# 國立交通大學

電機與控制工程學系

碩

應用於初次側調整控制器之高效率及低成本

士論文

膝點電壓追蹤調整技術

Primary-Side Regulator with Self-Calibration Knee Voltage Detection

(KVD) Technique for High Efficiency and Low Cost

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中華民國一百零一年十一月

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用於初次側調整控制器之高效率及低成本膝點電壓追蹤調整技術

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#### 摘要

在現今社會,可攜式產品已經成為人人不可或缺的必備工具。隨著電子產品的蓬勃 發展,可充電電池也成為目前最適合可攜式產品使用的行動電源。因此,如何以最理想 且安全的方式將能量傳遞到電池,對電池進行最快速也最有效率的充電是一個重要的課 題。基於通用串行總線充電變成一種趨勢,從交流市電直接對電子產品充電是現在大部 分可攜式產品的充電方式。初次側調整控制器是一種高效率而且低成本的充電器,同時 也是一種能容忍市電的高輸入電壓隔離式充電器。為了確保充電器在定電流充電模式與 定電壓充電模式皆能保持穩定且平穩切換,本切換式充電器將定電流充電迴路與定電壓 充電迴路並聯,且同時達到兩者的穩定性。但是初次側調整控制器與一般控制器最大的 分別就是它並沒有直接的迴授路徑來獲取輸出資訊,因此如何準確從輔助繞組中去取得 膝點電壓進而去控制整個系統變成一個重要問題。

本篇論文完成一具有膝點電壓偵測電路,同時針對偵測的時間做自我的調整來避免 發生偵測錯誤。不同於以往的方式,這次提出的偵測電路不僅能準確的偵測膝點電壓, 並不需要外部原件來做修正,同時也使所有的控制路徑在定電流充電模式與定電壓充電 模式皆能保持穩定且平穩切換。為了使效率更進一步提升,波谷切換以及動態頻率切換 被應用在定電壓充電模式。

### Primary-Side Regulator with Self-Calibration Knee Voltage Detection (KVD) Technique for High Efficiency and Low Cost

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#### Abstract

Nowadays portable devices have been considered a necessity by a lot of people and have become an essential part of everyday life. With the rapid growth in the consumer electronics, rechargeable mobile battery bank has proved to be the most compatible and satisfactory solution for portable devices. Therefore, it will be an important task for us to create a fast and efficient battery charging method with safe delivery of energy to the battery. Since universal serial bus (USB) charging method is a common trend now, most of the portable devices are charged via alternating current (AC) supply combine with USB. Primary-side regulator (PSR) is a high efficiency and low cost solution for power applications. It is a high-input voltage isolated charger compatible with the AC supply. To stabilize and to smoothly transit between the constant voltage and the constant current modes, the constant voltage and constant current loops are connected in parallel in the proposed PSR charger. However, the prominent difference between the PSR and conventional regulators is that the PSR does not have direct feedback loop to obtain the output information. Hence, it is a major challenge to precisely detect knee voltage from the auxiliary winding and thus to accurately control the entire system.

This thesis introduces the PSR with self-calibration knee voltage detection (KVD)

technique, which it can perform self-calibration based on the detection period for error checking and correction. Moreover, the new detection method not only can precisely get the knee voltage without any external components, but also can have all control paths stabilized. The transition smoothly changes between the constant voltage and the constant current modes. Valley switching with a dynamic frequency switching is applied in the constant voltage mode in order to enhance its efficiency and performance.



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iv

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## Contents

CHAPTER 1 1
INTRODUCTION 1
1.1 THE BASIC CONCEPT OF THE ISOLATED CONVERTER
1.1.1 Architecture of Asymmetrical Isolated Converters5
1.1.2 Architecture of Symmetrical Isolated Converters
1.2 MOTIVATION
1.3 THESIS ORGANIZATION
CHAPTER 2 14
BASIC DEFINITION PRINCIPLES OF FLYBACK CONVERTERS
2.1 THE BASIC OPERATION OF FLYBACK CONVERTER15
2.2 Non-Ideal Phenomenon of Flyback Converter in DCM
2.3 Losses and Efficiency Analysis
2.3.1 Conduction Loss
2.3.2 Switching Loss
2.3.3 Quiescent Loss
2.3.4 Efficiency
CHAPTER 3
THE PROPOSED PRIMARY-SIDE REGULATOR WITH SELF-CALIBRATION KNEE
VOLTAGE DETECTION (KVD) TECHNIQUE
3.1 SIGNIFICANT ADVANTAGES OF PSR FLYBACK CONVERTER COMPARED TO CONVENTIONAL
DESIGN
3.2 THE CONVENTIONAL CONTROL OF PSR26
3.3 THE PROPOSED CHARGER BY THE PSR CONTROLLER WITH THE KVD TECHNIQUE
CHAPTER 4
THE PROPOSED KVD TECHNIQUE

# **FIGURE CAPTIONS**

Fig. 1. Isolated power topologies with complexity and efficiency
Fig. 2. Flyback converter
Fig. 3. Forward converter
Fig. 4. Push-pull converter
Fig. 5. Half-bridge converter
Fig. 6. Full-bridge converter
Fig. 7. Flyback converter operates in DCM and CCM16
Fig. 8. (a) Non-ideal flyback converter. (b) Waveform of flyback converter20
Fig. 9. Transient waveform of $V_{DS}$ and $I_D$ curve in switching losses on power MOSFET21
Fig. 10. (a) Conventional flyback converter. (b) Flyback converter with the PSR controller. 25
Fig. 11. (a) Operation of the PSR power stage. (b) Knee voltage reveals the $V_0$ information. 27
Fig. 12. (a) Sampling pulse generator. (b) Sampling pulse with different expected voltage's
operation
Fig. 13. (a) Adjust circuit. (b) Different regulation reference
Fig. 14. The S/H of knee point according to $V_{DET}$ and $V_{DELAY}$
Fig. 15. Proposed PSR controller
Fig. 16. Constant Current Operation in the PSR controller
Fig. 17. Constant voltage operation in the PSR controller
Fig. 18. The definition of CC/CV operation with output current/voltage
Fig. 19. The transition from the CC operation to the CV operation
Fig. 20. (a) The operation of the dynamic frequency technique. (b) The switching frequency
versus the output current. (c) The slight variation of the switching frequency if one of the
valley voltages is selected

Fig. 21. (a) The current calculator circuit. (b) The timing diagrams.	.41
Fig. 22. (a) The KVD circuit. (b) Timing diagrams of the KVD technique	.43
Fig. 23. The circuit of subtractor.	.44
Fig. 24. Flow chart with state machine of Self-Calibrator	.46
Fig. 25. (a) Self-calibrator circuit. (b) Waveforms in different Mode	.47
Fig. 26. Up/down counter.	47
Fig. 27. (a) Equivalent small signal model of the proposed PSR in CV regulation. (b)	
Waveforms of the dynamic frequency technique.	50
Fig. 28. Chip micrograph	51
Fig. 29. Simulation results of the PSR operation in the DCM.	53
Fig. 30. Simulation results of the current calculator	53
Fig. 31. Simulation results of the KVD technique.	54
Fig. 32. (a) Self-Calibrator in Mode 2 to Mode 4 (b) Self-Calibrator form Mode 2 to Mode	3.
	55
Fig. 33. (a) PSR Operation Changing from CC to CV. (b) Dynamic Frequency in CV	
Regulation	56
Fig. 34. Charging Sequence of PSR.	57
Fig. 35. The output voltage versus the knee voltage.	58

# **Table Captions**

TABLE I Different types of isolated converters.	4
TABLE II Comparison of flyback converter operating at CCM and DCM	17
TABLE III Design Specifications	51



## **Chapter 1**

### Introduction

The isolated architecture is widely used in nowadays power system because of it has many advantages. Such as it is quite safety and convince to design in wide range voltage difference situation between output and input voltage. Flyback [1] converter is one of isolated converter [2]. Unlike the conventional power system, isolated converter uses a pair of coils to transmit electric power via magnetic coupling. It protects the back-end device from high input voltage through the isolation from transformer. In view of the portable device become a trend, one of control methods of flyback called primary-side regulator (PSR) becomes more important.

Recently, the portable devices like personal digital assistants, smart phones, laptops and digital cameras etc., have become the most popular applications [3]. Rechargeable batteries combine universal serial bus (USB) charging method are used in these applications for green energy and linking devices to personal computer. Also most of the portable devices are charged via alternating current (AC) supply. PSR is a high efficiency and low cost solution for these power applications. It is also a high input voltage isolated charger compatible with AC supply.

