

## 附表

表 3.1 遺傳演算法模組測試，參數與條件設定

|                   |      |
|-------------------|------|
| 族群數(population)   | 20   |
| 演化世代(generations) | 150  |
| 突變率               | 0.08 |
| $x_1$ 搜尋範圍        | -2~2 |
| $x_2$ 搜尋範圍        | -3~3 |

表 3.2 參考模型測試，參數與條件設定

|                     |         |
|---------------------|---------|
| 族群數(population)     | 50      |
| 演化世代(generations)   | 1000    |
| 設計變數                | 17      |
| 設計變數範圍              | 0.1~2.0 |
| 突變率                 | 0.08    |
| $\psi$ 懲罰因子         | 1.05    |
| $\alpha$ 違反限制常數指數因子 | 1       |

表 5.1.1 例一，FSD 收斂過程

| No.       | A <sub>1</sub> | A <sub>2</sub> | A <sub>3</sub> | A <sub>4</sub> | A <sub>5</sub> | A <sub>6</sub> | A <sub>7</sub> | A <sub>8</sub> | A <sub>9</sub> | A <sub>10</sub> |
|-----------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|-----------------|
| 0         | 1.00           | 1.0000         | 1.0000         | 1.0000         | 1.0000         | 1.0000         | 1.0000         | 1.0000         | 1.0000         | 1.0000          |
| 1         | 7.44           | 1.2141         | 8.5557         | 2.7859         | 0.6584         | 1.2141         | 6.4428         | 4.8709         | 3.9399         | 1.7170          |
| 2         | 7.24           | 0.9266         | 8.7577         | 3.0734         | 0.1690         | 0.9266         | 6.7284         | 4.5853         | 4.3464         | 1.3105          |
| 3         | 7.25           | 0.7410         | 8.7440         | 3.2590         | 0.0030         | 0.7410         | 6.7091         | 4.6047         | 4.6089         | 1.0480          |
| 4         | 7.38           | 0.6100         | 8.6105         | 3.3900         | 0.0005         | 0.6100         | 6.5202         | 4.7935         | 4.7942         | 0.8627          |
| 5         | 7.50           | 0.4953         | 8.4954         | 3.5047         | 0.0001         | 0.4953         | 6.3575         | 4.9562         | 4.9563         | 0.7005          |
| 6         | 7.60           | 0.3973         | 8.3973         | 3.6027         | 0.0000         | 0.3973         | 6.2187         | 5.0950         | 5.0950         | 0.5619          |
| 7         | 7.68           | 0.3151         | 8.3151         | 3.6849         | 0.0000         | 0.3151         | 6.1024         | 5.2113         | 5.2113         | 0.4456          |
| 8         | 7.75           | 0.2473         | 8.2473         | 3.7527         | 0.0000         | 0.2473         | 6.0067         | 5.3071         | 5.3071         | 0.3498          |
| 9         | 7.80           | 0.1925         | 8.1925         | 3.8075         | 0.0000         | 0.1925         | 5.9291         | 5.3847         | 5.3847         | 0.2722          |
| 10        | 7.85           | 0.1487         | 8.1487         | 3.8513         | 0.0000         | 0.1487         | 5.8671         | 5.4466         | 5.4466         | 0.2102          |
| 11        | 7.88           | 0.1141         | 8.1141         | 3.8859         | 0.0000         | 0.1141         | 5.8182         | 5.4955         | 5.4955         | 0.1614          |
| 12        | 7.91           | 0.0871         | 8.0871         | 3.9129         | 0.0000         | 0.0871         | 5.7801         | 5.5336         | 5.5336         | 0.1232          |
| 13        | 7.93           | 0.0663         | 8.0663         | 3.9337         | 0.0000         | 0.0663         | 5.7506         | 5.5631         | 5.5631         | 0.0937          |
| 14        | 7.94           | 0.0502         | 8.0502         | 3.9498         | 0.0000         | 0.0502         | 5.7279         | 5.5858         | 5.5858         | 0.0710          |
| 15        | 7.96           | 0.0380         | 8.0380         | 3.9620         | 0.0000         | 0.0380         | 5.7106         | 5.6031         | 5.6031         | 0.0537          |
| 16        | 7.97           | 0.0287         | 8.0287         | 3.9713         | 0.0000         | 0.0287         | 5.6974         | 5.6163         | 5.6163         | 0.0405          |
| 17        | 7.97           | 0.0216         | 8.0216         | 3.9784         | 0.0000         | 0.0216         | 5.6874         | 5.6263         | 5.6263         | 0.0306          |
| 18        | 7.98           | 0.0163         | 8.0163         | 3.9837         | 0.0000         | 0.0163         | 5.6799         | 5.6339         | 5.6339         | 0.0230          |
| 19        | 7.98           | 0.0122         | 8.0122         | 3.9878         | 0.0000         | 0.0122         | 5.6742         | 5.6396         | 5.6396         | 0.0173          |
| 20        | 7.99           | 0.0092         | 8.0092         | 3.9908         | 0.0000         | 0.0092         | 5.6699         | 5.6439         | 5.6439         | 0.0130          |
| 21        | 7.99           | 0.0069         | 8.0069         | 3.9931         | 0.0000         | 0.0069         | 5.6666         | 5.6471         | 5.6471         | 0.0098          |
| 22        | 7.99           | 0.0052         | 8.0052         | 3.9948         | 0.0000         | 0.0052         | 5.6642         | 5.6495         | 5.6495         | 0.0073          |
| 23        | 7.99           | 0.0039         | 8.0039         | 3.9961         | 0.0000         | 0.0039         | 5.6624         | 5.6514         | 5.6514         | 0.0055          |
| 24        | 7.99           | 0.0029         | 8.0029         | 3.9971         | 0.0000         | 0.0029         | 5.6610         | 5.6527         | 5.6527         | 0.0041          |
| 25        | 7.99           | 0.0022         | 8.0022         | 3.9978         | 0.0000         | 0.0022         | 5.6600         | 5.6538         | 5.6538         | 0.0031          |
| 26        | 7.99           | 0.0016         | 8.0016         | 3.9984         | 0.0000         | 0.0016         | 5.6592         | 5.6545         | 5.6545         | 0.0023          |
| 27        | 7.99           | 0.0012         | 8.0012         | 3.9988         | 0.0000         | 0.0012         | 5.6586         | 5.6551         | 5.6551         | 0.0017          |
| 28        | 7.99           | 0.0009         | 8.0009         | 3.9991         | 0.0000         | 0.0009         | 5.6582         | 5.6556         | 5.6556         | 0.0013          |
| 29        | 7.99           | 0.0007         | 8.0007         | 3.9993         | 0.0000         | 0.0007         | 5.6578         | 5.6559         | 5.6559         | 0.0010          |
| 30        | 7.99           | 0.0005         | 8.0005         | 3.9995         | 0.0000         | 0.0005         | 5.6576         | 5.6561         | 5.6561         | 0.0007          |
| 31        | 7.99           | 0.0004         | 8.0004         | 3.9996         | 0.0000         | 0.0004         | 5.6574         | 5.6563         | 5.6563         | 0.0006          |
| 32        | 7.99           | 0.0003         | 8.0003         | 3.9997         | 0.0000         | 0.0003         | 5.6573         | 5.6564         | 5.6564         | 0.0004          |
| 33        | 7.99           | 0.0002         | 8.0002         | 3.9998         | 0.0000         | 0.0002         | 5.6572         | 5.6565         | 5.6565         | 0.0003          |
| 34        | 7.99           | 0.0002         | 8.0002         | 3.9998         | 0.0000         | 0.0002         | 5.6571         | 5.6566         | 5.6566         | 0.0002          |
| 35        | 7.99           | 0.0001         | 8.0001         | 3.9999         | 0.0000         | 0.0001         | 5.6570         | 5.6567         | 5.6567         | 0.0002          |
| 36        | 7.99           | 0.0001         | 8.0001         | 3.9999         | 0.0000         | 0.0001         | 5.6570         | 5.6567         | 5.6567         | 0.0001          |
| 37        | 7.99           | 0.0001         | 8.0001         | 3.9999         | 0.0000         | 0.0001         | 5.6570         | 5.6568         | 5.6568         | 0.0001          |
| 38        | 8.00           | 0.0001         | 8.0001         | 4.0000         | 0.0000         | 0.0001         | 5.6569         | 5.6568         | 5.6568         | 0.0001          |
| 39        | 8.00           | 0.0000         | 8.0000         | 4.0000         | 0.0000         | 0.0000         | 5.6569         | 5.6568         | 5.6568         | 0.0001          |
| <b>40</b> | <b>8.00</b>    | <b>0.0000</b>  | <b>8.0000</b>  | <b>4.0000</b>  | <b>0.0000</b>  | <b>0.0000</b>  | <b>5.6569</b>  | <b>5.6568</b>  | <b>5.6568</b>  | <b>0.0000</b>   |

表 5.1.2 例一，A<sub>F</sub>經結構分析後節點位移

| Joint displacement(in) |               |               |
|------------------------|---------------|---------------|
| Joint No.              | X Translation | Y Translation |
| 1                      | 1.4592e+00    | -6.6408e+00   |
| 2                      | -1.8000e+00   | -7.1999e+00   |
| 3                      | 8.9999e-01    | -2.7000e+00   |
| 4                      | -9.0001e-01   | -2.7000e+00   |
| 5                      | 0.0000e+00    | 0.0000e+00    |
| 6                      | 0.0000e+00    | 0.0000e+00    |

表 5.1.3 例一，A<sub>F</sub>經結構分析後桿件應力

| Member Axial Stress(ksi) |              |
|--------------------------|--------------|
| Member No.               | Axial Stress |
| 1                        | 25.000       |
| 2                        | 15.532       |
| 3                        | -25.000      |
| 4                        | -25.000      |
| 5                        | 0.002        |
| 6                        | 15.532       |
| 7                        | 25.000       |
| 8                        | -25.000      |
| 9                        | 25.000       |
| 10                       | -21.966      |

表 5.1.4 例一，第一次搜尋結果( $\alpha=1$ )

| Step1  |   | $\alpha=1$           |         |           |                              |         |                | K=2108.1                |                       |                       |
|--------|---|----------------------|---------|-----------|------------------------------|---------|----------------|-------------------------|-----------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$<br>(4-6) | $u_i$   | $S_i$     | $\Delta_i$<br>(4-2)          | $W_i$   | $I_i$<br>(4-7) | $\Delta_i'(K)$<br>(4-8) | $A_i^{(1)}$<br>(4-9)  | $A_i^{(2)}$<br>(4-10) |
| 1      | 360   | 8.0000               | 1.9999  | 199.9985  | 1.7999                       | 288.000 | 0.0062         | 0.4781                  | 30.1195               | 30.4885               |
| 2      | 360   | 0.0001               | 0.0000  | 0.0016    | 0.0000                       | 0.004   | 0.0000         | 0.0000                  | 0.1000                | 0.1012                |
| 3      | 360   | 8.0000               | -1.0001 | -200.0016 | 0.9001                       | 288.000 | 0.0031         | 0.3267                  | 22.0376               | 22.3076               |
| 4      | 360   | 4.0000               | -1.0000 | -99.9985  | 0.9000                       | 144.000 | 0.0062         | 0.2390                  | 15.0598               | 15.2443               |
| 5      | 360   | 0.0001               | -0.0001 | 0.0000    | 0.0000                       | 0.004   | 0.0000         | 0.0000                  | 0.1000                | 0.1012                |
| 6      | 360   | 0.0001               | 0.0000  | 0.0016    | 0.0000                       | 0.004   | 0.0000         | 0.0000                  | 0.1000                | 0.1012                |
| 7      | 509.12  | 5.6569               | 0.0001  | 141.4236  | 0.0002                       | 288.000 | 0.0000         | 0.0002                  | 5.6603                | 5.7296                |
| 8      | 509.12  | 5.6569               | -1.4141 | -141.4192 | 1.7998                       | 288.000 | 0.0062         | 0.4781                  | 21.2972               | 21.5581               |
| 9      | 509.12  | 5.6569               | 1.4142  | 141.4192  | 1.7999                       | 288.000 | 0.0062         | 0.4781                  | 21.2978               | 21.5587               |
| 10     | 509.12  | 0.0001               | 0.0000  | -0.0022   | 0.0000                       | 0.005   | 0.0000         | 0.0000                  | 0.1000                | 0.1012                |
|        |   |                      |         |           | $\Delta = 7.200(\downarrow)$ |         |                | 2.000( $\downarrow$ )   | 2.025( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | <ul style="list-style-type: none"> <li>● 桿件 5 應力為 -36.1 ksi，超過容許應力 25 ksi。</li> <li>● 節點 1 位移為 2.1201 in(<math>\downarrow</math>)，超過容許位移 2 in。</li> <li>● 總重量為：4952.39 lb。</li> </ul> |                      |         |           |                              |         |                |                         |                       |                       |

表 5.1.5 例一， $\alpha=3.6$  時之斷面修正

|        |   | $\alpha=3.6$ |         |           |                              |          |        | K=0                   |                       |                       |
|--------|---|--------------|---------|-----------|------------------------------|----------|--------|-----------------------|-----------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$  | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$    | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$           | $A_i^{(2)}$           |
| 1      | 360   | 28.8000      | 1.9999  | 199.9985  | 0.5000                       | 1036.800 | 0.0005 | 0.5000                | 28.8000               | 28.7165               |
| 2      | 360   | 0.0004       | 0.0000  | 0.0016    | 0.0000                       | 0.013    | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 3      | 360   | 28.8000      | -1.0001 | -200.0016 | 0.2500                       | 1036.800 | 0.0002 | 0.2500                | 28.8000               | 28.7165               |
| 4      | 360   | 14.4000      | -1.0000 | -99.9985  | 0.2500                       | 518.400  | 0.0005 | 0.2500                | 14.4000               | 14.3582               |
| 5      | 360   | 0.0004       | -0.0001 | 0.0000    | 0.0000                       | 0.013    | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 6      | 360   | 0.0004       | 0.0000  | 0.0016    | 0.0000                       | 0.013    | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 7      | 509.12  | 20.3647      | 0.0001  | 141.4236  | 0.0000                       | 1036.801 | 0.0000 | 0.0000                | 20.3647               | 20.3056               |
| 8      | 509.12  | 20.3647      | -1.4141 | -141.4192 | 0.4999                       | 1036.799 | 0.0005 | 0.4999                | 20.3647               | 20.3056               |
| 9      | 509.12  | 20.3647      | 1.4142  | 141.4192  | 0.5000                       | 1036.799 | 0.0005 | 0.5000                | 20.3647               | 20.3056               |
| 10     | 509.12  | 0.0004       | 0.0000  | -0.0022   | 0.0000                       | 0.018    | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
|        |   |              |         |           | $\Delta = 2.000(\downarrow)$ |          |        | 2.000( $\downarrow$ ) | 2.000( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | <ul style="list-style-type: none"> <li>● 桿件皆滿足容許應力限制。</li> <li>● 位移皆滿足容許位移限制。</li> <li>● 總重量：5701.75 lb。</li> </ul> |              |         |           |                              |          |        |                       |                       |                       |

