

國立交通大學  
電子工程學系電子研究所

碩士論文

超薄雙閘極金氧半場效電晶體與矽奈米線電晶體

涵蓋通道背向散射效應之物理解析模型

Channel Backscattering Based Analytic Model

for Double-Gate MOSFETs and Silicon Nanowire Transistors

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## 摘要

根據通道背向散射效應的基本理論，其物理解析式模型主要是建立在源極到通道的能障頂端上的  $k_B T$  layer 內。經由利用一維 Schrödinger 和 Poisson 模擬，再透過不同結構模型的運算，可驗證此模型之正確性；或者利用 Monte Carlo 原理去模擬在不同條件下之電子束反射與透射的關係，亦可做為檢驗此模型之依據。此論文將分別針對超薄雙閘極金氧半場效電晶體和矽奈米線電晶體的模型來做模擬分析與比較，並且得出合理的結果。

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## Abstract

According to the fundamental theory of the channel backscattering, a physically based analytic model is established in the  $k_B T$  layer at the peak of the source-channel barrier. By using the 1-D Schrödinger-Poisson simulation and the evaluations of the underlying different structures, the validity of the model can be corroborated. Simulation for the forward and backward flux relation under different conditions by the Monte Carlo technique can also confirm the validity of the model. In this thesis, a series of physically-based analytic models applied to ultra-thin double-gate MOSFETs and silicon nanowire transistors are analyzed and testified. The reasonable results are achieved.

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# Chapter 1

## Introduction

As the feature lengths of metal-oxide-semiconductor field effect transistors (MOSFETs) continue to scale into the nanoscale regime, short channel effects become more and more significant and quantum mechanics is expected to govern the underlying transport details. Consequently, an effective gate control is required for a nanoscale MOSFET to achieve good device performance. Therefore, some advanced MOSFET structures such as double-gate MOSFETs or silicon nanowire transistors (SNWTs) have been proposed and explored in the past years to exhibit their good gate controllability. It is generally recognized that while carriers, during the operation of the device, encounter significant space confinements and few scatterings, the conventional semiconductor transport theory would lose its accuracy in addressing such situations. In order to deal with this issue, channel backscattering theory has recently been introduced to provide the mesoscopic aspects of carrier transport in nanoscale MOSFETs [1]-[7].

The channel backscattering theory describes a wave-like transport of carriers through the channel from source to drain. In the schematic illustration of the theory for the saturation case shown in Figure 1-1, a  $k_B T$  layer, where  $k_B$  is Boltzmann's constant and  $T$  is the temperature, represents the region from the peak of the source-channel junction barrier down by a thermal energy of  $k_B T$ , and its width is denoted by  $l$  [2]-[7]. This specific zone located near the source critically determines the current drive at the drain

$$I_D = Q_{tot} v_{inj} \frac{1-r_C}{1+r_C} \quad (1.1)$$

where  $Q_{tot}$  is the total charge density per unit area at the top of the source-channel junction barrier,  $v_{inj}$  the thermal injection velocity at the top of the source-channel junction barrier, and  $r_C$  is the channel backscattering coefficient through the layer. The term  $Q_{tot}/(1+r_C)$  is related to the carriers injected from the source and  $(1-r_C)$  is the ratio of carriers traveling across the barrier to the drain. The theory also argues that the backscattering coefficient  $r_C$  is functionally linked to both the quasi-thermal-equilibrium mean-free-path  $\lambda$  for backscattering and the width  $l$  of the  $k_B T$  layer

$$r_C = \frac{1}{1 + \frac{\lambda}{l}} \quad (1.2)$$



In this thesis, a 2-D physically-based analytic model established at the peak of the source-channel barrier for double-gate MOSFETs [8]-[11] and a 1-D model for silicon nanowire transistors [8], [11]-[14] with channel length down to 25nm and 10 nm, respectively, have been demonstrated. Additionally, an the 1-D Monte Carlo particle simulation [8] is utilized to explore the backscattering coefficient  $r_C$ , and its mean-free-path  $\lambda$  is straightforwardly extracted to investigate the low-field mobility of electrons in silicon [6].

This thesis is organized as follows. In Chapter 2, we exhibit the 2-D model for double-gate MOSFETs and compare it with Monte Carlo simulation results [9]. Subsequently, in Chapter 3, the low-field mobility of

electrons in silicon with Monte Carlo particle simulation is studied [6]. In Chapter 4, the 1-D model for the silicon nanowire transistors is demonstrated and compared with another model called Büttiker probes [12]. Finally, a conclusion of the work will be shown in Chapter 5.



## Chapter 2

### Physically Based Analytic Model for 2-D Devices

#### 2.1 Device Under Study

Figure 2-1 describes the cross section of the double-gate MOSFET structure under study: a 1.5-nm-thick silicon film double-gate MOSFETs with channel length equal to 25 nm. The gate length  $L$  is equal to the channel length. The top and bottom gate oxide thickness are  $t_{ox}=1.5$  nm, and the Si body thickness  $t_{si}$  is also 1.5 nm. The n+ source and drain are degenerately doped at a level of  $10^{20}$  /cm<sup>3</sup>, and the whole channel region is undoped. The low-field mobility is assumed to be 120 cm<sup>2</sup>/V-sec, and the work function of the top and bottom gate is 4.25 eV. All the simulations are conducted at room temperature ( $T=300$  K). To obtain the steady-state behavior of the device, the same voltage of 0.56V is applied to both the top gate and bottom gate, which results in the same work function with symmetry.

#### 2.2 Model Establishment

With the concepts of the elementary scattering theory, we established a 2-D model for the double-gate system. Figure 2-2 shows the conduction band profile from source to drain along with the electron energy versus wave vector plot at the peak of the barrier showing the ratio of backward to forward flux,  $r_{BF}$ . The forward flux from the source side brings a carrier density  $n_s(+)$  and the backward flux is  $n_s(-)$ . Then the ratio  $r_{BF}$  can be defined as

$$r_{BF} = \frac{n_S(-)}{n_S(+)} \quad (2.1)$$

At the top of the source-channel junction barrier, the total carrier density  $n_S$  is

$$n_S = n_S(+) + n_S(-) \quad (2.2)$$

and

$$n_S = \sum_i n_S^i \quad (2.3)$$

Here  $n_S^i$  is the carrier density with subband  $i$ . It can be developed that

$$n_S^i = (1 + r_{BF}) \left[ \frac{m_d^i k_B T}{2\pi \hbar^2} \right] n_v^i \ln \left( 1 + e^{\frac{E_F - E_i}{k_B T}} \right) \quad (2.4)$$

where  $n_v^i$  is the valley degeneracy and  $m_d^i$  is the density-of-states effective mass for subband  $i$ .

