

# Triplet quantum chain process in the photoisomerization of 9-*cis* retinal as revealed by nanosecond time-resolved infrared spectroscopy

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## ARTICLE INFO

### Article history:

Received 1 March 2010

Received in revised form 20 April 2010

Accepted 20 April 2010

Available online 28 April 2010

### Keywords:

Triplet quantum chain

Photoisomerization

9-*Cis* retinal

Nanosecond time-resolved infrared spectroscopy

Photodynamics

## ABSTRACT

The mechanism of the photoisomerization of 9-*cis* retinal has been studied by nanosecond time-resolved infrared spectroscopy. A cyclohexane solution of 9-*cis* retinal was photoexcited at 349 nm and the subsequent photodynamics were traced. A singular value decomposition (SVD) analysis of the time-resolved infrared data shows that there are two distinct isomerization pathways. One is the triplet pathway that takes place in the picosecond time regime from 9-*cis* to all-*trans*. The other involves the energy transfer between the all-*trans* triplet state and the 9-*cis* ground state with the resultant 9-*cis* triplet state subsequently reproducing the all-*trans* by fast isomerization on the triplet potential surface. This quantum chain process occurs in the microsecond time regime.

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## 1. Introduction

Retinal has four C=C double bonds that give rise to the four mono-*cis* isomers, the 7-*cis*, 9-*cis*, 11-*cis* and 13-*cis* forms. These isomers undergo *cis*–*trans* isomerization upon photoexcitation. Photoisomerization of retinyl chromophores has been extensively studied in relation to their functions as the photo-receptors in retinoid proteins like rhodopsin and bacteriorhodopsin [1]. Photoisomerization of the retinal molecule itself is also of considerable interest as a prototype unimolecular chemical reaction. A characteristic feature is known for the photoisomerization of retinal in organic solvents. The photoisomerization efficiency is not symmetrical with respect to *cis* and *trans*; the quantum yield of photoisomerization is much higher in the *cis* to *trans* direction than in the *trans* to *cis* [2–4]. This asymmetry is not found for many of ethylene derivatives in which the photoisomerization efficiency is similar for the *trans* to *cis* and the *cis* to *trans* directions [5].

The origin of this asymmetry in the photoisomerization of retinal was elucidated with time-resolved spectroscopies. Transient Raman spectroscopy first showed that the photoexcitation of the 7-*cis*, 9-*cis*, 11-*cis* isomers generated an identical transient Raman spectrum that was assigned to the all-*trans* triplet state. It was considered that isomerization of 7-*cis* (or 9-*cis*, 11-*cis*-) to all-*trans*

took place on the lowest triplet potential surface (one-way photoisomerization) [6]. Picosecond time-resolved absorption spectroscopy then showed that the 9-*cis*  $T_1$  species isomerizes to all-*trans* in sub-nanosecond time regime [7]. Picosecond 2D-CARS and femtosecond absorption experiments clarified that the 9-*cis* to all-*trans* conversion time was 880 ps on the triplet potential surface [8,9]. The photoisomerization of all-*trans* retinal was studied with nanosecond time-resolved infrared spectroscopy [10]. It was found that, immediately after photoexcitation, the all-*trans*  $T_1$  state was generated within the time resolution of the system and decayed to the all-*trans*  $S_0$  state with no isomerization. It was also found that a very fast isomerization pathway existed from the all-*trans* to 13-*cis*/9-*cis* via the excited singlet state. Femtosecond ultraviolet–visible absorption spectroscopy clearly showed that this all-*trans* to mono-*cis* photoisomerization took place via the  $S_2$  state [11,12]. These time-resolved spectroscopic studies have clearly showed that the *cis* to *trans* photoisomerization of retinal proceeds predominantly on the excited triplet potential surface but that the *trans* to *cis* proceeds via the second excited singlet state. The *cis*–*trans* asymmetry originates from the different pathways of the photoisomerization.

