fig.3-5. It is easier to form $cis-ONONO₂ via i-TS2. Although the reaction coordinate of i-TS1 and i-TS2 is similar, which$ breaks the N-N bond and creates a new O-N bond, their energies are highly different, as presented in Fig3-5. According to the discussion in Section 3.2.1, cis-ONONO₂ and cis-ONONO₂ 2 optimized by B3LYP/6-311++G(3df,2p) can possibly exist, and we consider them in the N_2O_4 isomerization reactrion. The two NO_2 group in cis-ONONO₂ is

perpendicular, and the cis-ONONO₂ 2 is similar to trans-ONONO₂, which has long ON-ONO2 bond as shown in Fig.3-4. The cis-ONONO2 structure cannot directly transform to trans-ONONO₂; the cis-ONONO₂ first transforms to cis-ONONO₂ 2 via i-TS3, which corresponds to the rotation of the ONO group. Since the cis-ONONO₂ 2 and trans-ONONO₂ both have the long $ON-ONO₂$ bond, the i-TS4, which corresponds to the rotation of the ON group connect between cis- $ONONO₂$ and trans- $ONONO₂$ molecules. Since i-TS3 and i-TS4 are the transition state of the internal rotations, the activation energy of cis-trans isomerization is very small, their imaginary frequencies are 42 and 188 cm⁻¹ for i-TS3 and i-TS4. The energy barrier of i-TS4 for the cis-to-trans direction is only 1.71 kcal/mol at the G2M(CC1) level. However, that of i-TS3 is lower than cis-ONONO₂ and cis-ONONO₂ 2 by 1.5 and 0.23 kcal/mol, respectively. It may be due to a computational error, since the energy difference is less than 0.02 kcal/mol by B3LYP/6-311++G(3df,2p). The calculated energies of species and transition states at the G2M(CC1) level are very close to those by CCSD(T) $/6-311++G(3df,2p)$, as shown Table 3-8. Since the activation energy for trans-ONONO₂ formation from N_2O_4 is higher than that for cis-ONONO₂ by 32 and 32.3 kcal/mol at G2M(CC1) and CCSD(T)/6-311++G(3df,2p), respectively, the possible channel is that N_2O_4 transforms to cis- $ONONO₂$ first and later trans- $ONONO₂$ forms. This lowest-energy channel is consistent with the phenomenon observed by St. Louis and Crawford.

The rate constants with Eckart's tunneling correction of isomerizations are calculated by TST using the energy barrier predicted by G2M(CC1) values are shown in Table3-7. We consider the reactions between the two isomers, including N_2O_4 to trans-ONONO₂ via i-TS1, N_2O_4 to cis-ONON O_2 via i-TS2, and both directions of cis-ONON O_2 to trans-ONON O_2 via i-TS3, and the Arrhenius plots and the three-parameters fitting the expressions for the rate constants are shown in Fig:3-6. According to the kinetic calculations at temperatures varying from 100 to 1000K, we confirm that the formation of trans-ONONO₂ accounts for N_2O_4 isomerization to cis-ONONO2 via i-TS2 followed by cis-trans isomerization via i-TS3 and i-TS4 with very high rate constant.

(b)

(c)

Fig3-4: (a) The geometries in the PES of N_2O_4 isomerization are determined at B3LYP/ 6-311++G(3df,2p) level, (b) PW91PW91/6-311++G(3df,2p) level, (c) BHandHLYP/ 6-311++ $G(3df,2p)$ level, and (d) CCSD/6-311+ $G(d,p)$ The value in parentheses is noted for Mulliken charge.

Fig3-5: The PES of N₂O₄ isomerization, whose energies are calculated by G2M(CC1)//B3LYP/6-311++G(3df,2p).

Species or Transition States	Moments of inertia $I_i(a.u)$	Vibrational Frequency u_i (cm ⁻¹)
$N_2O_4(D_{2h})$	273.2, 500.4, 773.7	87, 222, 293, 446, 490, 704, 760, 850, 1307, 1450, 1787, 1826
trans-ONONO ₂ (C_s)	151.2, 773.8, 925.0	9, 131, 209, 294, 486, 647, 786, 801, 945, 1330, 1709, 1934
$cis-ONONO2(Cs, non-planar)$	244.9, 605.7, 632.1	73, 135, 179, 285, 542, 564, 693, 862, 909, 1360, 1683, 1845
cis-ONONO ₂ _2 (C_1 , non-planar)	195.3, 634.6, 770.1	39, 188, 205, 294, 601, 623, 748, 823, 876, 1312, 1667, 1989
cis-ONONO ₂ _3 (C_s , planar)	171.0, 673.2, 844.2	34i, 168, 202, 278, 590, 654, 761, 798, 892, 1310, 1649, 2038
i-TS1 (C_s)	216.1, 716.5, 777.2	638i, 125, 250, 273, 375, 426, 714, 751, 1178, 1332, 1634, 1952
i-TS2 (C_1)	277.2, 730.3, 967.5	454i, 55, 116, 133, 149, 259, 633, 789, 1254, 1406, 1716, 1756
i-TS3 (C_1)	241.6, 595.4, 636.9	42i, 152, 178, 259, 549, 591, 700, 841, 893, 1336, 1753, 1829
i-TS4 (C_1)	173.6, 687.8, 807.7	188i, 77, 181, 288, 616, 666, 707, 791, 910, 1304, 1643, 2034
NO ₂ (C _{2v})	7.4, 137.6, 145.0	767, 1395, 1703
$NO(C_1)$	0.0, 34.9, 34.9	1979
NO ₃ (C _{3h})	129.4, 130.0, 259.4	220, 248, 810, 1103, 1121, 1137
$NO+(C1)$	0.0, 29.8, 29.8	2487
NO ₃ (C _{3h})	135.1, 135.3, 270.5	710, 711, 849, 1072, 1379, 1381

Table3-7: Moments of inertia (I_A , I_B , I_C) and vibration frequencies of the species in N_2O_4 isomerization computed at B3LYP/6-311++G(3df,2p).
Species or Transition States	ZPE ^b	B3LYP	CCSD(T)	CCSD(T)		
		$/6 - 311 + + G(3df, 2p)$	$/6 - 311 + G(d,p)^c$	$(6-311++G(3df,2p)^c)$	$G2M(CC1)^c$	ΔH_0°
$N_2O_4(D_{2h})$	14.61	-410.308886	-409.3648607	-409.6067069	-409.7113339	
trans-ONONO ₂ (C_s)	13.27	10.21	6.1	6.19	5.86	
cis-ONONO ₂ (C_s , non-planar)	13.05	12.51	9.63	9.72	9.61	
$cis-ONONO2$ (C ₁ , non-planar)	13.39	12.54	8.48	8.69	8.34	
i-TS1 (Cs)	12.88	40.32	42.48	42.86	42.18	
i -TS2 $(C1)$	11.82	37.09	19.15	23.2	22.03	
i -TS3 $(C1)$	12.98	12.54	8.33		8.11	
i -TS4 $(C1)$	13.18	14.77	$10.27 -$	10.59	10.05	
$2\,\text{NO}_2\,(\text{C}_{2v})$	11.05	9.98	9.01	11.86	15.58	12.7, 12.9
$NO + NO3$	9.46	34.53	31.71	35.25	38.37	
$NO^+ + NO_3^-$	12.28	165.92	153.97	157.33	156.86	

Table3-8: Relative energies of species in N_2O_4 isomerization reaction at various theoretical levels. ^a

^a: The relative energy (kcal/mol) is taken the energy of N_2O_4 (D_{2h}) as reference, whose energy unit is hartree/molecule.

^b: The ZPE is determined by B3LYP/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every specie.

 c : The energies are including single-point energies, based on geometries of B3LYP/6-311++G(3df,2p), and ZPE.

Table 3-9: The heat of dissociation for N_2O_4 to $2NO_2$ at 0K and one atmosphere.

	$CCSD(T)$ $CCSD(T)$		CCSD(T)	CCSD(T)	CCSD(T)	$G2M(CC1)^{b}$ Exp.	
					/cc-pVDZ ^a /aug-cc-pVDZ ^a /cc-pVTZ ^a /6-311+G(d,p) ^b /6-311++G(3df,3p) ^b		
ΔH_0°		1.39	14.61	9.01	11.86	15.58	$12.7^{\circ}, 12.9^{\circ}$

^a: reference (17); ^b: this work, the methods are single-point calculation based on B3LYP/6-311++G(3df,2p) level. ^c: reference (27); d : reference (28)

Method	$r(N-N)$	$r(N-O)$	\angle (O-N-O)
$MP2/6-31G(d)a$	1.824	1.214	135.2
B3LYP/6-31G(d) ^a	1.783	1.196	134.6
B3LYP/6-311++G(3df,2p) ^b	1.8	1.184	134.8
B3LYP/6-311++G(d,p) ^c	1.81	1.188	134.8
B3PW91/6-311++G(d,p) ^c	1.783	1.183	134.8
B3P86/6-311++G(d,p) ^c	1.773	1.183	134.8
B1PB95/6-311++G(d,p) ^c	1.775	1.181	134.9
B1LYP/6-311++G(d,p) ^c	1.793	1.186	134.7
MPW1PW91/6-311++G(d,p) ^c	1.757	1.18	134.7
PBE1PBE/6-311++G(d,p) ^c	1.754	1.18	134.8
PW91PW91/6-311++G(3df,2p) ^b	1.858	1.195	134.8
BHandHLYP/6-311++G(3df,2p) ^b	1.68	1.167	134.4
$QCISD/6-311++G(d,p)^c$	1.701	1.19	134.2
CASSCF/cc-pVDZ ^d	1.806	1.171	134.4
CASSCF/cc-pVTZ ^d	1.806	1.168	134.1
È CASSCF/QT ^e	1.803	1.167	134
CASPT2/QT ^e	1.794	1.191	134.8
$CCSD/6-311+G(d,p)^{b}$	1.695	1.187	134.2
CCSD(T)/TZP2f ^d	1.752	1.195	134.7
$CCSD(T)/cc-pVDZd$	1.776	1.2	135.2
$CCSD(T)/aug-cc-pVDZd$	1.78	1.204	134.7
$CCSD(T)/cc-pVTZd$	1.774	1.194	134.8
Exp. f	1.756	1.19	134.4
Exp. (ED) ^h	1.776(4)	1.191(4)	134.6(5)
Exp. (XRD) ⁱ	1.712(17)	1.189(12)	134.8(15)
Exp. $(ND)^j$	1.7561(9)	1.1893(5)	134.40(7)
Exp. $\left(\text{IRR}\right)^k$	1.756(10)	1.196(5)	133.7(5)

Table 3-10: Comparison of geometries (bond length in \AA and bond angle in deg) of N₂O₄ by different computational methods and experimental results.