With the model for the above double-gate system, A self-consistent Schrödinger-Poisson simulation [8] was performed on a 1-D upper metal-gate oxide-silicon film-gate oxide-bottom metal system, yielding channel subband levels and Fermi level versus gate voltage as shown in Figure 2-3. According to the 1-D simulation results in Figure 2-4, almost all

of the electrons occupy the first subband of the two-fold valley (i.e.  $n_v^i=2$ ), therefore the carrier density only on the first subband (i.e.  $i=1$ ,  $n_s^1=n_s$ ) can be reasonably calculated [3]. With the same subband and Fermi-level, the effective thermal injection velocity at the top of source-junction barrier is as follows:

$$v_{inj}^i = \sqrt{\frac{2k_B T m_C^i}{\pi m_d^{i2}}} \left( \frac{\mathfrak{F}_{1/2}(\eta_F)}{\ln(1 + e^{\eta_F})} \right) \quad (2.5)$$

$$\mathfrak{F}_{1/2}(\eta_F) = \frac{1}{\Gamma\left(\frac{3}{2}\right)} \int_0^\infty \frac{\eta^{1/2} d\eta}{1 + e^{\eta - \eta_F}} = \frac{2}{\sqrt{\pi}} \int_0^\infty \frac{\eta^{1/2} d\eta}{1 + e^{\eta - \eta_F}}$$

$$\eta_F = \frac{E_F - E_i}{k_B T}$$



where  $m_C^i$  is the conductivity effective mass for subband  $i$ ,  $E_i$  the energy level of subband  $i$ ,  $E_F$  the Fermi-level, and  $\mathfrak{F}_{1/2}$  is the Fermi-Dirac integral of order 1/2. For two-fold valley,  $m_C^i = m_d^i = m_t$ , where the transverse effective mass  $m_t = 0.19m_0$ .

The mean-free-path for backscattering is exhibited as follows:

$$\lambda = 2 \frac{k_B T}{q} \frac{\mu}{v_{inj}} \frac{(1 + e^{\eta_F}) \ln(1 + e^{\eta_F})}{e^{\eta_F}} \quad (2.6)$$

where  $\mu$  is the quasi-equilibrium mobility. The backscattering coefficient  $r_C$  is



$$r_c = \frac{1}{1 + \frac{\lambda}{l}} \quad (2.7)$$

where  $l$  is the width of the  $k_B T$  layer. The drain current can therefore be obtained:

$$I_{DS} = qn_s v_{inj} \frac{1 - r_c}{1 + r_c} \quad (2.8)$$

### 2.3 Analysis with 2-D model

Figure 2-5 is the flow chart of our analysis. According to MOS electrostatics [3], we have

$$qn_s = C_{eff} [V_G - (V_{tho} - DIBL \times V_D)] \quad (2.9)$$

The effective gate capacitance  $C_{eff}$  and quasi-equilibrium threshold voltage  $V_{tho}$  can be assessed via the Schrödinger-Poisson solver under zero DIBL [8]. The  $k_B T$  layer widths are extracted from the simulated potential profiles for different scattering areas cited in [9] as shown in Figure 2-6.

In case 1, the carriers scattering only occurs in the  $k_B T$  layer is considered. Hence, the ratio of backward to forward flux  $r_{BF}$  is equal to the channel backscattering coefficient  $r_c$  [5]. Through the iteration method with initial  $r_{BF} = 0$ , the convergent  $r_{BF}$  is obtained. Afterwards, the drain current called  $I_{D(\text{without } Q)}$  can be calculated. In case 2, we considered that after the

carriers pass through the  $k_B T$  layer, additional elastic and inelastic scattering effect may occur [9]. Consequently, the flux plot is shown in Figure 2-7. We have transformed the flux plot to apply to our model as shown in Figure 2-8, where the  $r_{BF}$  can be shown as a function of  $r_c$ :

$$r_{BF} = r_c + (1 - r_c) \frac{Q'}{Q_{inv}} \quad (2.10)$$

The term  $Q_{inv}$  is defined as the carriers injected from source and  $Q'$  the carriers reflected from the scattering zone after the carriers pass through the  $k_B T$  layer. After iteration process, the coefficient of  $r_{BF}$  is obtained with the drain current of

$$I_{DS} = qn_S v_{inj} \frac{1 - r_{BF}}{1 + r_{BF}} \quad (2.11)$$


Here the  $I_{DS}$  is called  $I_{D(\text{with } Q')}$  to imply that the additional elastic and inelastic scattering effects are considered.

## 2.4 Results

To examine the validity of the channel backscattering theory, we have compared the calculated results with those from 2-D Monte Carlo particle simulation [9]. The calculation values in case 2 are considerably consistent with the Monte Carlo particle simulation results as exhibited in Figure 2-9. Furthermore, corroborating evidence in terms of the height of the source-channel junction barrier is given in Figure 2-10. However, as the

mobility  $\mu$  or scattering time is increased by a factor of 5, implying that the channel length is effectively reduced from 25nm down to 5nm, the calculated drain currents is also consistent with the Monte Carlo particle simulation results as shown in Figure 2-11. Consequently, the channel backscattering theory remains valid in this study.



## Chapter 3

### Low-Field Mobility of Electrons in Bulk Silicon

#### 3.1 Channel Backscattering Coefficient

In this study, if the channel is under low electric field conditions, the width of the  $k_B T$  layer  $l$  calculated according to its definition is wide enough to be larger than the channel length  $L$ . Therefore, the backscattering coefficient can be estimated from

$$r_{co} = \frac{L}{L + \lambda} \quad (3.1)$$

where  $\lambda$  is the mean-free-path,  $L$  is the channel length which is smaller than the  $k_B T$  layer width  $l$ , implying that the scattering effect is only assumed to occur in channel. When a strong channel electric field is present, i.e.  $l < L$ , the backscattering coefficient can be accordingly estimated from

$$r_c = \frac{l}{l + \lambda} \quad (3.2)$$

#### 3.2 Electron Transport Simulation

In order to explore the backscattering coefficient  $r_c$ , we have simulated electron transport through one-dimensional silicon devices by the Monte Carlo technique [8]. A model “channel” with length  $L = 80$  nm or 20 nm is divided into 100 grids to analyze the forward and backward flux in

