

國立交通大學

電信工程研究所

碩士論文

運用改良式重複樹狀搜尋策略的低複雜度軟性輸出球狀解碼器
Low-Complexity Soft-Output Sphere Decoding with Modified Repeated Tree
Search Strategy

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中華民國一〇二年六月

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摘 要



針對 MIMO 技術的各種解碼器早已提出，但是對於如何達到好的複雜度-效能平衡，目前仍然是個挑戰。在此篇碩士論文中，我們提出了改良式的重複樹狀搜索的低複雜度軟性輸出球狀解碼器，並以模擬來說明其具有好的複雜度-效能平衡，並且是可由硬體來實現的。接著我們更進一步的將此改良式的重複樹狀搜索的低複雜度軟性輸出球狀解碼器應用於干擾調變未知下的干擾消除。模擬結果顯示相較於傳統的廣義概度比例測試法，我們所提的方法可以在耗費較少的資源和較低的複雜度下達到同樣好的調變偵測率和區塊錯誤率。

Low-Complexity Soft-Output Sphere Decoding with Modified Repeated Tree Search Strategy

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ABSTRACT

Various detectors for multiple-in-multiple-out (MIMO) technologies have been proposed, yet to achieve a good complexity-performance tradeoff still remains a challenge problem. In this thesis, we proposed a low complexity soft-output sphere decoding, called modified repeated tree search (RTS), that can achieve good complexity-performance tradeoff and is suitable for hardware implementation. We further apply the modified RTS for interference cancellation with unknown interference modulation. Simulation results show that a good modulation classification rate and block error rate (BLER) can be achieved with lesser complexity and resources consumed when it is compared with the traditional general likelihood ratio test (GLRT).

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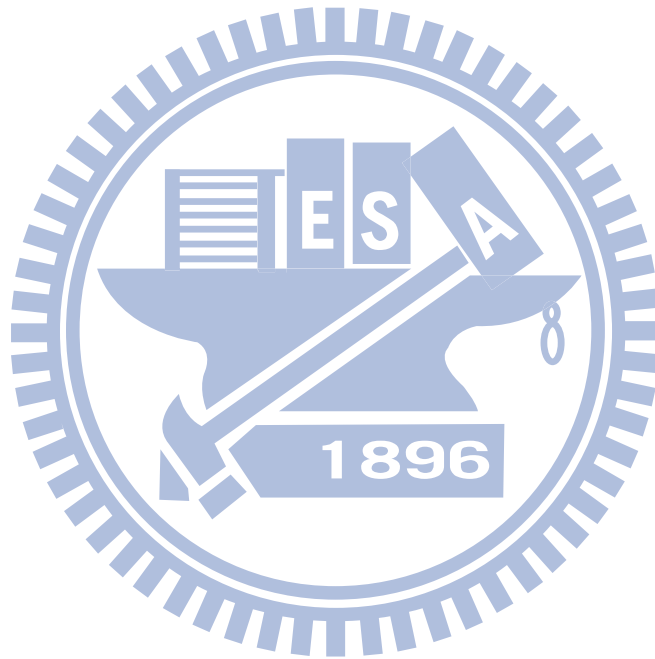
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Chapter 1

Introduction

With increasing demand on system throughput, multiple-input-multiple-output (MIMO) techniques become a trend in current and future communication technologies. Modern communications standards such as IEEE 802.11n, Worldwide Interoperability for Microwave Access (WiMAX), and Long Term Evolution (LTE), all accommodate the MIMO techniques into their standards.

Along this trend, several linear detecting methods such as zero-forcing (ZF) and minimum mean square error (MMSE) detectors have been proposed for MIMO systems. Due to linearity property, these linear detectors have low and fixed complexities and hence can be easily hardware-implemented. Their resulting performance however would sacrifice a certain degree of MIMO antenna gain. On the other hand, a brutal-force maximum-likelihood (ML) detector finds the optimal codeword at a price of huge and thus impractical complexity. To compromise, the so-called sphere decoding [2, 3] (SD) algorithm maintains a good tradeoff between performance and complexity by searching the (near-ML) best codeword among those within a sphere.

The SD algorithms can be categorized into two classes: hard-output SD algorithms and soft-output SD algorithms. As their names reveal, a hard-output SD algorithm outputs estimates of information bits, while a soft-output one generates the soft likelihood information for each bit, which can be used to co-work with a soft-input outer decoder such as the turbo decoder. The combination of the soft-output SD algorithm

and the soft-input outer decoder can then provide significant performance gain over the hard-output SD algorithm [4, 5, 6].

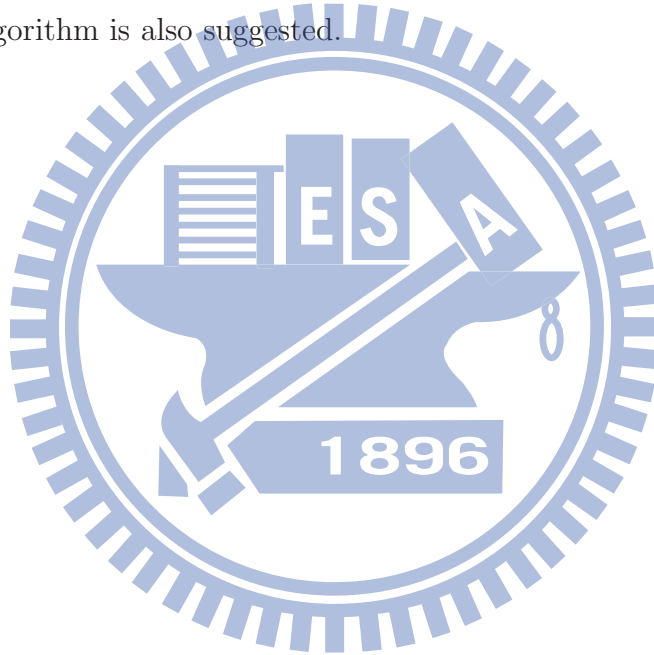
In order to generate soft likelihood information for each bit, more complexity is induced for the soft-output SD algorithm when being compared with a hard-output one. Some methods have thus been proposed for the reduction of complexity of the soft-output SD algorithm (with possibly a slight degradation in performance) such as log-likelihood ratio (LLR) clipping and channel matrix regularization [5]. A drawback of these methods, when considering their hardware implementation, is that they have varying complexity. The authors in [6] then resolved this problem by proposing a fixed-complexity soft-output SD algorithm, named *smart ordering candidate adding* (SOCA). Notably, the fixed complexity of the SOCA is actually higher than the average complexity of the soft-output SD algorithm in [5]. The merit of being more easily hardware-implementable of the former due to its fixed complexity nonetheless makes it a better choice in practical application.

In this thesis, we propose in Chapter 3 a new soft-output SD algorithm, which will be referred to as the modified repeated tree search (RTS) SD algorithm [1]. The proposed modified RTS SD algorithm guarantees a practically low complexity upper limit and hence is suitable for hardware implementation. From simulations, our modified RTS SD algorithm can provide a better performance-complexity trade-off in comparison with the SOCA, and its complexity upper limit is clearly smaller than the 99.9-percentile complexity of the single tree search (STS) SD algorithm in [5], where the 99.9-percentile complexity should be the designed maximum complexity allowable for the hardware implementation of a varying complexity soft-output SD algorithm like the STS.

We next investigate in Chapter 4 the interference cancellation (IC) over MIMO systems. Different from treating the interference as a part of the background noise as conventional detection problem does, we now attempt to cancel the interference from other users. Usually, the modulation scheme of the interference from other users is un-

known to the receiver. Estimation of the possible modulation scheme of interferences thus becomes essential. In [14], Shim *et al.* proposed to use a modified general likelihood ratio test (GLRT) to perform IC with unknown interference modulation scheme, and a bias term is added to the GLRT quantity to balance the impact from different modulation schemes. We then found that the bias term in [14] has not been optimized. An additional 1 dB gain can actually be resulted under the block error rate of 0.01 if we optimize this bias term. Subsequently, we continue to find that the previously proposed modified RTS can be further modified to resolve the IC problem with unknown interference modulation scheme. Details will be given in Chapter 4.

In the end, we conclude our thesis in Chapter 5. Possible extension of the proposed modified RTS SD algorithm is also suggested.



Chapter 2

System Model and Background

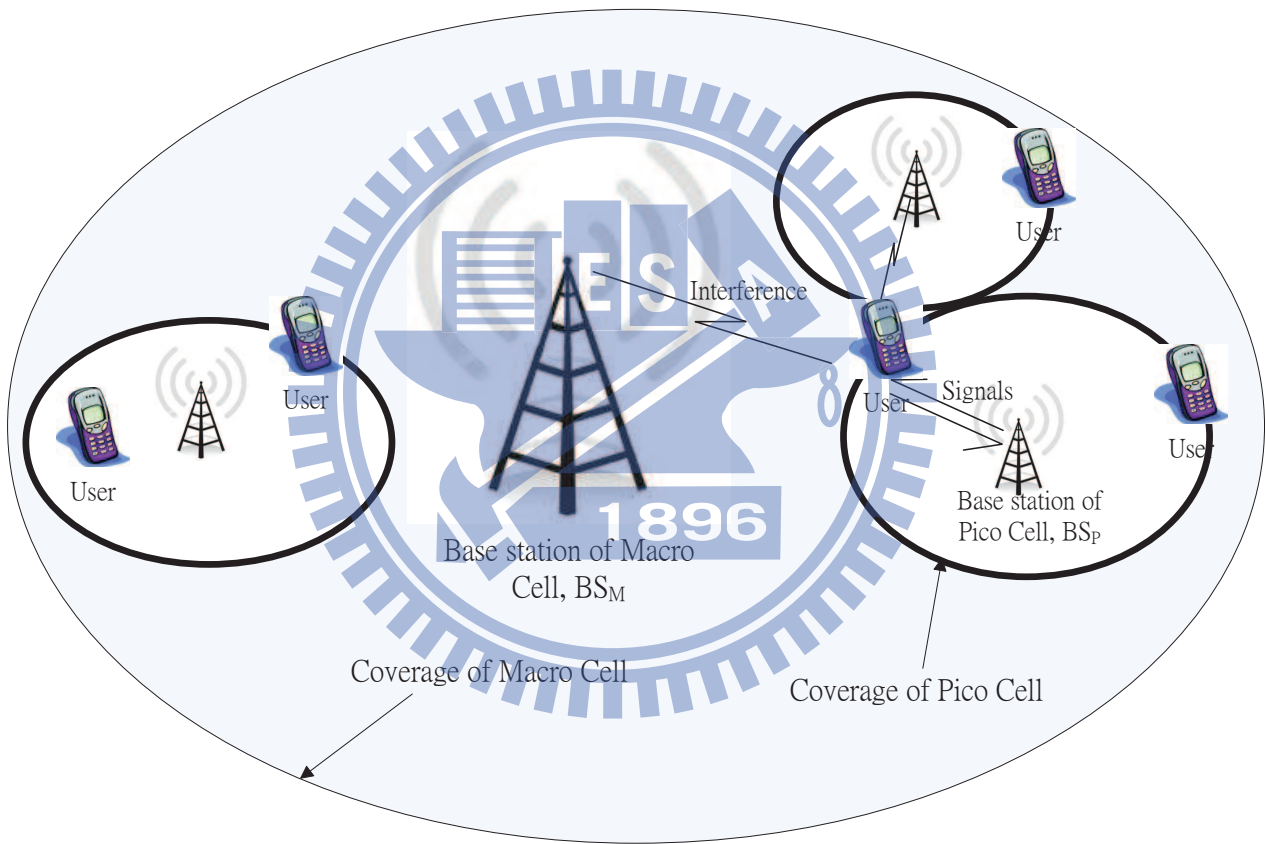


Figure 2.1: Illustration of a heterogeneous network

In a heterogeneous network such as the one in Fig. 2.1, different wireless access technologies respectively for macro and pico cells may be deployed so as to fit their

characteristics. A macro cell often provides a large radio coverage with a high power base station, while a pico cell is deployed either for areas with high concentration of users or as a coverage extension for indoor communications. In particular, when deploying pico cells within macro cells, more radio resources can be allocated, thereby improving the spectrum efficiency and system throughput. These merits however will unavoidably introduce more inter-cell interference to a single user. The techniques to effectively cancel the inter-cell interferences thus become essential in a heterogeneous network. Since users in the pico cell (respectively, macro cell) may not know the modulation schemes of other users in the macro cell (respectively, pico cell), this makes the MIMO detection and interference cancellation even more challenging.

In the later sections of this chapter, we will formulate the problem we focus in this thesis and then brief the existing technologies that have been proposed to solve it.

2.1 System Model

The MIMO system that we consider in this thesis can be modeled as:

$$\mathbf{y} = \mathbf{H}_s \mathbf{P}_s \mathbf{x}_s + \mathbf{H}_i \mathbf{P}_i \mathbf{x}_i + \mathbf{n} \quad (2.1)$$

where \mathbf{H}_s and \mathbf{H}_i represent respectively the channel matrices for signal and interference, and \mathbf{P}_s and \mathbf{P}_i are respectively the precoder matrices for signal and interference. Here, \mathbf{x}_s is the signal the receiver desires, and \mathbf{x}_i denotes the interference signal. The length of \mathbf{x}_s and \mathbf{x}_i are N_s and N_i , respectively. The last term \mathbf{n} represents the usual additive white Gaussian noise (AWGN). Note that in a heterogeneous network such as the LTE, which densely distributes with small cells, the interference power of $\mathbf{H}_i \mathbf{P}_i \mathbf{x}_i$ may be larger than the signal power of $\mathbf{H}_s \mathbf{P}_s \mathbf{x}_s$, which makes cancellation technologies essential to such system.