Another mechanism that favors the *cis* to *trans* isomerization of retinal is the triplet quantum chain process, in which the *trans* excited triplet state generated from the *cis* by the one-way isomerization reacts with the ground state *cis* molecule to generate the *cis* excited triplet state and the *trans* ground state. The *cis* excited triplet state thus formed further isomerizes on the triplet potential

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surface to the *trans*. The possibility of this triplet quantum chain process has been pointed out from the concentration dependence of the quantum yield of photoisomerization [4,13,14]. In the present paper, we use time-resolved infrared spectroscopy to directly monitor the triplet quantum chain process in the photoisomerization of 9-*cis* retinal.

## 2. Experimental

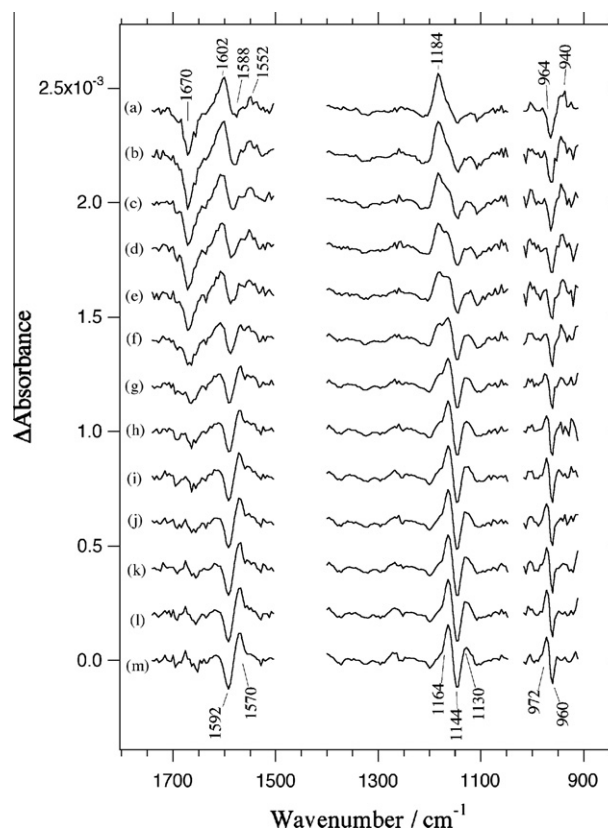
The experimental arrangements for AC-coupled nanosecond time-resolved infrared spectroscopy with a dispersive spectrometer (JASCO TRIR-1000) have been described in detail in previous papers [15–17]. A photovoltaic MCT detector (Kolmar Technologies, Inc. KV103-1-A-1-SMA) was used for fast infrared detection. The time resolution was about 50 ns. Signals from the MCT detector are first amplified with a preamplifier and then averaged on a digital oscilloscope (Tektronix DSA602). A sampling rate of data acquisition was every 40 ns for the experiments described here. The third harmonic of a cw Q-switched Nd:YLF Laser (Spectra Physics TFR, 5 ns pulse width, 190 Hz repetition rate, 30 mJ) at 349 nm) was used for photoexcitation. Infrared absorption spectra were obtained at intervals of  $4\text{ cm}^{-1}$  with a spectral resolution of  $16\text{ cm}^{-1}$ . A cyclohexane solution of retinal was circulated with peristaltic pump to eliminate the influence of the photoisomerization products. A flowing sample cell with two BaF<sub>2</sub> windows was used. Solutions were bubbled with argon gas during the measurements in order to eliminate the effect of oxygen. Samples of all-*trans*-retinal and 9-*cis*-retinal were purchased from Sigma and used as received. Cyclohexane was purchased from Wako Pure Chemical Industry, Ltd. and used without further purification. All measurements were carried out at room temperature.