each grid, and a constant electric field is applied. Figure 3-1 shows the schematic structure of the simulation in the model “channel”. The doping concentration is set to be  $8 \times 10^{17} / \text{cm}^3$  and the temperature is 300 K. From the definition of backscattering coefficient, we have

$$r_c = \frac{\text{flux}(-)}{\text{flux}(+)} = \frac{n^- v^-}{n^+ v^+} \quad (3.3)$$

$$\frac{n^-}{n^+} = \frac{\int_{-\infty}^0 f(v) dv}{\int_0^{\infty} f(v) dv}$$

$$\frac{v^-}{v^+} = \frac{\frac{\int_{-\infty}^0 f(v) v dv}{\int_{-\infty}^0 f(v) dv}}{\frac{\int_0^{\infty} f(v) v dv}{\int_0^{\infty} f(v) dv}}$$



where  $n^\pm$  is the electron density for forward/backward direction, and  $v^\pm$  is the average velocity for forward/backward direction. Fig. 3-2 shows an example case of the schematic velocity distribution. Here the backscattering coefficient  $r_c$  is just equal to the area ratio of negative to positive. Figure 3-3 shows the simulated backscattering coefficient of Monte Carlo evaluation under electric field from 10 V/cm to  $10^6$  V/cm for  $L = 80$  nm and  $L = 20$  nm. It is obvious that the backscattering coefficient is nearly constant at low electric field as a linear region. In contrast to low electric field, the backscattering coefficient for the higher electric field is lower in the saturation region, which is close to the ballistic limit.

### 3.3 Low-Field Mobility of Electrons

From the channel backscattering theory, since the backscattering coefficient  $r_C$  is functionally linked to both the quasi-thermal-equilibrium mean-free-path  $\lambda$  for backscattering and the width  $l$  of the  $k_B T$  layer, the mean-free-path  $\lambda$  can be obtained by fitting method. With the Monte Carlo simulation at different temperatures, the mean-free-path  $\lambda$  is extracted as shown in Figure 3-4. The mean-free-path is physically increased with the decrease of the temperature. Furthermore, the low-field mobility of electrons is calculated as shown in Figure 3-5. As a result, it is considerably reasonable [6] to keep the channel backscattering theory remaining valid in this study.

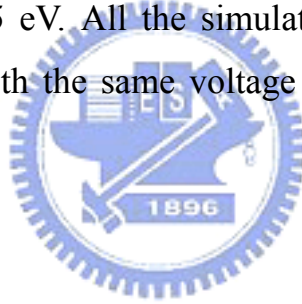


## Chapter 4

### Physically Based Analytic Model for 1-D case

#### 4.1 Device Under Study

Figure 4-1 describes the diagram of the Si nanowire transistor structure under study: a cylindrical SNWT with  $\langle 100 \rangle$  oriented channel length equal to 10 nm. The gate length  $L$  is equal to the channel length. The silicon body thickness  $T_{Si}$  is 3 nm, and the oxide thickness is 1 nm. The source/drain doping concentration is  $2 \times 10^{20} / \text{cm}^3$  and the channel region is undoped. The low-field mobility is assumed to be  $200 \text{ cm}^2/\text{V}\cdot\text{sec}$ , and the work function of the gate all around is 4.05 eV. All the simulations are conducted at room temperature ( $T=300 \text{ K}$ ) with the same voltage of 0.4V applied to both the gate and the drain.



#### 4.2 Model Establishment

Similar to Chapter 2 of this thesis, we have also established a 1-D model for the nanowire transistor system with the concepts of the elementary scattering theory [11].

For 1-D case, the density-of-states is exhibited as follows:

$$D_{1D}(E) = \frac{2}{\pi \hbar} \sqrt{\frac{m_d}{2}} \frac{1}{\sqrt{E - E_C}} \quad (4.1)$$

with a factor 2 to indicate the two carrier transportation directions in the

nanowire. Under steady-state, non-equilibrium conditions,

$$\frac{dN(E)}{dt} = 0 \quad (4.2)$$

and we can solve it for the steady-state number of electrons in the device. Consequently, the total number of electrons is obtained via integration over the energy in the device as

$$n_s^i = (1 + r_{BF}) \sqrt{\frac{m_d^i k_B T}{2\pi\hbar^2}} n_v^i \mathfrak{F}_{-1/2}(\eta_F) \quad (4.3)$$

where  $n_v^i$  is the valley degeneracy,  $m_d^i$  is the density-of-states effective mass for subband  $i$ , and  $\mathfrak{F}_{-1/2}$  is the Fermi-Dirac integral of order  $-1/2$  as shown below

$$\mathfrak{F}_{-1/2}(\eta_F) = \frac{1}{\Gamma\left(\frac{1}{2}\right)} \int_0^\infty \frac{\eta^{-1/2} d\eta}{1 + e^{\eta - \eta_F}} = \frac{1}{\sqrt{\pi}} \int_0^\infty \frac{\eta^{1/2} d\eta}{1 + e^{\eta - \eta_F}} \quad (4.4)$$

$$\eta_F = \frac{E_F - E_i}{k_B T}$$

where  $E_i$  is the energy level of subband  $i$ , and  $E_F$  is the Fermi-level. In this study, it is assumed that almost all of the electrons occupy the lowest subband (i.e.  $i=1$ ,  $n_s^1 = n_s$ ), which is the first subband of the four-fold valley (i.e.  $n_v^i=4$ ) [13], [14].



With the drain current contributed by subband,  $i$ ,

$$I = \frac{2qk_B T}{h} \left[ \ln(1 + e^{\eta_F}) \right] \quad (4.5)$$

$$= qn_s v_{inj}$$

the effective thermal injection velocity at the top of source-junction barrier is as follows [4].

$$v_{inj} = \sqrt{\frac{2k_B T}{\pi m_d^i}} \left( \frac{\ln(1 + e^{\eta_F})}{\mathfrak{F}_{-1/2}(\eta_F)} \right) \quad (4.6)$$

The mean-free-path for backscattering is exhibited as follows [10].

$$\lambda = 2 \frac{k_B T}{q} \frac{\mu}{v_{inj}} \frac{\mathfrak{F}_{-1/2}(\eta_F)}{\mathfrak{F}_{-3/2}(\eta_F)} \quad (4.7)$$

where  $\mu$  is the quasi-equilibrium mobility. The backscattering coefficient  $r_C$  is

$$r_C = \frac{1}{1 + \frac{\lambda}{l}} \quad (4.8)$$

then the drain current can be obtained as follows.

$$I_{DS} = qn_s v_{inj} \frac{1-r_C}{1+r_C} \quad (4.9)$$

### 4.3 Analysis with 1-D model

Similar to Chapter 2, by using the Schrödinger-Poisson solver, the effective gate capacitance  $C_{eff}$  and quasi-equilibrium threshold voltage  $V_{tho}$  can be obtained with the relationship as follows:

$$qn_s = C_{eff} (V_G - V_{tho}) \quad (4.10)$$

The  $k_B T$  layer widths are extracted from the potential profiles of Fig. 3 in [12]. The density-of-states effective mass is  $0.28m_0$  as shown in Figure 4-2 for wire diameter  $T_{Si}$  equal to 3 nm [14]. Following the case 1 of the flow chart in Chapter 2, the drain current at  $V_G=V_D=0.4V$  can be obtained.