表 5.1.6 例一，第 2 次搜尋結果 ( $\alpha=2.3$ )

| Step2  |   | $\alpha=2.3$ |         |           |                              |         |        | K=1330.7              |                       |                       |
|--------|---|--------------|---------|-----------|------------------------------|---------|--------|-----------------------|-----------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$  | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$           | $A_i^{(2)}$           |
| 1      | 360   | 18.4000      | 1.9999  | 199.9985  | 0.7826                       | 662.400 | 0.0012 | 0.4880                | 29.5094               | 29.5552               |
| 2      | 360   | 0.0002       | 0.0000  | 0.0016    | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                | 0.1002                |
| 3      | 360   | 18.4000      | -1.0001 | -200.0016 | 0.3913                       | 662.400 | 0.0006 | 0.2928                | 24.5911               | 24.6292               |
| 4      | 360   | 9.2000       | -1.0000 | -99.9985  | 0.3913                       | 331.200 | 0.0012 | 0.2440                | 14.7547               | 14.7776               |
| 5      | 360   | 0.0002       | -0.0001 | 0.0000    | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                | 0.1002                |
| 6      | 360   | 0.0002       | 0.0000  | 0.0016    | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                | 0.1002                |
| 7      | 509.12  | 13.0108      | 0.0001  | 141.4236  | 0.0001                       | 662.401 | 0.0000 | 0.0001                | 13.0117               | 13.0319               |
| 8      | 509.12  | 13.0108      | -1.4141 | -141.4192 | 0.7825                       | 662.400 | 0.0012 | 0.4879                | 20.8659               | 20.8983               |
| 9      | 509.12  | 13.0108      | 1.4142  | 141.4192  | 0.7826                       | 662.400 | 0.0012 | 0.4880                | 20.8664               | 20.8987               |
| 10     | 509.12  | 0.0002       | 0.0000  | -0.0022   | 0.0000                       | 0.012   | 0.0000 | 0.0000                | 0.1000                | 0.1002                |
|        |   |              |         |           | $\Delta = 3.130(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.003( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5289.98 lb。 |              |         |           |                              |         |        |                       |                       |                       |

表 5.1.7 例一，第 3 次搜尋結果 ( $\alpha=1.650000$ )

| Step3  |   | $\alpha=$<br>1.650000 |         |           |                             |         |        | K=1791.54             |                        |                       |
|--------|---|-----------------------|---------|-----------|-----------------------------|---------|--------|-----------------------|------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$           | $u_i$   | $S_i$     | $\Delta_i$                  | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$            | $A_i^{(2)}$           |
| 1      | 360   | 13.2000               | 1.9999  | 199.9985  | 1.0909                      | 475.200 | 0.0023 | 0.4824                | 29.8466                | 30.0003               |
| 2      | 360   | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                 | 0.1005                |
| 3      | 360   | 13.2000               | -1.0001 | -200.0016 | 0.5455                      | 475.200 | 0.0011 | 0.3120                | 23.0778                | 23.1966               |
| 4      | 360   | 6.6000                | -1.0000 | -99.9985  | 0.5454                      | 237.600 | 0.0023 | 0.2412                | 14.9233                | 15.0002               |
| 5      | 360   | 0.0002                | -0.0001 | 0.0000    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                 | 0.1005                |
| 6      | 360   | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                 | 0.1005                |
| 7      | 509.12  | 9.3338                | 0.0001  | 141.4236  | 0.0001                      | 475.200 | 0.0000 | 0.0001                | 9.3356                 | 9.3837                |
| 8      | 509.12  | 9.3338                | -1.4141 | -141.4192 | 1.0908                      | 475.200 | 0.0023 | 0.4824                | 21.1042                | 21.2129               |
| 9      | 509.12  | 9.3338                | 1.4142  | 141.4192  | 1.0909                      | 475.200 | 0.0023 | 0.4824                | 21.1048                | 21.2135               |
| 10     | 509.12  | 0.0002                | 0.0000  | -0.0022   | 0.0000                      | 0.008   | 0.0000 | 0.0000                | 0.1000                 | 0.1005                |
|        |   |                       |         |           | $\Delta =4.364(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0103( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5108.80 lb。 |                       |         |           |                             |         |        |                       |                        |                       |

表 5.1.8 例一，第 4 次搜尋結果 ( $\alpha=1.325000$ )

| Step4  |  | $\alpha=$<br>1.325000 |         |           |                             |         |        |                       | K=1969.36               |                       |  |
|--------|--|-----------------------|---------|-----------|-----------------------------|---------|--------|-----------------------|-------------------------|-----------------------|--|
| No.    | $L_i$  | $A_i^{(0)}$           | $u_i$   | $S_i$     | $\Delta_i$                  | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |  |
| 1      | 360  | 10.6000               | 1.9999  | 199.9985  | 1.3584                      | 381.600 | 0.0036 | 0.4800                | 30.0010                 | 30.2305               |  |
| 2      | 360  | 0.0001                | 0.0000  | 0.0016    | 0.0000                      | 0.005   | 0.0000 | 0.0000                | 0.1000                  | 0.1008                |  |
| 3      | 360  | 10.6000               | -1.0001 | -200.0016 | 0.6793                      | 381.600 | 0.0018 | 0.3200                | 22.5004                 | 22.6726               |  |
| 4      | 360  | 5.3000                | -1.0000 | -99.9985  | 0.6792                      | 190.800 | 0.0036 | 0.2400                | 15.0006                 | 15.1153               |  |
| 5      | 360  | 0.0001                | -0.0001 | 0.0000    | 0.0000                      | 0.005   | 0.0000 | 0.0000                | 0.1000                  | 0.1008                |  |
| 6      | 360  | 0.0001                | 0.0000  | 0.0016    | 0.0000                      | 0.005   | 0.0000 | 0.0000                | 0.1000                  | 0.1008                |  |
| 7      | 509.12   | 7.4953                | 0.0001  | 141.4236  | 0.0001                      | 381.600 | 0.0000 | 0.0001                | 7.4978                  | 7.5551                |  |
| 8      | 509.12   | 7.4953                | -1.4141 | -141.4192 | 1.3583                      | 381.600 | 0.0036 | 0.4799                | 21.2134                 | 21.3757               |  |
| 9      | 509.12   | 7.4953                | 1.4142  | 141.4192  | 1.3584                      | 381.600 | 0.0036 | 0.4800                | 21.2140                 | 21.3763               |  |
| 10     | 509.12   | 0.0001                | 0.0000  | -0.0022   | 0.0000                      | 0.007   | 0.0000 | 0.0000                | 0.1000                  | 0.1008                |  |
|        |  |                       |         |           | $\Delta =5.434(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0153 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |  |
| Result | 桿件皆滿足容許應力限制。<br>節點 1 位移為 2.0374 in( $\downarrow$ )，超過容許位移 2 in。<br>總重量：5025.89 lb。 |                       |         |           |                             |         |        |                       |                         |                       |  |



表 5.1.9 例一，第 5 次搜尋結果 ( $\alpha=1.487500$ )

| Step5  |   | $\alpha=$<br>1.487500 |         |           |                             |         |        | K=1885.86             |                         |                       |
|--------|---|-----------------------|---------|-----------|-----------------------------|---------|--------|-----------------------|-------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$           | $u_i$   | $S_i$     | $\Delta_i$                  | $W_i$   | $I_i$  | $\Delta_i'(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |
| 1      | 360   | 11.9000               | 1.9999  | 199.9985  | 1.2100                      | 428.400 | 0.0028 | 0.4811                | 29.9318                 | 30.1144               |
| 2      | 360   | 0.0001                | 0.0000  | 0.0016    | 0.0000                      | 0.005   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 3      | 360   | 11.9000               | -1.0001 | -200.0016 | 0.6051                      | 428.400 | 0.0014 | 0.3161                | 22.7776                 | 22.9165               |
| 4      | 360   | 5.9500                | -1.0000 | -99.9985  | 0.6050                      | 214.200 | 0.0028 | 0.2405                | 14.9660                 | 15.0572               |
| 5      | 360   | 0.0001                | -0.0001 | 0.0000    | 0.0000                      | 0.005   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 6      | 360   | 0.0001                | 0.0000  | 0.0016    | 0.0000                      | 0.005   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 7      | 509.12  | 8.4146                | 0.0001  | 141.4236  | 0.0001                      | 428.400 | 0.0000 | 0.0001                | 8.4166                  | 8.4680                |
| 8      | 509.12  | 8.4146                | -1.4141 | -141.4192 | 1.2100                      | 428.400 | 0.0028 | 0.4811                | 21.1645                 | 21.2936               |
| 9      | 509.12  | 8.4146                | 1.4142  | 141.4192  | 1.2100                      | 428.400 | 0.0028 | 0.4811                | 21.1650                 | 21.2942               |
| 10     | 509.12  | 0.0001                | 0.0000  | -0.0022   | 0.0000                      | 0.008   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
|        |   |                       |         |           | $\Delta =4.840(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0122 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | <p>桿件皆滿足容許應力限制。</p> <p>節點 1 位移為 2.0083in(<math>\downarrow</math>)，超過容許位移 2 in。</p> <p>總重量：5066.50 lb。</p> |                       |         |           |                             |         |        |                       |                         |                       |

表 5.1.10 例一，第 6 次搜尋結果 ( $\alpha = 1.568750$ )

| Step6  |   | $\alpha =$<br>1.568750 |         |           |                              |         |        | K=1840.64             |                         |                       |
|--------|---|------------------------|---------|-----------|------------------------------|---------|--------|-----------------------|-------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$            | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |
| 1      | 360   | 12.5500                | 1.9999  | 199.9985  | 1.1473                       | 451.800 | 0.0025 | 0.4817                | 29.8951                 | 30.0566               |
| 2      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1005                |
| 3      | 360   | 12.5500                | -1.0001 | -200.0016 | 0.5738                       | 451.800 | 0.0013 | 0.3141                | 22.9274                 | 23.0512               |
| 4      | 360   | 6.2750                 | -1.0000 | -99.9985  | 0.5737                       | 225.900 | 0.0025 | 0.2408                | 14.9476                 | 15.0283               |
| 5      | 360   | 0.0002                 | -0.0001 | 0.0000    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1005                |
| 6      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1005                |
| 7      | 509.12  | 8.8742                 | 0.0001  | 141.4236  | 0.0001                       | 451.800 | 0.0000 | 0.0001                | 8.8761                  | 8.9240                |
| 8      | 509.12  | 8.8742                 | -1.4141 | -141.4192 | 1.1473                       | 451.800 | 0.0025 | 0.4816                | 21.1385                 | 21.2527               |
| 9      | 509.12  | 8.8742                 | 1.4142  | 141.4192  | 1.1474                       | 451.800 | 0.0025 | 0.4817                | 21.1391                 | 21.2533               |
| 10     | 509.12  | 0.0002                 | 0.0000  | -0.0022   | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                  | 0.1005                |
|        |   |                        |         |           | $\Delta = 4.590(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0122 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5087.26 lb。 |                        |         |           |                              |         |        |                       |                         |                       |

表 5.1.11 例一，第 7 次搜尋結果 ( $\alpha = 1.528125$ )

| Step7  |   | $\alpha =$<br>1.528125 |         |           |                              |         |        | K=1862.54             |                         |                       |
|--------|---|------------------------|---------|-----------|------------------------------|---------|--------|-----------------------|-------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$            | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$   | $I_i$  | $\Delta_i'(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |
| 1      | 360   | 12.2250                | 1.9999  | 199.9985  | 1.1779                       | 440.100 | 0.0027 | 0.4814                | 29.9136                 | 30.0856               |
| 2      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 3      | 360   | 12.2250                | -1.0001 | -200.0016 | 0.5890                       | 440.100 | 0.0013 | 0.3151                | 22.8516                 | 22.9830               |
| 4      | 360   | 6.1125                 | -1.0000 | -99.9985  | 0.5889                       | 220.050 | 0.0027 | 0.2407                | 14.9569                 | 15.0429               |
| 5      | 360   | 0.0002                 | -0.0001 | 0.0000    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 6      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 7      | 509.12  | 8.6444                 | 0.0001  | 141.4236  | 0.0001                       | 440.100 | 0.0000 | 0.0001                | 8.6464                  | 8.6961                |
| 8      | 509.12  | 8.6444                 | -1.4141 | -141.4192 | 1.1778                       | 440.100 | 0.0027 | 0.4813                | 21.1516                 | 21.2733               |
| 9      | 509.12  | 8.6444                 | 1.4142  | 141.4192  | 1.1779                       | 440.100 | 0.0027 | 0.4814                | 21.1522                 | 21.2738               |
| 10     | 509.12  | 0.0002                 | 0.0000  | -0.0022   | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
|        |   |                        |         |           | $\Delta = 4.712(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0115 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>節點 1 位移為 2.0018in( $\downarrow$ )，超過容許位移 2 in。<br>總重量：5076.87 lb。 |                        |         |           |                              |         |        |                       |                         |                       |

表 5.1.12 例一，第 8 次搜尋結果 ( $\alpha = 1.548438$ )

| Step8  |   | $\alpha =$<br>1.548438 |         |           |                              |         |        | K=1852.16             |                         |                       |
|--------|---|------------------------|---------|-----------|------------------------------|---------|--------|-----------------------|-------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$            | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$   | $I_i$  | $\Delta_i'(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |
| 1      | 360   | 12.3875                | 1.9999  | 199.9985  | 1.1624                       | 445.950 | 0.0026 | 0.4815                | 29.9044                 | 30.0704               |
| 2      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 3      | 360   | 12.3875                | -1.0001 | -200.0016 | 0.5813                       | 445.950 | 0.0013 | 0.3146                | 22.8893                 | 23.0163               |
| 4      | 360   | 6.1938                 | -1.0000 | -99.9985  | 0.5812                       | 222.975 | 0.0026 | 0.2408                | 14.9523                 | 15.0352               |
| 5      | 360   | 0.0002                 | -0.0001 | 0.0000    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 6      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 7      | 509.12  | 8.7593                 | 0.0001  | 141.4236  | 0.0001                       | 445.950 | 0.0000 | 0.0001                | 8.7612                  | 8.8099                |
| 8      | 509.12  | 8.7593                 | -1.4141 | -141.4192 | 1.1623                       | 445.950 | 0.0026 | 0.4815                | 21.1451                 | 21.2625               |
| 9      | 509.12  | 8.7593                 | 1.4142  | 141.4192  | 1.1624                       | 445.950 | 0.0026 | 0.4815                | 21.1457                 | 21.2630               |
| 10     | 509.12  | 0.0002                 | 0.0000  | -0.0022   | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
|        |   |                        |         |           | $\Delta = 4.650(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0111 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5081.94 lb。 |                        |         |           |                              |         |        |                       |                         |                       |