^a: reference (16); ^b: this work; ^c: reference (29); ^d: reference (17); ^e: cc-PVQZ for nitrogen and cc-PVTZ for oxygen, reference(30); f : reference (18); g : Uncertainties attached to the last significant digits are given in parentheses.; h : Electron diffraction in gas phase at T=294K, reference (31); ⁱ:X-ray diffraction in solid state at T=25K, reference (32); ^j: Neutron diffraction at T=20K, reference (33); ^g: Infrared roationally resolved measurement at T≒50K, reference (34)

Method	ω_1 (a _u)	$\omega_2(b_{2u})$	ω_3 (ag)	ω_4 (b_{3u})	ω_5 (b_{3g})	ω_6 (b _{2g})	ω_7 (b_{1u})	ω_8 (a _g)	ω_9 (b_{1u})	ω_{10} (a _g)	ω_{11} (b _{3g})	ω_{12} (b _{2u})
B3LYP/6-311++G(3df,2p) ^a	87	222	293	446	490	704	760	850	1307	1450	1787	1826
B3LYP/6-311++G(d,p) ^b	83	225	292	436	492	673	762	849	1306	1448	1794	1828
B3PW91/6-311++G(d,p) ^b	83	236	304	449	508	693	775	859	1336	1474	1844	1878
B3P86/6-311++G(d,p) ^b	84	239	310	450	512	695	776	861	1339	1475	1848	1882
B1PB95/6-311++G(d,p) ^b	86	256	318	452	512	696	776	861	1345	1483	1859	1894
B1LYP/6-311++G(d,p) ^b	83	235	301	447	502	687	770	855	1316	1456	1805	1839
MPW1PW91/6-311++G(d,p) ^b	83	249	319	463	524	711	786	858	1356	1489	1870	1904
PBE1PBE/6-311++G(d,p) ^b	84	252	322	464	527	714	787	869	1361	1492	1878	1913
PW91PW91/6-311++G(3df,2p) ^a	86	190	264	401	449	641	727	821	1264	1407	1738	1773
BHandHLYP/6-311++G(3df,2p) ^a	85	292	366	526	569	820	823	899	1410	1524	1897	1940
$QCISD/6-311++G(d,p)^{b}$	53	282	352	474	540896	684	783	858	1328	1428	1791	1818
$CASSCF/cc-pVDZc$	98	210	221	430	482	682	826	877	1457	1558	2043	2067
CASSCF/cc-pVTZ ^c	93	230	246	454	502	716	831	884	1439	1598	2013	5035
$CCSD/6-311+G(d,p)^{a}$	49	288	353	480	548	631	793	862	1347	1445	1837	1871
$CCSD(T)/cc-pVDZc$	95	232	278	434	495	677	759	820	1301	1414	1803	1834
$CCSD(T)/aug-cc-pVDZc$	80	222	273	429	463	677	737	804	1273	1389	1741	1788
$CCSD(T)/cc-pVTZc$	92	249	302	454	512	711	763	829	1288	1398	1782	1813
$Exp.$ ^d				441	484	707	776	826	1294	1413	1777	1818
Exp. ^e	82	265	282	428	480	676	751	812	1261	1383	1724	1757

Table3-11: Calculated and Experimental Vibrational Frequencies (in cm^{-1}) of N_2O_4

^a: this work; ^b: reference (29); ^c: reference (17); ^d: Harmonic frequencies, reference (35); ^e: Fundamental frequencies, reference (35)

	$cis-ONONO2$		$cis-ONONO_2$ 2			$cis-ONONO2$ 3		
	B3LYP/	B3LYP/	MP2/	MP2/	B3LYP/	B3LYP/	MP2/	
		6-311++G(3df,2p) ^a $ 6-311++G(3df,2p)$ ^a 6-31G [*]		$6-311G*^{b}$	$ 6-311++G(3df,2p) ^a$ 6-31G(d) ^c		$6-31G(d)^c$	$Exp.$ ^d
$NO2$ torsion	73	39	52.6	48.4	34i	55i	90i	
NO torsion	135	188	176.7	174.5	168	169	145	
NO ₂ rock	179	205	221.3	216.5	202	206	250	
$O-N(O)$ str	285	294	337.2	336.1	278	270	286	304
N-O-N bend	542	601	604.9	616.9 _°	590	588	674	488
$NO2$ wag	564	623	638.2	662.1	654	620	802	641
$O=N-O$ bend	693	748	729.2	745.4	(761)	769	902	
$NO2$ bend	862	823	785	799	798	791	965	783
$O-N(O_2)$ str	909	876	871	888.5896	892	872	1055	905
$NO2$ s-str	1360	1312	1298.1	1301.9	1310	1338	1568	1290
$NO2$ a-str	1683	1667	1832.5	1826.8	1649	1722	1950	1645
NO str e	1845	1989	1919.3	1959.8	2038	1986	2165	1829

Table3-12: Calculated (B3LYP) and Experimental Vibrational Frequencies (in cm⁻¹) of cis-ONONO₂.

^a: this work; ^b: reference (36); ^c: reference (16); ^d: reference (37); ^e: the assignment of frequencies is from reference (36)

		$cis-ONONO2$		$cis-ONONO_2$ 2			
	B3LYP/	PW91PW91/	BHandHLYP/	CCSD/	B3LYP/	PW91PW91/	Exp. ^a
	$6-311++G(3df,2p)$		$6-311++G(3df,2p)$ 6-311++G(3df,2p)	$6-311+G(d,p)$		$ 6-311++G(3df,2p) 6-311++G(3df,2p) $	
$NO2$ torsion	73	48	36	43	39	39	
NO torsion	135	159	212	218	188	175	
NO ₂ rock	179	179	270	236	205	220	
$O-N(O)$ str	285	205	375 111177	343	294	280	304
N-O-N bend	542	404	637	601	601	537	488
$NO2$ wag	564	475	647	625	623	579	641
$O=N-O$ bend	693	747	794 \bullet	759	748	700	
$NO2$ bend	862	817	926	883	823	789	783
$O-N(O_2)$ str	909	1249	987	917	876	813	905
$NO2$ s-str	1360	1359	1445	1373 1896	1312	1265	1290
$NO2$ a-str	1683	1519	1855	1779	1667	1637	1645
NO str e	1845	1792	1930	1853	1989	1878	1829

Table3-13: Calculated Vibrational Frequencies (in cm⁻¹) of the cis-ONONO₂ and cis-ONONO₂_2 structures.

^a: reference (37)

		$cis-ONONO2$ ₃		
	B3LYP/	PW91PW91/	BHandHLYP/	CCSD/
	$6-311++G(3df,2p)$	$6-311++G(3df,2p)$	$6-311++G(3df,2p)$	$6-311+G(d,p)$
$NO2$ torsion	34i	32i	52i	71i
NO torsion	168	181	152	126
NO ₂ rock	202	186	228	222
$O-N(O)$ str	278	266	268	263
N-O-N bend	590	562	633	608
$NO2$ wag	654	SEARCH I 590	738	699
$O=N-O$ bend	761	717	836	787
$NO2$ bend	798	762	864	794
$O-N(O_2)$ str	892	832	1001	929
$NO2$ s-str	1310	1258 896	1425	1358
$NO2$ a-str	1649	1600	1758	1708
NO str ^e	2038	1943	2163	2023

Table3-14: Calculated Vibrational Frequencies (in cm^{-1}) of the cis-ONONO₂_3 structures.

	B3LYP/	PW91PW91/	BHandHLYP/	CCSD/	MP2/	MP2/	B3LYP/	MP2/			
		6-311++G(3df,2p) ^a 6-311++G(3df,2p) ^a 6-311++G(3df,2p) ^a 6-311+G(d,p) ^a 6-31G [*] ^b						6-311G [*] 6-31G(d) ^c 6-31G(d) ^c	$Exp.$ ^d	Exp.	$Exp.$ ^e
$NO2$ torsion	88	26	32i	84	43.6	64.4	29	31i			
NO torsion	131	135	144	130	116.3	113	140	123			
NO ₂ rock	209	191	252	252	215.1	220.6	214	205			
$O-N(O)$ str	294	289	320	349	316.1	319.4	322	310	304		310
N-O-N bend	486	424	552	545	497.1	517.6	477	489	524	564	489
$O=N-O$ bend	647	582	745	683	633.4	653.8	636	636	660	679	636
$NO2$ wag	786	746	849	774	745.3	761.4	760	751	794	782	778
$NO2$ bend	801	766	863	847	783	810.6	797	778			
$O-N(O_2)$ str	945	895	1054	990	$0925 -$	933.8	954	926	916	882	926
$NO2$ s-str	1330	1287	1444	1377	1312.8	1313.7	1353	1315	1290	1280	1315
$NO2$ a-str	1709	1686	1827	176396	1845.5	1863.9	1769	1839	1584	1576	1839
NO str ^f	1934	1850	2002	1898	1868.8	1895.5	1906	1871	1899-1889	1961	1871

Table3-15: Computational and Experimental Vibrational Frequencies (in cm⁻¹) of trans-ONONO₂.^g

^a: this work; ^b: reference (36); ^c: reference (16); ^d: reference (37); ^e: bands observed at liquid-helium temperature in oxygen matrix, reference (38); ^e: reference (39); ^f: the assignment of frequencies is from reference (36); ^g: the trans-ONONO₂ geometries of different are different, which depend on the optimized methods.

Fig3-6: Arrhenius plots and three-parameters fitting expressions for the rate constants. (a) The faster reaction is N_2O_4 to cis-ONONO₂ via i-TS2, and the lower one is N_2O_4 to trans-ONONO2 via i-TS1. \mathcal{L} 1896

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3.3 $N_2H_4 + N_2O_4$ reaction

 In the 3.2 section, we have discussed the properties of the three isomers, including $N_2O_4(D_{2h})$, trans-ONONO₂(C_s), and cis-ONONO₂(C_s) molecules. Since under real experimental conditions the combustion reaction may produce these molecules to react with the N_2H_4 molecule, the PES of N_2H_4 +trans-ONONO₂, N_2H_4 +cis-ONONO₂, and $N_2H_4 + N_2O_4(D_{2h})$ reactions should be considered. Even though these reactions are complex, which contain four nitrogen atoms, four oxygen atoms, and four hydrogen atoms, fortunately, all of the dimer reactions are on their singlet surface without spin-contamination problems unlike the monomer reaction, $N_2H_4 + NO_2$.