### 4.4 Results

To examine the validity of the channel backscattering theory on 1-D case, we have compared the calculated results with those from another model called Büttiker probes [12]. The calculated drain currents appear to lie a little above the Büttiker probes ones as shown in Fig. 4-3. It suggests that the importance of the source-to-drain tunneling is increased for channel length down to below 10 nm. The existing channel backscattering formula might be improved with consideration of the source-to-drain tunneling effect.

## Chapter 5

### Conclusion

The physically based analytic models of the ultra-thin film double-gate MOSFETs and silicon nanowire transistors have been established. The validity of the models has been confirmed using sophisticated simulations such as 1-D Schrödinger-Poisson solving, 2-D and 1-D ballistic I-V simulations, and 1-D Monte Carlo particle simulations with the scattering in the channel. The issues of concern have been focused on the effect of backward to forward flux ratio on the thermal injection velocity at the top of the source-channel junction barrier. It is argued that the backward to forward flux ratio can determine the channel backscattering coefficient in the framework of the channel backscattering theory.



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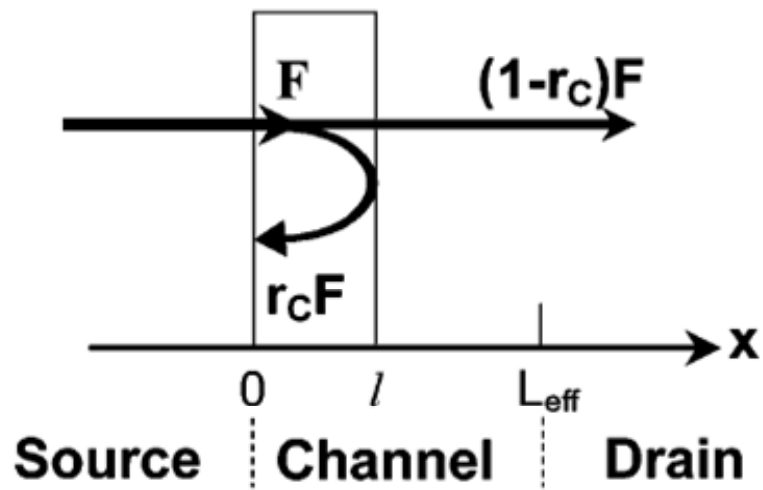


Fig. 1-1 Schematic diagram of channel backscattering theory.  $F$  is the incident flux from the source,  $l$  is the critical length over which a  $k_B T/q$  drop is developed, and  $r_c$  is the channel backscattering coefficient. The channel length  $L_{eff}$  is the physical gate length minus the source/drain extensions.

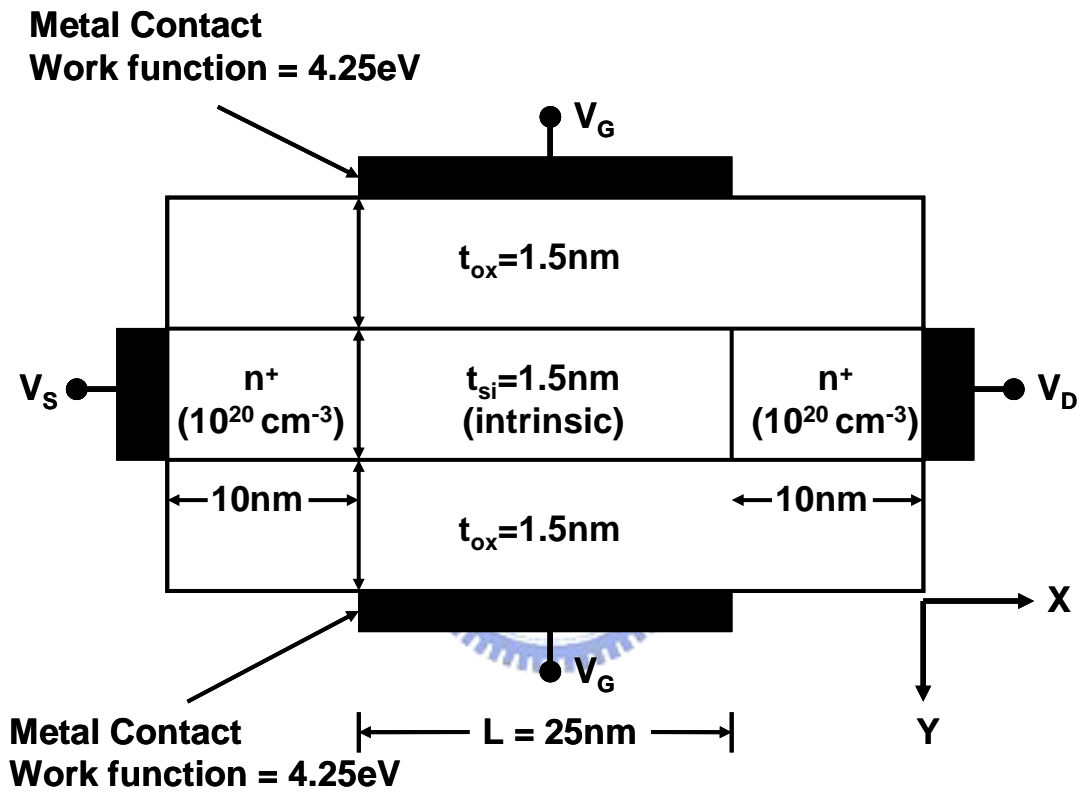


Fig. 2-1 Schematic cross section of the device under study.