表 5.1.13 例一，第 9 次搜尋結果 ( $\alpha = 1.538281$ )

| Step9  |   | $\alpha =$<br>1.538281 |         |           |                              |         |        | K=1857.87             |                         |                       |
|--------|---|------------------------|---------|-----------|------------------------------|---------|--------|-----------------------|-------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$            | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |
| 1      | 360   | 12.3063                | 1.9999  | 199.9985  | 1.1701                       | 443.025 | 0.0026 | 0.4814                | 29.9090                 | 30.0780               |
| 2      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 3      | 360   | 12.3063                | -1.0001 | -200.0016 | 0.5851                       | 443.025 | 0.0013 | 0.3148                | 22.8704                 | 22.9996               |
| 4      | 360   | 6.1531                 | -1.0000 | -99.9985  | 0.5850                       | 221.513 | 0.0026 | 0.2407                | 14.9546                 | 15.0391               |
| 5      | 360   | 0.0002                 | -0.0001 | 0.0000    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 6      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 7      | 509.12  | 8.7018                 | 0.0001  | 141.4236  | 0.0001                       | 443.025 | 0.0000 | 0.0001                | 8.7038                  | 8.7530                |
| 8      | 509.12  | 8.7018                 | -1.4141 | -141.4192 | 1.1700                       | 443.025 | 0.0026 | 0.4814                | 21.1484                 | 21.2679               |
| 9      | 509.12  | 8.7018                 | 1.4142  | 141.4192  | 1.1701                       | 443.025 | 0.0026 | 0.4814                | 21.1489                 | 21.2684               |
| 10     | 509.12  | 0.0002                 | 0.0000  | -0.0022   | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
|        |   |                        |         |           | $\Delta = 4.681(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0113 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>節點 1 位移為 2.0003in( $\downarrow$ )，超過容許位移 2 in。<br>總重量：5079.40 lb。 |                        |         |           |                              |         |        |                       |                         |                       |

表 5.1.14 例一，第 10 次搜尋結果 ( $\alpha = 1.543359$ )

| Step10 |   | $\alpha =$<br>1.543359 |         |           |                              |         |        | K=1855.02             |                         |                       |
|--------|---|------------------------|---------|-----------|------------------------------|---------|--------|-----------------------|-------------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$            | $u_i$   | $S_i$     | $\Delta_i$                   | $W_i$   | $I_i$  | $\Delta_i'(K)$        | $A_i^{(1)}$             | $A_i^{(2)}$           |
| 1      | 360   | 12.3469                | 1.9999  | 199.9985  | 1.1662                       | 444.488 | 0.0026 | 0.4815                | 29.9067                 | 30.0742               |
| 2      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 3      | 360   | 12.3469                | -1.0001 | -200.0016 | 0.5832                       | 444.488 | 0.0013 | 0.3147                | 22.8798                 | 23.0079               |
| 4      | 360   | 6.1734                 | -1.0000 | -99.9985  | 0.5831                       | 222.244 | 0.0026 | 0.2407                | 14.9534                 | 15.0372               |
| 5      | 360   | 0.0002                 | -0.0001 | 0.0000    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 6      | 360   | 0.0002                 | 0.0000  | 0.0016    | 0.0000                       | 0.006   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
| 7      | 509.12  | 8.7306                 | 0.0001  | 141.4236  | 0.0001                       | 444.488 | 0.0000 | 0.0001                | 8.7325                  | 8.7814                |
| 8      | 509.12  | 8.7306                 | -1.4141 | -141.4192 | 1.1662                       | 444.487 | 0.0026 | 0.4815                | 21.1468                 | 21.2652               |
| 9      | 509.12  | 8.7306                 | 1.4142  | 141.4192  | 1.1662                       | 444.487 | 0.0026 | 0.4815                | 21.1473                 | 21.2657               |
| 10     | 509.12  | 0.0002                 | 0.0000  | -0.0022   | 0.0000                       | 0.008   | 0.0000 | 0.0000                | 0.1000                  | 0.1006                |
|        |   |                        |         |           | $\Delta = 4.665(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.0112 ( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5080.67 lb。 |                        |         |           |                              |         |        |                       |                         |                       |

表 5.1.15 例一，第 11 次搜尋結果 ( $\alpha=1.540820$ )

| Step11 |   | $\alpha=$<br>1.540820 |         |           |                             |         |        | K=1856.44             |                       |                       |
|--------|---|-----------------------|---------|-----------|-----------------------------|---------|--------|-----------------------|-----------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$           | $u_i$   | $S_i$     | $\Delta_i$                  | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$           | $A_i^{(2)}$           |
| 1      | 360   | 12.3266               | 1.9999  | 199.9985  | 1.1681                      | 443.756 | 0.0026 | 0.4815                | 29.9079               | 30.0769               |
| 2      | 360   | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
| 3      | 360   | 12.3266               | -1.0001 | -200.0016 | 0.5842                      | 443.756 | 0.0013 | 0.3148                | 22.8751               | 23.0043               |
| 4      | 360   | 6.1633                | -1.0000 | -99.9985  | 0.5841                      | 221.878 | 0.0026 | 0.2407                | 14.9540               | 15.0385               |
| 5      | 360   | 0.0002                | -0.0001 | 0.0000    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
| 6      | 360   | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
| 7      | 509.12  | 8.7162                | 0.0001  | 141.4236  | 0.0001                      | 443.757 | 0.0000 | 0.0001                | 8.7182                | 8.7674                |
| 8      | 509.12  | 8.7162                | -1.4141 | -141.4192 | 1.1681                      | 443.756 | 0.0026 | 0.4814                | 21.1476               | 21.2670               |
| 9      | 509.12  | 8.7162                | 1.4142  | 141.4192  | 1.1682                      | 443.756 | 0.0026 | 0.4815                | 21.1481               | 21.2676               |
| 10     | 509.12  | 0.0002                | 0.0000  | -0.0022   | 0.0000                      | 0.008   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
|        |   |                       |         |           | $\Delta =4.673(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.013( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5080.16 lb。 |                       |         |           |                             |         |        |                       |                       |                       |

表 5.1.16 例一，第 12 次搜尋結果 ( $\alpha=1.539551$ )

| Step12 |  | $\alpha=$<br>1.539551 |         |           |                             |         |        |                       | K=1857.2              |                       |  |
|--------|--|-----------------------|---------|-----------|-----------------------------|---------|--------|-----------------------|-----------------------|-----------------------|--|
| No.    | $L_i$  | $A_i^{(0)}$           | $u_i$   | $S_i$     | $\Delta_i$                  | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$           | $A_i^{(2)}$           |  |
| 1      | 360  | 12.3164               | 1.9999  | 199.9985  | 1.1691                      | 443.391 | 0.0026 | 0.4814                | 29.9085               | 30.0774               |  |
| 2      | 360  | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |  |
| 3      | 360  | 12.3164               | -1.0001 | -200.0016 | 0.5846                      | 443.391 | 0.0013 | 0.3148                | 22.8727               | 23.0019               |  |
| 4      | 360  | 6.1582                | -1.0000 | -99.9985  | 0.5846                      | 221.695 | 0.0026 | 0.2407                | 14.9543               | 15.0388               |  |
| 5      | 360  | 0.0002                | -0.0001 | 0.0000    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |  |
| 6      | 360  | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |  |
| 7      | 509.12   | 8.7090                | 0.0001  | 141.4236  | 0.0001                      | 443.391 | 0.0000 | 0.0001                | 8.7110                | 8.7602                |  |
| 8      | 509.12   | 8.7090                | -1.4141 | -141.4192 | 1.1690                      | 443.390 | 0.0026 | 0.4814                | 21.1480               | 21.2675               |  |
| 9      | 509.12   | 8.7090                | 1.4142  | 141.4192  | 1.1691                      | 443.390 | 0.0026 | 0.4814                | 21.1485               | 21.2680               |  |
| 10     | 509.12   | 0.0002                | 0.0000  | -0.0022   | 0.0000                      | 0.008   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |  |
|        |  |                       |         |           | $\Delta =4.677(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.013( $\downarrow$ ) | 2.000( $\downarrow$ ) |  |
| Result | <p>桿件皆滿足容許應力限制。<br/>           節點 1 位移為 2.0001 in(<math>\downarrow</math>)，超過容許位移 2 in。<br/>           總重量：5079.78 lb。</p> |                       |         |           |                             |         |        |                       |                       |                       |  |



表 5.1.17 例一，第 13 次搜尋結果 ( $\alpha=1.540186$ )

| Step13 |   | $\alpha=$<br>1.540186 |         |           |                             |         |        | K=1856.8              |                       |                       |
|--------|---|-----------------------|---------|-----------|-----------------------------|---------|--------|-----------------------|-----------------------|-----------------------|
| No.    | $L_i$   | $A_i^{(0)}$           | $u_i$   | $S_i$     | $\Delta_i$                  | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$           | $A_i^{(2)}$           |
| 1      | 360   | 12.3215               | 1.9999  | 199.9985  | 1.1686                      | 443.573 | 0.0026 | 0.4814                | 29.9082               | 30.0772               |
| 2      | 360   | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
| 3      | 360   | 12.3215               | -1.0001 | -200.0016 | 0.5844                      | 443.573 | 0.0013 | 0.3148                | 22.8739               | 23.0031               |
| 4      | 360   | 6.1607                | -1.0000 | -99.9985  | 0.5843                      | 221.787 | 0.0026 | 0.2407                | 14.9541               | 15.0386               |
| 5      | 360   | 0.0002                | -0.0001 | 0.0000    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
| 6      | 360   | 0.0002                | 0.0000  | 0.0016    | 0.0000                      | 0.006   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
| 7      | 509.12  | 8.7126                | 0.0001  | 141.4236  | 0.0001                      | 443.574 | 0.0000 | 0.0001                | 8.7146                | 8.7638                |
| 8      | 509.12  | 8.7126                | -1.4141 | -141.4192 | 1.1686                      | 443.573 | 0.0026 | 0.4814                | 21.1478               | 21.2673               |
| 9      | 509.12  | 8.7126                | 1.4142  | 141.4192  | 1.1686                      | 443.573 | 0.0026 | 0.4815                | 21.1483               | 21.2678               |
| 10     | 509.12  | 0.0002                | 0.0000  | -0.0022   | 0.0000                      | 0.008   | 0.0000 | 0.0000                | 0.1000                | 0.1006                |
|        |   |                       |         |           | $\Delta =4.675(\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 2.013( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | 桿件皆滿足容許應力限制。<br>位移皆滿足容許位移限制。<br>總重量：5079.97 lb。 |                       |         |           |                             |         |        |                       |                       |                       |

表 5.1.18 例一，啟發式最佳化設計搜尋點與相對重量

| 搜尋過程 |          |             |     |
|------|----------|-------------|-----|
| No.  | $\alpha$ | Weight (lb) | T/F |
| 1    | 1.000000 | 4952.39     | F   |
| 2    | 2.300000 | 5289.98     | T   |
| 3    | 1.650000 | 5108.80     | T   |
| 4    | 1.325000 | 5025.89     | F   |
| 5    | 1.487500 | 5066.50     | F   |
| 6    | 1.568750 | 5087.26     | T   |
| 7    | 1.528125 | 5076.87     | F   |
| 8    | 1.548438 | 5081.94     | T   |
| 9    | 1.538281 | 5079.40     | F   |
| 10   | 1.543359 | 5080.67     | T   |
| 11   | 1.540820 | 5080.16     | T   |
| 12   | 1.539551 | 5079.78     | F   |
| 13   | 1.540186 | 5079.97     | T   |

T：可行設計

F：非可行設計

表 5.1.19 例一，最佳斷面經結構分析後節點位移

| Joint displacement(in) |               |               |
|------------------------|---------------|---------------|
| Joint No.              | X Translation | Y Translation |
| 1                      | 2.4172E-01    | -2.0000E+00   |
| 2                      | -5.4925E-01   | -2.0000E+00   |
| 3                      | 2.4179E-01    | -7.3018E-01   |
| 4                      | -3.0987E-01   | -1.4486E+00   |
| 5                      | 0.0000E+00    | 0.0000E+00    |
| 6                      | 0.0000E+00    | 0.0000E+00    |

表 5.1.20 例一，最佳斷面經結構分析後桿件應力

| Member Axial Stress(ksi) |              |
|--------------------------|--------------|
| Member No.               | Axial Stress |
| 1                        | -6.716       |
| 2                        | 0.002        |
| 3                        | 8.607        |
| 4                        | 6.650        |
| 5                        | -19.957      |
| 6                        | 0.002        |
| 7                        | -15.816      |
| 8                        | 6.783        |
| 9                        | -6.650       |
| 10                       | -0.003       |

表 5.1.21 例一，最佳化斷面比較表

| Area (in <sup>2</sup> ) | Schmit and Farshi [18] | Schmit and Miura[19] | Venkayya[15] | Gellatly and Berke [16] | Dobbs and Nelson [17] | Rizzi [20] | K.S and Geen [21] | This work |
|-------------------------|------------------------|----------------------|--------------|-------------------------|-----------------------|------------|-------------------|-----------|
|                         |                        | CON-MIN              |              |                         |                       |            |                   |           |
| A <sub>1</sub>          | 33.430                 | 30.570               | 30.420       | 31.350                  | 30.500                | 30.730     | 30.150            | 30.077    |
| A <sub>2</sub>          | 0.100                  | 0.369                | 0.128        | 0.100                   | 0.100                 | 0.100      | 0.102             | 0.101     |
| A <sub>3</sub>          | 24.260                 | 23.970               | 23.410       | 20.030                  | 23.290                | 23.930     | 22.710            | 23.003    |
| A <sub>4</sub>          | 14.260                 | 14.730               | 14.910       | 15.600                  | 15.430                | 14.730     | 15.270            | 15.039    |
| A <sub>5</sub>          | 0.100                  | 0.100                | 0.101        | 0.140                   | 0.100                 | 0.100      | 0.102             | 0.101     |
| A <sub>6</sub>          | 0.100                  | 0.364                | 0.101        | 0.240                   | 0.210                 | 0.100      | 0.544             | 0.101     |
| A <sub>7</sub>          | 8.388                  | 8.547                | 8.696        | 8.350                   | 7.649                 | 8.542      | 7.541             | 8.764     |
| A <sub>8</sub>          | 20.740                 | 21.110               | 21.080       | 22.210                  | 20.98                 | 20.950     | 21.560            | 21.267    |
| A <sub>9</sub>          | 19.690                 | 20.770               | 21.080       | 22.060                  | 21.82                 | 21.840     | 21.450            | 21.268    |
| A <sub>10</sub>         | 0.100                  | 0.320                | 0.186        | 0.100                   | 0.100                 | 0.100      | 0.100             | 0.101     |
| Weight (lb)             | 5089.00                | 5107.30              | 5084.90      | 5112.00                 | 5080.00               | 5076.66    | 5057.88           | 5080.05   |