## 3. Results and discussion

### 3.1. Time-resolved infrared difference spectra

Time-resolved infrared difference spectra of photoexcited 9-*cis* retinal in cyclohexane (3.5 mM) are shown in Fig. 1. These difference spectra, which correspond to the light-on minus light-off signal, were obtained directly with the AC-coupled method [15–17]. Spectra were averaged over the delay time ranges shown in the caption. The wavenumber regions around  $1450\text{ cm}^{-1}$  and  $1030\text{ cm}^{-1}$  were blocked by the strong absorption bands of cyclohexane. Negative peaks at 1670, 1588, 964  $\text{cm}^{-1}$  show the depletion of 9-*cis* retinal in the ground state by the photoexcitation. Positive peaks at 1602, 1552, 1184 and 940  $\text{cm}^{-1}$  represent the production of transient species. After the delay of 18  $\mu\text{s}$  (Fig. 1m) the observed difference spectrum shows no further temporal change. The difference spectrum after 18  $\mu\text{s}$  is identical with the difference spectrum between the all-*trans* isomer and the 9-*cis* isomer in the ground state. The negative peaks at 1592, 1144, and 960  $\text{cm}^{-1}$  are ascribed to 9-*cis* S<sub>0</sub>. The positive peaks at 1570, 1164, 1130, and 972  $\text{cm}^{-1}$  are ascribed to all-*trans* S<sub>0</sub>. It is thus indicated that the photoexcitation of 9-*cis* retinal in cyclohexane solution causes the photoisomerization to the all-*trans* isomer.

Temporal profiles of the signal observed at four different wavenumbers are shown in Fig. 2. The best fit of those curves with the single exponential function convoluted with the instrumental response are shown as solid lines in Fig. 2. A global fitting analysis of these curves gives a single time constant of 5  $\mu\text{s}$ . The positive peaks at 1184  $\text{cm}^{-1}$  (Fig. 2c) and 1600  $\text{cm}^{-1}$  (Fig. 2d) are assigned to the all-*trans* triplet state [10]. They show instantaneous rise and along with decay with the time constant of 5  $\mu\text{s}$ . The response of the present time-resolved infrared apparatus is not sufficient to



**Fig. 1.** Time-resolved infrared difference spectra of photoexcited 9-*cis* retinal in cyclohexane. (a) 0 ns–0.4  $\mu\text{s}$ , (b) 0.4  $\mu\text{s}$ –0.8  $\mu\text{s}$ , (c) 0.8  $\mu\text{s}$ –1.2  $\mu\text{s}$ , (d) 1.2  $\mu\text{s}$ –1.6  $\mu\text{s}$ , (e) 1.6  $\mu\text{s}$ –2  $\mu\text{s}$ , (f) 2  $\mu\text{s}$ –4  $\mu\text{s}$ , (g) 4  $\mu\text{s}$ –6  $\mu\text{s}$ , (h) 6  $\mu\text{s}$ –8  $\mu\text{s}$ , (i) 8  $\mu\text{s}$ –10  $\mu\text{s}$ , (j) 10  $\mu\text{s}$ –12  $\mu\text{s}$ , (k) 12  $\mu\text{s}$ –14  $\mu\text{s}$ , (l) 14  $\mu\text{s}$ –16  $\mu\text{s}$  and (m) 16  $\mu\text{s}$ –18  $\mu\text{s}$ .

resolve the fast rise (880 ps) of the all-*trans* triplet state from the 9-*cis*.

The negative band at  $1144\text{ cm}^{-1}$  (Fig. 2a) represents the depletion of 9-*cis* retinal in the ground state. Neither all-*trans* T<sub>1</sub> nor all-*trans* S<sub>0</sub> show a band at  $1144\text{ cm}^{-1}$ . The temporal profiles of this band observed for three different concentrations are shown in Fig. 3. The signal can be separated into two temporal components. One is the instantaneous decrease of the signal (denoted as I<sub>1</sub> in the trace Fig. 3a), which is ascribed to the instantaneous depletion of 9-*cis* S<sub>0</sub> by the photoexcitation. The other is denoted as I<sub>2</sub> in the trace Fig. 3b, which is ascribed to the delayed depletion of 9-*cis* S<sub>0</sub> in the microsecond time regime. The second component suggests that there is a pathway that consumes the ground state of 9-*cis* retinal in the microsecond regime. The contribution of the I<sub>2</sub> component to the whole amount of the 9-*cis* S<sub>0</sub> depletion depends on the concentration of retinal. At a high concentration (Fig. 3a, 3.2 mM), the amplitude of I<sub>2</sub> is comparable to that of I<sub>1</sub>. At a low concentration (Fig. 3c, 0.28 mM), the amplitude of I<sub>2</sub> becomes negligible. The intensity of the  $1144\text{ cm}^{-1}$  band decreases at the rate of 5  $\mu\text{s}$ , which is the same as that of the decay of all-*trans* T<sub>1</sub>. This fact indicates that an interaction between the 9-*cis* S<sub>0</sub> and all-*trans* T<sub>1</sub> is involved in the photoprocess.