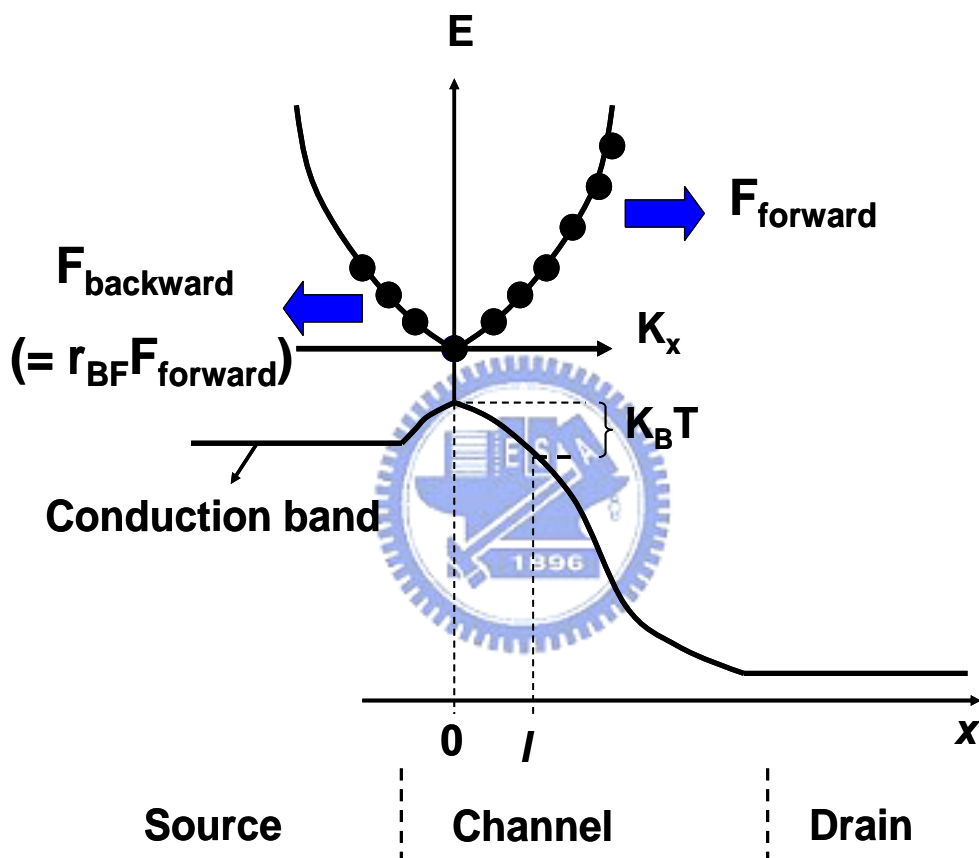


Fig. 2-2 Schematic conduction-band profile from source to drain. An  $E$ - $k$  diagram is plotted showing forward and backward flux at the peak of the source-channel barrier.

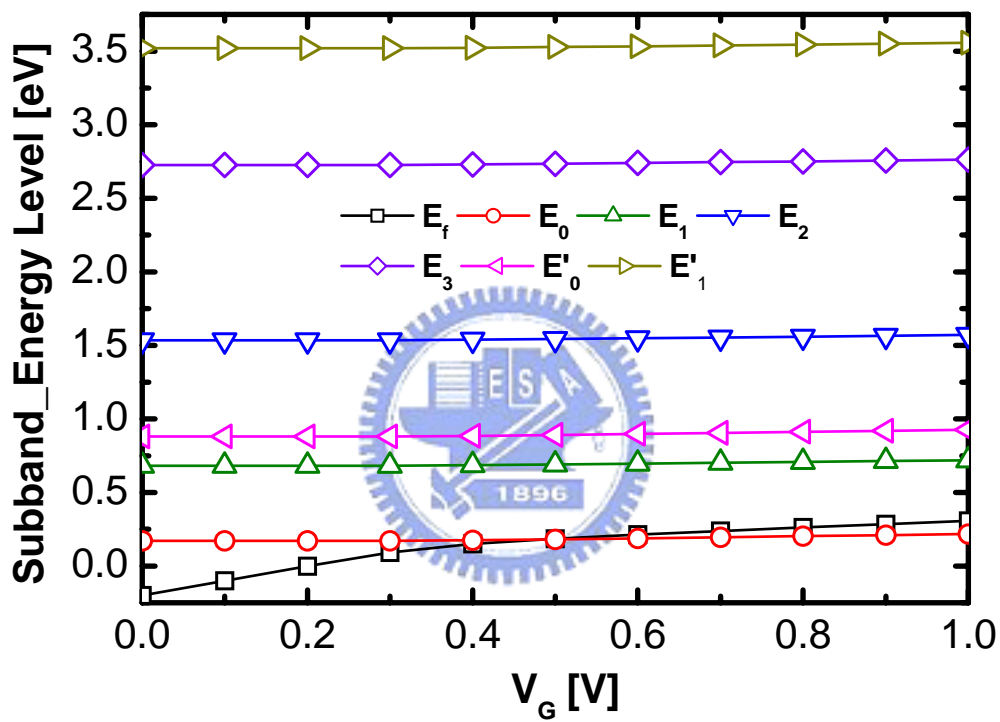


Fig. 2-3 Channel subband levels and Fermi level versus gate voltage obtained from 1-D self-consistent Schrödinger-Poisson simulation.