The proposed PSR is using the topology of flyback converter and used for battery charger. Also the self-calibration with knee voltage detection (KVD) technique is proposed to enhance the accuracy of sensing battery voltage. The improving of the sensing accuracy can make the charging sequence changing precisely between constant current (CC) and constant

voltage (CV). It can prevent overcharging for battery [4] [5] and improve the efficiency of the system.



#### **1.1 The Basic Concept of the Isolated Converter**

The switching mode charger can be classified according to system topology. The most important distinction is isolated converters and non-isolated ones. Most of the electrical equipment needs the isolation for high-voltage safety consideration. The advantages about isolation such as the separation of direct contact from input to output, and the improved common-mode voltage rejection from input source. Moreover, there are some standards defined by different institutions in different countries such as the U.S. specifications (UL, CSA) and the European specifications (IEC, EN). Every product on the market must be approved by these institutions.

The isolated power converters have many different topologies according to the application of output watts of electrical device. Fig. 1. shows some common isolated topologies that apply in different output power. Each topology has different designed complexity and conversion efficiency. TABLE I shows some different types of isolated converters and some of its characteristic.

According to the operation of the isolated converter, there are two types of isolated topologies like asymmetrical and symmetrical. The asymmetrical type uses only one switch to transfer the energy from primary side to output side through the transformer such as flyback and forward. And the symmetrical type always uses an even number of switches. Compare to asymmetrical converters, it is better exploits the transformer's magnetic circuit than in asymmetrical converters. So, smaller size and weight can be achieved. In other words, if it uses the same size of transformer, the symmetrical type could supply more output power. The three most common symmetrical structures are push-pull, half bridge and full bridge.



### **1.1.1 Architecture of Asymmetrical Isolated**

#### **Converters**

One of the most common asymmetrical isolated converters is flyback converter. The flyback converter is used in both AC/DC and DC/DC conversion with galvanic isolation between the input and any outputs. More precisely, the flyback converter is a buck-boost converter with the inductor split to form a transformer, so that the voltage ratios are multiplied with an additional advantage of isolation. When driving for example a plasma lamp or a voltage multiplier the rectifying diode of the buck-boost converter is left out and the device is called a flyback transformer.

Fig. 2 shows the structure of flyback converter [6]. When the switch is closed, the primary of the transformer is directly connected to the input voltage source. The primary current and magnetic flux in the transformer is increasing, and storing energy in the transformer. The voltage induced in the secondary winding is negative, so the diode is reverse-biased (i.e., blocked). When the switch is opened, the primary current and magnetic flux drops. The secondary voltage is positive, forward-biasing the diode, allowing current to flow from the transformer. The energy from the transformer core recharges the capacitor and supplies the load. The output capacitor supplies energy to the output load. The operation of storing energy in the transformer before transferring to the output of the converter allows the topology to easily generate multiple outputs with little additional circuitry, although the output voltages have to be able to match each other through the turns ratio. Also there is a need for a controlling rail which has to be loaded before load is applied to the uncontrolled rails, this is to allow the PWM to open up and supply enough energy to the transformer. If the turns ratio of the transformer  $n=N_P/N_S$  and D means the duty cycle of on-time, the conversion ratio of  $V_{IN}$  and  $V_O$  is shown below. Flyback regulators are mainly used for an output power ranging

from 5W up to 250W. Flyback topology is dedicated to multiple low cost output switch mode power supply as there is no filter inductor on the output.



The forward converter as shown in Fig. 3 is a DC/DC converter that uses a transformer to increase or decrease the output voltage (depending on the transformer ratio) and provide galvanic isolation for the load [7]. With multiple output windings, it is possible to provide both higher and lower voltage outputs. It operates in a manner similar to the flyback converter, but is generally more energy efficient. A flyback converter stores energy as a magnetic field in an inductor air gap during the time the converter switching element (transistor) is conducting. When the switch turns off, the stored magnetic field collapses and the energy is transferred to the output of the flyback converter as electric current. The flyback converter can be viewed as two inductors sharing a common core. In contrast the forward converter (which is based on a transformer) does not store energy during the conduction time of the switching element - transformers cannot store a significant amount of energy unlike inductors. Instead, energy is passed directly to the output of the forward converter by transformer action during the switch

conduction phase. The demagnetization and primary windings have to be tightly coupled to reduce the voltage spike more than the theoretical *2Vin* occurring at turn-off across the power switch. Besides, forward regulators are commonly used for output power up to 300W.



Fig. 3. Forward converter.

### **1.1.2 Architecture of Symmetrical Isolated**

**Converters**There are three types of symmetrical isolated converters will be introduced below. Firstly, push-pull has two switches and two diodes as shown in Fig. 4.  $S_1$ and  $S_2$  switches are alternately turned on. The push-pull converter is also a type of DC-to-DC converter, a switching converter that uses a transformer to change the voltage of a DC power supply. The distinguishing feature of a push-pull converter is that the transformer primary is supplied with current from the input line by pairs of transistors in a symmetrical circuit. The transistors are alternately switched on and off, periodically reversing the current in the transformer. Therefore current is drawn from the line during both halves of the switching cycle. This contrasts with buck-boost converters, in which the input current is supplied by a single transistor which is switched on and off, so current is only drawn from the line during half the switching cycle. During the other half the output power is supplied by energy stored in inductors or capacitors in the power supply. Push-pull converters have steadier input current, create less noise on the input line, and are more efficient in higher power -100 applications. 



Fig. 4. Push-pull converter.

Fig. 5 shows the PWM half bridge DC-DC converter, which contains two transistors, a transformer and a rectifier. It main advantage is that the voltage stresses of the transistors are low and equal to the maximum dc input voltage of converter. Another advantage is that the core saturation problems are minimized because the dc component of the current through the primary is zero due to the coupling or blocking capacitors in series with the primary. This topology can be used for an output power capability up to 500W.



Fig. 5. Half-bridge converter.

Fig. 6 shows the structure of full bridge converter. Because of the number of components, the full bridge is for high power applications, ranging from 500 up to 2000W. Sometimes, power transformers are paralleled to provide higher output power. Switch pairs  $S_1$  and  $S_3$ ,  $S_2$ 

and  $S_4$  are alternately driven. The full bridge provides twice the output power of the half bridge circuit with the same switch ratings. Nevertheless, this topology requires four switches and clamping diodes.

Many types of isolated converter are designed for different application according to the output voltage and load current. And the power supply designs are often tailored to specific applications. For the lower power application such as LED tube and notebook, the flyback converter is used in this thesis.



Fig. 6. Full-bridge converter.

#### **1.2 Motivation**

Almost all high-performance portable products use rechargeable batteries, because it is reusable for green energy. Also the personal computer now is used to synchronous with portable device through USB. So charging the battery from AC input through USB becomes the important issue in nowadays. The most common charging method in present days is the CC-CV (Constant Current-Constant Voltage) method. First, the charger charges the battery in constant current to the specified voltage. Once the battery reaches the rated voltage, the charger enters the constant voltage mode and keeps the battery in stable voltage.

To protect the battery from being overcharged, the charging process needs to switch from CC phase to CV phase to gradually reduced the charge current until the process is finished [8] [9]. So the transition time of two phases is also needed to be carefully designed. How to sense the correct output voltage and current is the key point to changing precisely from CC to CV.

This thesis proposed a robust isolated switch-mode charger instead of a conventional charger to guarantee the protection for application of portable product. For the entire isolated converter, flyback converter appears commonly in the electrical devices around modern people because of the lower output power application. The combination of flyback converter for charger application is called primary side regulator (PSR). This proposed PSR is using self-calibration knee voltage detection (KVD) technique to achieve the correct sensing voltage. By changing the CC and CV phase precisely to prevent overcharge, it can also enhance the efficiency of whole system.

### **1.3 Thesis Organization**

The thesis introduces the isolated charger PSR based on flyback converter and charging sequence. The basic concept and operation of flyback converter organized in Chapter 2. The proposed CC and CV regulation method compare to conventional is described in Chapter 3. The circuits implementations are demonstrate in Chapter 4.

Finally, the whole system chip simulation, simulation specification, conclusions and future work are presented in Chapter 5.