表 5.2.1 例二，啟發式最佳化設計搜尋點與其相對重量

| 搜尋過程 |          |            |     |
|------|----------|------------|-----|
| No.  | $\alpha$ | Weight(lb) | T/F |
| 1    | 1.000000 | 4510.99    | F   |
| 2    | 2.300000 | 5138.41    | T   |
| 3    | 1.650000 | 4798.02    | T   |
| 4    | 1.325000 | 4646.46    | F   |
| 5    | 1.487500 | 4720.48    | T   |
| 6    | 1.406250 | 4682.84    | F   |
| 7    | 1.446875 | 4701.64    | F   |
| 8    | 1.467188 | 4710.94    | F   |
| 9    | 1.477344 | 4715.82    | T   |
| 10   | 1.472266 | 4713.26    | T   |
| 11   | 1.469727 | 4712.10    | T   |
| 12   | 1.468457 | 4711.63    | T   |
| 13   | 1.467822 | 4711.29    | F   |
| 14   | 1.468140 | 4711.46    | T   |

T：可行設計；

F：非可行設計

表 5.2.2 例二，最佳斷面經結構分析後節點位移

| Joint displacement(in) |               |               |
|------------------------|---------------|---------------|
| Joint No.              | X Translation | Y Translation |
| 1                      | 4.4097E-02    | -1.404E+00    |
| 2                      | -6.1402E-01   | -2.000E+00    |
| 3                      | 2.3243E-01    | -6.370E-01    |
| 4                      | -3.5570E-01   | -1.537E+00    |
| 5                      | 0.0000E+00    | 0.000E+00     |
| 6                      | 0.0000E+00    | 0.000E+00     |

表 5.2.3 例二，最佳斷面結構分析後桿件應力

| Member Axial Stress(ksi) |              |
|--------------------------|--------------|
| Member No.               | Axial Stress |
| 1                        | -6.456       |
| 2                        | 5.232        |
| 3                        | 9.881        |
| 4                        | 7.175        |
| 5                        | -24.988      |
| 6                        | -16.566      |
| 7                        | -16.401      |
| 8                        | 5.619        |
| 9                        | -7.175       |
| 10                       | -7.399       |

表 5.2.4 例二，最佳化斷面比較表。

| Area (in <sup>2</sup> ) | Schmit and Farshi [18] | Schmit and Miura[19] CON-MIN | Venkayya [15] | Dobbs and Nelson [17] | Khan and Willmert [22] | K.S and Geen [21] | This work |
|-------------------------|------------------------|------------------------------|---------------|-----------------------|------------------------|-------------------|-----------|
| A1                      | 24.290                 | 23.550                       | 25.190        | 25.810                | 24.720                 | 23.250            | 23.710    |
| A2                      | 0.100                  | 0.176                        | 0.363         | 0.100                 | 0.100                  | 0.102             | 0.102     |
| A3                      | 23.350                 | 25.200                       | 25.420        | 27.230                | 26.540                 | 25.730            | 24.990    |
| A4                      | 13.660                 | 14.390                       | 14.330        | 16.650                | 13.220                 | 14.510            | 14.011    |
| A5                      | 0.100                  | 0.100                        | 0.417         | 0.100                 | 0.108                  | 0.100             | 0.102     |
| A6                      | 1.969                  | 1.967                        | 3.144         | 2.024                 | 4.835                  | 1.977             | 2.986     |
| A7                      | 12.670                 | 12.400                       | 12.080        | 12.780                | 12.660                 | 12.210            | 12.668    |
| A8                      | 12.540                 | 12.860                       | 14.610        | 14.220                | 13.780                 | 12.610            | 13.359    |
| A9                      | 21.970                 | 20.410                       | 20.260        | 22.140                | 18.440                 | 20.360            | 19.815    |
| A10                     | 0.100                  | 0.100                        | 0.513         | 0.100                 | 0.100                  | 0.100             | 0.102     |
| Weight (lb)             | 4691.84                | 4684.11                      | 4895.60       | 5059.70               | 4792.52                | 4668.81           | 4711.52   |

表 5.3.1 例三，平面 17 根桁架，搜尋點與其相對重量

| 搜尋過程 |          |             |     |
|------|----------|-------------|-----|
| No.  | $\alpha$ | Weight (lb) | T/F |
| 1    | 1.000000 | 2582.09     | T   |
| 2    | 0.500000 | 2582.18     | T   |
| 3    | 0.250000 | 2582.09     | T   |
| 4    | 0.125000 | 2582.12     | T   |
| 5    | 0.062500 | 2582.08     | T   |
| 6    | 0.031250 | 2582.10     | T   |
| 7    | 0.015625 | 2582.06     | T   |
| 8    | 0.007813 | 2582.18     | T   |
| 9    | 0.003906 | 2582.16     | T   |
| 10   | 0.001953 | 2582.18     | T   |
| 11   | 0.000977 | 2582.14     | T   |

T：可行設計

F：非可行設計

表 5.3.2 例三，最佳斷面結構分析後節點位移

| Joint displacement(in) |               |               |
|------------------------|---------------|---------------|
| Joint No.              | X Translation | Y Translation |
| 1                      | 0.0000E+00    | 0.0000E+00    |
| 2                      | 0.0000E+00    | 0.0000E+00    |
| 3                      | -8.4132E-02   | -2.4567E-01   |
| 4                      | 8.3294E-02    | -2.4774E-01   |
| 5                      | -1.6733E-01   | -6.6291E-01   |
| 6                      | 1.6763E-01    | -6.5310E-01   |
| 7                      | -2.5211E-01   | -1.2008E+00   |
| 8                      | 2.5072E-01    | -1.2460E+00   |
| 9                      | -3.3575E-01   | -1.9998E+00   |

表 5.3.3 例三，最佳斷面結構分析後桿件應力

| Member Axial Stress |                    |
|---------------------|--------------------|
| Member No.          | Axial Stress (ksi) |
| 1                   | -24.988            |
| 2                   | -24.230            |
| 3                   | 25.240             |
| 4                   | 0.622              |
| 5                   | -25.301            |
| 6                   | -24.683            |
| 7                   | 24.958             |
| 8                   | -2.943             |
| 9                   | -24.927            |
| 10                  | -19.189            |
| 11                  | 25.435             |
| 12                  | 13.569             |
| 13                  | -25.097            |
| 14                  | 25.094             |
| 15                  | 24.667             |
| 16                  | 23.351             |
| 17                  | 24.756             |

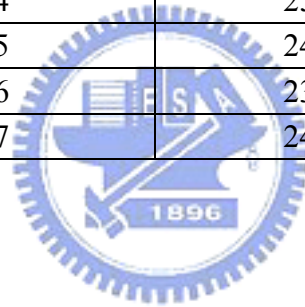


表 5.3.4 例三，最佳化斷面比較表

| Area(in <sup>2</sup> ) | Khot and Berke[25] | Adeli and Kumar[23] | K.S and Geen[21] | This work |
|------------------------|--------------------|---------------------|------------------|-----------|
| A <sub>1</sub>         | 15.930             | 16.029              | 15.821           | 15.937    |
| A <sub>2</sub>         | 0.100              | 0.107               | 0.108            | 0.100     |
| A <sub>3</sub>         | 12.070             | 12.183              | 11.996           | 11.953    |
| A <sub>4</sub>         | 0.100              | 0.110               | 0.100            | 0.100     |
| A <sub>5</sub>         | 8.067              | 8.417               | 8.150            | 7.969     |
| A <sub>6</sub>         | 5.562              | 5.715               | 5.507            | 5.635     |
| A <sub>7</sub>         | 11.933             | 11.331              | 11.829           | 11.953    |
| A <sub>8</sub>         | 0.100              | 0.105               | 0.100            | 0.100     |
| A <sub>9</sub>         | 7.945              | 7.301               | 7.934            | 7.969     |
| A <sub>10</sub>        | 0.100              | 0.115               | 0.100            | 0.100     |
| A <sub>11</sub>        | 4.055              | 4.406               | 4.093            | 3.984     |
| A <sub>12</sub>        | 0.100              | 0.101               | 0.100            | 0.100     |
| A <sub>13</sub>        | 5.657              | 5.611               | 5.660            | 5.635     |
| A <sub>14</sub>        | 4.000              | 4.406               | 4.061            | 3.984     |
| A <sub>15</sub>        | 5.558              | 5.152               | 5.656            | 5.635     |
| A <sub>16</sub>        | 0.100              | 0.107               | 0.100            | 0.100     |
| A <sub>17</sub>        | 5.579              | 5.286               | 5.582            | 5.635     |
| Weight (lb)            | 2581.89            | 2594.42             | 2580.81          | 2582.17   |



表 5.3.5 例三，第 1 次搜尋結果 ( $\alpha=1$ )

| Step1  |   | $\alpha=1$  |         |           |                               |         |        | K=963.95              |                       |                       |
|--------|---|-------------|---------|-----------|-------------------------------|---------|--------|-----------------------|-----------------------|-----------------------|
| No.    | $L_i$                                     | $A_i^{(0)}$ | $u_i$   | $S_i$     | $\Delta_i$                    | $W_i$   | $I_i$  | $\Delta'_i(K)$        | $A_i^{(1)}$           | $A_i^{(2)}$           |
| 1      | 100.00                                    | 8.0000      | 4.0000  | 399.9990  | 0.6667                        | 214.399 | 0.0031 | 0.3334                | 15.9947               | 15.9371               |
| 2      | 141.42                                    | 0.0001      | 0.0000  | 0.0013    | 0.0000                        | 0.004   | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 3      | 100.00                                    | 6.0000      | -3.0000 | -300.0010 | 0.5000                        | 160.801 | 0.0031 | 0.2501                | 11.9961               | 11.9529               |
| 4      | 100.00                                    | 0.0001      | 0.0000  | 0.0000    | 0.0000                        | 0.003   | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 5      | 100.00                                    | 4.0000      | 2.0000  | 200.0010  | 0.3333                        | 107.201 | 0.0031 | 0.1667                | 7.9974                | 7.9686                |
| 6      | 141.42                                    | 2.8284      | 1.4142  | 141.4200  | 0.3333                        | 107.199 | 0.0031 | 0.1667                | 5.6549                | 5.6346                |
| 7      | 100.00                                    | 6.0000      | -3.0000 | -299.9990 | 0.5000                        | 160.799 | 0.0031 | 0.2501                | 11.9960               | 11.9528               |
| 8      | 100.00                                    | 0.0001      | 0.0000  | 0.0000    | 0.0000                        | 0.003   | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 9      | 100.00                                    | 4.0000      | 2.0000  | 199.9990  | 0.3333                        | 107.199 | 0.0031 | 0.1667                | 7.9973                | 7.9685                |
| 10     | 141.42                                    | 0.0001      | 0.0000  | 0.0013    | 0.0000                        | 0.004   | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 11     | 100.00                                    | 2.0000      | -1.0000 | -100.0010 | 0.1667                        | 53.601  | 0.0031 | 0.0834                | 3.9987                | 3.9843                |
| 12     | 100.00                                    | 0.0001      | 0.0000  | -0.0009   | 0.0000                        | 0.003   | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 13     | 141.42                                    | 2.8284      | 1.4142  | 141.4210  | 0.3333                        | 107.200 | 0.0031 | 0.1667                | 5.6550                | 5.6346                |
| 14     | 100.00                                    | 2.0000      | -1.0000 | -100.0000 | 0.1667                        | 53.600  | 0.0031 | 0.0834                | 3.9987                | 3.9843                |
| 15     | 141.42                                    | 2.8284      | -1.4142 | -141.4200 | 0.3333                        | 107.199 | 0.0031 | 0.1667                | 5.6549                | 5.6346                |
| 16     | 141.42                                    | 0.0001      | 0.0000  | -0.0013   | 0.0000                        | 0.004   | 0.0000 | 0.0000                | 0.1000                | 0.1000                |
| 17     | 141.42                                    | 2.8284      | -1.4142 | -141.4200 | 0.3333                        | 107.199 | 0.0031 | 0.1667                | 5.6549                | 5.6346                |
|        |   |             |         |           | $\Delta = 4.000 (\downarrow)$ |         |        | 2.000( $\downarrow$ ) | 1.993( $\downarrow$ ) | 2.000( $\downarrow$ ) |
| Result | ● 桿件皆滿足容許應力限制。位移皆滿足容許位移限制。總重量：2582.09 lb。 |             |         |           |                               |         |        |                       |                       |                       |

表 5.4.1 例四，空間 72 根桿件桁架設計，斷面連結情形

| Group number | Members                          |
|--------------|----------------------------------|
| 1            | A <sub>1</sub> -A <sub>4</sub>   |
| 2            | A <sub>5</sub> -A <sub>12</sub>  |
| 3            | A <sub>13</sub> -A <sub>16</sub> |
| 4            | A <sub>17</sub> -A <sub>18</sub> |
| 5            | A <sub>19</sub> -A <sub>22</sub> |
| 6            | A <sub>23</sub> -A <sub>30</sub> |
| 7            | A <sub>31</sub> -A <sub>34</sub> |
| 8            | A <sub>35</sub> -A <sub>36</sub> |
| 9            | A <sub>37</sub> -A <sub>40</sub> |
| 10           | A <sub>41</sub> -A <sub>48</sub> |
| 11           | A <sub>49</sub> -A <sub>52</sub> |
| 12           | A <sub>53</sub> -A <sub>54</sub> |
| 13           | A <sub>55</sub> -A <sub>58</sub> |
| 14           | A <sub>59</sub> -A <sub>66</sub> |
| 15           | A <sub>67</sub> -A <sub>70</sub> |
| 16           | A <sub>71</sub> -A <sub>72</sub> |



表 5.4.2 例四，空間 72 根桿件桁架，設計條件與限制

限制條件

位移限制： $\Delta_j$ ，x與y方向，j=1...20

應力限制： $-25 \text{ ksi} \leq \sigma_{\text{allow}} \leq 25 \text{ ksi}$ ，i=1...72

最小桿件面積限制： $0.1 \text{ in}^2 \leq A_i$ ，i=1...72

受力情形

| No. | 節點 | x (kips) | y (kips) | z (kips) |
|-----|----|----------|----------|----------|
| 1   | 17 | 5        | 5        | -5       |