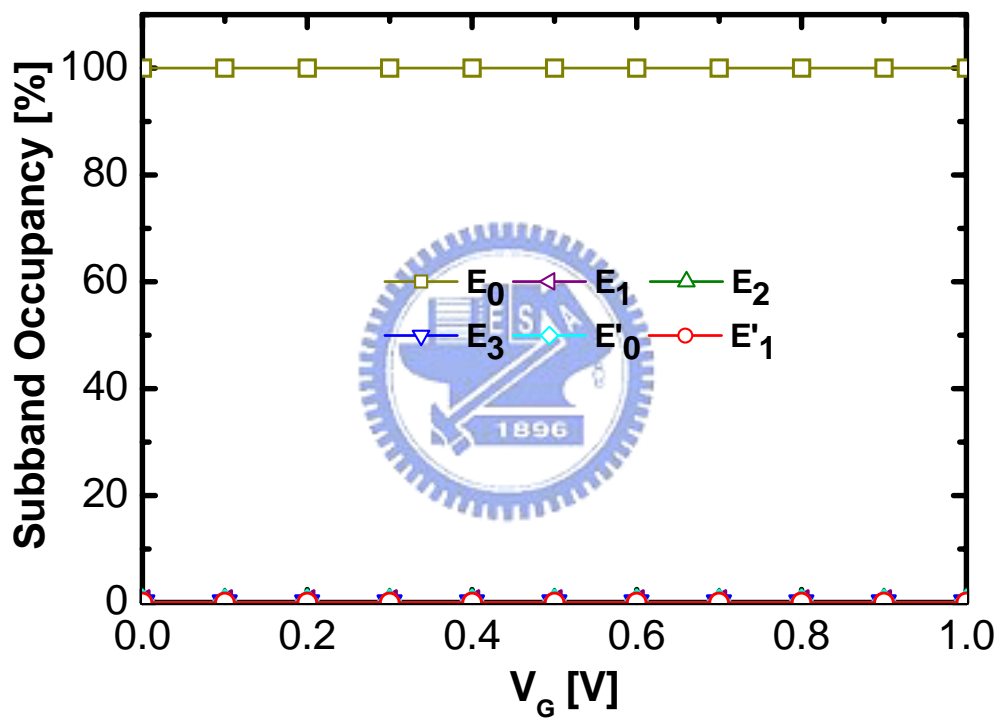


Fig. 2-4 Channel subband level occupancy versus gate voltage from 1-D self-consistent Schrödinger-Poisson simulation.

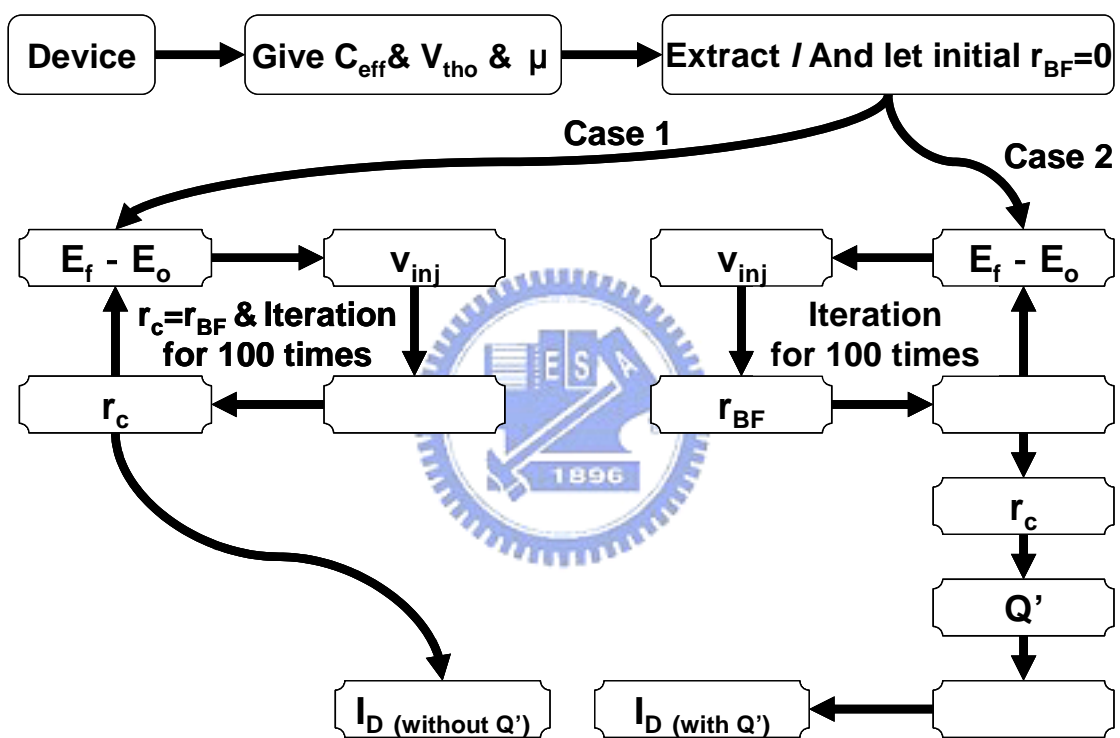


Fig. 2-5 Flowchart of our analysis.

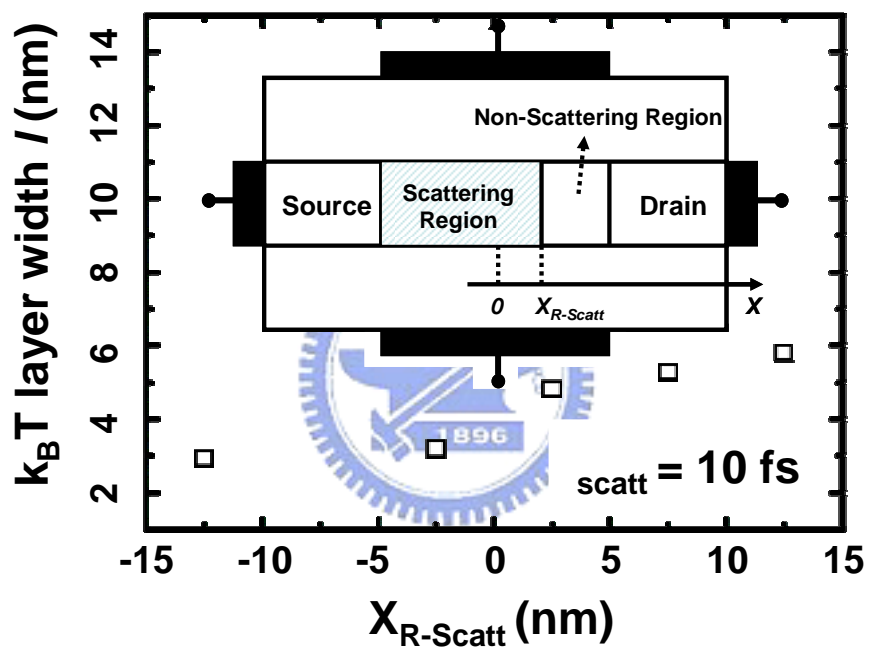


Fig. 2-6  $k_B T$  layer width versus  $X_{R-Scatt}$  quoted from [9] for  $L=25$ nm. The inset shows the definition of  $X_{R-Scatt}$ .