2.2 Prior Detection Algorithms

2.2.1 Linear Receivers

Traditional so-called type-I linear receivers for solving MIMO detection problems can be written as:

$$\mathbf{w}_{\text{MMSE},1} = \tilde{\mathbf{H}}_s^H \left(\tilde{\mathbf{H}}_s \tilde{\mathbf{H}}_s^H + \text{diag}(\sigma_{\text{IN},i}^2) \right)^{-1} \quad (2.2)$$

where $\tilde{\mathbf{H}}_s = \mathbf{H}_s \mathbf{P}_s$, and $\sigma_{\text{IN},i}^2$ is the equivalent noise variance that incorporates the interference power. Another MMSE receiver [17] that is generally classified as type II considers the impact of interference, and its resulting estimate can be written as:

$$\mathbf{w}_{\text{MMSE},2} = \tilde{\mathbf{H}}_s^H \left(\tilde{\mathbf{H}}_s \tilde{\mathbf{H}}_s^H + \tilde{\mathbf{H}}_i \tilde{\mathbf{H}}_i^H + \text{diag}(\sigma_{\text{IN}}^2) \right)^{-1} \quad (2.3)$$

where $\tilde{\mathbf{H}}_i = \mathbf{H}_i \mathbf{P}_i$, and σ_{IN}^2 is the noise variance. Although optimal from the statistical aspect, the MMSE receivers are known to be sensitive to correlations among antennas [18].

2.2.2 Sequential Interference Cancellation

When the interference power is seemingly larger than the signal power, alternative non-linear sequential interference cancellation (SIC) scheme has been proposed in the literature [15][19]. This method detects and cancels the interferences, starting from the current dominating one, in sequence, and afterwards recover the desired signals. It can be further categorized as symbol-SIC (S-SIC) and codeword-SIC (C-SIC) [19].

The S-SIC applies interference cancellation independently to each subcarrier as shown in Fig. 2.3. The S-SIC is known to suffer serious error propagation when symbol error rate is high. In certain cases, the performance of the S-SIC may be even worse than that of an MMSE receiver.

To resolve this error-propagation problem, the C-SIC, as illustrated in Fig. 2.4, performs error correction for interference codeword before interference cancellation, and thus can significantly improve the performance in comparison with the S-SIC. A restriction

of the C-SIC scheme is that the code rate and modulation of the interference code-word must be known at the receiver; this however is not guaranteed in the current LTE standard.

2.2.3 Sphere Decoding

A technique that recently gains much attention in the practice of interference cancellation is the sphere decoding (SD). The sphere decoding technique can maintain the maximum-likelihood performance under a practically appropriate complexity, and hence is recently used by many researchers for signal detection problem in MIMO systems. Again, the system model can be expressed as:

$$\begin{aligned}
 \mathbf{y} &= \mathbf{H}_s \mathbf{P}_s \mathbf{x}_s + \mathbf{H}_i \mathbf{P}_i \mathbf{x}_i + \mathbf{n} \\
 &= [\mathbf{H}_s \mathbf{P}_s \quad \mathbf{H}_i \mathbf{P}_i] [\mathbf{x}_s \quad \mathbf{x}_i]^T + \mathbf{n} \\
 &= \mathbf{H} \mathbf{x} + \mathbf{n}
 \end{aligned} \tag{2.4}$$

where $\mathbf{H} \triangleq [\mathbf{H}_s \mathbf{P}_s \quad \mathbf{H}_i \mathbf{P}_i]$, and $\mathbf{x} \triangleq [\mathbf{x}_s \quad \mathbf{x}_i]^T$.

Before we continue the presentation of the main results in this chapter, we should tell the main difference between the system model considered in Chapter 3 and that in Chapter 4. In Chapter 3, we only consider an interference-free scenario, where there is no interference signal (i.e., $N_i = 0$), while in Chapter 4, interference \mathbf{x}_i will interfere the demodulation of \mathbf{x}_s and hence $N_i > 0$.

Specifically, in Chapter 3, the symbol vector \mathbf{x} only contains \mathbf{x}_s . As such, an MIMO system with N_T transmit layers and N_R receive layers is considered, where $N_T \leq N_R$. The symbol transmitted from each antenna represents Q coded information bits, namely, the information bits are mapped to 2^Q complex constellation points. For example, $Q = 2$ for QPSK, and $Q = 4$ for 16-QAM. We further assume that the covariance matrix of \mathbf{x} satisfies $E\{\mathbf{x}\mathbf{x}^H\} = \mathbf{I}_{N_T}$, and each entry in \mathbf{H} is complex Gaussian distributed with mean zero and variance $1/N_T$. The noise \mathbf{n} is independent Gaussian distributed with

mean zero and variance N_0 . As a result of the above setting, the signal-to-noise ratio (SNR) per receive antenna is exactly $1/N_0$.

As a contrast in Chapter 4, we assume that the receiver contains totally N_i layers of interference and N_s layers of desired signals, where $N_i + N_s = N_T$. Again, the symbol transmitted from each antenna is constituted of Q coded information bits, and the information bits are mapped into 2^Q constellation points. The modulation for \mathbf{x}_s is known to the receiver; however, the modulation for \mathbf{x}_i is only known to belong to a set of candidate schemes. The covariance matrix of \mathbf{x} still satisfies $E\{\mathbf{x}\mathbf{x}^H\} = \mathbf{I}_{N_T}$, which means signals and interferences have equal power. Similar to those assume in Chapter 3, the entry in the N_R -by- N_T matrix \mathbf{H} is assumed to be complex Gaussian distributed with mean zero and variance $1/N_T$, and additive noise \mathbf{n} has independent complex Gaussian components with mean zero and variance N_0 . The SNR per receive antenna thus remains $1/N_0$.

Now we return to the introduction of the SD algorithm. The SD algorithm is beneficially adopted for MIMO signal detection since it guarantees finding the maximum-likelihood (ML) symbol vector with considerable reduction of demodulation/decoding complexity in comparison with the brutal force ML detector. The idea behind the SD algorithm is that it sets a sphere centered at the received symbol vector with a properly chosen radius. Only the candidate vectors that lie inside the sphere are needed to be checked, thereby reducing its complexity.

The SD algorithm has two steps: 1) per-processing step and 2) tree search step. The pre-processing step QR-decomposes the channel matrix \mathbf{H} :

$$\mathbf{H} = \mathbf{Q} \begin{bmatrix} \mathbf{R} \\ \mathbf{0}_{(N_R - N_T) \times N_T} \end{bmatrix}, \quad (2.5)$$

where \mathbf{Q} is an unitary $N_R \times N_R$ matrix, and \mathbf{R} is an $N_T \times N_T$ upper triangular matrix with real-valued diagonal elements. Since \mathbf{Q} is unitary, we can left-multiply (2.4) by \mathbf{Q}^H

to yield a modified input-output relation:

$$\tilde{\mathbf{y}} = \mathbf{Q}^H \mathbf{y} = \mathbf{Q}^H \mathbf{H} \mathbf{x} + \mathbf{Q}^H \mathbf{n} = \mathbf{R} \mathbf{x} + \tilde{\mathbf{n}},$$

where $\tilde{\mathbf{n}}$ remains independent Gaussian distributed with mean zero and variance N_0 . In matrix form, this relation can be written as:

$$\begin{bmatrix} \tilde{y}_1 \\ \vdots \\ \tilde{y}_{N_T} \end{bmatrix} = \begin{bmatrix} r_{1,1} & r_{1,2} & \cdots & r_{1,N_T} \\ 0 & r_{2,2} & \cdots & r_{2,N_T} \\ \vdots & \ddots & \ddots & \vdots \\ 0 & \cdots & 0 & r_{N_T,N_T} \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_{N_T} \end{bmatrix} + \begin{bmatrix} \tilde{n}_1 \\ \vdots \\ \tilde{n}_{N_T} \end{bmatrix}.$$

With this modified relation, the tree-search step can be executed according to (2.6) below:

$$\begin{aligned} \hat{\mathbf{x}}_{\text{ML}} &= \arg \min_{\mathbf{x} \in \mathcal{O}^{N_T}} \|\tilde{\mathbf{y}} - \mathbf{R} \mathbf{x}\|^2 \\ &= \arg \min_{\mathbf{x} \in \mathcal{O}^{N_T}} \sum_{i=1}^{N_T} \left| \tilde{y}_i - \sum_{j=i}^{N_T} r_{i,j} x_j \right|^2. \end{aligned} \quad (2.6)$$

In the literature, three major tree-search algorithms have been proposed, which are respectively named depth-first search [5], breadth-first search [7], and best-first search [8] algorithms. These algorithms basically produce hard-output \mathbf{x}_{ML} . Instead, we wish to investigate the soft-output SD algorithm in this thesis, which will be briefed in the next section.

2.2.4 Soft-Output Sphere Decoding and Methods for Complexity Reduction

Denote by $x_{j,b}$ the b th bit in the constellation point corresponding to the j th entry of vector \mathbf{x} . In order to reduce the decoding complexity, the true LLR for bit $x_{j,b}$ is replaced by its Max-Log approximation [5, 9]:

$$L(x_{j,b}) = \min_{\mathbf{x} \in \mathcal{X}_{j,b}^{(0)}} \|\mathbf{y} - \mathbf{H} \mathbf{x}\|^2 - \min_{\mathbf{x} \in \mathcal{X}_{j,b}^{(1)}} \|\mathbf{y} - \mathbf{H} \mathbf{x}\|^2, \quad (2.7)$$

where $\mathcal{X}_{j,b}^{(0)}$ and $\mathcal{X}_{j,b}^{(1)}$ are sets of vectors that have the b th bit in the j th entry equal to 0 and 1, respectively. Applying this idea to the QR-decomposition-refined relation

$\tilde{\mathbf{y}} = \mathbf{R}\mathbf{x} + \tilde{\mathbf{n}}$, we now obtain an equivalent version of Eq. (2.7):

$$L(x_{j,b}) = \min_{\mathbf{x} \in \mathcal{X}_{j,b}^{(0)}} \|\tilde{\mathbf{y}} - \mathbf{R}\mathbf{x}\|^2 - \min_{\mathbf{x} \in \mathcal{X}_{j,b}^{(1)}} \|\tilde{\mathbf{y}} - \mathbf{R}\mathbf{x}\|^2. \quad (2.8)$$

We then solve the above equation by using the SD-based tree search.

Several tree traversal strategies have been proposed in the literature. They are respectively described below:

1. Repeated Tree Search (RTS)

The main idea of the RTS [4] is to compute the soft LLR value based on the ML solution found by the hard-output SD algorithm. This strategy may re-do some branch computations, resulting in a significant complexity waste.

2. Single Tree Search (STS)

When being compared with the RTS, the STS is much more efficient since every branch in the tree is visited at most once. The STS finds the ML solution via the hard-output SD algorithm, and simultaneously identifies the counter-hypothesis paths corresponding to the ML solution. Thus, the branch computations will not be repeated, which saves the significant complexity in comparison with the RTS. Its largely varying complexity however may make its hardware implementation a challenging task.

3. Smart Ordering and Candidate Adding (SOCA) Algorithm

Aiming to solve to complexity variation problem in the SD algorithm like the STS, the authors in [6] proposed another algorithm named the SOCA in a way that by performing QR decomposition with a smart ordering criterion, together with predefined numbers of per-layer candidates to be searched, the complexity can be made fixed and hence achieve a good performance-complexity trade-off.

We end this chapter by remarking that some other complexity reduction techniques

such as LLR clipping, LLR sorting and regularization can also be combined with the above algorithms to further reduce the complexity [4, 5, 6].