### 3.2. SVD analysis

The time-resolved infrared difference spectra shown in Fig. 1 have been analyzed with the singular value decomposition (SVD) method. The decomposed spectral and temporal components obtained are shown in Fig. 4 for the largest four singular values, which are 0.00952, 0.00463, 0.00170, 0.00166. It is obvious from

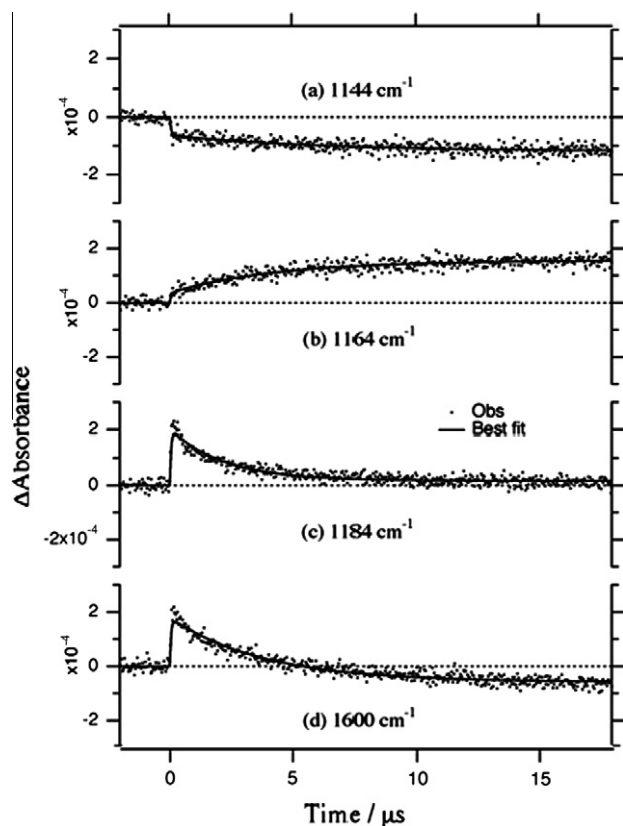


Fig. 2. Temporal profiles observed at 1144  $\text{cm}^{-1}$  (a), 1164  $\text{cm}^{-1}$  (b), 1184  $\text{cm}^{-1}$  (c) and 1600  $\text{cm}^{-1}$  (d). The dotted lines show the observed signals and the solid lines show best fits with exponential functions.

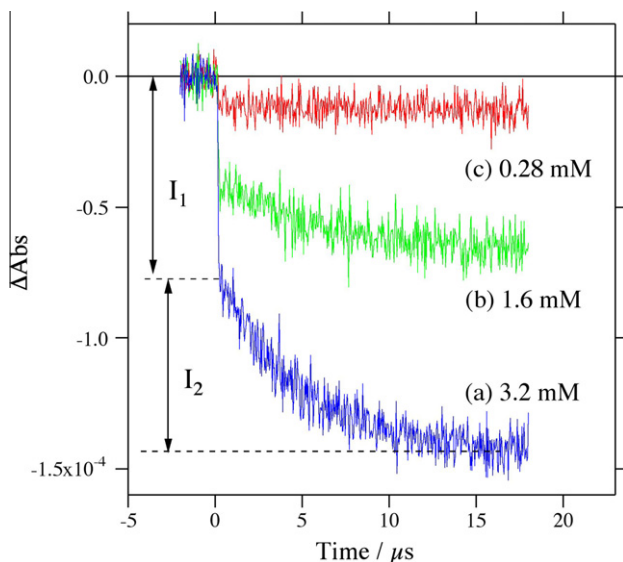


Fig. 3. Decay curves observed at 1144  $\text{cm}^{-1}$  for three different concentrations of retinal. (a)  $3.2 \times 10^{-3}$  M, (b)  $1.6 \times 10^{-3}$  M, (c)  $2.8 \times 10^{-4}$  M.

the figure that two of the four components (Fig. 4a and b for the spectrum, and Fig. 4e and f for the temporal profile) are dominant and that the third and the fourth components contain no meaningful features. Thus, the third and fourth components are discarded in the following analysis.