$3.3.1$ N₂H₄ + trans-ONONO₂ reaction and N₂H₄ + cis-ONONO₂ reaction

In this section, we consider the reaction of N_2H_4 + trans-ONONO₂ and cis-ONONO₂ molecules. The geometries of stationary points, such as reactants, intermediates, transition states, and products, in the reactions are computed by the B3LYP/ 6-311++G(3df,2p) method, as shown in Fig3-7. The single-point energies for the full potential energy surface, as presented in Fig.3-8, are calculated by G2M(CC3) instead of G2M(CC1) due to the larger number of atoms in this system. Since the trans-ONONO₂ and cis-ONONO₂ are of C_s symmetry, we make the notations of C_s -Complexes and C_s -TSs in the PES for clarity. Moreover, in order to compare the PES of $N_2H_4 + N_2O_4(D_{2h})$ reaction more easily, the energy of the most stable reactants, $N_2H_4 + N_2O_4(D_{2h})$, is taken as the reference energy in these reactions. The moments of inertia and vibrational frequencies are listed in Table3-16, and the energies of all species obtained by different computational methods are shown in Table3-17.

The N_2H_4 + trans-ONONO₂ reaction provides the lowest-energy path in all of $N_2H_4 + N_2O_4$ reactions. In the beginning, trans-ONONO₂ forms an intermediate, C_s-complex1,

with N_2H_4 molecule, as shown in Fig3-7. In order to form hydrogen bonds and decrease the energy, the N-N bond of N_2H_4 twists to make two hydrogen atoms upward to terminal oxygen atom of trans-ONONO₂. Furthermore, as we discussed the trans-ONONO₂ molecule in the previous section, the bond length of $ON-ONO₂$ is 1.621Å, and the ON group has a positive charge distribution, whereas the $ONO₂$ group has a negative electron distribution. These special properties make the $ON-ONO₂$ bond in C_s -complex1 to be much longer than the individual molecule by 0.661\AA , but the ON group still connects with the ONO₂ group. On the other hand, the attraction of ONO₂ makes the N-H bond longer than that in N₂H₄ by 0.06Å. Therefore, C_s -Complex1 has a lower energy than the reactants, N_2H_4 + trans-ONONO₂. C_s -TS1 is a six-member ring structure, and the ring is composed of the N-O-N-O atoms of trans-ONONO₂, (in which the first N belongs to the NO group,) and the N-H atoms of N₂H₄. The major motion of TS is that the ON group breaks the connection with $ONO₂$ and forms an N-N bond with N_2H_3 , and the bonding hydrogen atom transfers to ONO_2 group to form a stable nitric acid. The two doublet radicals, N_2H_3 and NO , are unstable, and the unpair electrons would prefer to decrease energy by forming the H2NN(H)NO molecule, which is stable and the process is exothermic. This molecule may decompose into many small reactive molecules, and we will discuss this decomposition reaction in the next section. Moreover, it is well-known that nitric acid, $HONO₂$, may decompose into $NO₂$ gas at high temperature, and the products from the decomposition of nitric acid, $OH + NO₂$, may react further and release more energy. The dihedral angle $[O-N-O-N]O₂$ is 160.1[°] and 154.8[°] for C_s -Complex1 and C_s -TS1, respectively, and the other angles and dihedral angles are similar. However, it is unreasonable that the energy of C_s -Complex1 is higher than C_s -TS1 by 1.17, 2.89, and 2.66 kcal/mol by the B3LYP/6-311++G(3dr,2p), CCSD(T)/6-311+G(3df,2p), G2M(CC3) methods, respectively, as shown in Table 3-17. However, the electronic energy of C_s -complex1 is lower than C_s -TS1 by 0.17 kcal/mol, and the result of IRC calculation also confirms that the energy

difference is only 0.00027 hartrees, as shown in Fig3-9. The zero-point energy (ZPE) of the C_s -complex1 is higher than that of the C_s -TS1 by 1.30 kcal/mol; therefore, we believe that the fact that the energy of the C_s -complex1 is higher than that of the C_s TS1 arises from the zero-point energy correction and computational errors. In addition, the free energy with ZPE correlation of the C_s -complex1 is higher than that of C_s -TS1 by 0.78 kcal/mol computed at B3LYP/6-311++G(3df,2p). Since the DFT calculations may have larger error in the geometry predictions than CCSD(T), the single-point calculation error would be increased based on the DFT geometries. Moreover, these structures on the major channel can be reoptimized by PW91PW91/6-311++G(3df,2p), and the geometries are similar with the results optimized by B3LYP, as presented in Fig.3-7. The moments of inertia and the frequencies are shown in Table3-18, and the relative energies are listed in Table3-19. The PW91PW91 results in energy have the same trend as these by B3LYP calculation, in which the electronic energy with ZPE correction of the C_s-TS1 is lower than that of C_s -Complex1 by 1.11 kcal/mol. However, the zero-point energy of the C_s -complex1 is higher than that of the C_s -TS1 by 2.4 kcal/mol optimized by PW91PW91/6-311++G(3df,2p). Therefore, this phenomenon arises from the zero-point energy correction and computational errors similar to those computed by B3LYP. The PESs of major channel in the trans-ONONO₂ + N_2H_4 reaction optimized by B3LYP/6-311++G(3df,2p) and PW91PW91/ 6-311++G(3df,2p) are shown in the Fig. 3-9. After all, the reaction of the major channel starts from the formation of C_s -complex1, and the barrierless hydrogen transfer via C_s -TS1 will react very fast kinetically. In order to get the correct relative energy, it may need a higher level of theory to optimize the geometries, such as the CCSD method.

In the N₂H₄ + cis-ONONO₂ reaction, there is one similar reaction path as N₂H₄ + trans-ONONO₂ reaction. The physical attraction and hydrogen bonding make N_2H_4 and cis-ONONO₂ form an intermediate, C_s -Complex3, and the structures of two molecules do not change much comparing with the structures of individual molecules, as shown in Fig3-7. The longest and weakest $ONO₂$ bond only elongates 0.02\AA , and the nearest distance between two molecules is 2.97Å for the bonding oxygen atom to the bonding hydrogen atom. That means the interaction between them is smaller than the situation in C_s -Complex1, and the energy of C_s -Complex3 is lower than N₂H₄+cis-ONONO₂ by 3.85 kcal/mol at the G2M(CC3) level. C_s -TS2 is a four-member ring structure, as shown in Fig. 3-7. In C_s -TS2, the N₂H₄ structure is similar to that in the C_s -Complex1 and C_s -TS1, and it rotates along the N-N bond to make two hydrogen atoms upward to the oxygen atom of $NO₂$. After moving over C_s-TS2 , the ONO-NO₂ bond breaks and one hydrogen atom transfer from N_2H_4 to the oxygen atom of the ONO group. This exothermic reaction produces the $H_2NN(H)NO_2$ molecule and nitrous acid, trans-HONO, which is the same products in the $N_2H_4+NO_2$ reaction. However, the energy barrier of four-member ring, C_s -TS2, is as high as 20.07 and 14.4 kcal/mol with respect to reference point and C_s -Complex3. Therefore, it is kinetically more difficult to react, comparing with the lowest-energy channel of N_2H_4 + trans-ONONO₂ reaction. For hydrogen transfer reactions involving $cis-ONONO₂$ and trans- $ONONO₂$, we notice that the weakest bond breaks as the reaction occurs. If we choose cis-ONONO₂_2 as the cis-reactant, then it would have similar transition states and products as those in the trans- $ONONO₂+N₂H₄$ reaction. Therefore, it is reasonable to not consider the other two possible structures in cis-isomer reacting with N_2H_4 . On the other hand, the imaginary frequencies of the two hydrogen transfer reaction are very small comparing the simple conventional hydrogen transfer reaction, whose value is around 1200 to 1500 1/cm, and it might be affected by other bonding or breaking motions in the ring of transition states. The effect of hydrogen bond is another important factor that affects the motion on the coordinate of reaction path.

The other two reaction channels of the $N_2H_4 + cis\text{-ONONO}_2$ reaction have similar reaction mechanisms, but the cis-ONONO₂ is in a different position related to the N_2H_4

molecule in the C_s -TS3 and C_s -TS5. These two reactions are originated from the C_s -Complex3, and they break the O-N bond to form the C_s -Complex5 and C_s -Complex7 via the C_s -TS3 and C_s -TS5, respectively. The C_s -TS3 and C_s -TS5 geometries show that the NO group of cis-ONONO₂ is on the top of the N_2H_4 molecule, and the ONO₂ group is in the middle of the N_2H_4 molecule and the NO group, which is like a sandwich structure, as shown in Fig3-7. The $NO₂$ group is tilted in both structures of C_s-TS3 and C_s-TS5 , and the lower position of oxygen atom is on the inner side and outer side of N_2H_4 for C_s -TS3 and C_s -TS5, respectively. The N_2H_4 molecules in the C_s-TS3 and C_s-TS5 have the similar geometries as those in C_s -TS1 and C_s -TS2, where the two hydrogen atoms of N_2H_4 turn upward to form the hydrogen bonds and thus decrease the system energy. In section3.1, the highest-energy path of the $N_2H_4+NO_2$ reaction has the same mechanism as the reaction channels through C_s-TS3 and C_s -TS5, and all of them have very high energy barriers. The NO_2 group is near and far away from the oxygen atom of $H_2NN(O)H_2$ in C_s-Complex5 and C_s-Complex7, respectively, due to the origins from the different geometries of transition states. Therefore, the C_s -Complex5 undergoes the hydrogen transfer reaction via C_s -TS4, which abstracts one hydrogen from the nitrogen connecting with oxygen in the $H_2NN(O)H_2$ moiety, giving C_5 -Complex6 which is composed of trans-HONO and $H_2NN(H)$ ONO molecules. On the other hand, the NO₂ group of Cs-Complex7 can also undergo a hydrogen transfer reaction from the nitrogen atom, which does not connect with oxygen in $H_2NN(O)H_2$ molecule, to produce trans-HONO + $H_2NN(H)ONO$. Finally, the C_s-Complex8, including a trans-HONO, a cis-HONO, and a cis-N₂H₂ molecule, form through C_s -TS6. However, even these two paths produces many exothermic products, but the mechanism, breaking $N-O$ bond of $NO₂$ and forming $N-O$ bond to N2H4 without hydrogen transfer, seems very difficult to occur comparing with other hydrogen-transfer channel, and it has the consistent results in both monomer and dimer reactions.