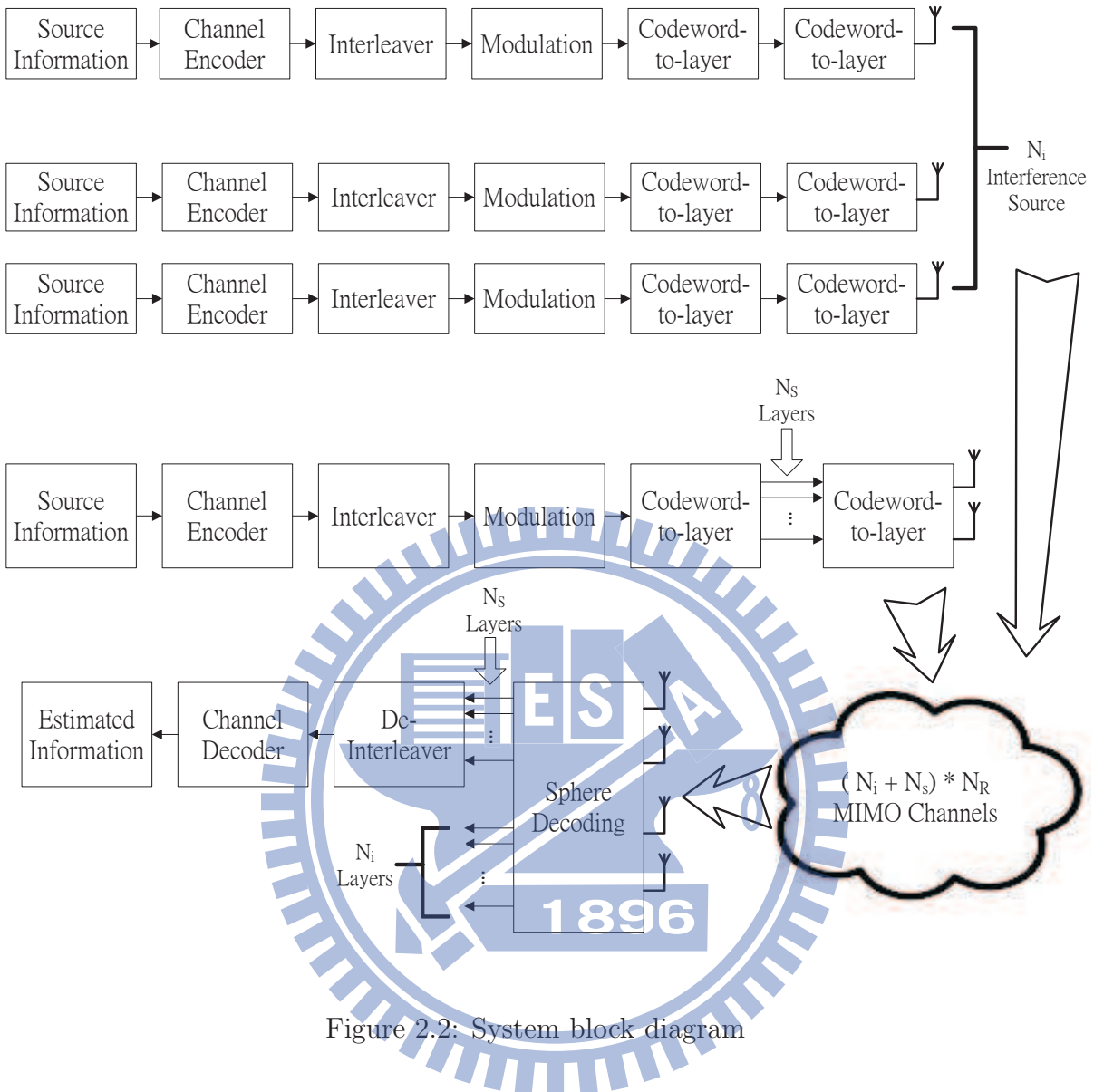


Figure 2.2: System block diagram

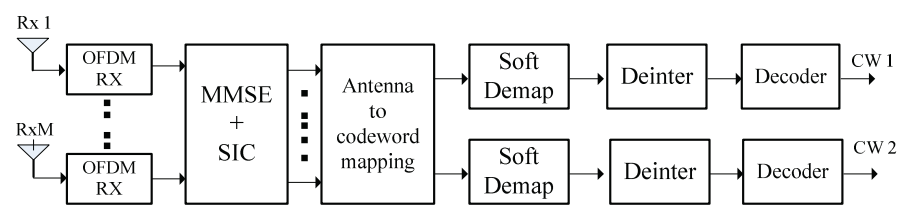


Figure 2.3: Structure of a symbol-SIC receiver

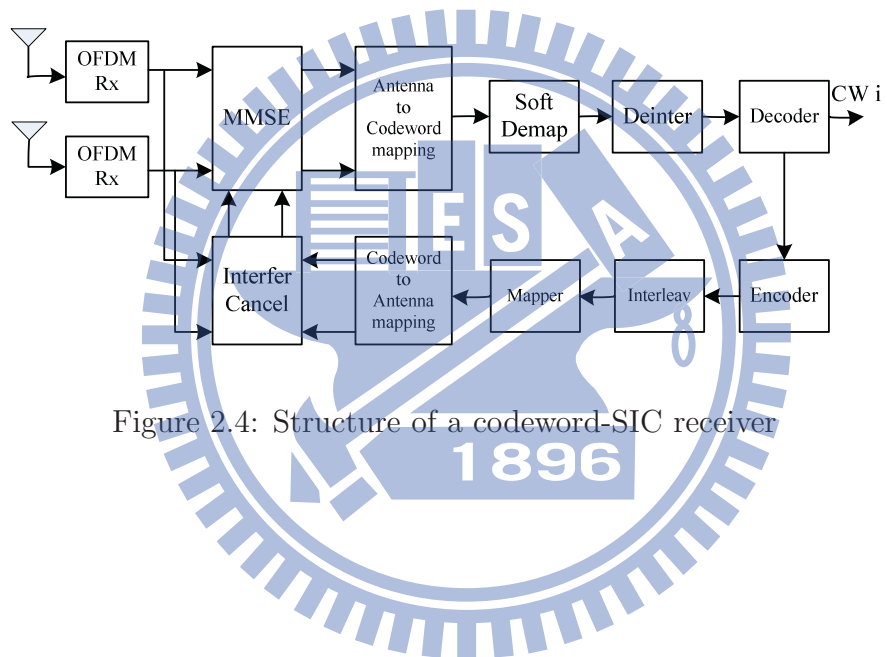


Figure 2.4: Structure of a codeword-SIC receiver

Chapter 3

Soft-Output Sphere Decoding with Modified Repeated Tree Search

In this chapter, we will first investigate the traditional soft-output sphere decoding algorithm for signal detection, followed by our proposal of the modified-RTS soft-output SD algorithm with complexity upper limit.

3.1 Modified RTS Traversal Strategy

Similar to the RTS tree traverse algorithm, our modified RTS algorithm has two stages. The first stage finds the hard-decision ML path, while the second stage examines counter hypothesis paths to generate the required soft output.

A suitable candidate algorithm for the first stage is the Schnorr-Euchner sphere decoder (SESD) with radius reduction [12]. It is an efficient depth-first tree search algorithm for finding the ML hard-output. Nevertheless, the SESD still has varying decoding complexity, and therefore, we propose to set an upper limit T_1 such that the first stage ends either when the ML hard-output is found or when the complexity upper limit T_1 is reached at which time the current best path is outputted instead.

From this setting, an expectation can be resulted. After imposing a complexity upper limit, we may find a near-ML path instead of the ML path. Our simulation results however show that with a small T_1 , the ML path can be located with high probability, and a good performance-complexity tradeoff can be obtained.

After the determination of the ML path (or a near-ML path), we perform the tree traverse in the second stage. Later, we will show that the second stage also has an upper complexity limit T_2 , and hence the overall complexity for the proposed modified RTS is limited by $(T_1 + T_2)$.

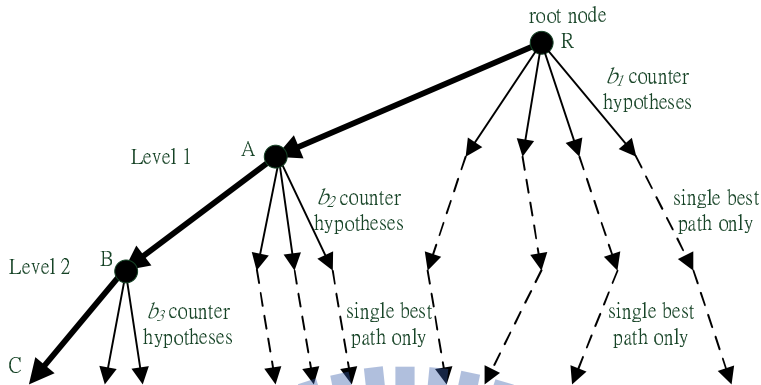


Figure 3.1: Illustration of the second stage with $N_T = 3$ and $\mathbf{b} = [b_1 \ b_2 \ b_3] = [4 \ 3 \ 2]$ for the proposed modified RTS. The thick solid line corresponds to the near-ML path obtained from the first stage.

Specifically, the second stage finds counter hypothesis paths based on the near-ML path obtained from the first stage. There can be as many as Q^{N_T} counter hypothesis paths. To save the complexity, we specify a vector $\mathbf{b} = [b_1, \dots, b_{N_T}]$ to restrict the number of counter hypothesis paths to be extended at each level, where $1 \leq b_i \leq Q$. Therefore, at level i , only those b_i paths with the smallest partial path metrics (i.e., distances to the received vector) are extended. As an example, suppose the modulation scheme adopted is 16-QAM, which gives immediately $Q = \log_2(16) = 4$. Assume that the symbol at the i th level of the ML path located at the first stage is $\hat{x}_i = 1000$. This gives us four counter hypothesis branches, specified by $\{0000, 1100, 1010, 1001\}$. Among these four counter hypothesis paths, only b_i of them are selected for further extension according to their Euclidean distances to the complex receive scalar \tilde{y}_i . For a better understanding, a simple illustration of the second stage is given in Fig. 3.1.

On the other hand, it is known that clipping the LLR value to make it within $\pm L_{\max}$

has essential effect on performance and complexity of the soft-output SD algorithm. Since $b_i \leq Q$, the counter hypothesis paths traversed by our modified RTS strategy may not include all the paths required by (2.8). In such case, the Max-Log approximated LLR value may become infinity. This makes the selection of the clipping limit L_{\max} very important in our modified RTS strategy. In fact, we observe that extending a path with the distance of its i th entry to \tilde{y}_i larger than L_{\max} will often result in no improvement in performance but induce only more complexity. Hence, we set a rule that a path will be abandoned once the distance of its i th entry to \tilde{y}_i is found to exceed L_{\max} , which can further reduce the complexity.

The upper complexity limit of the second stage can be computed as follows:

$$T_2 = \sum_{i=1}^{N_T} b_i (N_T + 1 - i). \quad (3.1)$$

The idea behind equation (3.1) is that the near-ML path expands b_i paths at level i , and each path visit b_i nodes until it reaches the bottom level. Again, as having been described, by only expanding those nodes with branch metrics within L_{\max} , the complexity of the second stage can be further reduced.

We close this section by summarizing the main ideas of the proposed modified RTS in the following:

- We adopt the SESD with an upper complexity limit T_1 in the first stage. It finds a near-ML path, guaranteeing having complexity no greater than T_1 . With a proper choice of T_1 , a good performance-complexity tradeoff is obtained.
- b_i counter hypothesis paths with the smallest metrics and also with metrics smaller than L_{\max} are extended in the second stage. This guarantees a complexity no greater than T_2 , and prevents a complexity waste in the second stage.

3.2 Simulation Results

We now compare our modified RTS with the STS and the SOCA.

Consider an MIMO system transmitted over Rayleigh fading channels with possibly spatial or temporal correlation. Fast fading and slow fading scenarios as specified in [6] are both considered, where in fast fading scenario, the channel realizations change per MIMO transmission, while in slow fading scenario, the channel realizations remain the same throughout an entire (turbo) transmission block but vary across (turbo) transmission blocks. We assume that all channel matrix realizations can be perfectly estimated at the receiver. Four transmit antennas and four receive antennas, (i.e. $N_T = N_R = 4$) and 16-QAM constellation are adopted.

Two kinds of channel coding schemes are tested. The first one is a 3GPP-specified punctured turbo code of code rate $R = 1/2$ with codeword length 2000 bits [10]. After passing the code through a 40×50 block interleaver, 500 16-QAM symbols are formed and transmitted. At the receiver, the 8-iteration Max-Log-MAP decoder is used for turbo decoding.

The second channel coding scheme used in our simulation is a 3GPP-specified (2, 1, 8) convolutional code of code rate $R = 1/2$. The codeword length is 720 bits. After convolutional encoding, 180 16-QAM symbols are fed into a 15×48 block interleaver before they are sent. At the receiver, the Viterbi decoder is used for the decoding of this convolutional code.

The upper complexity limit T_1 for the first stage in our modified RTS is set to 30, and the set of the restriction vectors \mathbf{b} examined in our simulation contains $\mathbf{b} = [4444]$, $[4442]$, $[4422]$, $[4222]$, and $[2222]$, which respectively result in $T_2 = 40, 38, 34, 28,$ and 20 . For the SOCA, the tested numbers of paths extended in the first level, i.e., b_1 , include 6, 14, 12, 10, 8, 6, and 4, which results complexities 88, 80, 72, 64, 56, 48, and 40, respectively. Note that for the SOCA, $b_i = 1$ for every $i > 1$.

It should be mentioned that the channel regularization algorithm [5] is used for all three algorithms, i.e., the STS, the SOCA, and our proposed modified RTS when performing the QR-decomposition step. In addition, the SQRD [13] is employed as the

sorting algorithm in QR decomposition for both the STS and our proposed modified RTS, while the SOQR in [6] is implemented for the SOCA.

The performance index that we adopt in this thesis is the minimum SNR required to achieve a block error rate of 10^{-2} after channel decoding. The complexity measure is the number of visited nodes during the tree search. This complexity measure is widely adopted for one-node-per-cycle hardware implementation architecture [11]. We are now ready to present the simulation results.