材料性質

彈性係數： $10^4 \text{ ksi}$

材料密度： $0.1 \text{ lb/in}^3$

表 5.4.3 例四，空間 72 根桿件桁架，桿件編號與節點編號之關係

| No. | B-Node | E-Node | No. | B-Node | E-Node |
|-----|--------|--------|-----|--------|--------|
| 1   | 1      | 5      | 37  | 9      | 13     |
| 2   | 2      | 6      | 38  | 10     | 14     |
| 3   | 3      | 7      | 39  | 11     | 15     |
| 4   | 4      | 8      | 40  | 12     | 16     |
| 5   | 2      | 5      | 41  | 10     | 13     |
| 6   | 1      | 6      | 42  | 9      | 14     |
| 7   | 2      | 7      | 43  | 10     | 15     |
| 8   | 3      | 6      | 44  | 11     | 14     |
| 9   | 3      | 8      | 45  | 11     | 16     |
| 10  | 4      | 7      | 46  | 12     | 15     |
| 11  | 1      | 8      | 47  | 9      | 16     |
| 12  | 4      | 5      | 48  | 12     | 13     |
| 13  | 5      | 6      | 49  | 13     | 14     |
| 14  | 6      | 7      | 50  | 14     | 15     |
| 15  | 7      | 8      | 51  | 15     | 16     |
| 16  | 5      | 8      | 52  | 13     | 16     |
| 17  | 5      | 7      | 53  | 13     | 15     |
| 18  | 6      | 8      | 54  | 14     | 16     |
| 19  | 5      | 9      | 55  | 13     | 17     |
| 20  | 6      | 10     | 56  | 14     | 18     |
| 21  | 7      | 11     | 57  | 15     | 19     |
| 22  | 8      | 12     | 58  | 16     | 20     |
| 23  | 6      | 9      | 59  | 14     | 17     |
| 24  | 5      | 10     | 60  | 13     | 18     |
| 25  | 6      | 11     | 61  | 14     | 19     |
| 26  | 7      | 10     | 62  | 15     | 18     |
| 27  | 7      | 12     | 63  | 15     | 20     |
| 28  | 8      | 11     | 64  | 16     | 19     |
| 29  | 5      | 12     | 65  | 13     | 20     |
| 30  | 8      | 9      | 66  | 16     | 17     |
| 31  | 9      | 10     | 67  | 17     | 18     |
| 32  | 10     | 11     | 68  | 18     | 19     |
| 33  | 11     | 12     | 69  | 19     | 20     |
| 34  | 9      | 12     | 70  | 17     | 20     |
| 35  | 9      | 11     | 71  | 17     | 19     |
| 36  | 10     | 12     | 72  | 18     | 20     |

表 5.4.4 例四， $\alpha=1$  時之啟發式斷面修正

| $\alpha=1$ |                                |                      |                 | K=              | $\Delta_{\text{real}}=$  |                       |                       |
|------------|--------------------------------|----------------------|-----------------|-----------------|--------------------------|-----------------------|-----------------------|
|            |                                |                      |                 | 1278.04         | 0.2494                   |                       |                       |
| No.        | $A_j^{(0)} = \alpha \cdot A_F$ | $\Delta_j$<br>(4-11) | $W_j$<br>(4-11) | $I_j$<br>(4-11) | $\Delta'_j(K)$<br>(4-12) | $A_j^{(1)}$<br>(4-13) | $A_j^{(2)}$<br>(4-14) |
| 1          | 0.2923                         | 0.3004               | 7.0162          | 0.0309          | 0.0341                   | 1.8604                | 1.8561                |
| 2          | 0.0709                         | 0.0000               | 7.6119          | 0.0395          | 0.0419                   | 0.5086                | 0.5074                |
| 3          | 0.0001                         | 0.0000               | 0.0048          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 4          | 0.0001                         | 0.1385               | 0.0034          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 5          | 0.2130                         | 0.3004               | 5.1125          | 0.0271          | 0.0232                   | 1.2714                | 1.2685                |
| 6          | 0.0709                         | 0.0001               | 7.6119          | 0.0395          | 0.0419                   | 0.5086                | 0.5075                |
| 7          | 0.0001                         | 0.0000               | 0.0048          | 0.0000          | 0.0001                   | 0.1000                | 0.1000                |
| 8          | 0.0001                         | 0.0394               | 0.0034          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 9          | 0.1177                         | 0.3005               | 2.8241          | 0.0140          | 0.0091                   | 0.5107                | 0.5095                |
| 10         | 0.0709                         | 0.0001               | 7.6119          | 0.0395          | 0.0419                   | 0.5087                | 0.5075                |
| 11         | 0.0001                         | 0.0075               | 0.0048          | 0.0000          | 0.0001                   | 0.1000                | 0.1000                |
| 12         | 0.0106                         | -0.0181              | 0.3584          | 0.0209          | 0.0014                   | 0.1000                | 0.1000                |
| 13         | 0.1291                         | 0.2741               | 3.0972          | 0.0000          | -0.0181                  | 0.1291                | 0.1288                |
| 14         | 0.0793                         | 0.1124               | 8.5146          | 0.0322          | 0.0422                   | 0.5150                | 0.5138                |
| 15         | 0.0687                         | 0.1118               | 3.2981          | 0.0341          | 0.0168                   | 0.4587                | 0.4576                |
| 16         | 0.0853                         | 0.3004               | 2.8962          | 0.0386          | 0.0158                   | 0.6053                | 0.6039                |

表 5.4.5 例四，黃金切割搜尋過程

| No. | I        | $X_L$    | $X_A$    | $X_B$    | $X_U$    |
|-----|----------|----------|----------|----------|----------|
| 1   | 1        | 0        | 0.381966 | 0.618034 | 1        |
| 2   | 0.618034 | 0.381966 | 0.618034 | 0.763932 | 1.000000 |
| 3   | 0.381966 | 0.618034 | 0.763932 | 0.854102 | 1.000000 |
| 4   | 0.236068 | 0.618034 | 0.708204 | 0.763932 | 0.854102 |
| 5   | 0.145898 | 0.708204 | 0.763932 | 0.798374 | 0.854102 |
| 6   | 0.090170 | 0.708204 | 0.742646 | 0.763932 | 0.798374 |
| 7   | 0.055728 | 0.742646 | 0.763932 | 0.777088 | 0.798374 |
| 8   | 0.034442 | 0.742646 | 0.755801 | 0.763932 | 0.777088 |
| 9   | 0.021286 | 0.755801 | 0.763932 | 0.768957 | 0.777088 |
| 10  | 0.013156 | 0.763932 | 0.768957 | 0.772063 | 0.777088 |
| 11  | 0.008131 | 0.768957 | 0.772063 | 0.773982 | 0.777088 |



表 5.4.6 例四，最佳斷面經結構分析後節點位移

| Joint displacement (in) |               |               |               |
|-------------------------|---------------|---------------|---------------|
| Joint No.               | X Translation | Y Translation | Z Translation |
| 1                       | 0.000E+00     | 0.000E+00     | 0.000E+00     |
| 2                       | 0.000E+00     | 0.000E+00     | 0.000E+00     |
| 3                       | 0.000E+00     | 0.000E+00     | 0.000E+00     |
| 4                       | 0.000E+00     | 0.000E+00     | 0.000E+00     |
| 5                       | 4.928E-02     | 4.928E-02     | 1.744E-02     |
| 6                       | 5.140E-02     | 4.036E-02     | -5.538E-03    |
| 7                       | 4.679E-02     | 4.679E-02     | -2.280E-02    |
| 8                       | 4.036E-02     | 5.140E-02     | -5.538E-03    |
| 9                       | 1.213E-01     | 1.213E-01     | 3.137E-02     |
| 10                      | 1.047E-01     | 8.869E-02     | -1.238E-02    |
| 11                      | 9.966E-02     | 9.966E-02     | -4.585E-02    |
| 12                      | 8.869E-02     | 1.047E-01     | -1.238E-02    |
| 13                      | 1.629E-01     | 1.629E-01     | 2.619E-02     |
| 14                      | 2.108E-01     | 1.468E-01     | -2.729E-02    |
| 15                      | 1.509E-01     | 1.509E-01     | -7.593E-02    |
| 16                      | 1.468E-01     | 2.108E-01     | -2.729E-02    |
| 17                      | 2.500E-01     | 2.500E-01     | -1.194E-01    |
| 18                      | 2.166E-01     | 2.047E-01     | -2.615E-02    |
| 19                      | 2.167E-01     | 2.167E-01     | -1.192E-01    |
| 20                      | 2.047E-01     | 2.166E-01     | -2.615E-02    |

表 5.4.7 例四，最佳斷面經結構分析後桿件應力

| No. | Stress(ksi) | No. | Stress(ksi) |
|-----|-------------|-----|-------------|
| 1   | 2.906       | 37  | -0.862      |
| 2   | -0.923      | 38  | -2.486      |
| 3   | -3.799      | 39  | -5.012      |
| 4   | -0.923      | 40  | -2.486      |
| 5   | -2.704      | 41  | -2.594      |
| 6   | 3.242       | 42  | 4.012       |
| 7   | 2.359       | 43  | 2.027       |
| 8   | -2.875      | 44  | -2.525      |
| 9   | -2.875      | 45  | -2.525      |
| 10  | 2.359       | 46  | 2.027       |
| 11  | 3.242       | 47  | 4.012       |
| 12  | -2.704      | 48  | -2.594      |
| 13  | 0.176       | 49  | 3.993       |
| 14  | 0.536       | 50  | 0.338       |
| 15  | 0.536       | 51  | 0.338       |
| 16  | 0.176       | 52  | 3.993       |
| 17  | -0.208      | 53  | -0.998      |
| 18  | 0.920       | 54  | 5.328       |
| 19  | 2.322       | 55  | -24.262     |
| 20  | -1.140      | 56  | 0.191       |
| 21  | -3.843      | 57  | -7.209      |
| 22  | -1.140      | 58  | 0.191       |
| 23  | -3.427      | 59  | -5.687      |
| 24  | 2.698       | 60  | 1.842       |
| 25  | 2.610       | 61  | 1.593       |
| 26  | -2.446      | 62  | -1.926      |
| 27  | -2.446      | 63  | -1.926      |
| 28  | 2.610       | 64  | 1.593       |
| 29  | 2.698       | 65  | 1.842       |
| 30  | -3.427      | 66  | -5.687      |
| 31  | -1.383      | 67  | -2.781      |
| 32  | 0.914       | 68  | 1.000       |
| 33  | 0.914       | 69  | 1.000       |
| 34  | -1.383      | 70  | -2.781      |
| 35  | -1.798      | 71  | -2.780      |

表 5.5.1 例五，空間 72 根桿件桁架，受力情形

| Loading data |              |          |          |          |
|--------------|--------------|----------|----------|----------|
| case number  | Joint number | x (kips) | y (kips) | z (kips) |
| 1            | 17           | 5        | 5        | -5       |
| 2            | 17           | 0        | 0        | -5       |
|              | 18           | 0        | 0        | -5       |
|              | 19           | 0        | 0        | -5       |
|              | 20           | 0        | 0        | -5       |

表 5.5.2 例五，FSD 設計斷面經結構分析後節點位移(載重一)

| Joint displacement (in) |               |               |               |
|-------------------------|---------------|---------------|---------------|
| Joint No.               | X Translation | Y Translation | Z Translation |
| 1                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 2                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 3                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 4                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 5                       | 3.3921E-01    | 3.3921E-01    | 9.7628E-02    |
| 6                       | 3.8755E-01    | 2.5708E-01    | -2.6498E-02   |
| 7                       | 3.1094E-01    | 3.1094E-01    | -1.5000E-01   |
| 8                       | 2.5708E-01    | 3.8755E-01    | -2.6498E-02   |
| 9                       | 8.5678E-01    | 8.5678E-01    | 1.6281E-01    |
| 10                      | 7.0362E-01    | 5.9669E-01    | -5.0513E-02   |
| 11                      | 6.6386E-01    | 6.6386E-01    | -2.9996E-01   |
| 12                      | 5.9669E-01    | 7.0362E-01    | -5.0513E-02   |
| 13                      | 1.0877E+00    | 1.0877E+00    | 1.3730E-01    |
| 14                      | 1.3480E+00    | 1.0490E+00    | -6.9459E-02   |
| 15                      | 1.0035E+00    | 1.0035E+00    | -3.9267E-01   |
| 16                      | 1.0490E+00    | 1.3480E+00    | -6.9459E-02   |
| 17                      | 1.7765E+00    | 1.7765E+00    | 3.6284E-02    |
| 18                      | 1.4769E+00    | 1.3879E+00    | -7.3394E-02   |
| 19                      | 1.4767E+00    | 1.4767E+00    | -4.2591E-01   |
| 20                      | 1.3879E+00    | 1.4769E+00    | -7.3394E-02   |



表 5.5.3 例五，FSD 設計斷面經結構分析後節點位移(載重二)

| Joint displacement (in) |               |               |               |
|-------------------------|---------------|---------------|---------------|
| Joint No.               | X Translation | Y Translation | Z Translation |
| 1                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 2                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 3                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 4                       | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 5                       | -5.3322E-02   | -5.3322E-02   | -1.0132E-01   |
| 6                       | 5.3322E-02    | -5.3322E-02   | -1.0132E-01   |
| 7                       | 5.3322E-02    | 5.3322E-02    | -1.0132E-01   |
| 8                       | -5.3322E-02   | 5.3322E-02    | -1.0132E-01   |
| 9                       | -1.2862E-02   | -1.2862E-02   | -2.3972E-01   |
| 10                      | 1.2862E-02    | -1.2862E-02   | -2.3972E-01   |
| 11                      | 1.2862E-02    | 1.2862E-02    | -2.3972E-01   |
| 12                      | -1.2862E-02   | 1.2862E-02    | -2.3972E-01   |
| 13                      | -6.5068E-02   | -6.5068E-02   | -3.8972E-01   |
| 14                      | 6.5068E-02    | -6.5068E-02   | -3.8972E-01   |
| 15                      | 6.5068E-02    | 6.5068E-02    | -3.8972E-01   |
| 16                      | -6.5068E-02   | 6.5068E-02    | -3.8972E-01   |
| 17                      | -1.6372E-03   | -1.6372E-03   | -5.3969E-01   |
| 18                      | 1.6372E-03    | -1.6372E-03   | -5.3969E-01   |
| 19                      | 1.6372E-03    | 1.6372E-03    | -5.3969E-01   |
| 20                      | -1.6372E-03   | 1.6372E-03    | -5.3969E-01   |