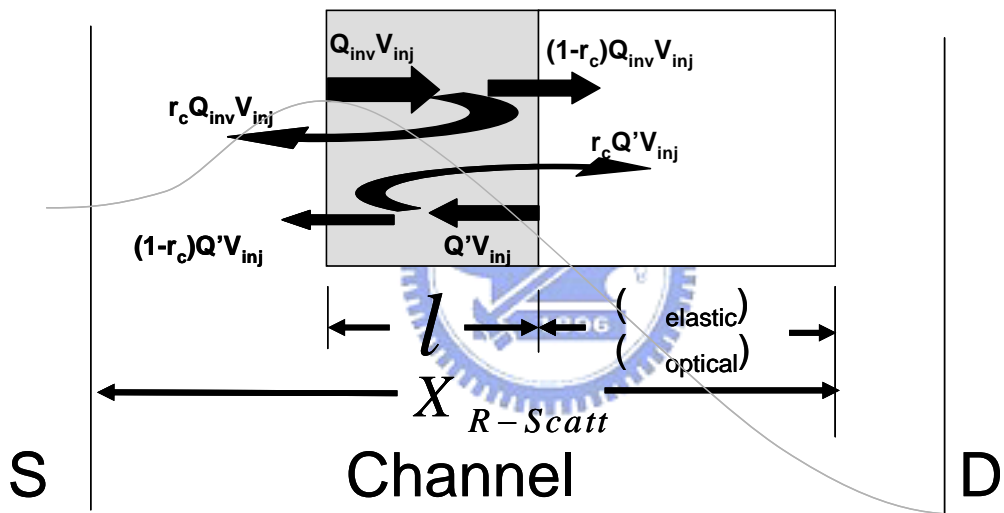


Fig. 2-7 Schematic flux profile in the  $k_B T$  layer when the factor  $Q'$  is considered.

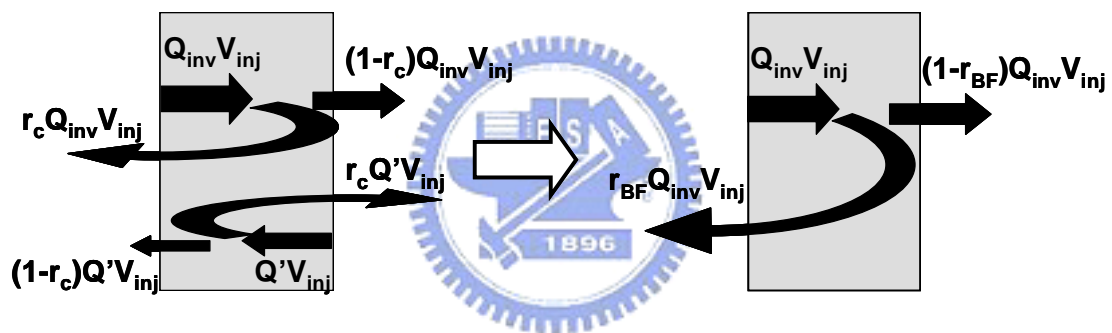


Fig. 2-8 In order to analyze, we must transform the flux profile to adapt our model.

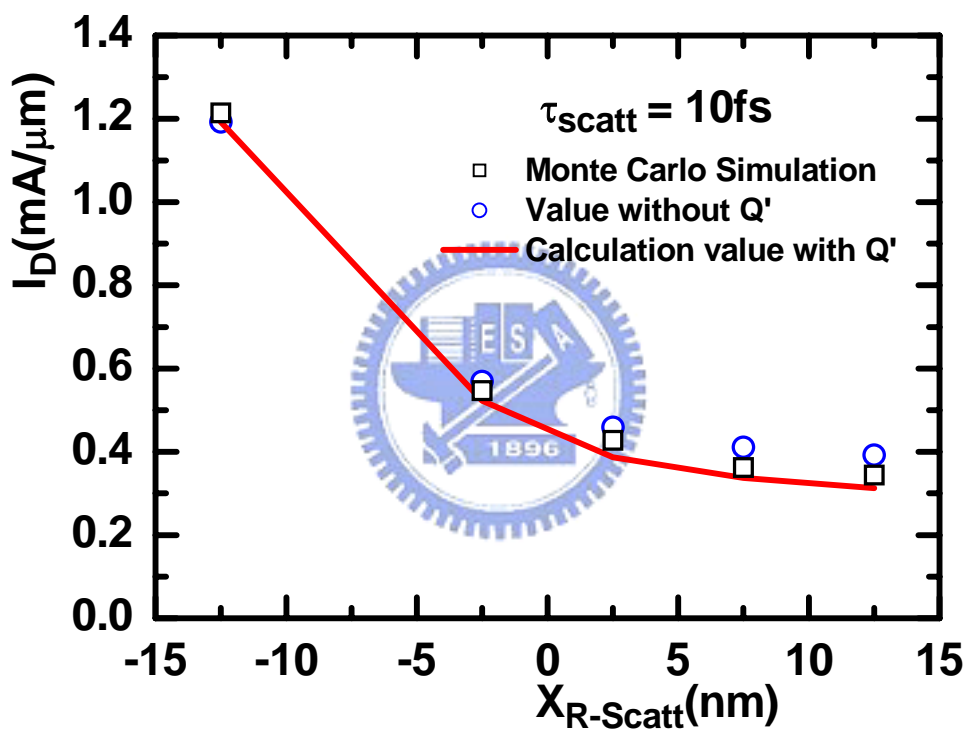


Fig. 2-9 Comparison of calculated drain current versus  $X_{R\text{-Scatt}}$  with that from Monte Carlo particle simulation.