We first examine what should be the proper selected value for L_{\max} . As previously mentioned, the value of L_{\max} chosen will affect performance and complexity of the STS, the SOCA and our modified RTS. As for the STS (as well as other algorithms), a larger L_{\max} implies a better performance but a larger complexity. We then show the performance-complexity tradeoff for the STS in Fig. 3.2. Later, an L_{\max} value will be chosen according to this figure.

For the SOCA and our modified RTS, the relationship between L_{\max} and performance-complexity tradeoff is a little messy. Various test results regarding different L_{\max} values are summarized in Figs. 3.3, 3.5, 3.4, and 3.6.

Specifically, in Fig. 3.3, the range of the tested L_{\max} values is ranged from 0.15 to 0.55 for the modified RTS under fast fading channels. We can clearly see from this figure that $L_{\max} = 0.25$ has the best complexity-performance trade-off. However, the implication from Fig. 3.4 is a little different under slow fading scenario. By testing L_{\max} from 0.15 to 0.55, we observe from Fig. 3.4 that under a slow fading environment, the smaller the L_{\max} , the better the performance-complexity tradeoff. To have a good balance choice that fits both fast fading and slow fading scenarios, we set $L_{\max} = 0.25$ for our modified RTS.

Similar tests, for which L_{\max} assumes values from 0.15 to 0.55, are performed for the SOCA. From Fig. 3.5, where the fast fading scenario is assumed, we observe that the performance-complexity tradeoff improves as L_{\max} increases. Notably, the simulation

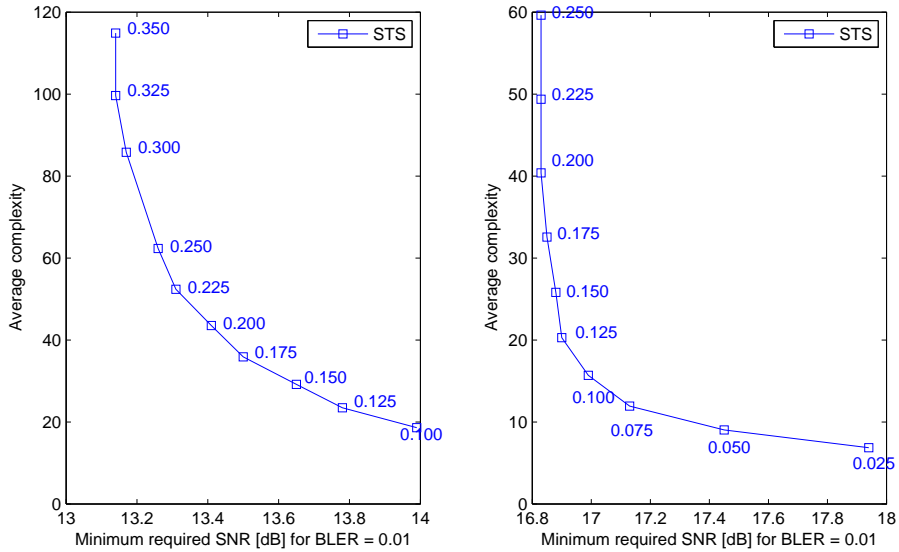


Figure 3.2: Impact of L_{\max} on the STS with turbo coding under fast (left subfigure) and slow (right subfigure) Rayleigh fading channels

results for L_{\max} ranging from 0.35 to 0.55 are almost indistinguishable. Under the slow fading scenario, however, different trends can be observed from Fig. 3.6. We note from this figure that when L_{\max} is larger than 0.2, the performance-complexity tradeoff begins to degrade. Again, to compromise between two different scenarios, we choose $L_{\max} = 0.3$ for the SOCA.

Figs. 3.7 and 3.8 illustrate how different T_1 affect BLERs and complexities. In short, we can see from Fig. 3.7 that under fast fading, the curve corresponding to $T_1 = 20$ has already approached the curve of $T_1 = \infty$. In Fig. 3.8, we then see that there is no visible gap between curves of $T_1 = 20$ and $T_1 = \infty$. Nonetheless, we set $T_1 = 30$ to secure the (near-)ML performance.

After the settlement of the parameters used, we are now ready to compare the STS and the SOCA with our modified-RTS algorithm. First, we remark on the simulations results regarding turbo coding and fast fading scenario. As observed in Fig. 3.9, the proposed modified RTS achieves the best performance-complexity tradeoff, when it is

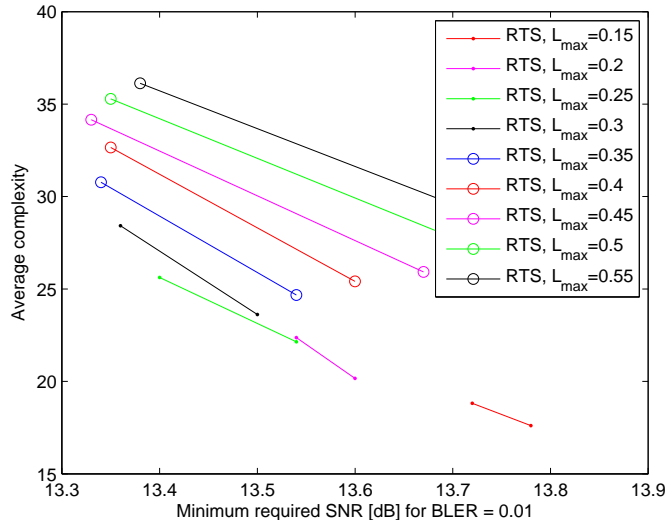


Figure 3.3: Impact of L_{\max} on the modified RTS with turbo coding under fast Rayleigh fading channels, where $\mathbf{b} = [4444]$ and $[2222]$ are employed.

compared with the STS and the SOCA. In order to examine the variation in complexity, we also record that the 99.9th percentile complexities of the STS and our modified RTS in this figure. Since the SOCA has a fixed decoding complexity, the average complexity of the SOCA is exactly the same as its 99.9th percentile complexity. It is shown in Fig. 3.9 that since the 99.9th percentile complexity of the STS is much higher than its average complexity, the STS may suffer with high variation of complexity and hence may become a challenge for hardware implementation. The high variation of complexity of the STS also makes varying its computational delay.

On the other hand, the gap between the average complexity and the 99.9th percentile complexity of the modified RTS is considerably much smaller than that of the STS. The 99.9th percentile complexity of the modified RTS is even just slightly higher than the (fixed) complexity of the SOCA. This indicates that the complexity upper limit ($T_1 + T_2$) we set for the modified RTS does decrease the variation of the decoding complexity, and therefore makes the soft-output SD algorithm more easily hardware-implementable.

Next we remark on the simulation results in the slow fading scenario. We observe

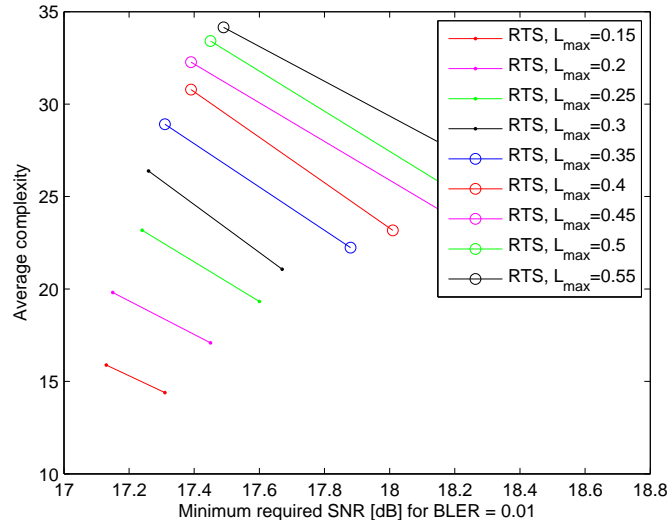


Figure 3.4: Impact of L_{\max} on the modified RTS with turbo coding under slow Rayleigh fading channels, where $\mathbf{b} = [4444]$ and $[2222]$ are employed.

from Fig. 3.10 that the STS achieves the best complexity-performance tradeoff in the sense of average complexity. However, nonetheless, the high complexity variation of the STS remains, which again challenges its hardware implementation. In particular, the 99.9th percentile complexity of the STS is six times larger than its average complexity. Similar conclusion as the one in the fast fading scenario can be obtained about the SOCA and the modified RTS that these two are more appropriate for hardware implementation due to their prohibitively bounded complexity. When comparing the modified RTS with the SOCA, the former requires a higher 99th percentile complexity but has a seemingly less average complexity.

In order to examine the impact on the coding algorithm such as turbo and convolutional codes, we re-do the previous simulations by replacing the turbo code with the convolutional code. The simulation results are summarized in Figs. 3.11 and 3.12. The results are similar to what obtained using the turbo code. As a result, the SOCA and the proposed modified RTS remain to be more attractive solutions for hardware implementation, regardless of the channel coding scheme.

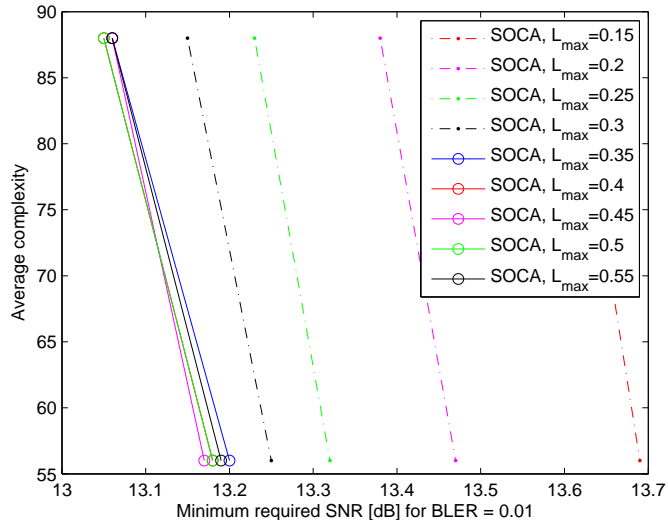


Figure 3.5: Impact of L_{\max} on the SOCA with turbo coding under fast Rayleigh fading channels, where $\mathbf{b}_1 = 16$ and 8 are employed.

In order to have more detailed insight on the complexities of the STS and our modified-RTS algorithm, we show the 50%-percentile, 90%-percentile, 99%-percentile, and 99.9%-percentile complexities in Figs. 3.13 and 3.14 in both fast and slow fading scenarios under turbo coding scheme. Evidently, the gaps among 50%-percentile, 90%-percentile, 99%-percentile, and 99.9%-percentile complexities for the modified RTS are much smaller than those of the STS.

We further investigate the complexity distribution of the STS with $L_{\max} = 0.2$ and also the complexity distribution of the modified RTS with $L_{\max} = 0.25$ and $\mathbf{b} = [4444]$ in Figs. 3.15 and 3.16, respectively. Note that to achieve a BLER of approximately 10^{-2} , the minimum SNR required for the STS is 13.41 dB, while the minimum SNR required for the modified RTS is 13.40 dB; so they are approximately operated at the same SNR. From the two figures, we can clearly see a drawback of the STS is its high complexity variation. Although its average complexity is only 44.57, its largest decoding complexity can be as large as 900 after testing 2,500,000 simulation samples. Such a high complexity variation of the STS may become a challenge for hardware implementation.

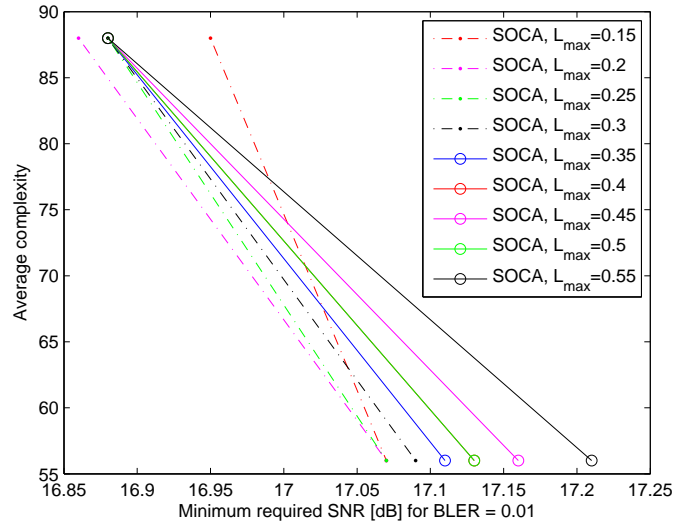
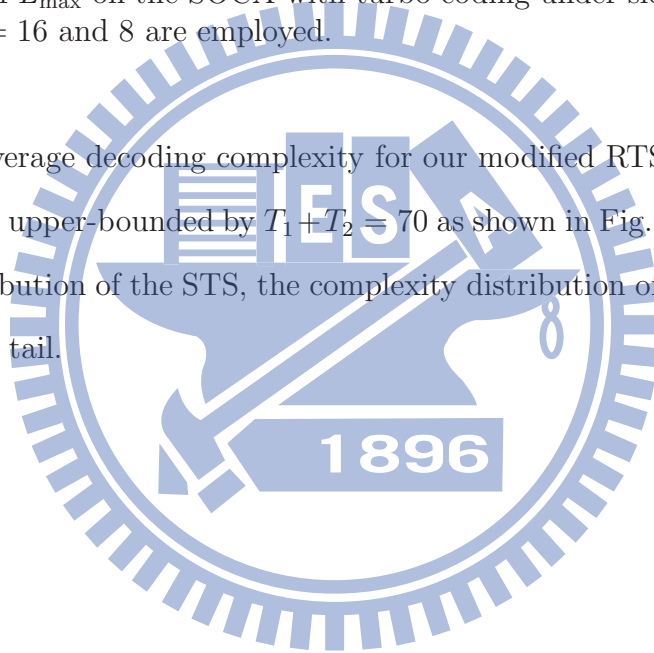


Figure 3.6: Impact of L_{\max} on the SOCA with turbo coding under slow Rayleigh fading channels, where $\mathbf{b}_1 = 16$ and 8 are employed.