## Chapter 2

## **Basic Definition Principles of Flyback**

## **Converters**

From the previous discussion, the isolated converter plays an important role in the use of high input voltage application. Also the flyback converter has many advantages in low power application. In order to understand the concept of the flyback converter, this chapter first described the operation of flyback converter in different modes. In addition, the consideration between modes is described in this chapter. The efficiency also considered into the operation. One of the control methods named Quasi-Resonant (QR) is used in the CV regulation to save the efficiency. Besides, the non-ideal effect is demonstrated after the modes description. These non-ideal factors affect the design of this topology. Then the efficiency and losses of the power system will also demonstrate in this chapter. 

<sup>m</sup>

### 2.1 The Basic Operation of Flyback Converter

All of the DC-DC converters' operation can be classified into discontinuous conduction mode (DCM) and continuous conduction mode (CCM) according to its switching timing. Continuous conduction mode means that the current in the energy transfer inductor never goes to zero between switching cycles. In discontinuous conduction mode (DCM) the current goes to zero during part of the switching cycle. Flyback converter can be operated in both modes depending on whether the primary inductance of the transformer is completely demagnetized or not. Fig. 7 shows the ideal waveform of flyback converter operating in DCM and CCM. The flow current of  $I_P$  and  $I_S$  represent the transformer's primary winding current and secondary winding current.  $I_O$  is the average current of output. And the  $V_S$  mean the voltage across power switch.

In DCM operation, the primary side current rises with the slope  $V_{IN}/L_m$  during the on time of power switch.  $L_m$  is the magnetizing inductance of transformer. And the secondary current falls with the slope  $V_{IN}/L_m$ , when the switch turns off. Therefore, it makes the current form a triangular wave. During the on time, the voltage across switch is the sum of input voltage and reflected voltage from output. Once the secondary current decreases to zero, the drain voltage drops to  $V_{IN}$ . On the other hand, the CCM operation makes the transformer's current never reach to zero. And the  $V_S$  is always at  $V_{IN}+(N_P/N_S)V_O$  during the switch is off.



Fig. 7. Flyback converter operates in DCM and CCM.

To analyze the DCM and CCM in detail, each mode has its own advantages and drawbacks. The DCM operation has many merits such as the zero turn on losses for the power switch, good line and load transient response, the feedback loop has only single pole is easy to stabilize, the smaller transformer size because of the sharper current slope, and the recovery time of rectifier is not critical that means current is zero well before reverse voltage is applied. But DCM operation still have some disadvantage such as the larger output ripple and high peak currents in rectifiers and power switches. The CCM operation is only good at small output ripple and the peak current of rectifier and switch is half the value of discontinuous mode. And its drawbacks are the rectifier losses of recovery time and the loop is difficult to stabilize owing to the two poles and right half plane zero.

TABLE II shows the comparison table of the flyback converter's operation between DCM and CCM. The blue color means the better performance than the other, and the red is opposite. Consequently, according to the table, the DCM operation in flyback converter has more advantages, so the DCM operation is common in flyback converter's control IC.

In general, flyback converter appears commonly in the electrical devices around modern people because of the lower output power application. Flyback converter has been employed operating both in continuous conduction mode (CCM) and discontinuous conduction mode (DCM) as well as critical conduction mode (CRM), boundary between CCM and DCM. Compared with CCM, BCM enjoys benefits such as soft switching, fast transient response, smaller transformer, and easier compensation for system's stability [10] - [12].

comparison of hyback converter operating at CCW and DCW					
	DCM	ССМ			
Transformer size	Small	Large			
Peak current of switch	Large	Small			
Output ripple	Large	Small			
<b>Recovery time rectifier</b>	Small	Large			
Loop compensation	Easy	Hard			
Line/Load transient response	Fast	Slow			
Soft switching	Yes	No			

	Comparison of fl	yback converter	operating at CCM	I and DCM
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TABLE II

#### 2.2 Non-Ideal Phenomenon of Flyback Converter in

#### DCM

The concept of flyback converter introduced in section 2.1 is the ideal. But flyback converter has non-ideal phenomenon. This section is describing the non-ideal when realize the flyback converter. First of all, the transformer has magnetizing inductance  $L_m$ . However, transformer also has leakage inductance  $L_K$  as shown in Fig. 8 (a). Leakage inductance is the property of an electrical transformer that causes a winding to appear to have some inductance in series with the mutually-coupled transformer windings. This is due to imperfect coupling of the windings and creation of leakage flux which does not link with all the turns of the winding. The leakage flux alternately stores and discharges magnetic energy with each electrical cycle and thus effectively acts as an inductor in series in each of the primary and secondary circuits. Leakage inductance is primarily caused by the design of the core and the windings.

To reduce the effect of  $L_K$  to the system, a simple circuit called snubber is applied, which composed by  $C_S$ ,  $R_S$  and  $D_S$  in Fig. 8 (a). It can be used in electrical systems with an inductive load to suppress instantaneous voltage spike across the power switches in case of sudden current flow. Transient voltage variation will be a source of electromagnetic interference (EMI) in other circuits. Additionally, if the instantaneous voltage spike across the device is beyond what the devices can tolerate, it may damage or destroy the devices. Thus, the snubber provides a short-term alternative current path around the current switching device so that the inductive element may be discharged more safely and quietly.

Inductive elements are often unintentional, but arise from the current loops implied by physical circuitry. While current switching is everywhere, snubbers will generally only be required where a major current path is switched, such as in power supplies. Snubbers are also often used to prevent arcing across the contacts of relays and switches and the electrical interference and welding/sticking of the contacts that can occur. In flyback converter, snubber is used to give a path to leakage inductance's resonant.

Second, the switch  $S_I$  has the parasitic capacitor  $C_{DS}$ . It is an unavoidable and usually unwanted capacitance that exists between the parts of an electronic component. All actual circuit elements such as inductors, diodes, and transistors have internal capacitance, which can cause their behavior to depart from that of 'ideal' circuit elements. In addition, there is always non-zero capacitance between any two conductors. Also the forward diode  $D_I$  has the forward drop  $V_D$ .

When switch turn off, the primary side current  $I_P$  is down to zero as shown in Fig. 8 (b). The magnetizing inductance  $L_m$  start to transfer energy to secondary side and make the current  $I_S$  starts to discharge. But there is only the magnetizing inductance can transfer energy, the leakage inductance has no path to secondary can discharge energy. Leakage inductance can only discharge to parasitic capacitor  $C_{DS}$ , and  $V_S$  start the first resonant in  $T_{LK}$  cause by  $L_K$  and  $C_{DS}$ . Also  $V_S$  reflect the output voltage  $V_O$  and forward voltage  $V_D$ . The forward voltage  $V_D$  is decreasing with  $I_S$  decreasing. When secondary current is discharging to zero, the forward voltage  $V_D$  is also zero. The reflected voltage only remain  $V_O$ .  $V_S$  is  $V_{IN}+(N_P/N_S)V_O$  at the end of discharge time. Also the charges in  $C_{DS}$  start to discharge to  $L_m$  and resonant to each other until next cycle. The resonant of  $C_{DS}$  and  $L_m$  makes the  $V_S$  have many valleys in  $T_{RE}$ . It can make the valley voltage down to nearly zero. By using these valleys properly, the flyback converter can turn to the next cycle in soft switching and improve the efficiency. This soft switching technique by turning on the switch when resonant to valley is also called Quasi-Resonant (QR) control in flyback converter.



Fig. 8. (a) Non-ideal flyback converter. (b) Waveform of flyback converter.

# 2.3 Losses and Efficiency Analysis

Power loss of switching regulators is the combination of the switching loss and the MOSFET's conduction loss as shown in equation (1). The power loss is important factor to determine efficiency and it is briefly introduced as following.

$$P_{MOSFET} = P_{SW} + P_{COND} \tag{1}$$

### **2.3.1 Conduction Loss**

The conduction loss is mainly related to high-side transistor loss and low-side transistor loss. High-side conduction loss is calculated straightforward that is just the  $I^2R$  loss timing the MOSFET's duty cycle as below:

$$P_{COND} = I_{OUT}^2 \cdot R_{DS(ON)} \cdot \frac{V_{OUT}}{V_{IN}}$$
(2)

Where  $R_{DS(ON)}$  is at the maximum equivalent resistor on operation MOSFET.

In the same way, low-side conduction loss is determined as (3).

$$P_{COND} = I_{OUT}^2 \cdot R_{DS(ON)} \cdot (1 - \frac{V_{OUT}}{V_{IN}})$$
(3)

### 2.3.2 Switching Loss

The switching interval begins when the high-side MOSFET driver turns on and begins to supply current power MOSFET's gate to charge its input capacitance. The switching loss is involved of the charge on the parasitic capacitor of switching node. Therefore, there is no switching loss until  $V_{GS}$  reaches the low-side MOSFET's  $V_{TH}$ .