 In Table3-17, comparing with the single-point energies between $CCSD(T)/6-311+G(d,p)$ and $G2M(CC3)$ methods, it is apparent that most of the energies calculated by G2M(CC3) is lower than those by the CCSD(T) method, but they have the similar energy differences between the intermediates and transition states in the same reaction channels. Such as the channel of hydrogen transfer in the $N_2H_4 + cis-ONONO_2$, the energy barrier is 24.32 and 24.6 kcal/mol predicted by $G2M(CC3)$ and $CCSD(T)/6-311+G(d,p)$ methods, respectively. According to the heat of reaction, which is calculated by the heat of formation in experimental data⁽²³⁾, the value of $G2M(CC3)$ is very close to the experimental result similar to the monomer reaction. However, the difference between CCSD(T)/ $6-311+G(d,p)$ and experimental value is 2.46 kcal/mol, which means that the smaller basis set in CCSD(T) calculations may be incorrect and unreliable.

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Fig3-7: (a) The stationary points in the PES of trans-ONONO₂ + N_2H_4 reaction and cis-ONONO₂ + N₂H₄ reaction are optimized by B3LYP/6-311++G(3df,2p), and (b) the stationary points on the major channel of trans-ONONO₂ + N_2H_4 reaction optimized by PW91PW91 /6-311++G(3df,2p).

Fig3-8: Potential Energy Surface of trans-ONONO₂ + N₂H₄ reaction and cis-ONONO₂ + N₂H₄ reactions, whose energies are calculated by G2M(CC3) // B3LYP/6-311++G(3df,2p).

Fig3-9: The IRC calculation of C_s-TS1 is determined by B3LYP/6-311++G(3df,2p) for reverse direction. The highest point is the position of C_s-TS1, and the lowest point is approaching to the C_s-Complex1. The energy difference is 0.00027 Hartree (0.17 kcal/mol).

Fig3-10: The comparison for the major channel of trans-ONONO₂ + N₂H₄ reaction optimized by B3LYP/6-311++G(3df,2p) and PW91PW91/ 6-311++G(3df,2p).

Table3-16: Moments of inertia (I_A , I_B , I_C) and vibration frequencies of the species in trans-ONONO₂ + N₂H₄ and cis-ONONO₂ + N₂H₄ reactions

computed at B3LYP/6-311++G(3df,2p).

Table3-17: Relative energies of species in trans-ONONO₂ + N_2H_4 reaction and cis-ONONO₂

		B3LYP/	CCSD(T)/	
	ZPE ^b	6-311++G(3df,2p) ^c 6-311+G(d,p) ^c		G2M(CC3)
$N_2O_4 + N_2H_4$	48.02	-522.173728	-520.93814	-521.3804132
trans-ONONO ₂ + N_2H_4	46.67	10.21	6.1	5.85
$cis-ONONO2 + N2H4$	46.46	12.51	9.63	9.52
complex1	48.45	-0.37	-3.07	-4.53
complex2	49.09	-14.5	-18.75	-20.25
complex3	47.28	10.9	5.3	5.67
complex4	48.84	-17.24	-23.89	-23.79
complex5	49.03	13.11	9.51	9.77
complex6	47.75	-1.98	-13.27	-11.33
complex7	48.9	16.93	11.8	8.96
complex8	45.5	-13.72	-25.96	-23.03
$H2NN(H)NO + HONO2$	47.88	-12.65	-13.95	-15.57
$H2NN(H)NO2 + trans-HONO$	47.93	-15.26	-19	-19.73
$H_2NN(H)$ -ONO + trans-HONO	46.42	3.31	-5.39	-3.83
$trans-HONO + cis-HONO + cis-N2H2$	42.73	-4.5	-14.72	$-12.19 (-12.26)^d$
TS1	47.12	-1.54	-5.96	-7.19
TS ₂	47.98	21.52	21.25	20.07
TS3	47.26	66.98	62.27	60.9
TS4	46.29	13.15	9.02	10.16
TS5	47.47	67.26	64.06	60.78
TS6	45.39	33.33	28.36	27.49

 $+$ N₂H₄ reaction predicted at various theoretical levels.^{a}

^a: The relative energy (kcal/mol) is calculated with the energy of N_2O_4 (D_{2h})+ N_2H_4 as reference, whose total energy unit is hartree/molecule.

^b: The ZPE is determined by B3LYP/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every species.

^c: The energies are including single-point energies, based on geometries of B3LYP/6-311++G(3df,2p), and ZPE.

^d: The heat of reaction in the experimental result is calculated by species of the reactants and products, whose heat of formation are from the reference (23).

Table3-18: Moments of inertia (I_A, I_B, I_C) and vibration frequencies of the species in the major channel of trans-ONONO₂ + N₂H₄ reaction computed at PW91PW91/6-311++G(3df,2p).

	ZPE ^b	PW91PW91	CCSD(T)	$G2M(CC3)^c$
		$/6 - 311 + G(3df,2p)$	$/6 - 311 + G(d,p)^c$	
$N_2O_4 + N_2H_4$	46.51	-522.0717000000	-520.9408055	-521.3819786
trans-ONONO ₂ +N ₂ H ₄	45.23	14.74	6.18	5.88
C_s -Complex1_PW91PW91	47.11	-2.17	-1.48	-3.27
C_s -Complex2_PW91PW91	47.51	-10.25	-17.61	-19.76
C_s -TS1-new PW91PW91	44.71	-3.28	-7.44	-8.66
$H_2NN(H)NO+HONO_2$	46.57	-6.58	-12.37	-14.56

Table3-19: Relative energies of species in the major channel of the trans-ONONO₂ + N₂H₄ reaction at various theoretical levels. ^a

^a: The relative energy (kcal/mol) is calculated with the energy of N_2O_4 (D_{2h})+ N_2H_4 as reference, whose total energy unit is hartree/molecule.

^b: The ZPE is determined by PW91PW91/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every species.

^c: The energies are including single-point energies, based on geometries of PW91PW91/6-311++G(3df,2p), and ZPE.

3.3.2 Decomposition of H2NN(H)NO molecule

The H₂NN(H)NO molecule is the product of the lowest-energy path in the N₂H₄ + isomeric N_2O_4 reactions, as discussed in the previous section. This molecule can be formed the combination of NO and N_2H_3 radicals, and we want to know whether there is another lower-energy path to produce highly reactive products in the decomposition reaction. The optimized geometries of stationary points, such as intermediates, transition states, and product molecules, in the reaction are determined at the B3LYP/ 6-311++G(3df,2p) level, as shown in Fig3-11. Further, the full potential energy surface of decomposition reaction is represented in Fig. 3-12, and the energies of species are predicted by the G2M(CC1) single-point calculation. Since this is the decomposition reaction of $H_2NN(H)NO$, we add a notation d in front of the complexes and TSs for easy recognition. The moments of inertia and vibrational frequencies of all species are listed in Table3-20, and the energies by G2M(CC1), CCSD(T)/6-311+G(d,p), and $CCSD(T)/6-311++G(3df,2p)$ are shown in Table 3-21.

The $H_2NN(H)NO$ molecule is a stable structure, and we separate $H_2NN(H)NO$ into three groups, including NH2, NH, and NO for conveniently explaining geometries. Since the two hydrogen atoms of $NH₂$ turn upward to NO tail, the hydrogen bonding makes molecule more stable. However, if the molecule undergoes a dissociation reaction to produce the N_2H_3+NO radicals, the hydrogen bonding will retard this reaction. Therefore, the possible path to dissociate into two radicals may be that $H_2NN(H)NO$ molecule first undergoes $NH₂$ rotation, to form d-Complex1 via d-TS1, turning the two H atoms into the opposite direction, and the energy of d-Complex1 raises as the hydrogen bonding disappears. Furthermore, d-Complex1 undergoes the dissociation reaction producing N_2H_3 and NO. The energy barrier of d-TS1 is 6.28 kcal/mol, which is the same as d-Complex1 at the G2M(CC1) level. At

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 $CCSD(T)/6-311++G(3df,2p)$, it is 6.82 kcal/mol which is higher than d-Complex1 by 0.54 kcal/mol. Moreover, the dissociation from d-Complex1 to N_2H_3+NO radicals needs 21.55 and 24.06 kcal/mol by G2M(CC1) and CCSD(T), respectively. Comparing the other channels in the H₂NN(H)NO molecule decomposition, the channel producing the N₂H₃+NO radicals is most likely with the lowest-energy path.

Another path is the hydrogen transfer from $NH₂$ group to the oxygen atom of the NO group in the $H_2NN(H)NO$ molecule via d-TS2; the energy barrier is only 18.75 and 19.17 kcal/mol with G2M(CC1) and CCSD(T)/6-311++G(3df,2p) methods, respectively. The d-TS2 has a five-member ring structure for hydrogen transfer, which is the major motion in this path, and the imaginary frequency is 1395 cm⁻¹ as shown in Table3-20. However, the N-N bond between the NO and NH group is as short as 1.279Å with an N=N double bond character; the dissociation of d-Complex2 to HON+cis-N2H2 requires very high energy, 62.45 kcal/mol above d-Complex2. In addition, the unstable HON molecule raises the system energy. Therefore, the formation of d-Complex2 does not lead to another lower-energy path for the decomposition of $H_2NN(H)NO$. Even though the energy of initial hydrogen transfer is low, the high dissociation energy makes this reaction channel be very hard to occur kinetically. On the other hand, the d-Complex2 may undergo a hydrogen transfer reaction via d-TS6, and the d-complex6 dissociates to highly active products, $N_3H_2 + OH$ radicals, without a barrier. However, the energy barrier of the hydrogen transfer via d-TS6 is 37.6 kcal/mol computed at $G2M(CC1)$ level. Since the N₃H₂ radical is highly unstable, the dissociation energy from d-Complex5 to N_3H_2 + OH is 58.3 kcal/mol. Therefore this channel seems to be difficult to occur kinetically.