Because SVD itself is a pure mathematical operation, only appropriate linear combinations of the components are physically

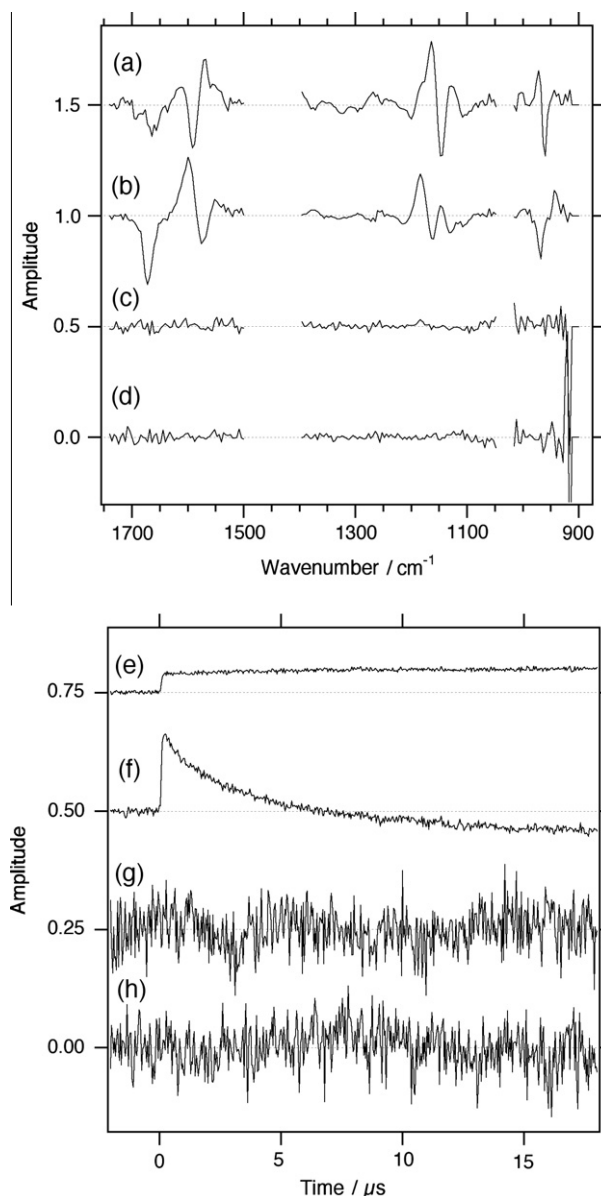


Fig. 4. Spectral components (a, b, c, d) and temporal components (e, f, g, h) obtained by the SVD analysis. The components correspond to the largest four singular values are shown in the descending order from the top to bottom.

meaningful. In general, a time-resolved spectroscopic data matrix  $\mathbf{A}$  consisting of  $N$  independent spectral components is written as a linear combination of the product of  $\mathbf{u}_k$  and  $\mathbf{v}_k$ , where  $\mathbf{u}_k$  is a column vector representing a temporal profile and  $\mathbf{v}_k$  is a row vector representing a spectral component.

$$\mathbf{A} = \sum_{k=1}^N w_k \mathbf{u}_k \cdot \mathbf{v}_k \quad (1)$$

Here,  $\mathbf{u}_k$  and  $\mathbf{v}_k$  are normalized and the coefficient  $w_k$  denotes the singular value. The operator dot represents the outer product of two vectors. If only two of the decomposed components are dominant and the rest of the components are discarded as noise, the time-resolved infrared data matrix  $\mathbf{A}$  is approximated as:

$$\mathbf{A} \approx w_1 \times \mathbf{u}_1 \cdot \mathbf{v}_1 + w_2 \times \mathbf{u}_2 \cdot \mathbf{v}_2. \quad (2)$$