Fig. 9. Transient waveform of  $V_{DS}$  and  $I_D$  curve in switching losses on power MOSFET.

When  $V_{GS}$  reaches  $V_{TH}$ , the input capacitance of gate is being charged and the MOSFET's drain current  $I_D$  is rising up linearly until it reaches the current  $I_L$  which is presumed to be  $I_{LOAD}$ . During this period  $(t_1)$  the MOSFET is sustaining the entire input voltage  $V_{IN}$  across it, the energy in MOSFET during  $t_1$  is:

$$P_{t_1} = t_1 \cdot \left(\frac{V_{IN} \cdot I_{LOAD}}{2}\right) \tag{4}$$

Sequentially, as the beginning time of second period  $t_2$ , the current flowing through high-side MOSFET is  $I_{LOAD}$ , and the  $V_{DS}$  begins to fall. All of the gate current will be going to recharge  $C_{GD}$ .  $C_{GD}$  is similar to the "Miller" capacitance of transistor, so  $t_2$  could be thought of as "Miller time". During this time the current is constant as  $I_{LOAD}$  and the voltage is falling fairly linearly from  $V_{IN}$  to 0, therefore:

$$P_{t_2} = t_2 \cdot \left(\frac{V_{IN} \cdot I_{OUT}}{2}\right) \tag{5}$$

The total switching loss for any given edge is just the power that occurs in each switching interval, multiplied by the duty cycle of the switching interval:

$$P_{SW} = \left(\frac{V_{IN} \cdot I_{OUT}}{2}\right) \cdot (t_1 + t_2) \cdot F_S$$

(6)

### 2.3.3 Quiescent Loss

The quiescent loss also called as static loss that was consumed by other controllers of switching regulators. The smaller quiescent loss also causes higher efficiency.

$$P_Q = V_{IN} \cdot I_Q \tag{7}$$

The other power losses that don't be mentioned above obeyed the rules of  $I^2 R$ .

### 2.3.4 Efficiency

The efficiency of switching regulator is defined as the ratio of the output power consumption and input power supplies, which is formed as below equation (8):

$$E_{ff} = \frac{P_{OUT}}{P_{IN}} = \frac{P_{OUT}}{P_{O} + P_{SW} + P_{COND} + P_{Q} + P_{Else}} \times 100\%$$
(8)

The total power consumption of input power supplies is involved of the output consumption ( $P_O$ ), switching loss ( $P_{SW}$ ), conduction loss ( $P_{COND}$ ), quiescent loss ( $P_Q$ ), and other losses ( $P_{Else}$ ) in parasitic elements. A high efficiency results in a high performance extending the battery life.



### **Chapter 3**

### **The Proposed Primary-Side Regulator with**

### **Self-Calibration Knee Voltage Detection**

### (KVD) Technique

In this chapter, the primary-side regulator (PSR) is adopted to the design of flyback converter to show some significant advantages compared to conventional flyback converter. Furthermore, the self-calibration knee voltage detection (KVD) technique is presented to get rid of the disadvantage of inaccuracy caused by the remove of the feedback path from the opto-coupler. That is to say, the charger implemented by the PSR flyback converter must have the precise sensing technique, self-calibration knee voltage detection (KVD) technique, to ensure accurate charging process.

### 3.1 Significant Advantages of PSR Flyback

### **Converter Compared to Conventional Design**

Figs. 10 (a) and (b) illustrate the architecture of conventional flyback converter and the PSR flyback converter, respectively. In Fig. 10(a), conventional flyback converter uses one feedback from the secondary side through the use of the opto-coupler. Unlike the power stage discussed in chapter 2, the transformer also includes the auxiliary winding  $N_A$  to reflect the input and output voltage information to the controller and to provide energy to the  $V_{DDH}$  after
the start-up procedure is ended. The *opto-coupler* and the *TL431* work as the error amplifier to get the output voltage information,  $V_{FB}$ .

The PSR as shown in Fig. 10 (b) is similar to flyback converter mostly. The difference between flyback converter and PSR is the external components of *opto-coupler* and *TL431*. Instead sensing output voltage by external component, PSR is using auxiliary winding  $N_A$  to replace it. Compared with the conventional secondary-side regulation approach, the PSR can reduce the total cost, component count, size and weight.



(b)

Fig. 10. (a) Conventional flyback converter. (b) Flyback converter with the PSR controller.

### **3.2 The Conventional Control of PSR**

Conventional PSR system structure is depicted in Fig. 10 (b). The input bulk capacitor  $C_{IN}$  is used after full-bridge rectifier to reduce the AC line voltage ripple, which has the switching frequency of 120 Hz. Thus, the  $V_{IN}$  has a near DC voltage. Besides, the current sensing resistor  $R_{CS}$  is used to sense input line current. The auxiliary winding  $N_A$  can not only sense the output voltage  $V_O$  through the voltage divider ( $R_{A1}$  and  $R_{A2}$ ) to get the voltage  $V_{DET}$  for the controller but also provide the power to the  $V_{DDH}$  if the controller works correctly.

Fig. 11(a) shows the basic operation of PSR. Instead of using secondary feedback components, the PSR can use the auxiliary winding to get the information of the output voltage  $V_O$ . During the inductor current discharge time  $T_{DIS}$ , the summation of the output voltage  $V_O$  and the diode forward voltage drop  $V_D$  is reflected to the auxiliary winding as the signal  $V_A$ . It is hard to get only the  $V_O$  information without being affected by the  $V_D$  from the  $V_A$ . Fortunately, at the end of the diode conduction time as depicted in Fig. 11(b), the auxiliary winding voltage simply reflects the  $V_O$  because the diode forward voltage drop decreases to zero as the diode forward current decreases to zero. By sampling the winding voltage at the end of the diode conduction time, the  $V_O$  information can be obtained as the knee voltage,  $(N_A/N_S)*V_O$ .



(a)



Fig. 11. (a) Operation of the PSR power stage. (b) Knee voltage reveals the V<sub>0</sub> information. Several literatures have been proposed to accurately get the information of knee voltage
[13] - [15]. Sampling pulse generator as depicted in Fig. 12 (a) is used to emulate the charging and discharging of the inductor current [13]. The current source I<sub>1</sub> combine with n-transistor M<sub>1</sub> and capacitor C<sub>1</sub> are used to be a delay circuit. The I<sub>4</sub>, M<sub>4</sub> and C<sub>3</sub> also do the same work. When the gate signal V<sub>GD</sub> is on, the p-transistor M<sub>2</sub> is also turned-on. The current source I<sub>2</sub>

then charges the capacitor  $C_2$  to produce a charge time. When  $V_{GD}$  is off, the n-transistor  $M_3$  is turned-on. The capacitor  $C_2$  is discharged by current source  $I_3$  to produce discharge time that is proportional to the charge time. When the voltage across  $C_2$  is discharged to zero, it also means the discharge time is over. Then sampling pulse  $V_{SP}$  is triggered to sample  $V_A$  as knee voltage.

However, the discharging slope of inductor current is proportional to the output voltage  $V_o$ . When output voltage is not equal to expected voltage, some error operation will occurred as depicted in Fig. 12 (b). If the expected voltage higher then output voltage, the too early operation will occur and the sampling voltage will higher than knee voltage. On the other hand, if the expected voltage lower then output voltage, the too late operation will occur and the sampling voltage. In worst case, it may sample the zero voltage.



Fig. 12. (a) Sampling pulse generator. (b) Sampling pulse with different expected

voltage's operation.

On the other hand, the regulation of  $V_O$  can be changed to regulate the summation of the  $V_O$  and the  $V_D$ . In [14], the summation of the  $V_O$  and the  $V_D$  can be derived by the proposed circuit in Fig. 13 (a). The  $V_O$  is expected to be regulated to  $V_{REF}$ . The  $V_D$  information can be got by the primary side current signal  $V_I$ . Therefore, the new reference  $V_{REF1}$  is equal to  $V_{REF} + \frac{V_I}{R_1} \cdot \frac{R_3}{R_2} \cdot R_{ext}$ . That is to say, if the sampling voltage **in the beginning of the discharging period after a blanking time** should be regulated to  $V_{REF1}$ , the  $V_O$  can be approximately regulated to the  $V_{REF}$  as shown in Fig. 13 (b).