As a contrary, the average decoding complexity for our modified RTS is only 25.62 and its true complexity is upper-bounded by $T_1 + T_2 = 70$ as shown in Fig. 3.16, where unlike the complexity distribution of the STS, the complexity distribution of the modified RTS does not have a long tail.



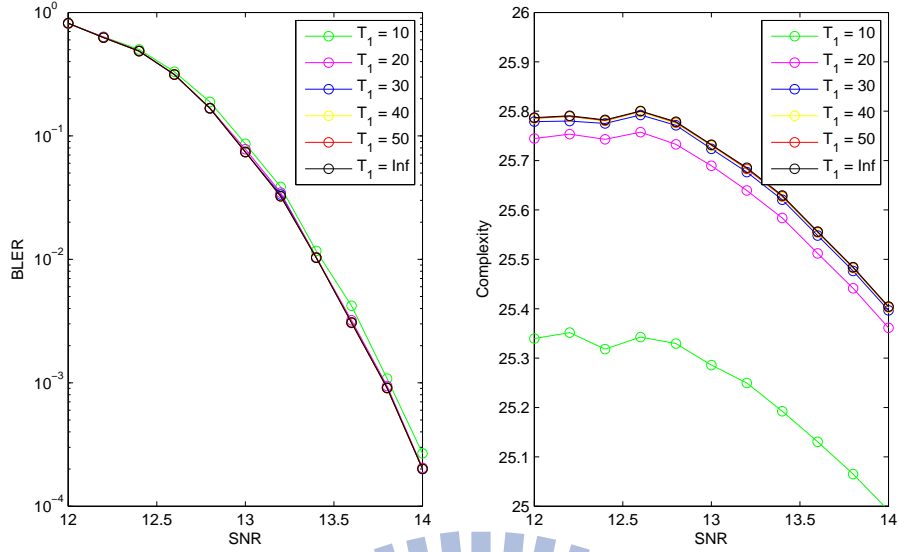


Figure 3.7: Impact of T_1 on BLERs and complexities under fast Rayleigh fading channels.

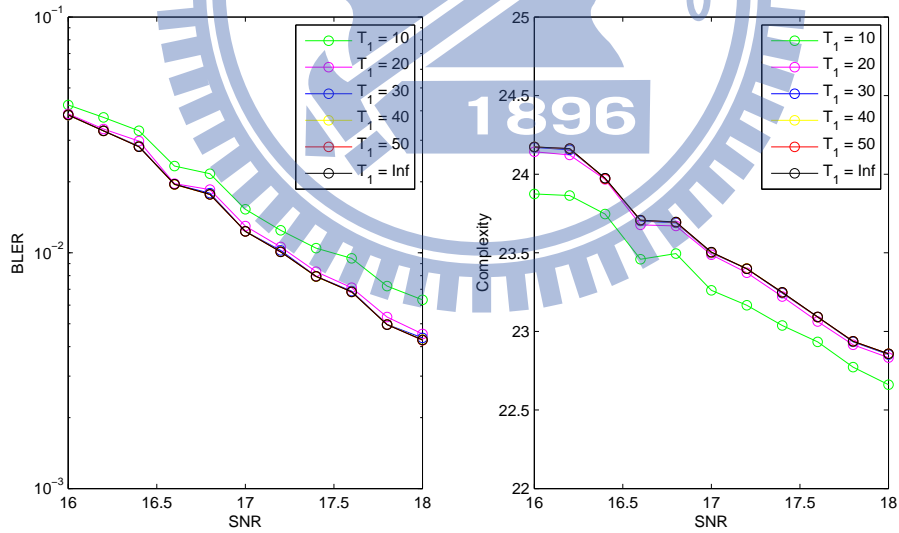


Figure 3.8: Impact of T_1 on BLERs and complexities under slow Rayleigh fading channels.

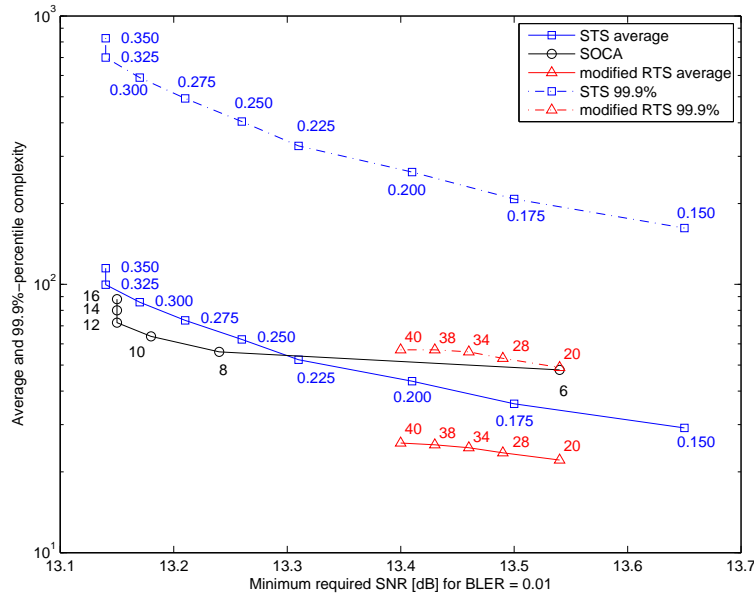


Figure 3.9: Performance versus complexity for the STS, the SOCA, and the modified RTS in fast Rayleigh fading channels. The numbers beside the STS marks are the L_{\max} values used. The numbers next to the SOCA curve correspond to b_1 . The number next to each modified RTS mark is T_2 .

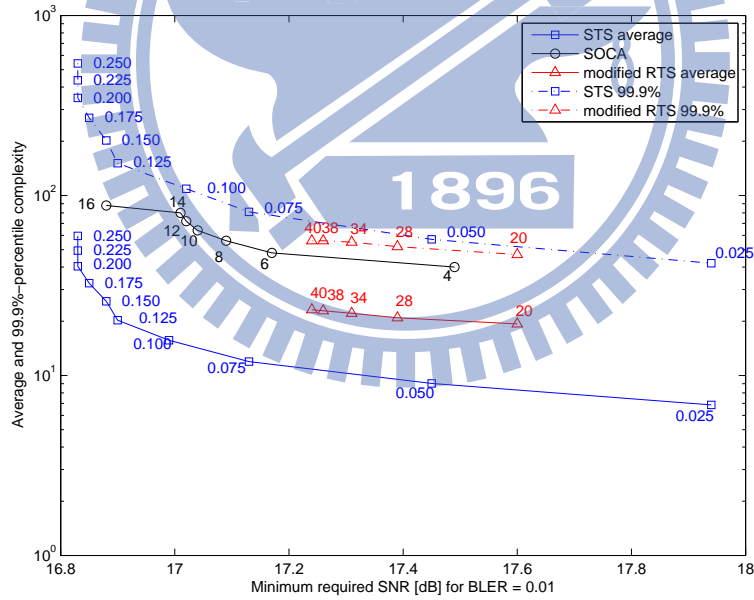


Figure 3.10: Performance versus complexity for the STS, the SOCA, and the modified RTS with turbo code in slow Rayleigh fading channels. The numbers beside the STS marks are the L_{\max} used. The numbers next to the SOCA curve correspond to b_1 . The number next to each modified RTS mark is T_2 .

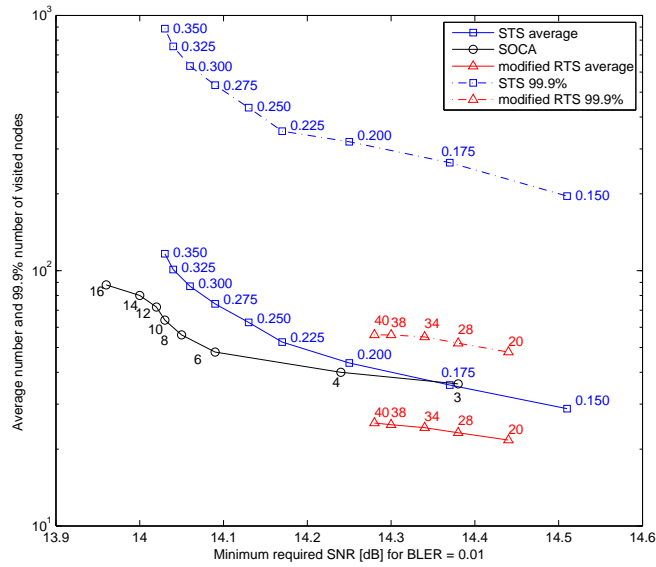


Figure 3.11: Performance versus complexity for the STS, the SOCA, and the modified RTS with convolutional code in fast Rayleigh fading channels. The numbers beside the STS marks are the L_{\max} used. The numbers next to the SOCA curve correspond to b_1 . The number next to each modified RTS mark is T_2 .

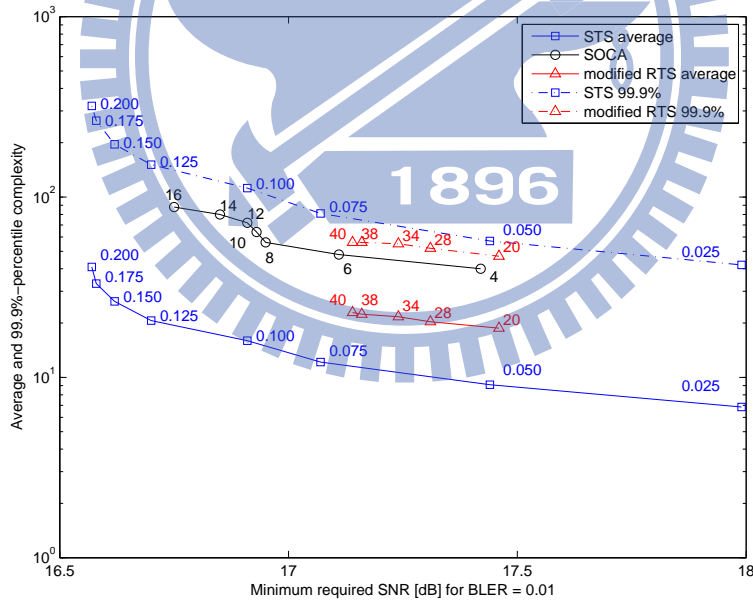


Figure 3.12: Performance versus complexity for the STS, the SOCA, and the modified RTS with convolutional code in slow Rayleigh fading channels. The numbers beside the STS marks are the L_{\max} used. The numbers next to the SOCA curve correspond to b_1 . The number next to each modified RTS mark is T_2 .

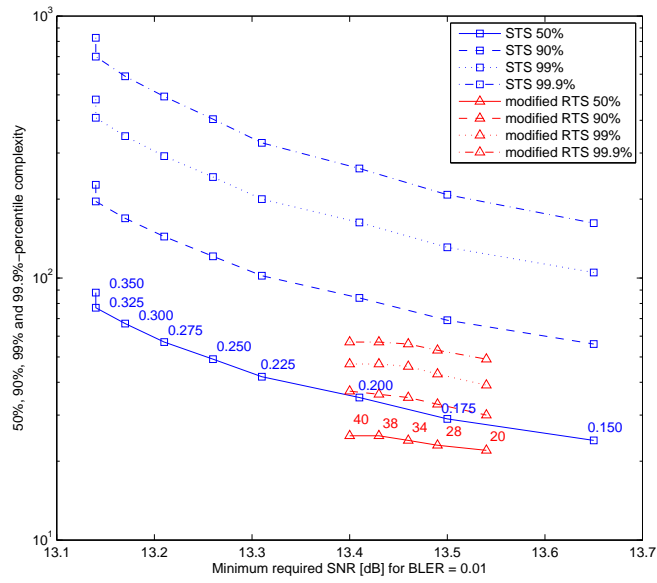


Figure 3.13: Performance versus different percentile-complexity for the STS and the modified RTS with turbo code in fast Rayleigh fading channels. The numbers beside the STS marks are the L_{\max} used. The number next to each modified RTS mark is T_2 .