There are two possible photoisomerization pathways for photoexcited 9-*cis* retinal. One is the known pathway that proceeds on the excited triplet potential; the excited triplet state of 9-*cis* retinal

isomerizes to the all-*trans* isomer with the time constant of 880 ps [8]. The other pathway is via the excited singlet state. The excited singlet state of 9-*cis* retinal might well isomerize to the excited singlet state of all-*trans* isomer, which subsequently relaxes either to all-*trans*  $T_1$  or to all-*trans*  $S_0$  in the picosecond regime [9]. The time resolution of the present experiment is about 50 ns. Consequently, the first pathway via the triplet manifold is expected to give an instantaneous rise of the all-*trans*  $T_1$  signal followed by a decay in the microsecond time regime. The latter pathway is expected to give an instantaneous rise of the signal of all-*trans*  $T_1$  and/or all-*trans*  $S_0$ . The temporal behavior of the signal at 1144  $\text{cm}^{-1}$  indicates that the depletion of 9-*cis*  $S_0$  proceeds also with the time constant of 5  $\mu\text{s}$  and this process has to be included in the photodynamics. Thus, the following five kinetics are assumed to describe the temporal behavior of the time-resolved spectra. (1) The instantaneous rise of all-*trans*  $T_1$  and its decay with the time constant of 5  $\mu\text{s}$ . (2) The instantaneous rise of all-*trans*  $T_1$  and all-*trans*  $S_0$ . (3) The instantaneous depletion of 9-*cis*  $S_0$  by the photoexcitation. (4) The growth of all-*trans*  $S_0$  with the time constant of 5  $\mu\text{s}$ . (5) The depletion 9-*cis*  $S_0$  with the time constant of 5  $\mu\text{s}$ . The combination of these five kinetics is expected to reproduce the time-resolved infrared data. Here we define the following temporal functions.

$$\begin{aligned} \text{Exp}_- &\equiv \text{Exp}_-(t) \equiv \begin{cases} 0 & (t < 0) \\ \exp(-k_0 t) & (t \geq 0) \end{cases} \\ \text{Exp}_+ &\equiv \text{Exp}_+(t) \equiv \begin{cases} 0 & (t < 0) \\ 1 - \exp(-k_0 t) & (t \geq 0) \end{cases} \\ \text{Step} &\equiv \text{Step}(t) \equiv \begin{cases} 0 & (t < 0) \\ 1 & (t \geq 0) \end{cases} \end{aligned} \quad (3)$$

The photoexcitation corresponds to  $t = 0$ . The function  $\text{Exp}_-$  describes an exponential decay with a rate constant of  $k_0$ , the  $\text{Exp}_+$  function describes an exponential growth with the same rate constant of  $k_0$ , and the Step function describes an instantaneous rise (positive) or depletion (negative). Note that the rate constant  $k_0$  corresponds to the observed time constant of 5  $\mu\text{s}$ . The  $\text{Exp}_-$  function represents the behavior of all-*trans*  $T_1$  signal in the kinetics (1). The  $\text{Exp}_+$  function represents the growth of the signal with the time constant of 5  $\mu\text{s}$  (kinetics (4) and (5)). The Step function represents the instantaneous signal change (kinetics (2) and (3)). Based on the five kinetic schemes,  $\mathbf{A}$  is represented as follows.

$$\begin{aligned} \mathbf{A} &= a_1 \times \mathbf{u}_{\text{exp}_-} \cdot \mathbf{v}_{\text{AT}-T} + a_2 \times \mathbf{u}_{\text{step}} \cdot \mathbf{v}_{\text{AT}-G} + a_3 \times \mathbf{u}_{\text{step}} \cdot \mathbf{v}_{9C-G} \\ &+ a_4 \times \mathbf{u}_{\text{exp}_+} \cdot \mathbf{v}_{\text{AT}-G} + a_5 \times \mathbf{u}_{\text{exp}_+} \cdot \mathbf{v}_{9C-G} \end{aligned} \quad (4)$$