However, the disadvantage is that it needs the external resistor  $R_{ext}$ . Because of the different forward diode has different forward voltage  $V_D$ . Using the same resistor cannot emulate different  $V_D$  correctly. An external resistor increase the cost and component count.



Fig. 13. (a) Adjust circuit. (b) Different regulation reference.

In [15], one RC circuit is utilized to generate a delayed waveform  $V_{DELAY}$  of the signal  $V_{DET}$  from the auxiliary winding. The original signal  $V_{DET}$  is used to determine the sampling time of the knee voltage from the  $V_{DELAY}$ . That is to say, in the beginning of the resonant period  $T_{RE}$  when the inductor current decreases to zero, the slope of the  $V_{DET}$  becomes extremely sharp. By comparing the slope of  $V_{DET}$  to a threshold value, it can determine if the

 $V_{DET}$  is in resonant period or not. Then sample the  $V_{DELAY}$  for knee voltage as depicted in Fig. 14.

However the slope of  $V_{DET}$  in resonant period depends on the LC values, which are transformer's magnetizing inductance  $L_m$  and power MOSFET parasitic capacitor  $C_{DS}$ . By using constant value compare to the slope of  $V_{DET}$  to determine the sampling time also needs to adjust the RC values for  $V_{DELAY}$  according to different LC values that can sample the correct knee voltage. In order to adjust the RC value, it needs external components. That also increase the cost and component count.

*V*<sub>DET</sub> *2. S/H the knee voltage by V*<sub>DELAY</sub>

1. When  $V_{DET}$  slope is sharp enough

Fig. 14. The S/H of knee point according to  $V_{DET}$  and  $V_{DELAY}$ .

# **3.3 The Proposed Charger by the PSR Controller**

### with the KVD Technique

The proposed PSR controller with the KVD technique is shown in Fig. 15. Similarly, the DCM is utilized in the PSR controller. Here, the PSR controller is used to control the charging process of the Li-Ion battery. That is to say, the PSR controller needs to have two control loops to provide the charging procedure of the constant current (CC) and the constant voltage (CV) stages.

The current information  $V_{CS}$  in (9) is derived from the primary side current  $I_P$  flowing through the sensing resistor  $R_{CS}$ , which is connected between the source of the power MOSFET and ground.

$$V_{CS} = I_P \times R_{CS}$$
 and  $V_{CS,PK} = I_{PK} \times R_{CS}$  where  $I_{PK}$  is the peak current. (9)

The  $V_I$  is proportional to the integration of the peak current information  $I_{PK}$  within one discharging time  $T_{DIS}$  in the current calculator circuit. Here, the  $T_{DIS}$  can be used to decide the integrating time. In the current loop, the modulation of the on-time of the CC stage is decided by the comparison result of the  $V_{RAMP}$  and the  $V_{ERR_I}$ , an error signal derived at the output of the error amplifier 1 (EA 1). As a result, the  $V_I$  can be regulated to the reference voltage  $V_{REF_I}$  to ensure constant current. Here, the CC stage is controlled by a constant switching frequency, which is determined by the oscillator OSC with a pulse signal  $V_{PULSE}$  as depicted in Fig. 16.

Here, the secondary side peak current  $I_{S,PK}$  can be expressed by the  $I_{PK}$  and shown in (10) according the turn ratio of  $N_P/N_S$  where the primary winding and the secondary winding have  $N_P$  turns and  $N_S$  turns, respectively.

$$I_{S,PK} = I_{PK} \times \frac{N_P}{N_S} = \frac{V_{CS,PK}}{R_{CS}} \times \frac{N_P}{N_S}$$
(10)

Thus, the average output current can be expressed as (11).

$$I_{O,avg} = \frac{1}{2 \times T_S} \times I_{S,PK} \times T_{DIS}$$
(11)

Substituting for  $I_{S,PK}$  from (10) gives (12).

$$I_{O,avg} = \frac{1}{2 \times T_S} \times \frac{V_{CS,PK}}{R_{CS}} \times \frac{N_P}{N_S} \times T_{DIS}$$
(12)

Interestingly, in the design of the PSR control, only two variables  $V_{CS,PK}$  and  $T_{DIS}$  are needed to be determined. That can easily achieve CC regulation with constant switching frequency.



Fig. 16. Constant Current Operation in the PSR controller.

On the other hand, the other voltage loop is used for constant voltage (CV) stage. From the auxiliary winding  $N_A$  in Fig. 10(b), the voltage information  $V_{DET}$  is a scaled down value of the  $V_A$  by the voltage divider, composed of the resistors  $R_{A1}$  and  $R_{A2}$ . The knee voltage detector (KVD) and the self-calibrator circuit are designed to get accurate output voltage information. Thus, the knee voltage  $V_V$  can be got without being affected by the diode forward voltage  $V_D$ . The  $V_V$  can be regulated to be close to the reference  $V_{REF_V}$  by the voltage loop. In the CV stage, the error signal  $V_{ERR_V}$  and the current sense signal  $V_{CS}$  are used to determine the on-time value as shown in Fig. 17. Besides, the switching frequency varies with the value of  $V_{ERR_V}$ . If the  $V_{ERR_V}$  becomes smaller, the switching frequency will be extended by the OSC circuit to reduce the switching power loss because the Quasi-Resonant (QR) technique is also used for zero voltage switching (ZVS) to improve the efficiency if there is a small input current.



Fig. 18 shows the charging procedure of the battery charger. It includes the CC and the CV stages. In the CC stage, the output voltage  $V_O$  is charged from the minimum voltage  $V_{O,min}$  to the nominal full-charged voltage  $V_{O,max}$  with a constant switching frequency, which is equal to  $1/T_S$ . The value of the  $V_{O,max}$  doesn't exceed the tolerance of the maximum allowable voltage of the battery while the  $V_{O,min}$  can ensure the PSR operates in the DCM.

The discharging current rate is proportional to the  $V_O$  as shown in (13). ,where  $L_m$  is the magnetizing inductance of the transformer.

$$\frac{dI_s}{dt} = -\left(\frac{N_P}{N_s}\right) \times \frac{V_O}{L_m}$$
(13)

In Fig. 17, the  $I_{PK}$  and the  $T_{DIS}$  can be derived as shown in (14) and (15), respectively.

$$I_{PK} = \frac{V_{IN}}{L_m} \times T_{ON} \text{ where } T_{ON} = DT_S$$
(14)

$$T_{DIS} = \frac{I_{S,PK}}{\left(\frac{N_P}{N_S}\right)^2 \times \frac{V_O}{L_m}} = \frac{I_{PK}}{\left(\frac{N_P}{N_S}\right) \times \frac{V_O}{L_m}} = \frac{N_P}{N_S} \times \frac{V_{IN}}{V_O} \times T_{ON}$$
(15)

In case of minimum output voltage  $V_{O,min}$ , the  $T_{DIS}$  in (15) has a maximum value of  $T_{DIS,max}$ . To ensure the discharging phase can be finished within one constant switching period  $T_S$ , the inequality in (16) should be made. That is, the operation is always kept in the DCM due to the inductor current can be decreased to zero within one switching period.

$$T_{ON} + T_{DIS,\max} = T_{ON} + \frac{N_s}{N_p} \times \frac{V_{IN}}{V_{O,\min}} \times T_{ON} \le T_s$$
(16)

Therefore, the initial point of the output  $V_{0,min}$  for the CC operation can be derived as shown in (17).

$$V_{O,\min} \ge \frac{D}{1-D} \times V_{IN} \times \frac{N_S}{N_P}$$
(17)

In other words, the startup circuit should ensure the output voltage is charged to  $V_{O,min}$  first. Then, the charger is switched to the CC operation with a constant current defined by the reference voltage  $V_{REF_{-}I}$ . Once the output is charged to the  $V_{O,max}$  with a constant switching frequency, the charger will be changed to the CV operation. In CV operation, the switching frequency varies with the value of the  $V_{ERR_{-}V}$ . Besides, the QR technique is effectively used to decrease the switching frequency for high efficiency. Consequently, the  $V_O$  is finally regulated to the  $V_{O,max}$  with a decreased charging current to end the whole charging function.



Fig. 18. The definition of CC/CV operation with output current/voltage.