表 5.5.4 例五，第一次啟發式斷面修正( $\alpha=1$ )

| $\alpha=1$ |                                |                      |                 | K=              | $\Delta_{\text{real}}=$  |                       |                       |
|------------|--------------------------------|----------------------|-----------------|-----------------|--------------------------|-----------------------|-----------------------|
|            |                                |                      |                 | 1341.21         | 0.2475                   |                       |                       |
| No.        | $A_j^{(0)} = \alpha \cdot A_F$ | $\Delta_j$<br>(4-11) | $W_j$<br>(4-11) | $I_j$<br>(4-15) | $\Delta'_j(K)$<br>(4-12) | $A_j^{(1)}$<br>(4-13) | $A_j^{(2)}$<br>(4-14) |
| 1          | 0.2968                         | 0.2142               | 7.1220          | 0.0301          | 0.0333                   | 1.9080                | 1.8889                |
| 2          | 0.0716                         | 0.2977               | 7.6860          | 0.0387          | 0.0409                   | 0.5210                | 0.5158                |
| 3          | 0.0001                         | 0.0000               | 0.0048          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 4          | 0.0001                         | 0.0000               | 0.0034          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 5          | 0.2162                         | 0.1353               | 5.1890          | 0.0261          | 0.0226                   | 1.2969                | 1.2839                |
| 6          | 0.0716                         | 0.2977               | 7.6860          | 0.0387          | 0.0409                   | 0.5211                | 0.5158                |
| 7          | 0.0001                         | 0.0000               | 0.0048          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 8          | 0.0001                         | 0.0000               | 0.0034          | 0.0000          | 0.0000                   | 0.1000                | 0.1000                |
| 9          | 0.2005                         | 0.0236               | 4.8120          | 0.0049          | 0.0086                   | 0.5519                | 0.5463                |
| 10         | 0.0716                         | 0.2978               | 7.6860          | 0.0387          | 0.0409                   | 0.5211                | 0.5159                |
| 11         | 0.0001                         | 0.0001               | 0.0048          | 0.0000          | 0.0001                   | 0.1000                | 0.1000                |
| 12         | 0.0030                         | 0.0024               | 0.1015          | 0.0241          | 0.0004                   | 0.1000                | 0.1000                |
| 13         | 0.1986                         | -0.0112              | 4.7659          | 0.0000          | -0.0112                  | 0.1986                | 0.1966                |
| 14         | 0.0740                         | 0.2899               | 7.9393          | 0.0365          | 0.0410                   | 0.5229                | 0.5177                |
| 15         | 0.0693                         | 0.1134               | 3.3259          | 0.0341          | 0.0166                   | 0.4737                | 0.4689                |
| 16         | 0.0913                         | 0.1156               | 3.0985          | 0.0373          | 0.0162                   | 0.6521                | 0.6456                |

表 5.5.5 例五，啟發式最佳化設計搜尋點與其相對重量

| 搜尋過程 |          |         |     |
|------|----------|---------|-----|
| No.  | $\alpha$ | W (lb)  | T/F |
| 1    | 1.000000 | 384.647 | T   |
| 2    | 0.500000 | 370.368 | F   |
| 3    | 0.750000 | 379.062 | F   |
| 4    | 0.875000 | 382.123 | T   |
| 5    | 0.812500 | 380.671 | T   |
| 6    | 0.781250 | 379.887 | F   |
| 7    | 0.796875 | 380.278 | F   |
| 8    | 0.804688 | 380.469 | T   |
| 9    | 0.800781 | 380.374 | T   |
| 10   | 0.798828 | 380.333 | T   |
| 11   | 0.797852 | 380.306 | F   |
| 12   | 0.798340 | 380.320 | F   |
| 13   | 0.798584 | 380.326 | T   |

T：可行設計

F：非可行設計

表 5.5.6 例五，最佳斷面經結構分析後節點位移

| Joint No. | Load 1        |               |               | Load 2        |               |               |
|-----------|---------------|---------------|---------------|---------------|---------------|---------------|
|           | X Translation | Y Translation | Z Translation | X Translation | Y Translation | Z Translation |
| 1         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 2         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 3         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 4         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 5         | 4.8481E-02    | 4.8481E-02    | 1.6659E-02    | -6.4959E-03   | -6.4959E-03   | -1.5884E-02   |
| 6         | 4.9582E-02    | 3.9472E-02    | -4.9685E-03   | 6.4959E-03    | -6.4959E-03   | -1.5884E-02   |
| 7         | 4.5921E-02    | 4.5921E-02    | -2.2704E-02   | 6.4959E-03    | 6.4959E-03    | -1.5884E-02   |
| 8         | 3.9472E-02    | 4.9582E-02    | -4.9685E-03   | -6.4959E-03   | 6.4959E-03    | -1.5884E-02   |
| 9         | 1.1621E-01    | 1.1621E-01    | 2.9593E-02    | -3.6625E-04   | -3.6625E-04   | -3.8824E-02   |
| 10        | 1.0271E-01    | 8.7549E-02    | -1.1116E-02   | 3.6625E-04    | -3.6625E-04   | -3.8824E-02   |
| 11        | 9.8232E-02    | 9.8232E-02    | -4.5997E-02   | 3.6625E-04    | 3.6625E-04    | -3.8824E-02   |
| 12        | 8.7549E-02    | 1.0271E-01    | -1.1116E-02   | -3.6625E-04   | 3.6625E-04    | -3.8824E-02   |
| 13        | 1.5988E-01    | 1.5988E-01    | 2.4036E-02    | -3.2884E-02   | -3.2884E-02   | -9.6792E-02   |
| 14        | 1.9921E-01    | 1.4722E-01    | -2.3396E-02   | 3.2884E-02    | -3.2884E-02   | -9.6792E-02   |
| 15        | 1.4976E-01    | 1.4976E-01    | -7.5557E-02   | 3.2884E-02    | 3.2884E-02    | -9.6792E-02   |
| 16        | 1.4722E-01    | 1.9921E-01    | -2.3396E-02   | -3.2884E-02   | 3.2884E-02    | -9.6792E-02   |
| 17        | 2.4992E-01    | 2.4992E-01    | -7.6244E-02   | -6.9699E-03   | -6.9699E-03   | -2.4619E-01   |
| 18        | 2.1493E-01    | 2.0392E-01    | -2.4595E-02   | 6.9699E-03    | -6.9699E-03   | -2.4619E-01   |
| 19        | 2.1584E-01    | 2.1584E-01    | -1.0682E-01   | 6.9699E-03    | 6.9699E-03    | -2.4619E-01   |
| 20        | 2.0392E-01    | 2.1493E-01    | -2.4595E-02   | -6.9699E-03   | 6.9699E-03    | -2.4619E-01   |

表 5.5.7 例五，最佳斷面經結構分析後桿件應力

| No. | Load 1  | Load 2  | No. | Load 1   | Load 2   |
|-----|---------|---------|-----|----------|----------|
| 1   | 2.7764  | -2.6474 | 37  | -0.9262  | -9.6615  |
| 2   | -0.8281 | -2.6474 | 38  | -2.0468  | -9.6615  |
| 3   | -3.7840 | -2.6474 | 39  | -4.9266  | -9.6615  |
| 4   | -0.8281 | -2.6474 | 40  | -2.0468  | -9.6615  |
| 5   | -2.6768 | -0.0964 | 41  | -2.6391  | 0.2844   |
| 6   | 3.1399  | -0.0964 | 42  | 3.7670   | 0.2844   |
| 7   | 2.3046  | -0.0964 | 43  | 1.9995   | 0.2844   |
| 8   | -2.7971 | -0.0964 | 44  | -2.5127  | 0.2844   |
| 9   | -2.7971 | -0.0964 | 45  | -2.5127  | 0.2844   |
| 10  | 2.3046  | -0.0964 | 46  | 1.9995   | 0.2844   |
| 11  | 3.1399  | -0.0964 | 47  | 3.7670   | 0.2844   |
| 12  | -2.6768 | -0.0964 | 48  | -2.6391  | 0.2844   |
| 13  | 0.0918  | 1.0827  | 49  | 3.2782   | 5.4807   |
| 14  | 0.5374  | 1.0827  | 50  | 0.2117   | 5.4807   |
| 15  | 0.5374  | 1.0827  | 51  | 0.2117   | 5.4807   |
| 16  | 0.0918  | 1.0827  | 52  | 3.2782   | 5.4807   |
| 17  | -0.2134 | 1.0827  | 53  | -0.8428  | 5.4807   |
| 18  | 0.8425  | 1.0827  | 54  | 4.3326   | 5.4807   |
| 19  | 2.1558  | -3.8232 | 55  | -16.7134 | -24.8996 |
| 20  | -1.0245 | -3.8232 | 56  | -0.1998  | -24.8996 |
| 21  | -3.8822 | -3.8232 | 57  | -5.2098  | -24.8996 |
| 22  | -1.0245 | -3.8232 | 58  | -0.1998  | -24.8996 |
| 23  | -3.2900 | -0.3072 | 59  | -5.1418  | -2.3230  |
| 24  | 2.6897  | -0.3072 | 60  | 2.0494   | -2.3230  |
| 25  | 2.5497  | -0.3072 | 61  | 1.7940   | -2.3230  |
| 26  | -2.3890 | -0.3072 | 62  | -1.9118  | -2.3230  |
| 27  | -2.3890 | -0.3072 | 63  | -1.9118  | -2.3230  |
| 28  | 2.5497  | -0.3072 | 64  | 1.7940   | -2.3230  |
| 29  | 2.6897  | -0.3072 | 65  | 2.0494   | -2.3230  |
| 30  | -3.2900 | -0.3072 | 66  | -5.1418  | -2.3230  |
| 31  | -1.1250 | 0.0610  | 67  | -2.9154  | 1.1617   |
| 32  | 0.8902  | 0.0610  | 68  | 0.9934   | 1.1617   |
| 33  | 0.8902  | 0.0610  | 69  | 0.9934   | 1.1617   |
| 34  | -1.1250 | 0.0610  | 70  | -2.9154  | 1.1617   |
| 35  | -1.4985 | 0.0610  | 71  | -2.8396  | 1.1617   |
| 36  | 1.2636  | 0.0610  | 72  | 0.9177   | 1.1617   |

※Note: Stresses are in kips

表 5.5.8 例五，最佳化斷面比較表

| No          | Optimal cross-sectional areas (in <sup>2</sup> ) |                      |        |                |                         |                       |             |                      |                     |                    |        |                   |           |       |
|-------------|--|----------------------|--------|----------------|-------------------------|-----------------------|-------------|----------------------|---------------------|--------------------|--------|-------------------|-----------|-------|
|             | Schmit and Farshi[18]                            | Schmit and Miura[19] |        | Ven-Kayya [15] | Gellatly and Berke [16] | Khan and Willmert[22] |             | Adeli and Kamal [24] | Berke and Khot [23] | Erbatur et al.[27] |        | K.S and Geen [21] | This work |       |
|             |  | NEWSUMT              | CONMIN |                |                         | $\eta=0.1$            | $\eta=0.15$ |                      |                     | GAOS1              | GAOS2  |                   |           |       |
| 1           | A <sub>1</sub> ~A <sub>4</sub>                   | 2.078                | 1.885  | 1.885          | 1.818                   | 1.464                 | 1.793       | 1.859                | 2.206               | 1.893              | 1.755  | 1.910             | 1.790     | 1.872 |
| 2           | A <sub>5</sub> ~A <sub>12</sub>                  | 0.503                | 0.513  | 0.512          | 0.524                   | 0.521                 | 0.522       | 0.526                | 0.533               | 0.517              | 0.505  | 0.525             | 0.521     | 0.512 |
| 3           | A <sub>13</sub> ~A <sub>16</sub>                 | 0.100                | 0.100  | 0.100          | 0.100                   | 0.100                 | 0.100       | 0.100                | 0.100               | 0.100              | 0.105  | 0.122             | 0.100     | 0.100 |
| 4           | A <sub>17</sub> ~A <sub>18</sub>                 | 0.100                | 0.100  | 0.100          | 0.100                   | 0.100                 | 0.100       | 0.100                | 0.100               | 0.100              | 0.155  | 0.103             | 0.100     | 0.100 |
| 5           | A <sub>19</sub> ~A <sub>22</sub>                 | 1.107                | 1.267  | 1.268          | 1.246                   | 1.024                 | 1.208       | 1.253                | 1.157               | 1.279              | 1.155  | 1.310             | 1.229     | 1.271 |
| 6           | A <sub>23</sub> ~A <sub>30</sub>                 | 0.579                | 0.512  | 0.511          | 0.524                   | 0.542                 | 0.521       | 0.524                | 0.569               | 0.515              | 0.585  | 0.498             | 0.522     | 0.512 |
| 7           | A <sub>31</sub> ~A <sub>34</sub>                 | 0.100                | 0.100  | 0.100          | 0.100                   | 0.100                 | 0.100       | 0.100                | 0.100               | 0.100              | 0.100  | 0.110             | 0.100     | 0.100 |
| 8           | A <sub>35</sub> ~A <sub>36</sub>                 | 0.100                | 0.100  | 0.100          | 0.100                   | 0.100                 | 0.100       | 0.100                | 0.100               | 0.100              | 0.100  | 0.103             | 0.100     | 0.100 |
| 9           | A <sub>37</sub> ~A <sub>40</sub>                 | 0.264                | 0.523  | 0.523          | 0.611                   | 0.552                 | 0.623       | 0.581                | 0.514               | 0.508              | 0.460  | 0.535             | 0.517     | 0.531 |
| 10          | A <sub>41</sub> ~A <sub>48</sub>                 | 0.548                | 0.517  | 0.516          | 0.532                   | 0.608                 | 0.523       | 0.527                | 0.479               | 0.520              | 0.530  | 0.535             | 0.504     | 0.512 |
| 11          | A <sub>49</sub> ~A <sub>52</sub>                 | 0.100                | 0.100  | 0.100          | 0.100                   | 0.100                 | 0.100       | 0.100                | 0.100               | 0.100              | 0.120  | 0.103             | 0.100     | 0.100 |
| 12          | A <sub>53</sub> ~A <sub>54</sub>                 | 0.151                | 0.100  | 0.113          | 0.100                   | 0.100                 | 0.196       | 0.158                | 0.100               | 0.100              | 0.165  | 0.111             | 0.101     | 0.100 |
| 13          | A <sub>55</sub> ~A <sub>58</sub>                 | 0.158                | 0.157  | 0.156          | 0.161                   | 0.149                 | 0.149       | 0.152                | 0.158               | 0.157              | 0.155  | 0.161             | 0.156     | 0.158 |
| 14          | A <sub>59</sub> ~A <sub>66</sub>                 | 0.594                | 0.546  | 0.548          | 0.557                   | 0.773                 | 0.570       | 0.561                | 0.550               | 0.539              | 0.535  | 0.544             | 0.547     | 0.513 |
| 15          | A <sub>67</sub> ~A <sub>70</sub>                 | 0.341                | 0.411  | 0.411          | 0.377                   | 0.453                 | 0.443       | 0.438                | 0.345               | 0.416              | 0.480  | 0.379             | 0.442     | 0.465 |
| 16          | A <sub>71</sub> ~A <sub>72</sub>                 | 0.608                | 0.570  | 0.561          | 0.506                   | 0.342                 | 0.519       | 0.532                | 0.498               | 0.551              | 0.520  | 0.521             | 0.590     | 0.640 |
| Weight (lb) |  | 388.63               | 379.64 | 379.79         | 381.2                   | 395.97                | 381.72      | 387.67               | 379.31              | 379.67             | 385.76 | 383.12            | 379.27    | 380.5 |