 The third reaction is also the hydrogen transfer via d-TS3, whose energy barrier is as high as 43.79 and 44.18 kcal/mol at the G2M(CC3) and CCSD(T)/6-311++G(3df,2p) levels, respectively, and the hydrogen atom is from nitrogen atom of the NH group to that of NO group to form d-Complex3. The d-Complex3 is as stable as the $H_2NN(H)NO$ molecule, since this complex also obeys by the Octet rule. However, it needs very high energy to dissociate the d-Complex3 into HNO and H_2NN molecules, similar to d-Complex2. The dissociation energy is 53.01 kcal/mol with respect of the d-Complex3, and it is too high to happen. The product, H_2NN , is an unstable molecule, which increases the system energy, therefore, we seek another reaction channel from d-Complex3 to produce the N_2H_2 and HNO. However, in order to form the d-Complex4, it should overcome d-TS4, whose energy barrier is 63.16 kcal/mol at the G2M(CC1) level. Even though d-TS5 is only higher than d-Complex4 by 8.32 kcal/mol, the final products HNO+trans-N₂H₂ are still controlled by the high barrier of d-TS4. In conclusion, these decomposition reaction channels cannot compete with the dissociation to NO+N2H3 radicals kinetically. 1896

In the present case, the $CCSD(T)/6-311++G(3df,2p)$ method has been used for comparison with the values of G2M(CC1), since the total number of atom is only seven. The energy differences between CCSD(T)/6-311++G(3df,2p) and G2M(CC1) methods are smaller than 1 kcal/mol for all species except for $NO+N₂H₃$, whose G2M value is lower than $CCSD(T)$ by 2.55 kcal/mol. The reason causing the larger energy difference for $NO+N₂H₃$ may be the spin contamination on the doublet molecules, since the G2M method use the projection method of MPn and higher level corrections to correct the problem of spin contamination. The other species in this decomposition reaction are all singlet, so the spin-contamination does not affect the energies of G2M and CCSD(T) methods. Therefore, the G2M(CC1) can generally provide good predictions as CCSD(T)/6-311++G(3df,2p) does, and it can also save the

computational resource. On the other hand, comparing with the CCSD(T)/6-311++G(3df,2p) and G2M(CC1) methods, the CCSD(T)/6-311+G(d,p) method underpredicts the energies of product molecules, and there is no systematic correlation for complexes and transition states.

Fig3-11: The stationary points in the PES of H2NN(H)NO decomposition are optimized by B3LYP/6-311++G(3df,2p)

Fig3-12: Potential Energy Surface of H₂NN(H)NO decomposition, whose energies are calculated by G2M(CC1) // B3LYP/6-311++G(3df,2p).

Table3-20: Moments of inertia (I_A, I_B, I_C) and vibration frequencies of the species in $H_2NN(H)NO$ decomposition computed at

Table3-21: Relative energies of species in H₂NN(H)NO decomposition computed at various theoretical levels.^a

	ZPE ^b	B3LYP	CCSD(T)		
		$/6 - 311 + C(3df,2p)^c$	$/6 - 311 + G(d,p)$	$/6 - 311 + G(3df, 2p)^c$	$G2M(CC1)^c$
$H_2NN(H)NO$	31.3	-151368.1213	-150999.8933	-151090.8409	-151137.0469
d -complex 1	31.01	5.57	6.02	6.32	6.28
d -complex 2	31.89	14.85	16.05	14.22	13.8
d -complex 3	32.42	-1.09	1.45	0.06	-0.37
d-complex4	31.57	28.16	34.29 6	30.64	29.82
d -complex 5	28.82	25.51	TATITUDE 25.13	28.29	28.01
d-complex6	31.7	5.74	5.88	6.02	5.89
N_2H_3+NO	27.56	31.07	26.48	30.38	27.83
$HON + cis-N2H2$	25.76	78.02	73.68	76.19	76.25
$HNO+H2NN$	25.79	53.27	49.31	52.76	52.69
$HNO+trans-N2H2$	26.51	32.83	29.37	33.43	33.31
N_3H_2+OH	25.72	53.62	56.52	60.49	64.16
$d-TS1$	30.79	5.96	6.9	6.86	6.28
$d-TS2$	29.12	18.76	20.05	19.17	18.75

^a: The relative energy (kcal/mol) is based on the energy of N_2O_4 (D_{2h})+ N_2H_4 as reference, whose energy unit is hartree/molecule.

^b: The ZPE is determined by B3LYP/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every species.

^c: The energies are including single-point energies, based on geometries of B3LYP/6-311++G(3df,2p), and ZPE.

3.3.3 $N_2H_4 + N_2O_4 (D_{2h})$ reaction

We consider the reaction of $N_2O_4(D_{2h})$ and N_2H_4 in this section. Since high-symmetry N_2O_4 (D_{2h}) molecule is less reactive than the monomer NO_2 , the reaction channels in $N_2H_4+N_2O_4$ (D_{2h}) are not as many intuitively. The products are the same as those in the previous reactions, such as $H_2NN(H)NO_2$, $H_2NN(H)ONO$, NO_2 , trans-HONO, cis-HONO, and N₂H₃ radical. All geometries of species in this potential energy surface are optimized at the B3LYP/6-311++G(3df,2p) level, and the details of bond lengths and angles are shown in Fig3-13. The potential energy surface is based on the single-point energies determined by G2M(CC3) in Fig3-14. It is easier to recognize the species in PES from other reactions, if we add a notation D_{2h} in front of the complexes and TSs. The information, including the moments of inertia and vibrational frequencies, are listed in Table3-22; moreover, the energies by different computational methods with the zero-point energy (ZPE) of B3LYP/6-311++G(3df,2p) are compared in Table3-23

The $N_2O_4(D_{2h})$ and N_2H_4 form an intermediate, D_{2h} -Complex1, due to the physical attraction and hydrogen bonding, and the energy is lower than the reactants by 6.98 kcal/mol at the G2M(CC3) level. Basically the N_2O_4 and N_2H_4 molecules in the D_{2h} -Complex1 have the same geometries as those in the individual molecules, the nearest distance between these two molecules is 2.662Å. There are three channels starting from D_{2h} -Complex1 in the PES, and the lowest-energy path is to produce the $H_2NN(H)NO_2$ and trans-HONO molecules via D_{2h} -TS1. The structure of five-member ring in D_{2h} -TS1 connects the two nitrogen and one oxygen atoms of N_2O_4 with one nitrogen atom and one hydrogen atom of N_2H_4 , as in Fig.3-13. The N-N bond of N_2O_4 twists to make the planes of two NO_2 group be perpendicular, and the nitrogen atom of the $NO₂$ group connects with the one of nitrogen atoms of the $N₂H₄$ molecule as the two oxygen atoms is parallel with the N-N bond of N_2H_4 upwardly. The

structure of N_2H_4 in the $D_{2h}TS1$ makes two hydrogen atoms point upward to one oxygen atom, and it forms the hydrogen bonds and reduces the system energy as in C_s -TS1 and C_s -TS2. The major motion of D_{2h} -TS1 is the hydrogen transfer to form the trans-HONO with the concerted formation of $H_2NN(H)NO_2$. The energy barrier is 14.16 and 21.14 kcal/mol above the reactants and D_{2h} -Complex1 at the G2M(CC3) level. The products $H_2NN(H)NO_2$ and trans-HONO, from D_{2h} -Complex2, have appeared in the N_2H_4 +cis-ONONO₂ reaction; therefore, we will discuss further about the decomposition reaction of $H_2NN(H)NO_2$ molecule in the next section. The D_{2h} -TS4 has the a six-member ring structure, as shown in Fig.3-13. The hydrogen transfer reaction from N_2H_4 to one of the NO_2 groups is accompanied by the formation N-O bond between N_2H_4 and the other NO₂ group, and the breaking of the N-N bond of N_2O_4 , producing trans-HONO and $H_2NN(H)ONO$. However, the energy barrier is higher than D_{2h} -TS1 by 6.7 kcal/mol. Comparing with the structure between two transition states, it is apparent that the D_{2h} -TS1 has tight connection with each element in the ring, whereas the ring structure of D_{2h} -TS4 is relatively loose. The N-N bond length of the N₂O₄ molecule is 2.257 and 2.672 Å in D_{2h} -TS1 and D_{2h} -TS4, respectively. The motion of breaking the N-N bond in D_{2h} -TS1 is more drastic than that in D_{2h} -TS4, which means that it needs to elongate the N-N bond before reaching the D_{2h} -TS4. Therefore, the barrier of D_{2h} -TS3 is higher than the D_{2h} -TS1. On the other hand, the products of the D_{2h} -TS4 are $H_2NN(H)ONO$ and trans-HONO molecules, dissociated from D_{2h} -Complex5, have also appeared in the cis-ONONO₂+N₂H₄ reaction, we will not discuss the decomposition of the H₂NN(H)ONO molecule due to the higher energy for its formation.

 D_{2h} -TS3 is the transition state which is not originated from the D_{2h} -Complex1 but directly from the reactants, N_2H_4 and N_2O_4 , attributable to the unique structure of the D_{2h} -TS3, which is the ball-like geometries with C_2 symmetry, and it is difficult to achieve this structure from other intermediates. Every oxygen atoms of N_2O_4 molecule connects with the hydrogen

atoms of N_2H_4 molecule without repetition, and the dihedral angle of four nitrogen atoms is 4° , which means nearly on one plane. Due to the C_2 symmetry, the distances between hydrogen atom and oxygen atom on the diagonal position are the same. One pair of N-O distance is short as 1.836Å, whereas the other pair of N-O distance is long as 2.406Å. This structure indicates that the two hydrogen transfer reaction occur concurrently in the D_{2h} -TS3 with the breaking N-N bond of the N_2O_4 molecule, and its energy barrier is 21.37 and 25.07 kcal/mol obtained at G2M(CC3) and CCSD(T)/6-311+G(d,p) levels. The reaction via the D_{2h} -TS3 produces the D_{2h} -Complex4, including two cis-HONO and one trans- N_2H_2 molecules, with 11.8 kcal/mol exothermally.