The transition from the CC to the CV is depicted in Fig.19. The on-time value is determined by the  $V_{RAMP}$  and the  $V_{ERR,I}$  in the CC operation. On the other hand, the on-time value is determined by the  $V_{ERR,V}$  and the  $V_{CS}$ . In the beginning of the charging procedure, the duty cycle is determined by the CC operation because the duty cycle decided by the CV operation is too large under a high  $V_{ERR,V}$ . Once the  $V_O$  is gradually charged to the nominal value, the  $V_{ERR,V}$  will be pulled lower than the  $V_{ERR,I}$ . The transition from the CC operation to the CV operation happens. In other words, the duty cycle decided by the CV operation will be smaller than that of the CC operation. Thus, a smooth transition can be made. Here, a flag signal  $V_{CV}$  is used to indicate the CV operation is enabled and to decrease the switching frequency. The CV operation uses the adaptive valley selection method to decrease the switching frequency. The correct to accordingly decrease the switching frequency for reducing switching power loss in the CV operation. Once the charging current is lower than a predefined value, the green mode is utilized to further reduce the switching power loss. Here, the green mode uses an ultra-low switching frequency for high efficiency.



Fig. 19. The transition from the CC operation to the CV operation.

The stored energy in the primary winding  $(N_P)$  starts to transfer to the output once the  $V_{GD}$  changes from high too low to turn off the power MOSFET as depicted in Fig. 20(a). Due to Lenz's Law, the  $V_{Drain}$  at the drain of power MOSFET jumps from zero to  $V_{IN}+nV_O$ . At this moment, the secondary current decreases toward zero, the parasitic capacitance  $C_{DS}$  at the  $V_{Drain}$  starts to discharge the stored charges to the  $L_m$  and induce voltage resonance at the  $V_{Drain}$ . Resonant effect with resonant frequency determined by  $C_{DS}$  and  $L_m$  is reflected to the auxiliary side simultaneously. To reduce switching loss, the optimum turn-on time happens at the valley of the  $V_{Drain}$  due to near zero voltage switching. Thus, the valley voltage detection of the resonant effect can determine the next turn-on of the power MOSFET.

In case of large output load current, the first valley is an optimum selection to rapidly deliver energy to the output owing to minimum off-time. Theoretically, the switching loss dominates the total power loss in case of small output load current. That is to say the first valley is not the optimum selection at light loads. The dynamic frequency technique selects one of the valleys according to the output load current for reducing switching frequency and switching power loss. In other words, in this technique, dynamic off-time control can be derived by the valley selection at different loads when the output load current decreases from large to small as illustrated in Fig. 20 (b).

At the CV stage, the error signal  $V_{ERR_V}$  is used to control the primary side current  $I_P$  so as to gradually decrease the output charging current  $I_O$ . If the output current continues to decrease, the switching frequency will locally increase in Fig. 20 (b) due to the decrease of the on-time if assuming that one of the valleys is selected; for example, the 2<sup>nd</sup> valley in Fig. 20 (c)) is selected. In other words, the selection of the valley can't continuously change from one valley to the other valley owing the quantization error at the valley selection. Once the valley selection is changed to the sequent next one, the switching frequency will have an instant decrease to further reduce the switching power loss. The local increase of the switching frequency won't result in large switching power loss. Contrarily, the instant decrease of the switching frequency caused by the change of the valley can greatly improve the efficiency.

In summary, the trend of the switching frequency is decreasing when output charging current decreases. Simultaneously, the resonant amplitude becomes smaller because of the parasitic resistance at the resonant path. Gradually decreased resonant voltage may result in the failure of the valley voltage detection. That is to say, for safety the next on-time needs to be triggered by another mechanism. Thus, the green mode is proposed to set the off-time a constant value for ensuring the correct operation of the converter and further improving efficiency at ultra-low current. Besides, the charging current won't have over-current since the maximum current is limited by the CC regulation for system.





Fig. 20. (a) The operation of the dynamic frequency technique. (b) The switching frequency versus the output current. (c) The slight variation of the switching frequency if one of the valley voltages is selected.

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# **Chapter 4**

### **The Proposed KVD Technique**

The proposed KVD technique includes the current calculator, the KVD circuit, and the self-calibrator. Section 4.1 introduces the current calculator circuit. Section 4.2 introduces the KVD circuit. To improve the accuracy of the KVD circuit, the self-calibrator is implemented in Section 4.3 with a complete operation of the CV stage. Finally, the system stability is described in Section 4.4.

### 4.1 The Current Calculator

The current calculator circuit as illustrated in Fig. 21(a) is used to calculate the average output current according to the derivation of (12). To ensure the constant current of the CC stage is defined by the  $V_{REF_I}$ , the  $V_I$  is derived as (18) and regulated to the  $V_{REF_I}$  in the CC loop where the ratio of  $k_3$  to  $k_2$  is the ratio of the current mirror  $M_3$  to  $M_2$ .

$$V_{I} = I_{charge} \times \frac{T_{DIS}}{C_{2}} \text{ where } I_{charge} = \frac{V_{CS,PK}}{R_{1}} \times \frac{k_{3}}{k_{2}}$$
(18)

Here, the peak current is indicated by the  $V_{CS,PK}$ , which can be determined and hold by the capacitor  $C_1$  if the  $V_{PWM}$  changes from high to low. The discharging time  $T_{DIS}$  is used to determine how long the capacitor  $C_2$  is charged by the  $I_{charge}$ , which is converted from the  $V_{CS,PK}$ . Thus, the value of the  $V_{CH}$  on the  $C_2$  is proportional to the product of the  $V_{CS,PK}$  and the  $T_{DIS}$ . At the end of discharging time, the sample-and-hold signal pulse  $V_{SHI}$  is triggered by the  $T_{DIS}$  to capture the  $V_{CH}$  as the  $V_I$ . After that, the  $V_{CH}$  is reset to zero by another one-shot signal  $V_{DIS}$  and ready for next switching cycle. To use the  $V_I$  to indicate the output average current  $I_{O,avg}$ , it is necessary to force (18) to be equal to (12). Then, (19) can be derived.

$$\frac{1}{R_1} \times \frac{k_3}{k_2} \times \frac{1}{C_2} = \frac{1}{2 \times T_S} \times \frac{1}{R_{CS}} \times \frac{N_P}{N_S}$$
(19)

Therefore, the selection of the values of  $R_1$ ,  $C_2$ ,  $k_2$  and  $k_3$  should follow the equation of (19). As a result, in the CC loop, the  $V_1$  can be regulated to the reference voltage  $V_{REF_1}$ , which indicates the desired output constant current. Fig. 21 (b) shows the timing diagrams of the current calculation circuit.



Fig. 21. (a) The current calculator circuit. (b) The timing diagrams.

#### 4.2 The Implementation of Knee Voltage Detector

The KVD circuit as illustrated in Fig. 22 is used to accurately track the knee point of auxiliary winding voltage for getting the output voltage without being affected by the diode forward voltage in the CV regulation. The  $V_{DET}$  is the scaled-down value of the  $V_A$  by the voltage divider and its minimum value is clamped to zero. Two delayed signals  $V_D$  and  $V_{DI}$  are derived by passing the  $V_{DET}$  through different RC circuit. Thus, the time constant of  $R_2C_2$  for the  $V_{DI}$  is two times that of  $R_1C_1$  for the  $V_D$ . The delay time of the  $V_{DI}$  is larger than that of the  $V_D$  as shown in Fig. 22 (b). Two subtractors in Fig. 22 (a) are used to calculate the difference between the  $V_D$  and the  $V_{DET}$  and the difference between the  $V_D$  and the  $V_{DI}$  during the off-time period. **Owing to the usage of RC delay, the function of the subtractor can be seen as a slope calculator to detect the knee voltage.** 



(a)



Fig. 22. (a) The KVD circuit. (b) Timing diagrams of the KVD technique.

The schematic of the subtractor is depicted in Fig. 23. Two voltage-to-current (V-to-I) converters are applied to convert two input signals  $V_L$  and  $V_S$  into two current signals. After the operation of three current mirrors,  $M_3 \sim M_8$ , the difference between the  $V_S$  and the  $V_L$  is converted to the difference current  $I_{diff}$ . Then, converting the  $I_{diff}$  to the  $V_{diff}$  in (20) by the resistor  $R_3$  can amplify the difference signal.

$$V_{Diff} = \begin{cases} \left(\frac{V_L}{R_2} - \frac{V_S}{R_1}\right) \times R_3 & \text{if } V_L > V_S, \\ 0 & \text{if } V_L \le V_S \end{cases}$$
(20)

Two outputs,  $V_1$  and  $V_2$ , from the two subtractors indicate the difference between the  $V_D$ and the  $V_{DET}$  and the difference between the  $V_D$  and the  $V_{DI}$ . By subtracting  $V_{DET}$  from  $V_D$  and  $V_D$  from  $V_{DI}$ , we can obtain  $V_1$  and  $V_2$ .