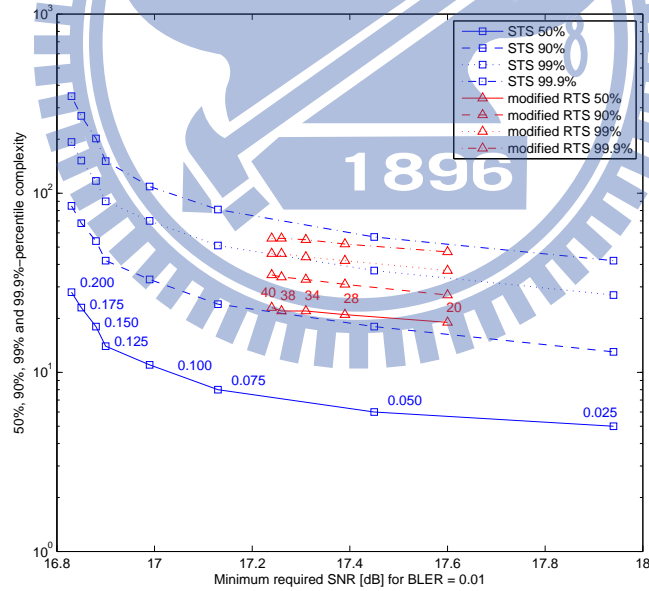


Figure 3.14: Performance versus different percentile-complexity for the STS and the modified RTS with turbo code in slow Rayleigh fading channels. The numbers beside the STS marks are the L_{\max} used. The number next to each modified RTS mark is T_2 .

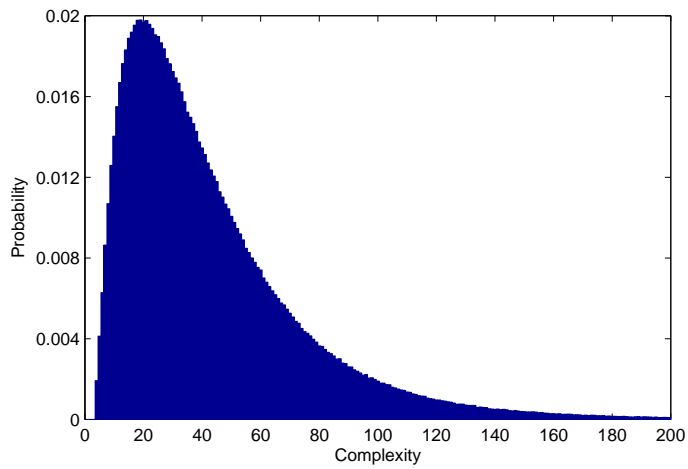


Figure 3.15: Complexity distribution of the STS with $L_{\max} = 0.2$. The maximum range of the complexity is 200, where the probability of complexity exceeding 200 is 0.0035.

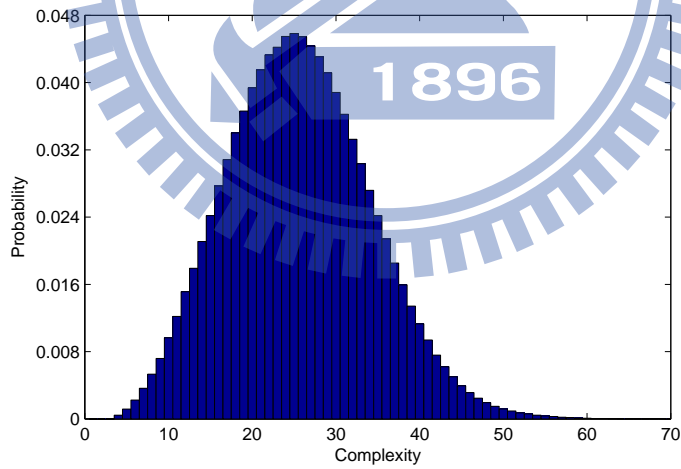


Figure 3.16: Complexity distribution of the modified RTS with $L_{\max} = 0.25$ and $\mathbf{b} = [4444]$.

Chapter 4

Interference Cancellation under Unknown Interference Modulation

In this chapter, we turn to a new interference cancellation problem, where the modulation scheme of the interference is unknown to the transceiving system.

As shown in the heterogeneous network in Fig. 4.1, a user camps on a pico cell (BS_P) may receive a strong inter-cell interference from a macro cell (BS_M), especially when the *cell range expansion* [15] is employed. The interference power from BS_M may be similar to or even larger than the signal power from BS_P so that without a proper inter-cell interference cancellation technique, successful communication is not possible.

As having been specified in Eq. (2.1), the general system model for interference cancellation problem can be formulated as

$$\mathbf{y} = \mathbf{H}_s \mathbf{P}_s \mathbf{x}_s + \mathbf{H}_i \mathbf{P}_i \mathbf{x}_i + \mathbf{n},$$

where $\mathbf{H}_i \mathbf{P}_i \mathbf{x}_i$ denotes the interference source, whose modulation scheme is now unknown to the receiver. This brings us to the problem of performing inter-cell interference with unknown interference modulation scheme.

In [14], joint modulation classification and detection using sphere decoding was proposed for high-speed downlink packet access (HSDPA) system, where exactly one interference source exists and only QPSK and 16QAM are the possible the modulation scheme of the interference. The authors then proposed a modified general likelihood

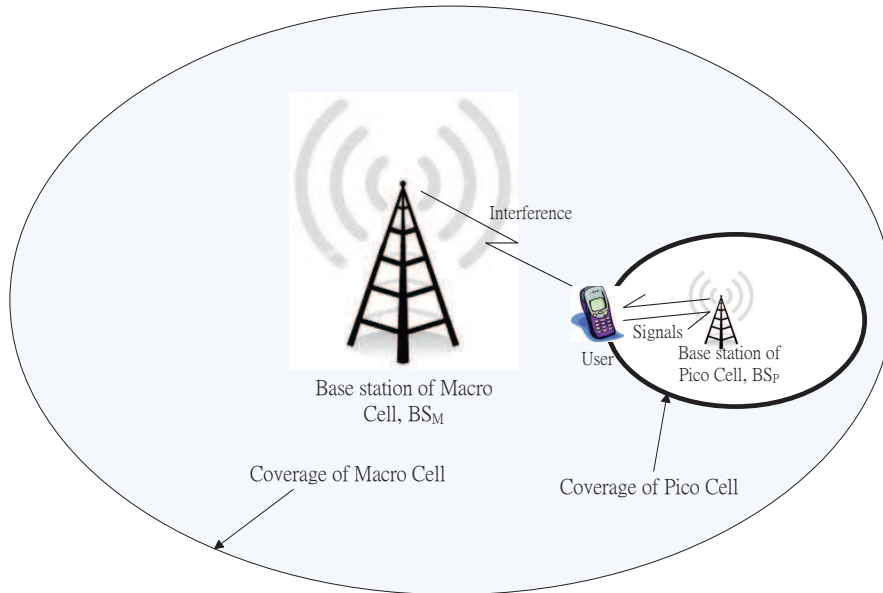


Figure 4.1: Illustration of interference from a marco cell to a user at the cell boundary of a pico cell

ratio test (GLRT) to deal with such a modulation classification problem. Basically, the modified GLRT is to perform a modified hypothesis testing so that all likelihoods of modulation hypotheses are calculated and compared in order to detect the modulation scheme of the interference source. The simulation results in [14] confirms that the modified GLRT method can output a promising modulation classification outcome for the HSDPA system. One drawback of the modified GLRT is that the number of hypotheses grows exponentially with the number of interference sources as well as the number of possible modulation schemes. This may result in an impractical modulation classification complexity for communication standards such as the LTE and LTE-Advanced.

In this chapter, we revisit our modified RTS in Chapter 3 to fit the new demand of performing inter-cell interference with unknown interference modulation scheme. With the inherited merit of the SD algorithm, the classification complexity can be considerably reduced in comparison with the modified GLRT. The main idea behind our proposal is to perform the SD algorithm for all possible modulation schemes for the interference on

the first few received symbols, and then declare the true modulation scheme by voting. Details will be given later.

4.1 Modified RTS for Joint Modulation Classification and Detection

In Chapter 2, we have shown that the modified RTS can provide a good performance-complexity tradeoff and meanwhile suits the need of hardware implementation under the assumption that the receiver knows the modulation schemes of and wishes to recover all symbols. With a new assumption that the modulation schemes of some unwanted received symbols (which are exactly the interferences) are unknown to the receiver, adjustment to the modified RTS must be done.

The new modified RTS for unknown interference modulations also retains the two-stage structure as shown in Fig. 4.2.

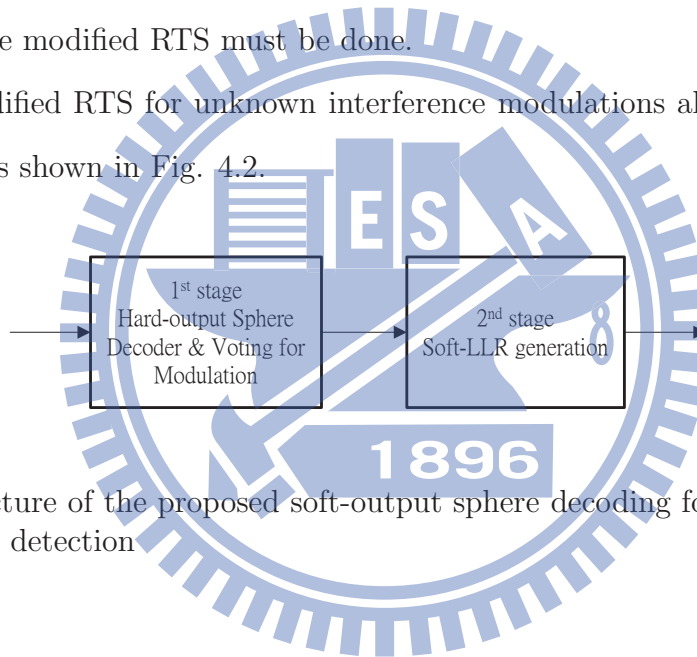


Figure 4.2: Structure of the proposed soft-output sphere decoding for joint modulation classification and detection

The first stage performs the hard-decision SD algorithm for the first N received symbols or received elements (REs) to generate N votes for possible modulation schemes. Then classification of the interference modulation scheme can be carried out by the so-called *unfair voting*. The second stage uses the modulation scheme determined in the first stage and performs detection of the wanted signals. Details will be given in the sequel.

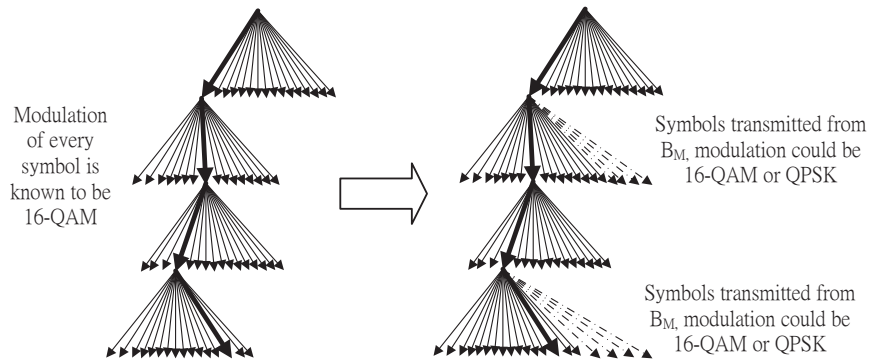


Figure 4.3: Illustration of the extended search tree for the 1st stage of the modified RTS for unknown interference modulation

4.1.1 The First Stage of the Modified RTS

In this first stage, the modified RTS again performs the hard-output SD algorithm to find the ML path but over extended modulation tree that contains all possible candidate modulation schemes for the interference. Hence, the main difference between the first stages of the modified RTS algorithms in this chapter and in previous chapter is the additional number of candidate modulation schemes for unknown interference. For example, if the modulation scheme of the interference may be either QPSK or 16QAM, each node on the search tree will have 20 children nodes, corresponding to the total number of QPSK symbols and 16QAM symbols. Such a new extended search tree is illustrated in Fig. 4.3.

After executing the first stage for N received elements (REs), we have the ML path for each RE, which suggests a modulation scheme for the interference. We can then decide or classify the modulation scheme of the interference via voting. It can be verified that different number of constellation points for different modulation scheme will give an unbalanced modulation classification error rate. For example, $\Pr(16\text{QAM}|\text{QPSK})$ is significantly larger than $\Pr(\text{QPSK}|16\text{QAM})$, where $\Pr(\text{modulation I}|\text{modulation II})$

denotes the error probability that modulation I is detected by the first stage of the modified RTS, while modulation II is the truly used one for the interference source.

Due to the unbalanced modulation error rate, we propose an “unfair voting” method by introduce a bias V_b such that the decision rule is

$$V_I + V_b \geq_{II}^I V_{II}, \quad (4.1)$$

where V_I and V_{II} denote the numbers of votes respectively for modulation I and modulation II. The parameters N and V_b will be later determined via simulations.

After performing N hard-output SD algorithms to determine the modulation scheme of the interference source via (4.1), those REs, whose ML paths suggest an alternative modulation scheme other than the decided one, will have to be re-done their corresponding hard-output SD algorithms with respect to the decided interference modulation scheme; otherwise the performance of the inter-cell interference cancellation may degrade significantly.

We end this subsection by emphasizing that although the first stage process that we described above is exemplified for two candidate interference modulation schemes as QPSK and 16QAM, it can be straightforwardly extended to three or more candidate interference modulation schemes, e.g., QPSK, 16QAM and 64QAM. Hence, one should be able to apply it to to-date LTE and LTE-Advanced standard.