The last reaction channel in the $N_2H_4 + N_2O_4(D_{2h})$ reaction is the transfer of only one hydrogen atom to an oxygen atom of N_2O_4 via D_{2h} -TS2, whose geometry is shown in Fig3-13. The seven-member ring is constructed by the H-N-N-N atoms of N_2H_4 and the O₂N group of N_2O_4 molecule; D_{2h} -TS2 has the C_1 symmetry. The distance between oxygen and hydrogen atoms on the side not being transferred is 2.255 Å, and the connection is built up by the hydrogen bond. On the other side of the seven-member ring, the hydrogen atom is 1.515Å far from the nitrogen atom of N₂H₄ and much closer to the oxygen atom of N₂O_{4,} 1.062 Å. The position of hydrogen atom in D_{2h} -TS2 is different comparing with the other transition states of hydrogen transfer, which is much closer to the bonding N atom of N_2H_4 and far away from the N or O atoms of N_2O_4 isomers. Therefore, it is believed that the high energy barrier predicted by B3LYP/6-311++G(3df,2p) is reasonable, since the hydrogen atom needs to elongate the N-H bond by raising energy. However, the prediction of CCSD(T)/6-311+G(d,p) and G2M(CC3) methods are very low, which is the contrary result to that of B3LYP, as shown in Table3-23. The IRC calculation confirms the large difference of energy between D_{2h} -Complex1 and D_{2h} -TS2. Therefore, we assume the strange results in CCSD(T) and G2M(CC3) single-point energy calculations are caused by the incorrect prediction in the

electronic energy instead the geometry optimized by B3LYP/6-311++G(3df,2p). Since the G2M methods are based on the correction with $CCSD(T)/6-311G(d,p)$, it is understandable that the G2M and CCSD(T) have problems at the same time. On the other hand, the D_{2h} -Complex3, composed of a N₂H₃ radical and cis-HONO molecule, forms with the breaking N-N bond of N_2O_4 after passing over the D_{2h} -TS2. The total energy of D_{2h} -Complex3 and NO₂ should be lower than that of D_{2h} -TS2, therefore, it is another proof that the single-point energies of CCSD(T) and G2M are incorrect.

In Table 3-23, comparing with the energies determined by $CCSD(T)/6-311+G(d,p)$ and G2M(CC3), it is difficult to summarize a systematic relationship. Most of the energies at $CCSD(T)/6-311+G(d,p)$ level is lower than those at $G2M(CC3)$, but it has a opposite relationship in transition states. Therefore, the difference of intermediate and transition states at CCSD(T) is larger than those at G2M. This is not consistent with the relationship in section3.3.1. Moreover, if we compare the heat of reaction with experimental results, it is apparent that the G2M(CC3) performs well for the production of cis-N₂H₂+ 2 cis-HONO only, whereas the $CCSD(T)/6-311+G(d,p)$ performs bad at both cases. Therefore, it is very important to decide which lower single-point energy computation can perform well for this larger system, and we will discuss this topic in section 3.3.5.

Observing the full PES of N_2H_4 with N_2O_4 isomers, it is consistent that all of the complexes passing over the TSs, including Cs-Complex2, 4, 6, 8 and D_{2h} -Complex2, 3, 4, 5, still need high energy to separate the product molecules. The dissociation energy of these complexes are 3~8 kcal/mol for two-molecular cases and 11~14 kcal/mol for three-molecular cases at the G2M(CC3) level. This phenomenon of high complexation energies is caused by the strong hydrogen bonds as appears in the $NO₂$ reaction, discussed in section 3.1. Even though these dissociation energies from complexes to molecules are high, most of the energies of final products are lower than the reactants, $N_2H_4 + N_2O_4$; they are all formed exothermically.

Fig3-13: The stationary points in the PES of N_2O_4 (D_{2h}) + N_2H_4 reaction are optimized by B3LYP/6-311++G(3df,2p)

G2M(CC3)//B3LYP/6-311++G(3df,2p) $N_2O_4(D_{2h})+N_2H_4$ **Reaction**

Fig3-14: Potential Energy Surface of the N₂O₄ (D_{2h}) + N₂H₄ reaction, whose energies are calculated by G2M(CC3) // B3LYP/6-311++G(3df,2p).

Table3-22: Moments of inertia (I_A, I_B, I_C) and vibration frequencies of the species in the N₂O₄ (D_{2h}) + N₂H₄ reaction computed at

B3LYP/6-311++G(3df,2p).

	ZPE ^b	B3LYP/	CCSD(T)/	$G2M(CC3)^c$	ΔH_{Exp}^d
		$6-311++G(3df,2p)$	$6-311+G(d,p)^c$		
$N_2O_4 + N_2H_4$	48.02	-522.173728	-520.938139	-521.3804132	
D_{2h} -Complex1	48.91	-3.03	-7.34	-6.98	
D_{2h} -Complex2	49.11	-17.74	-24.86	-24.94	
D_{2h} -Complex3 + NO ₂	39.04	3.73	2.18	8.28	
D_{2h} -Complex4	45.62	-16.87	$1117 - 29.36$	-26.26	
D_{2h} -Complex5	47.75	-1.98	-13.27	-11.33	
$H_2NN(H)NO_2+trans-HONO$	47.93	-15.26	-19	-19.73	
$cis-N2H2+2 cis-HONO$	42.69	-3.96	-13.66	-11.75	-11.75
$H_2NN(H)ONO+trans-HONO$	46.42	3.31	-5.39	-3.83	
trans-HONO+ N_2H_3 +NO ₂	42.92	13.94	12.64	19.05	15.94
D_{2h} -TS1	48.27	12.82	1896.25	14.16	
D_{2h} -TS2	44.24	38.18	-9.27	1.16	
D_{2h} -TS3	45.98	TAIL 23.67	25.07	21.37	
D_{2h} -TS4	43.32	36.57	19.94	20.86	

Table 3-23: Relative energies of species in N_2O_4 (D_{2h}) + N_2H_4 reaction computed at various theoretical levels. ^a

^a: The relative energy (kcal/mol) is taken the energy of N_2O_4 (D_{2h})+ N_2H_4 as reference, whose energy unit is hartree/molecule.

^b: The ZPE is determined by B3LYP/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every specie.

^c: The energies are including single-point energies, based on geometries of B3LYP/6-311++G(3df,2p), and ZPE.

^d:The heat of reaction in the experimental result is calculated by species of the reactants and products, whose heat of formation are from the reference (23).

3.3.4 Decomposition of $H_2NN(H)NO_2$ molecule

The $H_2NN(H)NO_2$ molecule is the product of lowest-energy path via D_{2h} -TS1 in the $N_2H_4+N_2O_4(D_{2h})$ reaction; it also appears in the lowest-energy path via C_s-TS2 in the $N_2H_4 + cis-ONONO_2 (C_s)$ reaction. In this section, we denote this molecule separately into three groups, including NH_2 , NH, and NO_2 , for describing the geometries in the PES conveniently. This molecule can be formed by the combination of $NO₂$ and $N₂H₃$ radicals. The products $H_2NN(H)NO_2$ + trans-HONO are energetically more stable than that of $H_2NN(H)NO + HONO_2$. However, the oxygen atoms of NO_2 group may provide more possibilities to generate the active and exothermic products in different channels of the decomposition reaction. All geometries of the optimized species, such as intermediates, transition states, and products, are shown in Fig3-15. To distinguish the complexes and TSs in this reaction, we make a notation "d2" in front of them. The PES represents all decomposition channels in Fig.3-16, and the relative energies of the species are determined by G2M(CC1) method. Moreover, the moments of inertia and vibrational frequencies of the species are listed in Table3-24, and the energies calculated by different methods as shown in Table3-25.

Since $H_2NN(H)NO_2$ is the most stable configuration on the PES, all of reaction channels start from this molecule, and there is no other configurations of the molecule appearing in the PES. The first decomposition path is to form the $NO₂$ and $N₂H₃$ radicals directly, with this dissociation energy of 38.23 kcal/mol at the G2M(CC1) level. Unlike the decomposition reaction of $H_2NN(H)NO$, whose dissociation energy is 27.86 kcal/mol, the high decomposition energy for $NO₂$ and $N₂H₃$ provides the possibility of another reaction channels to occur. The lowest-energy path is to form the trans-HONO and trans- N_2H_2 via d2-TS1, with a five-member ring structure. The ring connects the three nitrogen atoms, one oxygen atom, and one hydrogen atom of the $NH₂$ group, and the motion along the reaction coordinate is one hydrogen transfer reaction by breaking the N-N bond connecting $NO₂$ and NH groups. In order to help the hydrogen transfer reaction, the N-N bond connecting $NO₂$ and NH group elongate into 2.528Å with the N-N-N angle and N-N-O angle closely perpendicular. The energy barrier of the d2-TS1 is 26.6 kcal/mol at the G2M(CC1) level, and the following $d2$ -Complex1 could dissociate into trans-HONO and trans-N₂H₂.

 The d2-TS2 also has a five-member ring structure, with the same composition as $d2-TS1$; however, the N-N bond connecting $NO₂$ and NH groups shorten instead of elongating as d2-TS1. The oxygen atom of the $NO₂$ group is not on the top the nitrogen atom of $NH₂$ group, therefore, the hydrogen atom needs to get close to the oxygen by elongating the N-H to 1.610Å. The energy of hydrogen transfer is as high as 36.64 kcal/mol, and it produces the unstable intermediate d2-Complex3, whose energy is higher than d2-TS2 by 0.16 and 0.24 kcal/mol at the $G2M(CC1)$ and $CCSD(T)/6-311++G(3df,2p)$ levels, respectively. We believe that the minor difference is due to the calculation error of electronic energy for the unstable $d2$ -Complex3. In order to break the N-N bond connecting NO₂ and NH groups, $d2$ -Complex3 needs to cross the 4.93 kcal/mol barrier through d2-TS3 to form the d2-Complex4 of composing trans-HONO and cis-N₂H₂ molecules. The products are similar to those of d2-TS1; however, the highest energy barrier at d2-TS2 is higher than d2-TS1 by 10.04 and 9.56 kcal/mol at the G2M(CC1) and CCSD(T)/6-311++G(3df,2p) levels.

 The other hydrogen transfer channel goes through d2-TS4 to form d2-Complex4, and it is an intramolecular hydrogen transfer from the NH group to the oxygen atom of the $NO₂$ group. The energy barrier is high for this kind of intramolecular transfer, which is 37.8 and 38.07 kcal/mol by G2M and CCSD(T) methods. The product intermediate, d2-Complex4, is stable; however, the dissociation energy to form H_2NN and trans-HONO would be very high, as in the H2NN(H)NO case. Therefore, the d2-Complex4 can undergo another intramolecular hydrogen transfer from NH_2 group to the nitrogen atom in the middle of the molecule. Expectedly, the d2-TS5 creates a very high energy barrier, which is 69.38 kcal/mol above d2-Complex4. Even though the subsequent reaction, which is passing via d2-TS6 with 0.22kcal/mol height to form cis-HONO and trans- N_2H_2 molecules, has only minor barrier, this reaction channel cannot happen readily.