The  $V_2$  is larger than the  $V_1$  in the beginning time when the  $I_S$  starts to discharge to the output. At the end of discharging time, the  $V_{DET}$  will start to have the resonant effect. The difference between the  $V_D$  and the  $V_{DET}$  starts to rise. After more delay time, the  $V_2$  start to rise, too. When the  $V_1$  is equal to the  $V_2$ , the sample-and-hold signal  $V_{SH}$  will capture the  $V_D$  as the

 $V_V$ . The  $V_2$  can be seen as an adaptive reference to compared to the  $V_1$ . Because the relationship between the  $V_1$  and the  $V_2$  is a relative value, whatever the slope value of  $V_{DET}$  is,  $V_{SH}$  still can sample an accurate knee voltage.

On the other hand, the  $V_1$  and the  $V_2$  may have no crossing point under two conditions. One of the conditions when system is in startup, the output voltage is still very low. It causes the amplitude of  $V_{DET}$  in resonant period  $T_{RE}$  is quite small. That also makes the amplitude of  $V_1$  and  $V_2$  too small to determine  $V_{SH}$ . Another condition occurs when  $V_0$  is very close to regulation voltage. It causes the on time and discharge time becomes very short. That makes the  $V_D$  and  $V_{DI}$  are still on the rise when discharge time is over. It also causes  $V_1$  and  $V_2$  cannot determine  $V_{SH}$  correctly. The calibrated voltage  $V_{CA}$  is used to calibrate these errors and substitute the role of the reference voltage to decide one suitable signal  $V_{SH}$ .



Fig. 23. The circuit of subtractor.

### 4.3 The Implementation of Self-Calibrator

The self-calibrator is used to detect the knee voltage if the KVD circuit fails to get an accurate knee voltage. The sequence of the  $V_{PK}$  and the  $V_{PKI}$  will affect the value of the  $V_V$ .

To avoid some conditions that the  $V_{PK1}$  triggers the  $V_{SH}$  prior to the  $V_{PK}$ , the state machine is depicted as a flow chart in Fig. 24. Here, the n<sup>th</sup> cycle value of the  $V_{CA}$  is remarked as the  $V_{CA,n}$ . During the on-time period, the  $V_{CA}$  will keep the previous value and the values of the  $V_{PK}$  and the  $V_{PKI}$  are reset. The estimation period of the knee voltage is started in the beginning of the off-time and ended by the  $V_{END}$ , which is triggered by first valley of the  $V_{DET}$ . Changing the value of the  $V_{CA}$  based on different mode, precise CV regulation can be obtained. In this work, four modes are defined. When the  $V_{PK}$  and the  $V_{PK1}$  are all zero during the estimation period, it indicates the  $V_{SH}$  cannot change from low to high since the cross point between the  $V_1$  and the  $V_2$  doesn't happen and the  $V_{CA}$  is too high. This is the Mode-1 and the  $V_{CA}$  will be discharged in next sequent cycle to minimize the error. Another error may happen when the  $V_{PK1}$  is triggered prior to the  $V_{PK}$  because the  $V_{CA}$  is too low. When the  $V_{PK1}$  is triggered first, it leads the state machine into Mode-3. If the  $V_{PK}$  is still not triggered after the state is switched into Mode-3, it means that error is correctly fixed by the  $V_{CA}$ . The  $V_{CA}$  will not be changed in next sequent cycle. Contrarily, if the  $V_{PK}$  is triggered in Mode-3, the state will be switched into Mode-4. It means that the  $V_{CA}$  is too low and the  $V_{PKI}$  is triggered prior to the  $V_{PK}$ . In the next sequent cycle, the  $V_{CA}$  be charged to avoid the error.



Fig. 24. Flow chart with state machine of Self-Calibrator.

The self-calibrator circuit is shown in Fig. 25 (a) and corresponding waveforms in different mode is also shown in Fig. 25 (b). Then state machine determines the modes and sends the addition result,  $V_{ADD}$ , or the subtraction result,  $V_{SUB}$ . The up/down counter receives the result and sends out a 3-bits control signal. The 3-bits signal is used to control the switch of current sources to adjust the  $V_{CA}$ . Fig. 26 shows the up/down counter, which is composed of a 3-bits binary adder. It can add or subtract the result of (S1, S2, S3) one bit a time. Besides, there is another overflow limiting circuit to ensure the range of (S1, S2, S3) is from (0, 0, 0) to (1, 1, 1).



Fig. 26. Up/down counter.

### 4.4 The Stability of the System

Fig. 27 (a) shows an equivalent small signal model based on the architecture in Fig. 10 (b) and Fig. 15. The close loop can be divided into two parts, control-to-output transfer function,  $G_{CO}$ , and output-to-control transfer function,  $G_{OC}$ , [16]-[20]. As depicted in Fig. 27 (b), the  $I_{S,avg}$  is the average value of the secondary-side current  $I_S$  within one switching cycle as shown in (21). The switching period can be written as the function of error signal  $V_{ERR_V}$  as shown in (22), where K and C are constant values. The value of discharging time  $T_{DIS}$  depends on the current peak value  $I_{S,PK}$  and the discharging slope  $\frac{L_m}{V_O \cdot N_1^2}$  as shown in (23). Also secondary current peak value  $I_{S,PK}$  can be substituted for the relationship with input voltage  $V_{IN}$  and error signal  $V_{ERR_V}$  as shown in (24) (25). The  $I_{S,avg}$  can be expressed as the function of the output voltage  $V_O$ , error signal  $V_{ERR_V}$ , the inductor  $L_m$  and the sensing resistor  $R_{CS}$  in (26).

$$I_{S,avg} = \frac{\frac{1}{2} \times (T_{DIS} \times I_{S,PK})}{\frac{1}{f}(V_{ERR_V})}$$
(21)  
$$f(V_{ERR_V}) = K \cdot V_{ERR_V} + C$$
(22)  
$$T_{DIS} = I_{S,PK} \times \frac{L_m}{V_o \cdot N_1^2}$$
(23)  
$$I_{S,PK} = \frac{V_{IN}}{L_m} \cdot T_{ON} \cdot N_1$$
(24)  
$$T_{ON} = V_{ERR_V} \times \frac{L_m}{V_{IN}} \times \frac{1}{R_{CS}}$$
(25)

$$f(V_{ERR_V}) = K \cdot V_{ERR_V} + C$$
(22)

$$T_{DIS} = I_{S,PK} \times \frac{L_m}{V_o \cdot N_1^2}$$
(23)

$$I_{S,PK} = \frac{V_{IN}}{L_m} \cdot T_{ON} \cdot N_1 \tag{24}$$

$$V_{DN} = V_{ERR_V} \times \frac{L_m}{V_{IN}} \times \frac{1}{R_{CS}}$$
(25)

$$I_{S,avg} = \frac{\left(K \times V_{ERR_V}^{3} + C \times V_{ERR_V}^{2}\right) \times L_m}{2 \times V_O \times R_{CS}^{2}}$$
(26)

The averaged secondary-side current is, in general, a nonlinear function of the converter voltages and currents. Linearization at the quiescent operating point can derive the small ac current variation of the secondary-side as expressed in (27).

$$\hat{I}_{S,avg} = a_1 \cdot \hat{V}_{ERR_V} + a_2 \cdot \hat{V}_O \text{ where } \begin{pmatrix} a_1 = \frac{\partial I_{S,avg}}{\partial V_{ERR_V}} = \frac{3K \cdot V_{ERR_V}^2 \cdot L_m}{2 \cdot V_O \cdot R_C^2} \\ a_2 = \frac{\partial I_{S,avg}}{\partial V_O} = \frac{-K \cdot V_{ERR_V}^3 \cdot L_m}{2 \cdot V_O^2 \cdot R_C^2} \end{pmatrix}$$
(27)

The output voltage  $V_O$  is the product of the averaged secondary-side current  $I_{S,avg}$  and the output impedance  $Z_O$  which includes the output capacitor and equivalent output loading. The small ac current variation at the secondary-side flowing through the impedance  $Z_O$  determines the perturbation of  $V_O$  as expressed in (28). Therefore, the control-to-output transfer function  $G_{CO}(s)$  is depicted in (29), which simply contains one zero and one pole. The  $C_O$  and its equivalent series resistor (ESR)  $R_{esr}$  contribute one ESR zero at high frequencies. And the pole can be seen as the combination of  $C_O$  and the equivalent loading resistance  $R_L$ .