表 5.6.1 例六，啟發式最佳化設計搜尋點與其相對重量

| 搜尋過程 |          |         |     |
|------|----------|---------|-----|
| No.  | $\alpha$ | W (lb)  | T/F |
| 1    | 1.000000 | 366.890 | T   |
| 2    | 0.500000 | 351.887 | F   |
| 3    | 0.750000 | 361.201 | F   |
| 4    | 0.875000 | 364.318 | F   |
| 5    | 0.937500 | 365.656 | T   |
| 6    | 0.906250 | 365.005 | T   |
| 7    | 0.890625 | 364.673 | F   |
| 8    | 0.898438 | 364.833 | T   |
| 9    | 0.894531 | 364.754 | F   |
| 10   | 0.896484 | 364.801 | F   |
| 11   | 0.897461 | 364.810 | F   |

T：可行設計

F：非可行設計



表 5.6.2 例六，最佳斷面經結構分析後節點位移

| Joint No. | Load 1        |               |               | Load 2        |               |               |
|-----------|---------------|---------------|---------------|---------------|---------------|---------------|
|           | X Translation | Y Translation | Z Translation | X Translation | Y Translation | Z Translation |
| 1         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 2         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 3         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 4         | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    | 0.0000E+00    |
| 5         | 4.6463E-02    | 4.6463E-02    | 1.6333E-02    | -1.6107E-02   | -1.6107E-02   | -1.6539E-02   |
| 6         | 5.8811E-02    | 3.3185E-02    | -5.6763E-03   | 1.6107E-02    | -1.6107E-02   | -1.6539E-02   |
| 7         | 4.1956E-02    | 4.1956E-02    | -2.1987E-02   | 1.6107E-02    | 1.6107E-02    | -1.6539E-02   |
| 8         | 3.3185E-02    | 5.8811E-02    | -5.6763E-03   | -1.6107E-02   | 1.6107E-02    | -1.6539E-02   |
| 9         | 1.3313E-01    | 1.3313E-01    | 2.9374E-02    | 1.4491E-02    | 1.4491E-02    | -3.8401E-02   |
| 10        | 9.8202E-02    | 7.8540E-02    | -1.1045E-02   | -1.4491E-02   | 1.4491E-02    | -3.8401E-02   |
| 11        | 8.8346E-02    | 8.8346E-02    | -4.5399E-02   | -1.4491E-02   | -1.4491E-02   | -3.8401E-02   |
| 12        | 7.8540E-02    | 9.8202E-02    | -1.1045E-02   | 1.4491E-02    | -1.4491E-02   | -3.8401E-02   |
| 13        | 1.5167E-01    | 1.5167E-01    | 2.0928E-02    | -5.4476E-02   | -5.4476E-02   | -9.7081E-02   |
| 14        | 2.1710E-01    | 1.3506E-01    | -2.1400E-02   | 5.4476E-02    | -5.4476E-02   | -9.7081E-02   |
| 15        | 1.4201E-01    | 1.4201E-01    | -7.7043E-02   | 5.4476E-02    | 5.4476E-02    | -9.7081E-02   |
| 16        | 1.3506E-01    | 2.1710E-01    | -2.1400E-02   | -5.4476E-02   | 5.4476E-02    | -9.7081E-02   |
| 17        | 2.4995E-01    | 2.4995E-01    | -8.1201E-02   | -3.4134E-03   | -3.4134E-03   | -2.4691E-01   |
| 18        | 2.1022E-01    | 1.9859E-01    | -2.4357E-02   | 3.4134E-03    | -3.4134E-03   | -2.4691E-01   |
| 19        | 2.1120E-01    | 2.1120E-01    | -1.1017E-01   | 3.4134E-03    | 3.4134E-03    | -2.4691E-01   |
| 20        | 1.9859E-01    | 2.1022E-01    | -2.4357E-02   | -3.4134E-03   | 3.4134E-03    | -2.4691E-01   |

※Note: Displacements are in inch



表 5.6.3 例六，最佳斷面經結構分析後桿件應力

| No. | Load 1  | Load 2  | No. | Load 1   | Load 2   |
|-----|---------|---------|-----|----------|----------|
| 1   | 2.7222  | -2.7566 | 37  | -1.4076  | -9.7799  |
| 2   | -0.9460 | -2.7566 | 38  | -1.7260  | -9.7799  |
| 3   | -3.6646 | -2.7566 | 39  | -5.2740  | -9.7799  |
| 4   | -0.9460 | -2.7566 | 40  | -1.7260  | -9.7799  |
| 5   | -2.5531 | 0.5225  | 41  | -2.4990  | 0.7097   |
| 6   | 3.7316  | 0.5225  | 42  | 3.9055   | 0.7097   |
| 7   | 2.0642  | 0.5225  | 43  | 2.0317   | 0.7097   |
| 8   | -2.4015 | 0.5225  | 44  | -2.3142  | 0.7097   |
| 9   | -2.4015 | 0.5225  | 45  | -2.3142  | 0.7097   |
| 10  | 2.0642  | 0.5225  | 46  | 2.0317   | 0.7097   |
| 11  | 3.7316  | 0.5225  | 47  | 3.9055   | 0.7097   |
| 12  | -2.5531 | 0.5225  | 48  | -2.4990  | 0.7097   |
| 13  | 1.0291  | 2.6845  | 49  | 5.4520   | 9.0793   |
| 14  | 0.7309  | 2.6845  | 50  | 0.5797   | 9.0793   |
| 15  | 0.7309  | 2.6845  | 51  | 0.5797   | 9.0793   |
| 16  | 1.0291  | 2.6845  | 52  | 5.4520   | 9.0793   |
| 17  | -0.3756 | 2.6845  | 53  | -0.8049  | 9.0793   |
| 18  | 2.1356  | 2.6845  | 54  | 6.8366   | 9.0793   |
| 19  | 2.1735  | -3.6436 | 55  | -17.0216 | -24.9721 |
| 20  | -0.8947 | -3.6436 | 56  | -0.4927  | -24.9721 |
| 21  | -3.9020 | -3.6436 | 57  | -5.5215  | -24.9721 |
| 22  | -0.8947 | -3.6436 | 58  | -0.4927  | -24.9721 |
| 23  | -3.7861 | -0.6210 | 59  | -4.1833  | -1.1352  |
| 24  | 2.5367  | -0.6210 | 60  | 2.3934   | -1.1352  |
| 25  | 2.3533  | -0.6210 | 61  | 2.1169   | -1.1352  |
| 26  | -2.0742 | -0.6210 | 62  | -2.0156  | -1.1352  |
| 27  | -2.0742 | -0.6210 | 63  | -2.0156  | -1.1352  |
| 28  | 2.3533  | -0.6210 | 64  | 2.1169   | -1.1352  |
| 29  | 2.5367  | -0.6210 | 65  | 2.3934   | -1.1352  |
| 30  | -3.7861 | -0.6210 | 66  | -4.1833  | -1.1352  |
| 31  | -2.9106 | -2.4152 | 67  | -3.3108  | 0.5689   |
| 32  | 0.8172  | -2.4152 | 68  | 1.0505   | 0.5689   |
| 33  | 0.8172  | -2.4152 | 69  | 1.0505   | 0.5689   |
| 34  | -2.9106 | -2.4152 | 70  | -3.3108  | 0.5689   |
| 35  | -3.7319 | -2.4152 | 71  | -3.2291  | 0.5689   |
| 36  | 1.6385  | -2.4152 | 72  | 0.9687   | 0.5689   |

※Note: Stresses are in ksi

表 5.6.4 例六，最佳化斷面比較表。

| No.         |                                  | Optimal cross-sectional (in <sup>2</sup> ) |          |                    |                  | This work |
|-------------|----------------------------------|--|----------|--------------------|------------------|-----------|
|             |                                  | Sarma and Adeli[12]                        |          | Adeli and Park[25] | K.S and Geen[21] |           |
|             |                                  | Simple GA                                  | Fuzzy GA |                    |                  |           |
| 1           | A <sub>1</sub> ~A <sub>4</sub>   | 2.141                                      | 1.732    | 2.755              | 1.963            | 1.902     |
| 2           | A <sub>5</sub> ~A <sub>12</sub>  | 0.510                                      | 0.522    | 0.510              | 0.481            | 0.520     |
| 3           | A <sub>13</sub> ~A <sub>16</sub> | 0.054                                      | 0.010    | 0.010              | 0.010            | 0.010     |
| 4           | A <sub>17</sub> ~A <sub>18</sub> | 0.010                                      | 0.013    | 0.010              | 0.011            | 0.010     |
| 5           | A <sub>19</sub> ~A <sub>22</sub> | 1.489                                      | 1.345    | 1.370              | 1.233            | 1.293     |
| 6           | A <sub>23</sub> ~A <sub>30</sub> | 0.551                                      | 0.551    | 0.507              | 0.506            | 0.520     |
| 7           | A <sub>31</sub> ~A <sub>34</sub> | 0.057                                      | 0.010    | 0.010              | 0.011            | 0.010     |
| 8           | A <sub>35</sub> ~A <sub>36</sub> | 0.013                                      | 0.013    | 0.010              | 0.012            | 0.010     |
| 9           | A <sub>37</sub> ~A <sub>40</sub> | 0.565                                      | 0.492    | 0.481              | 0.538            | 0.545     |
| 10          | A <sub>41</sub> ~A <sub>48</sub> | 0.527                                      | 0.545    | 0.508              | 0.533            | 0.520     |
| 11          | A <sub>49</sub> ~A <sub>52</sub> | 0.010                                      | 0.066    | 0.010              | 0.010            | 0.010     |
| 12          | A <sub>53</sub> ~A <sub>54</sub> | 0.066                                      | 0.013    | 0.064              | 0.167            | 0.017     |
| 13          | A <sub>55</sub> ~A <sub>58</sub> | 0.174                                      | 0.178    | 0.215              | 0.161            | 0.179     |
| 14          | A <sub>59</sub> ~A <sub>66</sub> | 0.425                                      | 0.524    | 0.518              | 0.542            | 0.522     |
| 15          | A <sub>67</sub> ~A <sub>70</sub> | 0.437                                      | 0.396    | 0.419              | 0.478            | 0.472     |
| 16          | A <sub>71</sub> ~A <sub>72</sub> | 0.641                                      | 0.595    | 0.504              | 0.551            | 0.650     |
| Weight (lb) |                                  | 372.474                                    | 364.486  | 376.501            | 364.38           | 364.93    |

表 5.7.1 例七，空間 22 根桿件桁架，桿件編號與節點編號之關係

| No. | B-Node | E-Node | No. | B-Node | E-Node |
|-----|--------|--------|-----|--------|--------|
| 1   | 1      | 5      | 12  | 6      | 4      |
| 2   | 2      | 6      | 13  | 1      | 7      |
| 3   | 3      | 7      | 14  | 2      | 8      |
| 4   | 4      | 8      | 15  | 2      | 5      |
| 5   | 1      | 3      | 16  | 1      | 6      |
| 6   | 2      | 4      | 17  | 4      | 7      |
| 7   | 1      | 2      | 18  | 3      | 8      |
| 8   | 3      | 4      | 19  | 4      | 5      |
| 9   | 1      | 4      | 20  | 3      | 6      |
| 10  | 2      | 3      | 21  | 2      | 7      |
| 11  | 5      | 3      | 22  | 1      | 8      |



表 5.7.2 例七，空間 22 根桿件桁架，斷面連結情形

| Group number | Members                          |
|--------------|----------------------------------|
| 1            | A <sub>1</sub> -A <sub>4</sub>   |
| 2            | A <sub>5</sub> -A <sub>6</sub>   |
| 3            | A <sub>7</sub> -A <sub>8</sub>   |
| 4            | A <sub>9</sub> -A <sub>10</sub>  |
| 5            | A <sub>11</sub> -A <sub>14</sub> |
| 6            | A <sub>15</sub> -A <sub>18</sub> |
| 7            | A <sub>19</sub> -A <sub>22</sub> |

表 5.7.3 例七，空間 22 根桿件桁架，桿件應力限制

| Members                          | Compressive stress Limitations (ksi) | Tensile stress Limitations (ksi) |
|----------------------------------|--------------------------------------|----------------------------------|
| A <sub>1</sub> -A <sub>4</sub>   | 24.0                                 | 36.0                             |
| A <sub>5</sub> -A <sub>6</sub>   | 30.0                                 | 36.0                             |
| A <sub>7</sub> -A <sub>8</sub>   | 28.0                                 | 36.0                             |
| A <sub>9</sub> -A <sub>10</sub>  | 26.0                                 | 36.0                             |
| A <sub>11</sub> -A <sub>14</sub> | 22.0                                 | 36.0                             |
| A <sub>15</sub> -A <sub>18</sub> | 20.0                                 | 36.0                             |
| A <sub>19</sub> -A <sub>22</sub> | 18.0                                 | 36.0                             |



表 5.7.4 例七，空間 22 根桿件桁架，受力情形

| Node | Condition 1    |                |                | Condition 2    |                |                | Condition 3    |                |                |
|------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
|      | P <sub>X</sub> | P <sub>Y</sub> | P <sub>Z</sub> | P <sub>X</sub> | P <sub>Y</sub> | P <sub>Z</sub> | P <sub>X</sub> | P <sub>Y</sub> | P <sub>Z</sub> |
| 1    | -20.0          | 0.0            | -5.0           | -20.0          | -5.0           | 0.0            | -20.0          | 0.0            | -35.0          |
| 2    | -20.0          | 0.0            | -5.0           | -20.0          | -50.0          | 0.0            | -20.0          | 0.0            | 0.0            |
| 3    | -20.0          | 0.0            | -30.0          | -20.0          | -5.0           | 0.0            | -20.0          | 0.0            | 0.0            |
| 4    | -20.0          | 0.0            | -30.0          | -20.0          | -50.0          | 0.0            | -20.0          | 0.0            | -35.0          |

※Note: loads are in kips

表 5.7.5 例七，啟發式最佳化設計搜尋點與其相對重量

| 搜尋過程 |          |           |     |
|------|----------|-----------|-----|
| No.  | $\alpha$ | W (lb)    | T/F |
| 1    | 1.000000 | 990.11392 | T   |
| 2    | 1.235000 | 1066.0393 | T   |
| 3    | 1.117500 | 1032.1465 | T   |
| 4    | 1.058750 | 1012.2844 | F   |
| 5    | 1.088125 | 1022.3741 | F   |
| 6    | 1.102813 | 1027.2375 | T   |
| 7    | 1.095469 | 1024.8148 | F   |
| 8    | 1.099141 | 1026.0217 | F   |
| 9    | 1.100977 | 1026.6503 | T   |
| 10   | 1.100059 | 1026.3339 | T   |

T：可行設計

F：非可行設計

表 5.7.6 例七，最佳斷面經結構分析後節點位移

| Node | Load 1  |         |         | Load 2  |         |         | Load 3  |         |         |
|------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
|      | X       | Y       | Z       | X       | Y       | Z       | X       | Y       | Z       |
| 1    | 0.2356  | -0.0002 | -1.9163 | -0.3008 | -1.3129 | 0.0276  | -0.1497 | 0.5296  | 1.1757  |
| 2    | 0.2356  | 0.0002  | -1.9163 | 0.2294  | -1.6486 | 0.0224  | 0.0036  | 0.5571  | -1.0632 |
| 3    | -0.3787 | -0.0358 | -2.0000 | -0.3008 | -1.3129 | -0.0276 | 0.0036  | -0.5571 | 1.0632  |
| 4    | -0.3787 | 0.0358  | -2.0000 | 0.2294  | -1.6486 | -0.0224 | -0.1497 | -0.5296 | -1.1757 |
| 5    | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  |
| 6    | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  |
| 7    | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  |
| 8    | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  | 0.0000  |