4.1.2 The Second Stage of the Modified RTS

In the second stage of modified RTS, we will again generate the soft-output LLR values via the help of the counter hypothesis paths.

Since the receiver has no interest to recover the information contained within the interference, only the soft-output LLRs of the desired signals will be generated. For this reason, we modify the sorting and QR-decomposition (SQRD) algorithm [13] such that the symbols corresponding to the desired signals are placed in the first N_s levels of the search tree. Again, in these N_s levels, Q counter hypothesis paths are extended

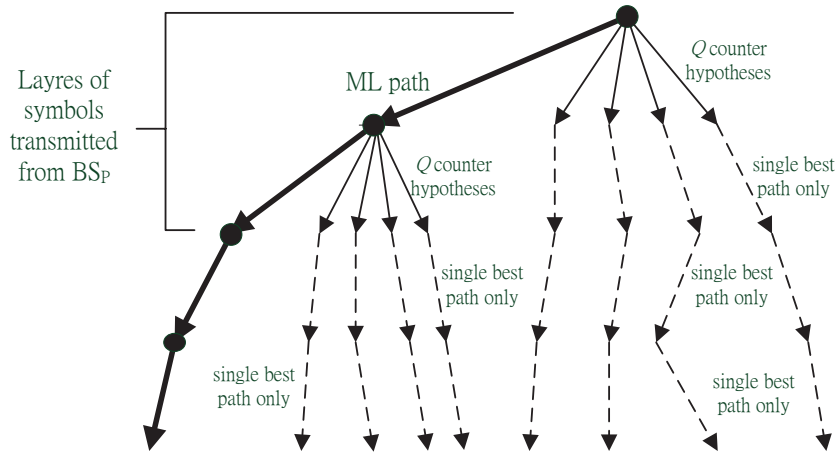


Figure 4.4: Illustration of the 2nd stage of the modified RTS for unknown interference modulation

in order to generate the soft-output LLR values. During this process, only the paths corresponding to the best candidate symbol are retained. The process will be repeated until the bottom level of the search tree is reached. An example of the second stage is illustrated in Fig. 4.4.

4.2 Simulation Results

In this section, simulation results for $N_s = N_i = 2$ and $N_R = 4$ will be presented, which corresponds to the system model

$$\begin{aligned}
 \mathbf{y} &= \mathbf{H}_s \mathbf{P}_s \mathbf{x}_s + \mathbf{H}_i \mathbf{P}_i \mathbf{x}_i + \mathbf{n} \\
 &= [\mathbf{H}_s \mathbf{P}_s \quad \mathbf{H}_i \mathbf{P}_i] \begin{bmatrix} x_1 \\ x_2 \\ i_1 \\ i_2 \end{bmatrix} + \mathbf{n},
 \end{aligned}$$

where \mathbf{n} denotes the additive white Gaussian noise. In the simulation, the modulations of the desired signals x_1 and x_2 are 16QAM, whereas the modulations of interferences i_1 and i_2 can be either 16QAM or QPSK and are unknown to the receiver. A 3GPP-

Algorithm 1 Modified SQRD Algorithm

```
1:  $\mathbf{R} = \mathbf{0}$ ,  $\mathbf{Q} = \mathbf{H}$ ,  $\mathbf{P} = \mathbf{I}_{N_T}$ 
2: for  $i = 1, \dots, N_s$  do
3:    $k_i = \arg \min_{j=1, \dots, N_s} |\mathbf{q}_j|^2$ 
4:   Exchange columns  $i$  and  $k_i$  in  $\mathbf{Q}$ ,  $\mathbf{R}$ , and  $\mathbf{P}$ 
5:    $r_{i,i} = |\mathbf{q}_i|$ 
6:    $\mathbf{q}_i = \mathbf{q}_i / r_{i,i}$ 
7:   for  $j = i + 1, \dots, N_T$  do
8:      $r_{i,j} = \mathbf{q}_i^H \mathbf{q}_j$ 
9:      $\mathbf{q}_j = \mathbf{q}_j - r_{i,j} \cdot \mathbf{q}_i$ 
10:  end for
11: end for
12: for  $i = N_s + 1, \dots, N_T$  do
13:    $k_i = \arg \min_{j=N_s+1, \dots, N_T} |\mathbf{q}_j|^2$ 
14:   Exchange columns  $i$  and  $k_i$  in  $\mathbf{Q}$ ,  $\mathbf{R}$ , and  $\mathbf{P}$ 
15:    $r_{i,i} = |\mathbf{q}_i|$ 
16:    $\mathbf{q}_i = \mathbf{q}_i / r_{i,i}$ 
17:   for  $j = i + 1, \dots, N_T$  do
18:      $r_{i,j} = \mathbf{q}_i^H \mathbf{q}_j$ 
19:      $\mathbf{q}_j = \mathbf{q}_j - r_{i,j} \cdot \mathbf{q}_i$ 
20:  end for
21: end for
```

specified punctured turbo code of code rate $R = 1/2$ and codeword length 1920 bits is adopted [10]. Under a 15×128 block interleaver, 480 16-QAM symbols are received at the receiver, in which the 8-iteration Max-Log-MAP decoder is used for turbo decoding. It is assumed that the channel coefficients can be perfectly estimated. Only the slow fading scenario is considered; hence, the parameter L_{\max} is set to be 0.2.

We first examine the impact on the correctness of modulation classifications in Fig. 4.5. The exact modulation schemes of the interference sources i_1 and i_2 are 16QAM and QPSK, respectively. For the incorrect modulation judgement of interference, two situations are thus examined. The modulation scheme of i_1 is wrongly declared as QPSK, and that of i_2 is wrongly decided to be 16QAM. We can then observe from Fig. 4.5 that any one incorrectly judgement on interference modulation scheme can seriously jeopardize the system performance, where the resultant BLERs decrease at a

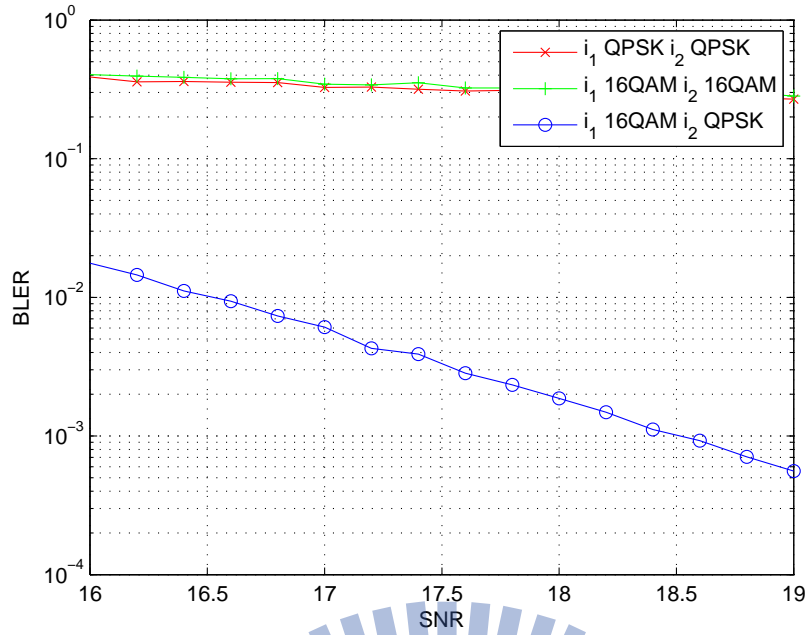


Figure 4.5: Comparison of BLERs between correct and erroneous declarations of modulation scheme for interferences

very low speed as the SNR grows.

Next, we investigate the modulation classification errors when only one RE is used. The modulation schemes of i_1 and i_2 are set as $\{16\text{QAM}, 16\text{QAM}\}$, $\{\text{QPSK}, 16\text{QAM}\}$, $\{\text{QPSK}, \text{QPSK}\}$ in the left, middle, and right subfigures of Fig. 4.6 respectively.¹

Similar to those examined in Fig. 4.6, we show the modulation classification error for one RE in Fig. 4.7, where the modulation schemes of i_1 and i_2 are now randomly chosen with equal probability from QPSK and 16QAM. Figure 4.7 again confirms that high-order modulations are favored in decision, particularly at the low SNR region.

Next, we examine the thresholds for unfair voting when taking $N = 8$ and $N = 16$ REs in Figs. 4.8 and 4.9, respectively. The interference modulation scheme to be compared is the modified GLRT in [14]. Note that since the number of total votes is an even number, we set the thresholds V_{bias} to be also even as for example setting $V_{\text{bias}} = 0$

¹It can be verified that the simulation result for the modulation scheme of i_1 and i_2 being $\{16\text{QAM}, \text{QPSK}\}$ is identical to that of i_1 and i_2 being $\{\text{QPSK}, 16\text{QAM}\}$. Therefore, we omit such case in Fig. 4.6.

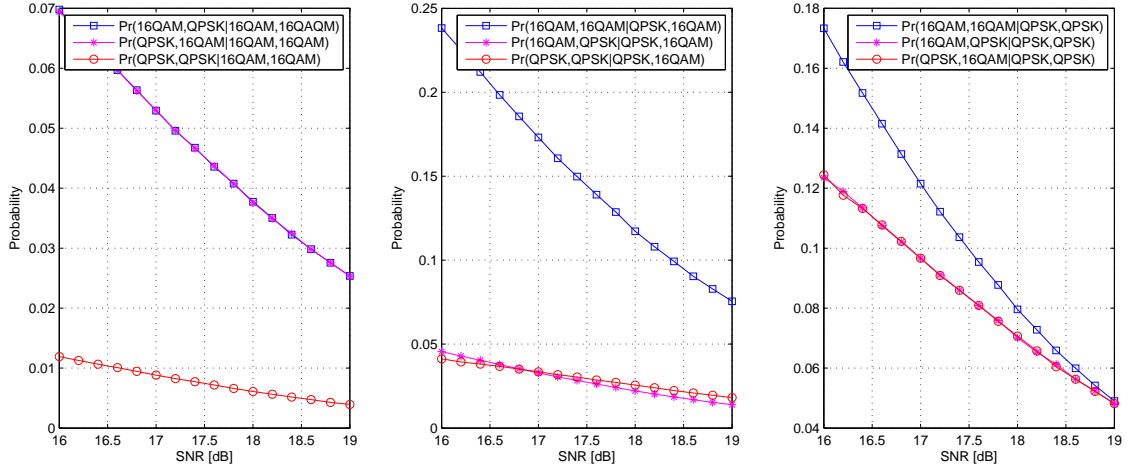


Figure 4.6: Modulation classification errors. The modulation schemes of i_1 and i_2 are set as $\{16\text{QAM}, 16\text{QAM}\}$, $\{\text{QPSK}, 16\text{QAM}\}$, $\{\text{QPSK}, \text{QPSK}\}$ from left to right in the three subfigures, respectively.

is equivalent to setting $V_{\text{bias}} = 1$, setting $V_{\text{bias}} = 2$ is equivalent to setting $V_{\text{bias}} = 3$, etc. In order to reduce the modulation classification error, we determine the threshold according to

$$\min_{V_{\text{bias}}} \{\max\{\Pr(\text{QPSK}|16\text{QAM}), P(16\text{QAM}|\text{QPSK})\}\}.$$

We then found that $V_{\text{bias}} = 2$ and $V_{\text{bias}} = 6$ achieve the above minimization values respectively for $N = 8$ and $N = 16$.

After identifying the V_{bias} , we next compare the performance of unfair voting with that of the modified GLRT [14]. In Fig. 4.10, the incorrect modulation classification error rates respectively using unfair voting and the modified GLRT are illustrated for both $N = 8$ and $N = 16$. In Fig. 4.11, the average complexity per receive antenna and the number of paths stored during the modulation classification stage are presented. Notably, the number of paths stored can be regarded as an index of memory storage required for the proposed algorithm. We can see from the two figures that the modified GLRT outperforms the proposed unfair voting in classification error rate; however, the superiority in classification error rate of the modified GLRT is obtained at the cost of a

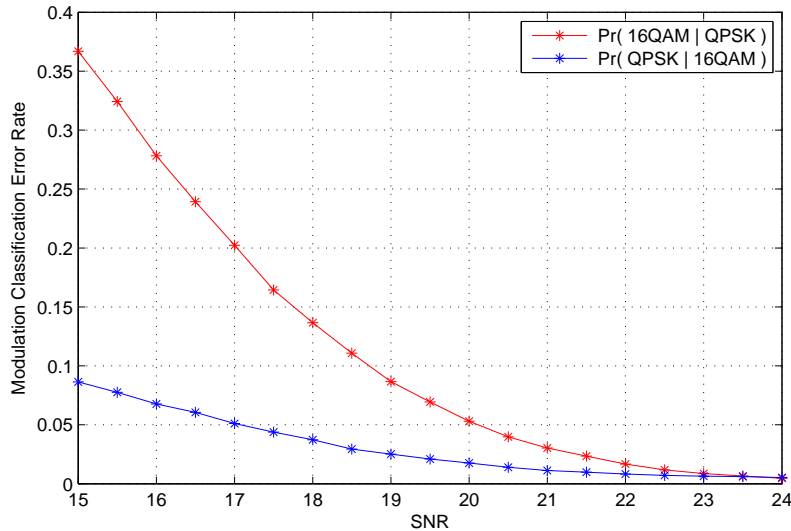


Figure 4.7: Modulation classification error. Modulation schemes of i_1 and i_2 are randomly chosen from QPSK and 16QAM.

higher complexity and higher storage requirement. The high complexity of the modified GLRT is due to that it checks the metrics of all possible hypotheses. In the scenario we simulated, the modified GLRT needs to examine the four cases of *i*) $i_1 \in \text{QPSK}$ and $i_2 \in \text{QPSK}$, *ii*) $i_1 \in \text{16QAM}$ and $i_2 \in \text{QPSK}$, *iii*) $i_1 \in \text{QPSK}$ and $i_2 \in \text{16QAM}$, and *iv*) $i_1 \in \text{16QAM}$ and $i_2 \in \text{16QAM}$. In addition, to determine the ML path as well as the ML path's metric for each hypothesis, the SESD algorithm should be executed four times. During this process, all information for each candidate path needs to be stored. For the above reasons, the modified GLRT requires a much higher complexity and storage requirement than our proposed unfair voting.