 Finally, there is another high-barrier path via the d2-TS7, whose energies are 109.44 and 111.24 kcal/mol higher than $H_2NN(H)NO_2$ molecule by G2M and CCSD(T) methods. The structure of d2-TS7 is of four-member ring, composing of three nitrogen atoms and one oxygen atom, and the original N-O bond of $NO₂$ breaks as the formation of new N-O bond with the $NH₂$ group. This phenomenon is consistent with the channel 1-4 in the monomer reaction, which has a very high barrier comparing with other hydrogen transfer reactions. After passing through d2-TS7, there are two possibilities to react further. One possibility is that d2-Complex7 undergoes the dissociation reaction to form H2NO and HNNO molecules by breaking the longest N-N bond, which is 1.500Å. The other possibility is to produce the HNO and HNN(H)O molecules via d2-TS8, whose barrier is 11.86 kcal/mol at the G2M(CC1) level. The d2-TS8 is of four-member ring, which includes the three nitrogen atoms and one hydrogen atom; the hydrogen transfer from the H₂NO group to the nitrogen of the NO group as the longest N-N bond in d2-Complex7 breaks. Even though the $HNO + HNN(H)O$ molecules are more stable than H_2NO and $HNNO$ molecules, the energy barrier of d2-TS8 is higher than the dissociation energy. However, these two reaction paths are very hard to occur kinetically due to the extremely high energy barrier of d2-TS7.

 In Table3-25, the difference between those determined by CCSD(T) /6-311++G(3df,2p) and G2M(CC1) are less than 1 kcal/mol. However, the energies calculated by CCSD(T) /6-311+G(d,p) have no systematic correlation with G2M(CC1). The $CCSD(T)/6-311+G(d,p)$ energies of some of the species are lower than $G2M(CC1)$ by over 3 kcal/mol, whereas some are higher than those by G2M(CC1) by 2~4 kcal/mol. This non-systematic relationship appears in all of the $N_2H_4 + N_2O_4$ isomeric reactions, therefore, the single-point energies calculated by the CCSD(T)/6-311+G(d,p) methods are again not reliable. In the next section, we will discuss the heats of reaction more precisely.

Fig3-16: Potential Energy Surface of H₂NN(H)NO₂ decomposition, whose energies are calculated by G2M(CC1) // B3LYP/6-311++G(3df,2p).

Table 3-24: Moments of inertia (I_A, I_B, I_C) and vibration frequencies of the species in H2NN(H)NO2 decomposition computed at B3LYP/6-311++G(3df,2p).

Species	or Moments of inertia	Vibrational Frequency v_i (cm ⁻¹)
Transition States $I_i(a.u)$		
		173, 313, 330, 498, 590, 790, 795, 851, 976, 1236,
$H_2NN(H)NO_2$	155.4, 394.6, 534.8	1315, 1367, 1430, 1663, 1705, 3472, 3562, 3577
		75, 84, 151, 180, 226, 301, 699, 894, 916, 1340,
$d2$ -Complex1	131.9, 869.9, 1001.8	1359, 1479, 1600, 1663, 1751, 3262, 3302, 3351
d 2-Complex2	156.1, 368.8, 523.3	161, 296, 395, 505, 553, 598, 749, 777, 899, 1118,
		1204, 1364, 1446, 1553, 1696, 2976, 3499, 3529
d 2-Complex3	61.5, 1229.1, 1290.6	27, 49, 121, 126, 219, 239, 701, 890, 920, 1276,
		1357, 1464, 1553, 1668, 1744, 3163, 3236, 3397
d 2-Complex4	153.9, 387.9, 539.8	290, 347, 371, 394, 533, 643, 666, 752, 974, 1134,
		1286, 1329, 1393, 1600, 1700, 3458, 3626, 3734
d 2-Complex5	165.3, 392.0, 546.0	152, 248, 315, 413, 460, 590, 637, 907, 916, 1037,
		1256, 1343, 1474, 1529, 1540, 3399, 3528, 3695
d2-Complex6	179.2, 670.6, 849.8	82, 129, 186, 191, 238, 362, 713, 958, 997, 1344,
		1356, 1471, 1599, 1662, 1667, 3089, 3258, 3303
d2-Complex7	92.3, 639.0, 664.8	110, 225, 337, 401, 621, 696, 803, 1031, 1132, 1205,
		1316, 1396, 1454, 1621, 1644, 3196, 3250, 3405
d 2-Complex8	123.7, 1093.3, 1217.0	22, 52, 111, 114, 177, 318, 684, 908, 1137, 1270,
		1426, 1530, 1553, 1621, 1687, 2971, 3263, 3406
$d2-TS1$	144.5, 598.0, 726.4	375i, 155, 240, 250, 349, 431, 778, 822, 1063, 1141,
		1277, 1483, 1553, 1567, 1693, 2613, 3454, 3488
$d2-TS2$	153.4, 366.7, 517.2	274i, 282, 426, 540, 566, 581, 767, 881, 944, 1100,
		1186, 1337, 1447, 1542, 13663, 2565, 3499, 3503
$d2-TS3$	161.2, 403.2, 554.6	552i, 203, 284, 449, 568, 686, 719, 767, 853, 983, 1293,
		1328, 1413, 1478, 1623, 3254, 3387, 3417
$d2-TS4$	168.6, 379.6, 538.3	1847i, 102, 195, 309, 657, 744, 750, 814, 1005, 1012,
		1232, 1302, 1323, 1606, 1669, 2275, 3451, 3539
$d2-TS5$	158.4, 400.2, 552.3	1604i, 253, 256, 313, 475, 505, 628, 661, 863, 956,
		1114, 1259, 1317, 1412, 1622, 2672, 3369, 3738
$d2-TS6$	168.1, 403.9, 547.8	374i, 192, 282, 336, 449, 539, 611, 834, 880, 1034,
		1261, 1307, 1452, 1509, 1530, 3272, 3462, 3687
$d2-TS7$	167.8, 340.1, 428.1	1250i, 103, 425, 503, 608, 664, 692, 838, 885, 1022,
		1046, 1198, 1319, 1466, 1600, 3393, 3423, 3576

Transition ZPE^b Species or		B3LYP/	CCSD(T)/	CCSD(T)/	
States		6-311++G(3df,2p) 6-311+G(d,p) ^c		$\frac{6\text{-}311\text{++G}(3\text{df},2p)}{6\text{-}2M(CC1)^c}$	
$H_2NN(H)NO_2$	35.23	-316.432294	-315.6739897	-315.8661044	-315.9584804
complex1	32.36	-0.27	-9.44	-4.44	-4.29
complex2	33.39	35.35	38.84	37.24	36.8
complex3	31.67	4.6	-3.45	0.95	1.02
complex4	34.11	12.59	4.6	4.28	4.13
complex5	33.51	34.63	34.05	34.35	33.4
complex6	32.36	-0.2	-8.63	-4.4	-4.09
complex7	34.08	37.21	35.97	36.98	36.66
complex8	31.81	25.6	18.43	22.04	21.97
$NO2+N2H3$	30.26	28.66	30.57	34.29	38.23
trans-HONO+ trans- N_2H_2	30.48	5.23	9.97	6.8	6.79
trans-HONO+H ₂ NN	29.45	25.68	29.9	26.13	26.17
trans-HONO+cis- N_2H_2	30.07	10.23	31.61	7.33	7.29
cis -HONO+trans-N ₂ H ₂	30.44	5.77	2.62	7.16	7.28
$H2NO+HNNO$	29.21	34.05	40.46	43.34	46.9
HNN(H)O+HNO	30.52	28.59	22.56	26.27	26.05
TS1	31.96	23.37	24.93	27.44	26.6
TS ₂	32.65	34.67	38.24	37	36.64
TS3	32.46	41.73	42.06	43.16	42.44
TS4	31.43	37.21	39.17	38.07	37.8
TS5	30.65	77.48	74.81	74.19	73.51
TS6	32.36	34.18	32.95	34.13	33.13
TS7	32.54	112.89	111.53	111.24	109.44
TS8	30.03	48.82	49.88	52.61	52.42

Table3-25: Relative energies of species in $H_2NN(H)NO_2$ decomposition computed at various

theoretical levels.^a

^a: The relative energy (kcal/mol) is based on the energy of $H_2NN(H)NO_2$ as reference, whose energy unit is hartree/molecule.

^b: The ZPE is determined by B3LYP/6-311++G(3df,2p) level, and the energy unit is kcal/mol for every specie.

^c: The energies are including single-point energies, based on geometries of B3LYP/6-311++G(3df,2p), and ZPE.

3.3.5 The single-point energies in $N_2H_4 + N_2O_4$ isomeric reactions

 In Table3-26, the energies of the reactant and product species predicted by different computational methods are listed. The heats of reaction can be easily calculated with the heats of formation for reactants and products, and the difference between experimental and computational values is the way to determine whether a computational method performs well in this system or not. In Table3-27, the average differences in heat of reaction on monomer reactions are -0.41, 0.2, -0.33, and -0.34 kcal/mol by $CCSD(T)/6-311+G(d,p)$, CCSD(T)/6-311++G(3df,2p), G2M(CC3), and G2M(CC1) methods, respectively. Although, the $CCSD(T)/6-311+G(d,p)$ is the worst, the difference between the errors computed by the CCSD(T) methods is only 0.6 kcal/mol. On the other hand, the G2M methods perform well and similarly. For the $N_2H_4 + N_2O_4$ reaction, which includes more number of molecules, the average difference between experimental and computational values is -2.94, 0.26, 0.72, and 0.88 kcal/mol by $CCSD(T)/6-311+G(d,p)$, $CCSD(T)/6-311+G(3df,2p)$, $G2M(CC3)$, and G2M(CC1) methods, respectively. The $CCSD(T)/6-311+G(d,p)$ method is still the worst; the difference is apparently large. Moreover, the error for every case is about the same, which is above -2 kcal/mol at least; therefore, the single-point energies calculated by $CCSD(T)/6-311+G(d,p)$ in dimer reaction are not reliable. On the other hand, the $CCSD(T)$ with a bigger basis set performs well in both dimer and monomer reactions. The large error with the G2M method is only for the case of $N_2H_4 + N_2O_4 \rightarrow$ trans-HONO+N₂H₃+NO₂, which is 2.67 and 2.57 by CC3 and CC1, respectively. For other cases, the G2M method provides better predictions than CCSD(T), and the most important thing is that CC3 and CC1 calculations maintain similar and stable performances. Even though the number of heavy atoms is too large to use the $CCSD(T)/6-311++G(3df,2p)$, the $G2M(CC3)$ method still provides reliable predictions for the $N_2H_4 + N_2O_4$ reaction system.