$$\hat{V}_{o} = \hat{I}_{s,avg} \cdot Z_{o} = \left(a_{1} \cdot \hat{V}_{ERR_{v}} + a_{2} \cdot \hat{V}_{o}\right) \cdot Z_{o}$$
(28)  
$$G_{Co} = \frac{\hat{V}_{o}}{\hat{V}_{ERR_{v}}} = \frac{Z_{o} \cdot a_{1}}{1 - Z_{o} \cdot a_{2}} = \frac{a_{1}}{1/R_{L} - a_{2}} \cdot \frac{1 + s \cdot C_{o} \cdot R_{esr}}{1 + \frac{s \cdot C_{o} \left(1 + R_{esr} \left(1/R_{L} - a_{2}\right)\right)}{1/R_{L} - a_{2}} \right)$$
(29)

As illustrated in Fig. 29(a), the transconductance of error amplifier *EA* is  $g_m$ . Thus, the output-to-control transfer-function  $G_{CO}(s)$  can be derived in (30).

$$G_{oc}(s) = \frac{\hat{V}_{ERR_{-V}}}{\hat{V}_{o}} = N_2 \times \frac{R_{A2}}{R_{A1} + R_{A2}} \times g_m \times \frac{R_C}{1 + sR_CC_C}$$
(30)

0

Hence, the transfer function  $G_{OC}(s)$  that contains one pole is used to compensate the zero in  $G_{CO}(s)$  should as pole-zero cancellation by choosing appropriate passive components. Thus, the pole in  $G_{CO}(s)$  is the dominant pole of the whole system. After the compensation, the system becomes the one-pole system and bandwidth is designed far away from the switching frequency.



Fig. 27. (a) Equivalent small signal model of the proposed PSR in CV regulation. (b) Waveforms of the dynamic frequency technique.

# Chapter 5

# Simulation Results,

The proposed PSR charger with the KVD technique was implemented in  $0.5\mu$ m 500V UHV process. The chip micrograph with an active area of 4 mm<sup>2</sup> is shown in Fig. 28. TABLE III is the design specification of PSR. The switching frequencies are 42 kHz and 1 kHz for CC stage and green mode, respectively. Besides, the switching frequency gradually decreases in CV stage if the output voltage is slowly regulated to 5V.



Fig. 28. Chip micrograph.

TABLE III	Design	Specifica	tions
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Technology	0.5µm 500V UHV
Input line voltage range $(V_{AC})$	90 V~264V(rms)
<i>Output voltage</i> $(V_O)$	1.5V~5V

Output current $(I_O)$	0A~1A
Primary side inductance $(L_P)$	2.3mH
Primary winding turns $(N_P)$	132T
Secondary winding turns $(N_S)$	<i>11T</i>
Auxiliary winding turns $(N_A)$	28T
Switching frequency (f <sub>SW</sub> )	1KHz~42kHz

In this chapter, the simulation results are shown in Section 5.1. The comparison with the prior arts is shown in Section 5.2. 

### **5.1 Simulation Results**

Fig. 29 shows the simulation results when the PSR operation is in the DCM. The primary-side and the secondary-side currents of the transformer  $I_P$  and  $I_S$  are with the triangular sharp. The  $V_{DET}$  has the resonant effect when the discharging time is over. In CC regulation, the calculated current value  $V_I$  must be a constant as shown in Fig. 30. The  $V_{CS}$  is sampled as the  $V_{CS,PK}$  when the  $V_{PWM}$  changes from high to low. Thus, the  $V_I$  can be derived by the charging result signal  $V_{CH}$  in the end of the discharging time  $T_{DIS}$ .



#### Fig. 29. Simulation results of the PSR operation in the DCM.



The KVD operation is also shown in Fig. 31.

Discharging time can be determined by comparing the  $V_V$  and the  $V_{DET}$ . The  $V_{DET}$  and two delayed signals  $V_D$  and  $V_{D1}$  are sent to two distinct subtractors to calculate the difference between the  $V_1$  and the  $V_2$ .

Using the  $V_1$  and the  $V_2$  can determine the timing of sample-and-hold signal  $V_{SH}$  by comparing  $V_1$  to  $V_2$  and  $V_1$  to  $V_{CA}$ . The comparison result is  $V_{PK}$  and  $V_{PK1}$  are sent into the self-calibrator circuit to decide the sequent operation mode.

Fig. 32 shows different conditions in the self-calibrator. When the  $V_{PK1}$  is prior to the  $V_{PK}$  as shown in Fig. 32 (a), the state machine will send out  $V_{ADD}$  to charge the value of the  $V_{CA}$ . It can let the sample-and-hold signal  $V_{SH}$  controlled by the  $V_{PK}$ . Another situation is the operation changes from Mode 2 to Mode 4 when the output voltage is close to the regulation voltage as depicted in Fig. 32 (b). Because the non-ideal RC circuit is not only affected by the

delay effect but also has the signal distortion. Furthermore, discharging time becomes small when the  $V_0$  is close to regulation voltage. The distortion will let the  $V_D$  and the  $V_{D1}$  need enough time to be sampled as two delayed signals. If the discharging time is not enough for sampling the  $V_D$  and the  $V_{D1}$ , the  $V_1$  and the  $V_2$  cannot have an obvious cross point. In other words, another decision signal  $V_{CA}$  is utilized to improve the accuracy when the previous decision method fails. At this time, the state machine will be switched into Mode 3, but the KVD circuit can continuously sample the knee voltage.



Fig. 31. Simulation results of the KVD technique.

m

ΠΠ



Fig. 32. (a) Self-Calibrator in Mode 2 to Mode 4 (b) Self-Calibrator form Mode 2 to Mode 3.

The proposed PSR's output voltage is designed from 1.5V to 5V. When the  $V_O$  is close to 5V, the voltage loop's error signal  $V_{ERR_V}$  is low enough for the  $V_{CS}$  to trigger the  $V_{CV}$  to decide the on-time value. Fig. 33 (a) shows the transition from the CC to the CV. In CV regulation, the valley selection mode is used. Every switching cycle in the CV stage select one of the

resonant valleys according to the loading condition. Simultaneously, the  $V_{ERR_V}$  is used to determine which one is the better solution from all resonant valleys. Lower the  $V_{ERR_V}$  is, lower switching frequency is since more valleys are selected. As a result, the CV regulation operates with a dynamic frequency as shown in Fig. 33 (b).



Fig. 33. (a) PSR Operation Changing from CC to CV. (b) Dynamic Frequency in CV

Regulation.

Whole the charging sequence is shown in Fig. 34. The  $V_O$  is charged from 1.5V to 5V. The  $V_I$  is a constant value in the CC regulation and the  $V_V$  is also constant in CV regulation. Two error signals illustrate the situation of voltage and current information. The CV stage is divided into two modes. One is valley selection mode and different valley is selected to decide different switching frequency due to the varied  $V_{ERR_V}$ . When the  $V_{ERR_V}$  is low enough, the CV regulation will be switched into the green mode for further reducing switching frequency.



Fig. 34. Charging Sequence of PSR.

### **5.2** Comparison with the Prior Arts

Fig. 35 is the statistical chart of the knee voltage corresponded to the output voltage. The KVD has an initial value of 0.6V when the system starts up. When the output voltage reaches to about 2V, the ideal knee voltage is 0.69V and the KVD technique starts to work. Through

the self-calibration, the knee voltage can be close to an ideal value when the output voltage is 5V. The difference between ideal and simulation values when the output voltage around 5V is 0.01V. As a result the control of the transition from the CC to the CV will be perfect.



# **Chapter 6**

# **Conclusions and Future Works**

### 6.1 Conclusions

To achieve isolated charger for high input voltage, PSR is proposed to apply for this application. But the most difficult to design PSR is how to sensing the correct value of output voltage. In other words, the knee voltage must be found in each cycle. The KVD technique with the self-calibrator is proposed to find precise knee voltage. The current calculator is also used to regulate the current loop. In the CV regulation, the switching frequency is adaptive according to the valley selection mode or the green mode to improve the efficiency.

### **6.2 Future Works**

The thesis proposed a technique to realize the isolated charger. However, the constant current regulation is still operating in constant frequency. The ZVS cannot apply in constant frequency. It will make the efficiency poor than that of the CV regulation due to the constant switching frequency. How to imply ZVS to CC regulation becomes an interesting topic.

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