We would like to add at the end of this discussion that the complexity and the number of paths required to be stored for the modified GLRT are actually proportional to the number of hypotheses, while those of the proposed unfair voting, are only proportional to N_i (i.e., the number of interferences), where the number of hypotheses grows exponentially as N_i increases.

In this thesis, we only consider QPSK and 16QAM as candidate modulation schemes

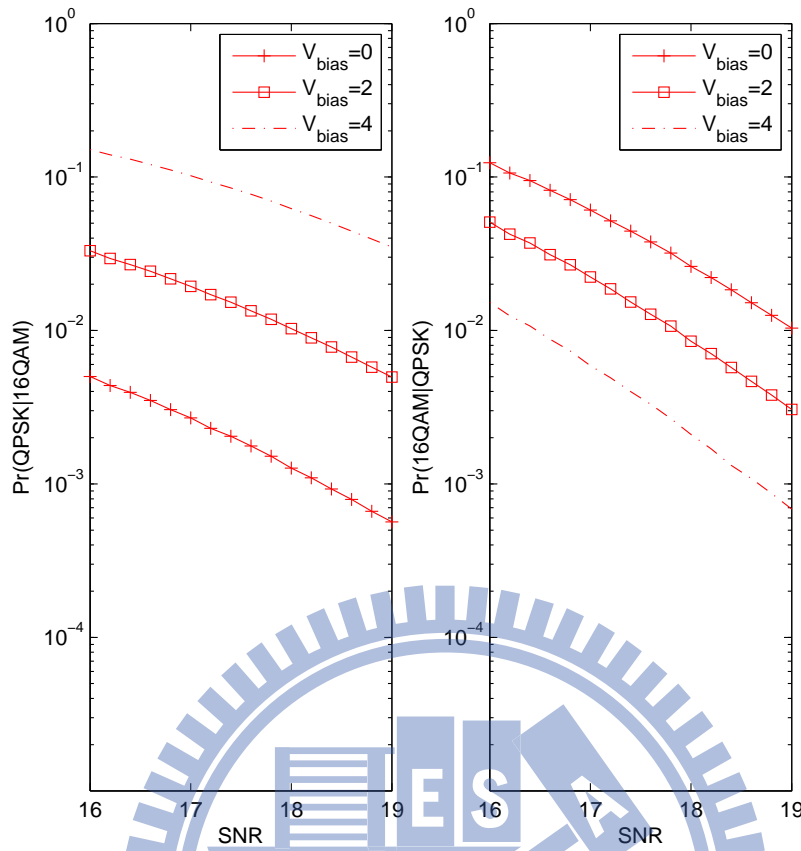


Figure 4.8: Classification errors for different V_{bias} subject to $N = 8$

for interferences. If 64QAM is additionally considered, then the complexity of the GLRT may grow dramatically and become impractical.

On the other hand, the performance gap in Fig. 4.10 regarding $\Pr(16\text{QAM}|\text{QPSK})$ may look huge; however, Figure 4.12 indicates that the simulated BLERs of the modified GLRT and the proposed unfair voting are not that deviated. We may accordingly conclude that the proposed unfair voting can achieve similar performance to the modified GLRT with a much smaller complexity and its simplicity in implementation makes it a suitable candidate for hardware implementation.

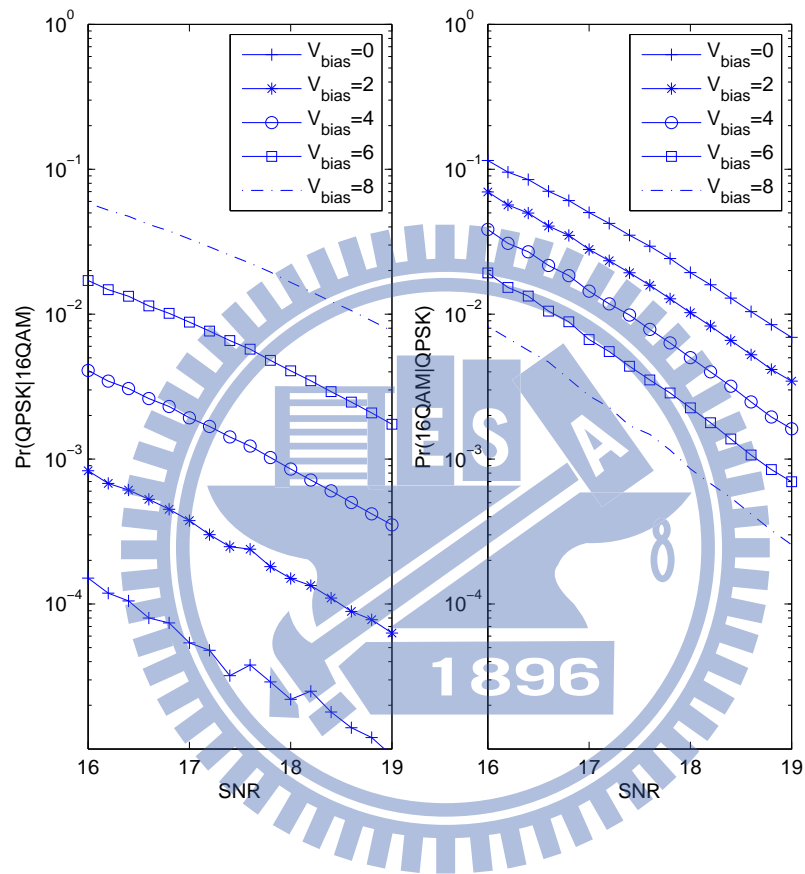


Figure 4.9: Classification errors for different V_{bias} subject to $N = 16$

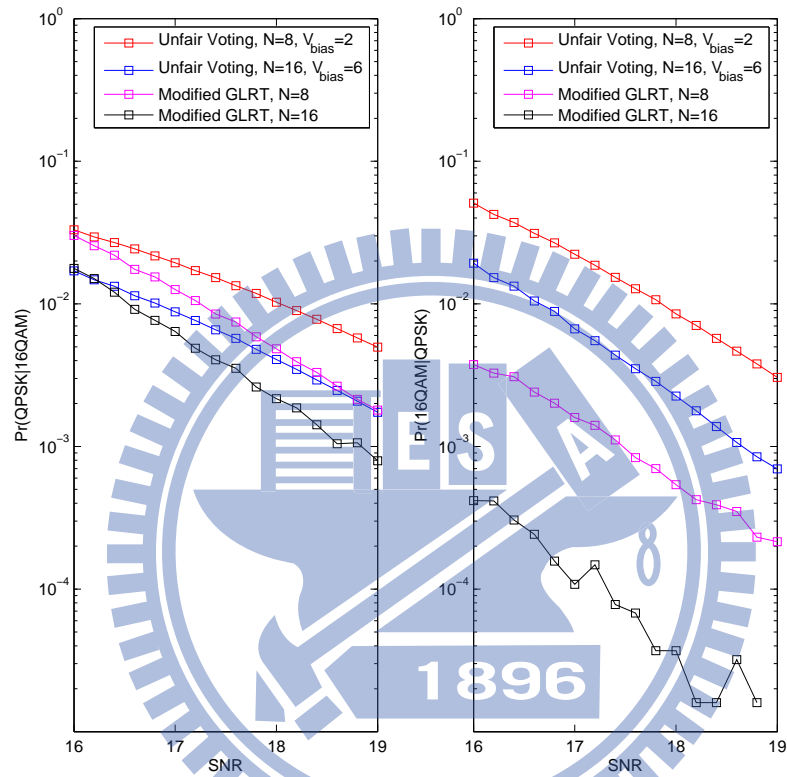


Figure 4.10: Modulation classification error rate for unfair voting and the modified GLRT

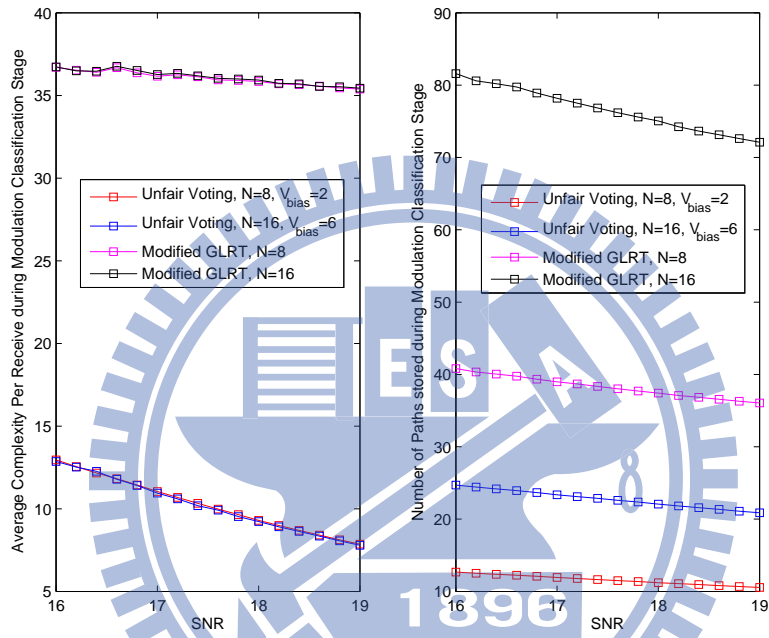


Figure 4.11: Average complexity and the numbers of paths stored during the modulation classification stage

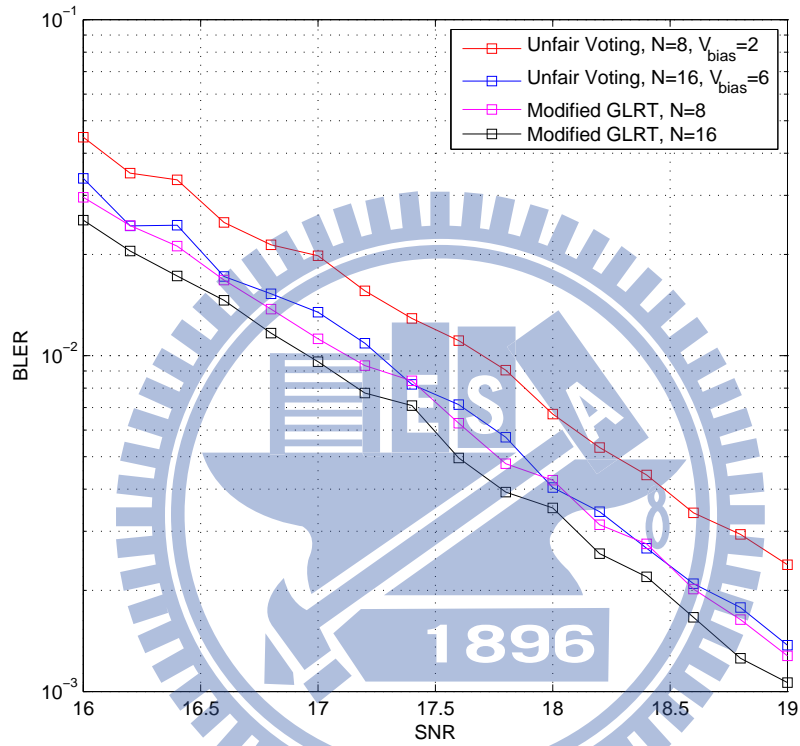


Figure 4.12: Block error rate of the modified GLRT and the proposed unfair voting

Chapter 5

Conclusion and Future Work

In this thesis, we proposed a soft-output SD algorithm, named the *modified RTS*, that can provide a good performance-complexity tradeoff and is appropriate for hardware implementation. Furthermore, based on the modified RTS, we further propose a simple method called *unfair voting* to perform the joint modulation classification and signal detection. Considering its simplicity and also its low requirement in storage, the proposed unfair voting becomes a good candidate for hardware implementation.

At this stage, the V_{bias} is actually determined based on simulations. Finding a theoretical footing for the selected V_{bias} could be an interesting future work. To examine the possibility of a soft voting rather than a hard voting could be another interesting subject to explore. Via these modifications, the modulation classification and the signal detection may become more reliable.

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