	Exp ^a	$CCSD(T)$ /	$CCSD(T)$ /	$G2M(CC3)^{b}$	$G2M(CC1)^{b}$
		$6-311+G(d,p)^b$	6-311++G(3df,2p) ^b		
N_2O_4	4.47	-409.3648607	-409.6067069	-409.6987294	-409.7113339
N_2H_4	26.14	-111.5732783	-111.6428137	-111.6816838	-111.6854736
cis-HONO	-16.844	-205.2927121	-205.4135918	-205.4627235	-205.4689568
trans-HONO	-17.36	-205.2944057	-205.4141683	-205.4634289	-205.4697452
N_2H_3	55.33	-110.9500308	-111.017559	-111.050437	-111.0543067
NO ₂	8.58	-204.67525	-204.7939044	-204.8368898	-204.8432513
NO	21.45	-129.641594	-129.7127854	-129.7154744	-129.7437266
$cis-N2H2$	52.56	-110.3744822	-110.4402507	-110.4736947	-110.4771367
HNO	24.49	-130.2099216	-130.284393	-130.3172662	-130.3213907

Table3-26: The heats of formation based on experimental and computational studies.

^a: The value is from reference (23) , and the unit is kcal/mol.

^b: The computational value is the sum of the zero-point energy of B3LYP/6-311++G(3df,2p) and the electronic energy at the specified method. The unit is hartree/molecule.

Table 3-27: The heats of reaction of $N_2H_4 + NO_2$ and $N_2H_4 + N_2O_4$ reaction computed by the values from Table3-24.^a 1896 CCSD(T)/ CCSD(T)/ Exp G2M(CC3) G2M(CC1) $6-311+G(d,p)$ 6-311++G(3df,2p) Reactants: $N_2H_4 + NO_2$ cis-HONO+N₂H₃ 3.76 3.63 3.49 3.40 3.40 trans-HONO+N₂H₃ 3.25 2.57 3.13 2.95 2.93 Reactants: $N_2H_4 + N_2O_4$ trans-HONO+cis-HONO+cis-N₂H₂ -12.26 -14.72 -11.60 -12.19 -11.94 trans-HONO+[$H_2NN(H)NO_2 \rightarrow$ -12.78 -15.78 -11.96 -12.64 -12.44 trans-HONO+cis-N₂H₂] cis-N₂H₂+ 2 cis-HONO -11.75 -13.66 -11.24 -11.75 -11.45 trans-HONO+N₂H₃+NO₂ 15.94 11.58 14.99 18.61 18.51

^a: All values are in the unit of kcal/mol

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IV. Conclusion

In this work, we have studied the mechanisms for reactions of N_2H_4 with NO_2 and N₂O₄ in order to understand why hydrazine and dinitrogen tetroxide react hypergolically. Moreover, the structures of the N_2O_4 isomers, which are still unknown experimentally, have been investigated. They include $N_2O_4(D_{2h})$, trans-ONONO₂, and cis-ONONO₂. Mechanistically, reactions of N_2H_4 with these isomers and NO_2 have been considered. The results show that the reactions taking place by hydrogen transfer are the lower-energy channels. The lowest energy channel has been identified to be the N_2H_4 + trans-ONONO₂ reaction, in which the two reactants form an intermediate, which can undergoes the hydrogen transfer reaction barrierlessly. Therefore, it is believed that the hypergolic reaction of N_2H_4 and N_2O_4 is initiated by the reaction of N_2H_4 with trans-ONONO₂, because the product $H_2NN(H)NO$ can directly dissociate to the N_2H_3 and NO with only 27.83 kcal/mol dissociation energy at the G2M(CC1) level. Other decomposition channels are too high to occur.

We predict the structures of the N_2O_4 isomers by B3LYP /6-311++G(3df,2p), and the deviations of their vibrational frequencies comparing with the experimental data are less than 25 cm^{-1} on average. The trans-ONONO₂ structure optimized by different methods including B3LYP, PW91PW91, BHandHLYP, and CCSD have similar results, indicating that the $ON-ONO₂$ bond is the longest. However, the cis- $ONONO₂$ isomer has two types of structures, with two longest bonds $ON-ONO_2$ and $ONO-NO_2$. The PES of the N_2O_4 isomerization describes the relationship among these N_2O_4 isomers, and the results are in agreement with experimental observations including the cis-trans isomerization and autoionization.

123 In other bimolecular reactions of the $N_2H_4 + N_2O_4$ system, hydrogen abstraction reactions are still the major and lower-energy channels; those involving N-O bond breaking

need to overcome much higher energy barriers. For the N_2H_4 and NO_2 reaction, the products of the lowest-energy path are cis-HONO and N_2H_3 , whose energy barrier is 7.57 kcal/mol calculated by G2M(CC1). Based on the Transition State Theory, the rate constant of the lowest-energy channel is $3.20 \times 10^{-25} T^{3.74}$ exp(-1662.5/T) cm³molecule⁻¹sec⁻¹ at T=100–4000 K. The other products, such as trans-HONO + N_2H_3 , HNO₂ + N_2H_3 , and $H_2NN(H)OH + NO$, have higher energy barriers than that for cis-HONO + N_2H_3 formation.

For the $N_2H_4 + N_2O_4(D_{2h})$ and $N_2H_4 + cis\text{-ONONO}$ reactions, the transition states of hydrogen transfer are all ring-like structures, including four-member to seven-member rings. The lowest-energy channels for both reactions form trans-HONO and $H_2NN(H)NO_2$ molecules, whose energy barriers are higher than their intermediates by 21.1 and 14.4 kcal/mol predicted at the G2M(CC3) level for $N_2H_4 + N_2O_4(D_{2h})$ and $N_2H_4 + cis-ONONO_2$ reactions, respectively. Furthermore, the $H_2NN(H)NO_2$ may decompose to trans- N_2H_2 and trans-HONO via five-member ring TS of 26.6 kcal/mol, or it may directly dissociate to N_2H_3 radical and $NO₂$ molecule with the dissociation energy of 38.23 kcal/mol computed by 1896 G2M(CC1).

In all calculations, the B3LYP calculations can provide a good prediction and save the computational resources for this eight heavy-atom system; it is the advantage of DFT methods. The G2M method provides reliable calculations of the single point energy as good as $CCSD(T)/6-311++G(3df,2p)$, and it also has smaller differences in heats of reaction comparing with experimental data.

i-TS2 (C_1)

 $cis\text{-ONONO}_2(C_s)$

cis-ONONO₂ 2 (C₁)

i-TS4 (C_1)

0 1

 $NO(C_1)$

0 2

 $0\;1$

 N_2O_4 _BHandHLYP (D_{2h})

O 0.65679200 -1.93907000 0.00000000 O $-0.97293100 -0.04619700$ 0.00000000

trans-ONONO₂_PW91PW91 (C_s)

0 1

A2.3 N_2H_4 and N_2O_4 Reactions A.2.3.1 trans-ONONO₂ + N₂O₄ and

 N_2O_4 ₋CCSD (D_{2h}) $0₁$

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$H_2NN(H)ONO(C_1)$

0 1

134

 H -1.15523300 -0.97362100 1.50443900 N -1.85522400 -1.19206200 0.79105500 H -2.65419000 -0.55989700 0.93735100

$H_2NN(H)NO_PW91PW91(C_1)$

0 1

d-complex2 (C_s)

d-TS5 (C_1)

 $\overline{0}$

trans- $N_2H_2(C_{2h})$

cis- $N_2H_2(C_{2v})$

 $NNH_2(C_{2v})$

$HON(C_1)$

0 1

 $HNO (C_1)$

0 1

A.2.3.3 $N_2O_4 (D_{2h}) + N_2H_4$ Reaction D2h-Complex1

N 0.00000000 0.00000000 0.00000000

N -0.40118132 -1.16347728 0.00082228

H -0.86993694 1.73863796 0.00000000 N -0.43011958 -0.56060123 1.19276361

D_{2h}-Complex3

0 2

0 1

O -1.00405009 -1.48070858 -1.75654151

 O -4.09256987 1.69651589 2.25849118 O -2.61907400 3.26416214 2.60658354

$\hbox{H}\qquad \quad \ 1.01721440\qquad \ 0.000000000\qquad \quad \ 0.00000000$ H -1.25591063 1.14706432 0.00000000 N -0.43943886 -1.25899531 0.03255080 H -1.43721070 -1.34815477 -0.11359212 H 0.15195576 -2.02551453 -0.25557582 N -3.19862049 1.20983737 -0.13703510 O -2.01764930 1.82757672 -0.00379603 O -3.14160839 0.01612593 -0.21744709 D2h-Complex4 0 1 N 0.00000000 0.00000000 0.00000000 H 1.03138220 0.00000000 0.00000000 H -0.70433782 1.84131974 0.00000000 D_{2h} -TS1 0 1 ${\bf N} \qquad \quad \ 0.00000000 \qquad \quad \ 0.00000000 \qquad \quad \ 0.00000000$ $\hbox{H}\qquad \quad \ 1.01601395\qquad \ 0.00000000\qquad \quad \ 0.00000000$ H -0.48051195 0.95300824 0.00000000 N -0.55729530 -0.85909462 0.91487088 H -0.49853578 -1.81907760 0.58306940 H -1.53023206 -0.60858295 1.05442677 O -1.69059917 1.86423788 -0.45496614 N -1.97381194 1.16198928 -1.46575939 O -2.90732216 1.41266758 -2.17427856 N -0.41161887 -0.44302930 -1.74483542 1 80 0.37935179 0.05247316 -2.49216788

D_{2h} -TS4

A.2.3.4 H2NN(H)NO2 Decomposition

$d2$ -Complex1 (C_1)

0 1

$d2$ -Complex4 (C_1)

0 1 ${\bf N} \hspace{1.5cm} 0.00000000 \hspace{1.5cm} 0.00000000 \hspace{1.5cm} 0.00000000$ $\emph{H} \qquad \quad 2.15462604 \qquad \quad 0.00000000 \qquad \quad 0.00000000$ N -1.35556970 0.21863235 0.00000000 H -1.65973949 0.81406689 0.76697340 H -1.82951771 -0.67129515 -0.04259768 N 0.62345358 0.92568371 0.58286900 O 2.01296346 0.80187947 0.52798334 O 0.18964004 1.90679564 1.17875213