※Note: Displacements are in inch

表 5.7.7 例六，最佳斷面經結構分析後桿件應力

| No. | Load 1  | Load 2  | Load 3  | Stress Limite |
|-----|---------|---------|---------|---------------|
| 1   | 9.817   | -12.532 | -6.236  |               |
| 2   | 9.817   | 9.557   | 0.151   | -24~36        |
| 3   | -15.779 | -12.532 | 0.151   |               |
| 4   | -15.779 | 9.557   | -6.236  |               |
| 5   | 10.468  | 6.899   | 14.065  | -30~36        |
| 6   | 10.468  | 5.591   | 14.065  |               |
| 7   | 0.027   | -27.980 | 2.290   | -28~36        |
| 8   | 5.967   | -27.980 | 2.290   |               |
| 9   | 5.296   | -17.449 | 29.326  | -26~36        |
| 10  | 5.296   | -17.449 | -17.499 |               |
| 11  | 10.800  | -10.934 | -13.154 |               |
| 12  | 10.800  | 8.881   | 9.084   | -22~36        |
| 13  | -15.119 | -10.934 | 9.084   |               |
| 14  | -15.119 | 8.881   | -13.154 |               |
| 15  | 7.856   | -19.832 | 9.406   |               |
| 16  | 7.856   | 11.855  | -13.816 | -20~36        |
| 17  | -12.027 | -19.832 | -13.816 |               |
| 18  | -12.027 | 11.855  | 9.406   |               |
| 19  | 9.364   | -17.985 | -0.692  |               |
| 20  | 9.364   | 11.169  | -2.210  | -18~36        |
| 21  | -12.339 | -17.985 | -2.210  |               |
| 22  | -12.339 | 11.169  | -0.692  |               |

※Note: Stresses are in ksi

表 5.7.8 例七，最佳化斷面比較表。

| No.         |                                  | Optimal cross-sectional (in <sup>2</sup> ) |                       |                  |           |
|-------------|----------------------------------|--|-----------------------|------------------|-----------|
|             |                                  | Sheu and Schmit[28]                        | Khan and Willmert[22] | K.S and Geen[21] | This work |
| 1           | A <sub>1</sub> -A <sub>4</sub>   | 2.629                                      | 2.563                 | 2.588            | 2.580     |
| 2           | A <sub>5</sub> -A <sub>6</sub>   | 1.162                                      | 1.553                 | 1.083            | 1.301     |
| 3           | A <sub>7</sub> -A <sub>8</sub>   | 0.343                                      | 0.281                 | 0.363            | 0.278     |
| 4           | A <sub>9</sub> -A <sub>10</sub>  | 0.423                                      | 0.512                 | 0.422            | 0.552     |
| 5           | A <sub>11</sub> -A <sub>14</sub> | 2.782                                      | 2.626                 | 2.827            | 2.820     |
| 6           | A <sub>15</sub> -A <sub>18</sub> | 2.173                                      | 2.131                 | 2.055            | 2.191     |
| 7           | A <sub>19</sub> -A <sub>22</sub> | 1.952                                      | 2.213                 | 2.044            | 1.917     |
| Weight (lb) |                                  | 1024.80                                    | 1034.74               | 1022.23          | 1026.32   |

表 5.8.1 例八，黃金切割搜尋過程

| No. | I        | $X_L$    | $X_A$    | $X_B$    | $X_U$    |
|-----|----------|----------|----------|----------|----------|
| 1   | 1.000000 | 0.000000 | 0.381966 | 0.618034 | 1.000000 |
| 2   | 0.618034 | 0.381966 | 0.618034 | 0.763932 | 1.000000 |
| 3   | 0.381966 | 0.618034 | 0.763932 | 0.854102 | 1.000000 |
| 4   | 0.236068 | 0.763932 | 0.854102 | 0.909830 | 1.000000 |
| 5   | 0.145898 | 0.854102 | 0.909830 | 0.944272 | 1.000000 |
| 6   | 0.090170 | 0.909830 | 0.944272 | 0.965558 | 1.000000 |
| 7   | 0.055728 | 0.909830 | 0.931116 | 0.944272 | 0.965558 |
| 8   | 0.034442 | 0.931116 | 0.944272 | 0.952403 | 0.965558 |
| 9   | 0.021286 | 0.931116 | 0.939247 | 0.944272 | 0.952403 |
| 10  | 0.013156 | 0.939247 | 0.944272 | 0.947378 | 0.952403 |
| 11  | 0.008131 | 0.939247 | 0.942353 | 0.944272 | 0.947378 |



表 5.8.2 例八，最佳斷面經結構分析後節點位移

| Node | X Translation (in) | Y Translation (in) | Z Translation (in) |
|------|--------------------|--------------------|--------------------|
| 1    | 0.2367             | 0.0053             | -1.9016            |
| 2    | 0.2367             | -0.0053            | -1.9016            |
| 3    | -0.3754            | 0.0048             | -1.9994            |
| 4    | -0.3754            | -0.0048            | -1.9994            |
| 5    | 0.0000             | 0.0000             | 0.0000             |
| 6    | 0.0000             | 0.0000             | 0.0000             |
| 7    | 0.0000             | 0.0000             | 0.0000             |
| 8    | 0.0000             | 0.0000             | 0.0000             |

表 5.8.3 例八，最佳斷面經結構分析後桿件應力

| No. | Stress (ksi) | Stress Limite (ksi) |
|-----|--------------|---------------------|
| 1   | 9.864        |                     |
| 2   | 9.864        |                     |
| 3   | -15.643      | -24~36              |
| 4   | -15.643      |                     |
| 5   | 12.224       |                     |
| 6   | 12.224       | -30~36              |
| 7   | -0.888       |                     |
| 8   | -0.799       | -28~36              |
| 9   | 3.177        |                     |
| 10  | 3.177        | -26~36              |
| 11  | 10.914       |                     |
| 12  | 10.914       |                     |
| 13  | -14.892      | -22~36              |
| 14  | -14.892      |                     |
| 15  | 7.803        |                     |
| 16  | 7.803        |                     |
| 17  | -12.594      | -20~36              |
| 18  | -12.594      |                     |
| 19  | 8.836        |                     |
| 20  | 8.836        | -18~36              |
| 21  | -12.239      |                     |
| 22  | -12.239      |                     |

表 5.8.4 例八，遺傳演算法參數與條件設定

|                     |         |
|---------------------|---------|
| 族群數(population)     | 50      |
| 演化世代(generations)   | 2000    |
| 設計變數                | 7       |
| 設計變數範圍              | 0.1~4.3 |
| 突變率                 | 0.08    |
| $\psi$ 懲罰因子         | 1       |
| $\alpha$ 違反限制常數指數因子 | 1       |



表 5.9.1 例九，空間 25 根桿件桁架，桿件編號與節點編號之關係表

| No. | B-Node | E-Node |
|-----|--------|--------|
| 1   | 1      | 2      |
| 2   | 1      | 4      |
| 3   | 2      | 3      |
| 4   | 1      | 5      |
| 5   | 2      | 6      |
| 6   | 2      | 5      |
| 7   | 2      | 4      |
| 8   | 1      | 3      |
| 9   | 1      | 6      |
| 10  | 3      | 6      |
| 11  | 4      | 5      |
| 12  | 3      | 4      |
| 13  | 5      | 6      |
| 14  | 3      | 10     |
| 15  | 6      | 7      |
| 16  | 4      | 9      |
| 17  | 5      | 8      |
| 18  | 3      | 8      |
| 19  | 4      | 7      |
| 20  | 6      | 9      |
| 21  | 5      | 10     |
| 22  | 3      | 7      |
| 23  | 4      | 8      |
| 24  | 5      | 9      |
| 25  | 6      | 10     |

表 5.9.2 例九，空間 25 根桿件桁架，斷面連結情形

| Group number | Members                          |
|--------------|----------------------------------|
| 1            | A <sub>1</sub>                   |
| 2            | A <sub>2</sub> -A <sub>5</sub>   |
| 3            | A <sub>6</sub> -A <sub>9</sub>   |
| 4            | A <sub>10</sub> -A <sub>11</sub> |
| 5            | A <sub>12</sub> -A <sub>13</sub> |
| 6            | A <sub>14</sub> -A <sub>17</sub> |
| 7            | A <sub>18</sub> -A <sub>21</sub> |
| 8            | A <sub>22</sub> -A <sub>25</sub> |

表 5.9.3 例九，空間 25 根桿件桁架，設計條件

| 限制條件   |    |          |          |          |
|--|----|----------|----------|----------|
| 位移限制： $\Delta_j$ ，x 與 y 方向，j=1,2   |    |          |          |          |
| 應力限制： $-40 \text{ ksi} \leq \sigma_{\text{allow}} \leq 40 \text{ ksi}$ ，i=1...25 |    |          |          |          |
| 最小桿件面積限制： $0.1 \text{ in}^2 \leq A_i$ ，i=1...25                                  |    |          |          |          |
| 受力情形   |    |          |          |          |
| No.  | 節點 | x (kips) | y (kips) | z (kips) |
| 1  | 1  | 1        | -10      | -10      |
|  | 2  | 0        | -10      | -10      |
|  | 3  | 0.5      | 0        | 0        |
|  | 6  | 0.6      | 0        | 0        |
| 材料性質   |    |          |          |          |
| 彈性係數： $10^4 \text{ ksi}$   |    |          |          |          |
| 材料密度： $0.1 \text{ lb/in}^3$  |    |          |          |          |

表 5.9.4 例九，啟發式設計過程搜尋點與其相對重量

| 搜尋過程 |          |             |     |
|------|----------|-------------|-----|
| No.  | $\alpha$ | Weight (lb) | T/F |
| 1    | 1.000000 | 470.360     | T   |
| 2    | 0.500000 | 470.344     | T   |
| 3    | 0.250000 | 470.366     | T   |
| 4    | 0.125000 | 470.369     | T   |
| 5    | 0.062500 | 470.363     | T   |
| 6    | 0.031250 | 470.365     | T   |
| 7    | 0.015625 | 470.358     | T   |
| 8    | 0.007813 | 470.364     | T   |
| 9    | 0.003906 | 470.353     | T   |
| 10   | 0.001953 | 470.359     | T   |
| 11   | 0.000977 | 470.349     | T   |

T：可行設計

F：非可行設計

表 5.9.5 例九，最佳斷面經結構分析後節點位移

| Node | X Translation<br>(in) | Y Translation<br>(in) | Z Translation<br>(in) |
|------|-----------------------|-----------------------|-----------------------|
| 1    | 0.0279                | -0.3500               | -0.0546               |
| 2    | 0.0284                | -0.3422               | -0.0426               |
| 3    | 0.0067                | 0.0229                | 0.0563                |
| 4    | 0.0239                | 0.0213                | 0.0670                |
| 5    | 0.0002                | 0.0371                | -0.1223               |
| 6    | 0.0414                | 0.0354                | -0.1390               |
| 7    | 0.0000                | 0.0000                | 0.0000                |
| 8    | 0.0000                | 0.0000                | 0.0000                |
| 9    | 0.0000                | 0.0000                | 0.0000                |
| 10   | 0.0000                | 0.0000                | 0.0000                |

表 5.9.6 例九，最佳斷面經結構分析後桿件應力

| No. | Stress (ksi) | No. | Stress (ksi) | No. | Stress (ksi) |
|-----|--------------|-----|--------------|-----|--------------|
| 1   | 0.064        | 11  | -2.105       | 21  | -3.011       |
| 2   | 0.861        | 12  | 2.295        | 22  | 2.589        |
| 3   | 3.192        | 13  | -5.485       | 23  | 2.177        |
| 4   | -5.766       | 14  | 2.801        | 24  | -5.570       |
| 5   | -3.223       | 15  | -4.933       | 25  | -5.112       |
| 6   | -5.483       | 16  | 2.482        |     |              |
| 7   | 2.344        | 17  | -5.286       |     |              |
| 8   | 2.544        | 18  | 0.998        |     |              |
| 9   | -5.265       | 19  | 2.638        |     |              |
| 10  | -1.667       | 20  | -5.295       |     |              |

表 5.9.7 例九，遺傳演算法參數與條件設定

|                     |       |
|---------------------|-------|
| 族群數(population)     | 50    |
| 演化世代(generations)   | 1000  |
| 設計變數                | 8     |
| 設計變數範圍              | 0.1~4 |
| 突變率                 | 0.08  |
| $\psi$ 懲罰因子         | 5     |
| $\alpha$ 違反限制常數指數因子 | 1     |

表 5.10.1 案例設計所需搜尋次數

|      | 例一 | 例二 | 例三 | 例四 | 例五 | 例六 | 例七 | 例八 | 例九 |
|------|----|----|----|----|----|----|----|----|----|
| 搜尋次數 | 13 | 14 | 11 | 11 | 13 | 11 | 10 | 11 | 11 |

表 5.10.2 案例設計所需結構分析次數

|        | 例一 | 例二 | 例三 | 例四 | 例五                 | 例六                 | 例七                  | 例八 | 例九 |
|--------|----|----|----|----|--------------------|--------------------|---------------------|----|----|
| FSD 階段 | 40 | 30 | 58 | 21 | 22*2+21<br>=<br>65 | 22*2+21<br>=<br>65 | 31*3+53<br>=<br>146 | 53 | 28 |
| 搜尋 階段  | 13 | 14 | 11 | 11 | 13                 | 11                 | 10                  | 11 | 11 |
| 總共次數   | 53 | 44 | 69 | 32 | 78                 | 76                 | 156                 | 64 | 39 |

表 5.10.3 最佳設計重量比較

|    | 文獻或<br>參考模型重量<br>(lb) | 本文重量<br>(lb) | 相對誤差   |
|----|-----------------------|--------------|--------|
| 例一 | 5057.88 [21]          | 5079.97      | 0.437% |
| 例二 | 4668.81 [21]          | 4711.52      | 0.915% |
| 例三 | 2580.81 [21]          | 2582.17      | 0.053% |
| 例四 | 379.07 [21]           | 370.12       | 2.319% |
| 例五 | 379.27 [26]           | 380.33       | 0.279% |
| 例六 | 364.33 [21]           | 364.93       | 0.165% |
| 例七 | 1022.23 [21]          | 1026.30      | 0.398% |
| 例八 | 861.82 [R]            | 861.72       | 0.012% |
| 例九 | 468.76 [R]            | 470.33       | 0.335% |

※R：Reference Model