Here,  $\mathbf{v}_{\text{AT}-T}$ ,  $\mathbf{v}_{\text{AT}-G}$  and  $\mathbf{v}_{9C-G}$  represent the spectra of all-*trans*  $T_1$ , all-*trans*  $S_0$ , and 9-*cis*  $S_0$ , respectively, and  $\mathbf{u}_{\text{exp}_-}$ ,  $\mathbf{u}_{\text{exp}_+}$  and  $\mathbf{u}_{\text{step}}$  represent the  $\text{Exp}_-$  function, the  $\text{Exp}_+$  function, and the Step function, respectively. The coefficients  $a_1$ ,  $a_2$ ,  $a_3$ ,  $a_4$  and  $a_5$  represent the contributions of the five terms. The Step function is given as a linear combination of the  $\text{Exp}_-$  and  $\text{Exp}_+$  functions as:  $\text{Step} = \text{Exp}_- + \text{Exp}_+$ . Substituting the Step function with  $\text{Exp}_- + \text{Exp}_+$ ,  $\mathbf{A}$  is represented as follows.

$$\begin{aligned} \mathbf{A} &= \mathbf{u}_{\text{exp}_-} \cdot (a_1 \times \mathbf{v}_{\text{AT}-T} + a_2 \times \mathbf{v}_{\text{AT}-G} + a_3 \times \mathbf{v}_{9C-G}) + \mathbf{u}_{\text{exp}_+} \\ &\cdot (a_2 \times \mathbf{v}_{\text{AT}-G} + a_3 \times \mathbf{v}_{9C-G} + a_4 \times \mathbf{v}_{\text{AT}-G} + a_5 \times \mathbf{v}_{9C-G}) \end{aligned} \quad (5)$$

Eq. (5) indicates that  $\mathbf{A}$  can be decomposed into two spectral components that have the temporal behaviors described with  $\mathbf{u}_{\text{exp}_-}$  and  $\mathbf{u}_{\text{exp}_+}$ . Appropriate linear combinations of the two SVD temporal components (Fig. 4e and f) should then make  $\mathbf{u}_{\text{exp}_-}$  and  $\mathbf{u}_{\text{exp}_+}$ . The coefficients of these appropriate linear combinations were obtained by a least-squares fitting of curves Fig. 4e and f to  $\mathbf{u}_{\text{exp}_-}$  and  $\mathbf{u}_{\text{exp}_+}$ . The spectral and temporal components thus determined are

shown in Fig. 5. The observed time-resolved infrared spectra were very well reconstructed from these SVD spectral and temporal components.

We now examine the physical meanings of the retrieved SVD components in Fig. 5. The spectral component Fig. 5b is identical with the difference spectrum between all-*trans*  $T_1$  and 9-*cis*  $S_0$  ( $a_1 > 0$ ,  $a_3 < 0$ ) with no contribution from all-*trans*  $S_0$  ( $a_2 = 0$ ). The temporal profiles Fig. 5d is explained in terms of the very fast (880 ps) rise of all-*trans*  $T_1$  and its subsequent relaxation to all-*trans*  $S_0$ . The spectral component Fig. 5a is identical with the difference spectrum between all-*trans*  $S_0$  and 9-*cis*  $S_0$  ( $a_2 + a_4 > 0$  and  $a_3 + a_5 < 0$ ) with no contribution from all-*trans*  $T_1$  ( $a_4 = 0$ ). The kinetics in Fig. 5c indicates that all-*trans*  $S_0$  is formed at the expense of 9-*cis*  $S_0$ .

### 3.3. Photoisomerization mechanism

The intensity of the 9-*cis*  $S_0$  band at 1144  $\text{cm}^{-1}$  (Fig. 2a) decreases at the rate of 5  $\mu\text{s}$ , which is the same rate as that of the decrease of the all-*trans*  $T_1$  bands at 1184  $\text{cm}^{-1}$  (Fig. 2c) and 1600  $\text{cm}^{-1}$  (Fig. 2d). This fact indicates that a reaction pathway exists that consumes 9-*cis*  $S_0$  by the interaction with all-*trans*  $T_1$ . The SVD analysis has shown that all-*trans*  $S_0$  is formed at the expense of 9-*cis*  $S_0$ . These two results indicate that the 9-*cis* to all-*trans* isomerization occurs through the interaction between all-*trans*  $T_1$  and 9-*cis*  $S_0$ :

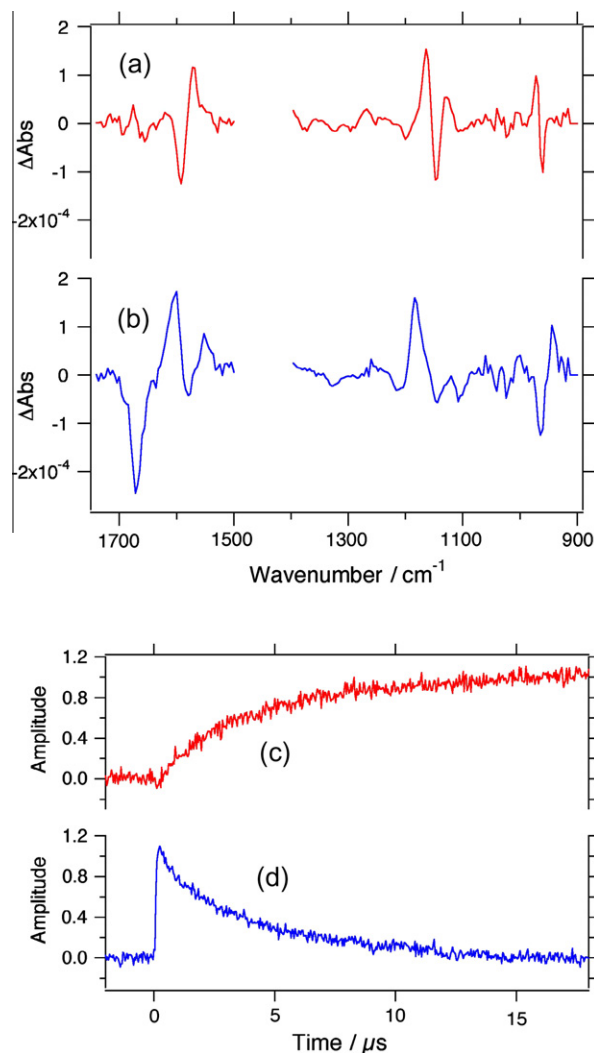
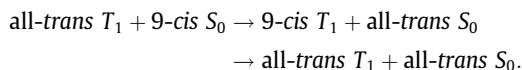


Fig. 5. Retrieved temporal (a, b) and spectral (c, d) components.





All-*trans*  $T_1$  is quenched by 9-*cis*  $S_0$  and 9-*cis*  $T_1$  and all-*trans*  $S_0$  are formed. The 9-*cis*  $T_1$  then isomerizes to all-*trans*  $T_1$  with the time constant of 880 ps [8]. The 9-*cis*  $T_1$  lifetime is too short to be detected with the present nanosecond time-resolved infrared experiment. All-*trans*- $T_1$  is thus reproduced after reacting with 9-*cis*  $S_0$  with a net isomerization from 9-*cis*  $S_0$  to all-*trans*  $S_0$ . The reproduced all-*trans*- $T_1$  can start another reaction with 9-*cis*  $S_0$ . This quantum chain process was suggested for *cis*–*trans* isomerization of retinal from the very large photoisomerization quantum yields [4,13,14]. To the best of our knowledge, the present time-resolved infrared study is the first direct observation of this quantum chain process.

The spectrum in Fig 5b contains only those of all-*trans*  $T_1$  and 9-*cis*  $S_0$ , though Eq. (5) indicates that it can also contain the spectrum all-*trans*  $S_0$ . The negligible contribution of all-*trans*  $S_0$  ( $a_2 = 0$ ) indicates that there is no instantaneous rise of all-*trans*  $S_0$  and that the isomerization pathway that includes the instantaneous formation of all-*trans*  $S_0$  from the 9-*cis* excited singlet state is minor, if possible at all. The photoisomerization of 9-*cis* to all-*trans* occurs predominantly on the excited triplet potential surface and not on the excited singlet state.

#### 4. Conclusions

Two distinct pathways have been found for the photoisomerization of 9-*cis* retinal. One is the triplet pathway in the picosecond

regime. Another takes place in the microsecond time regime through the energy transfer between all-*trans*  $T_1$  and 9-*cis*  $S_0$ . The latter includes the quantum chain process in which all-*trans*  $T_1$  is repeatedly reproduced with net isomerization of 9-*cis*  $S_0$  to all-*trans*  $S_0$ .

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