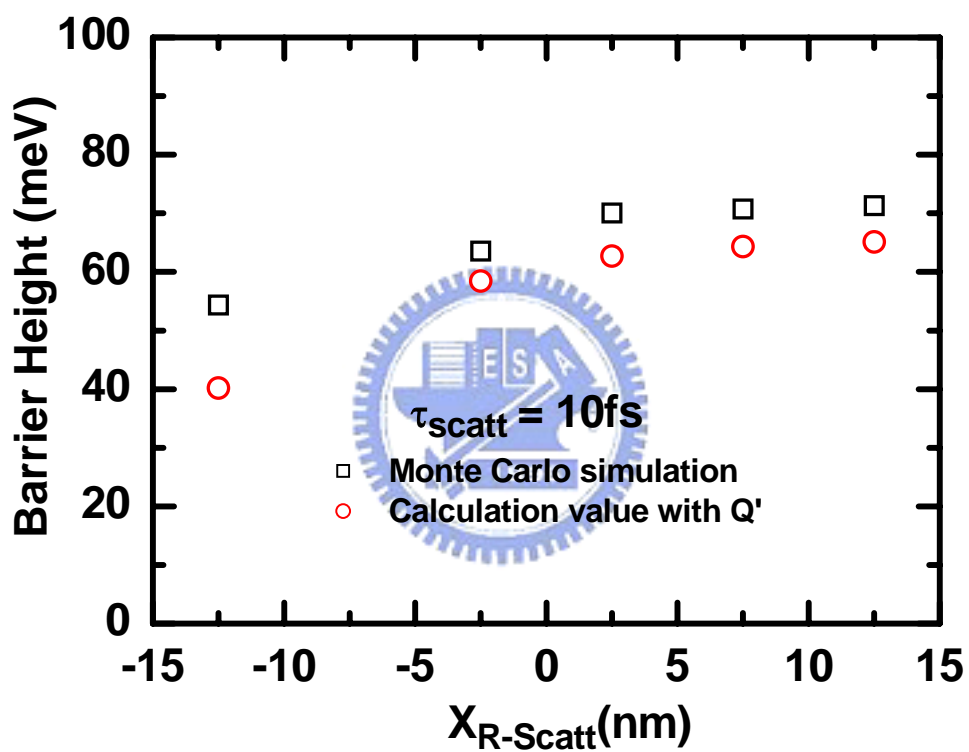


Fig. 2-10 Comparison of calculated barrier height versus  $X_{R-Scatt}$  with that from Monte Carlo particle simulation.

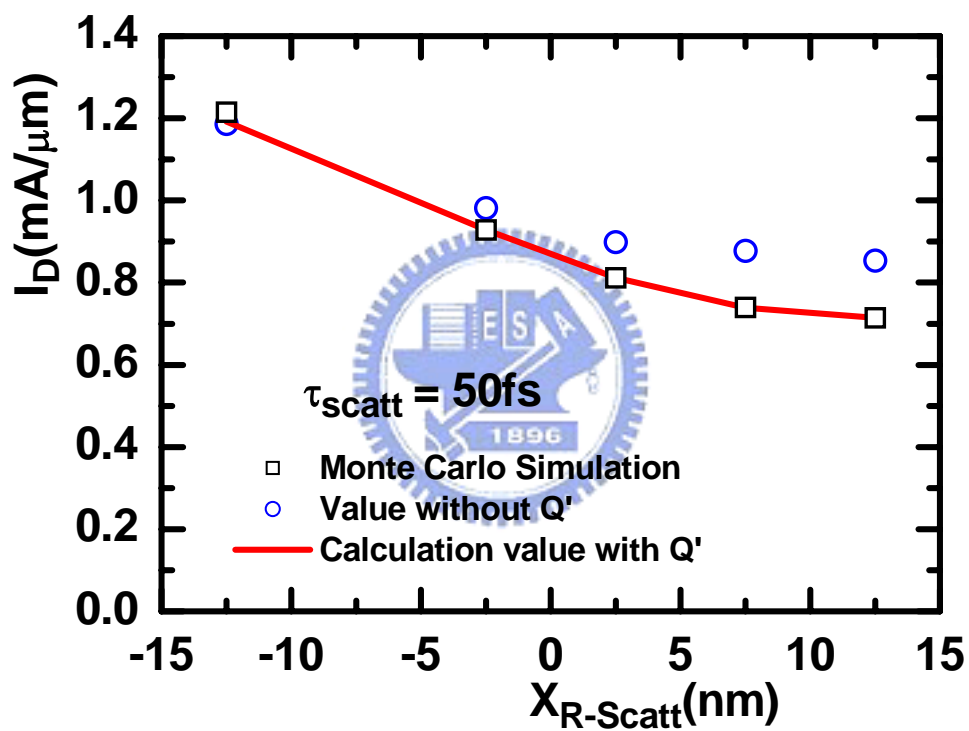


Fig. 2-11 Comparison of calculated drain current versus  $X_{R\text{-Scatt}}$  with that from Monte Carlo particle simulation.

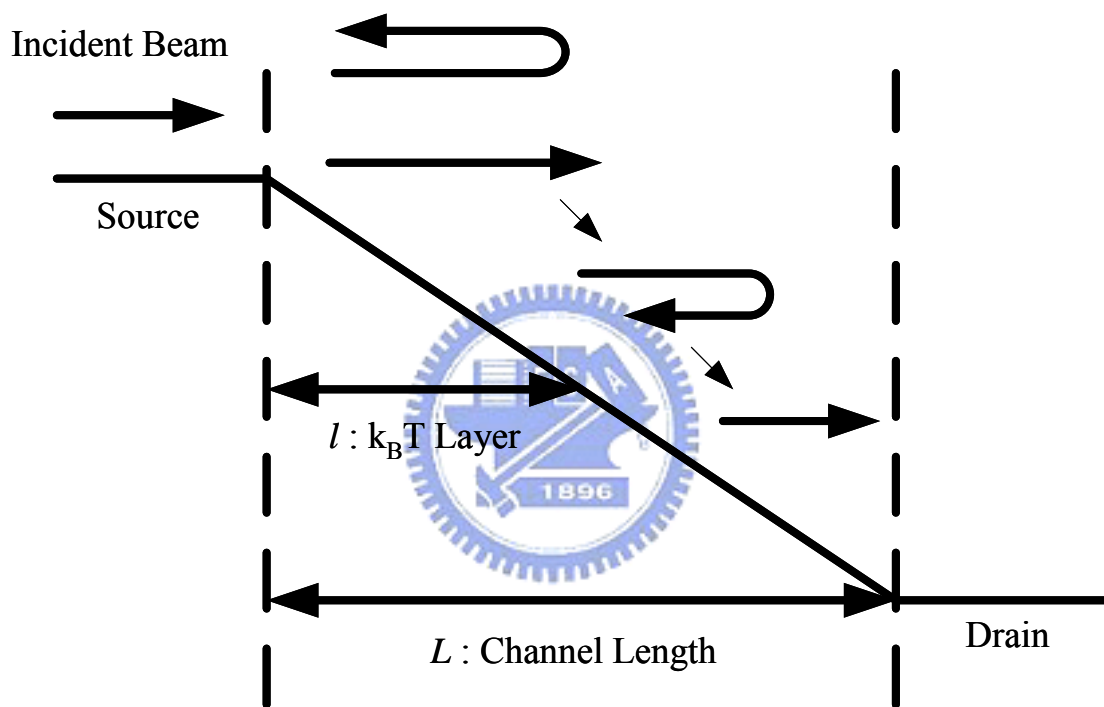


Fig. 3-1 Schematic structure of the simulation in the model “channel”.

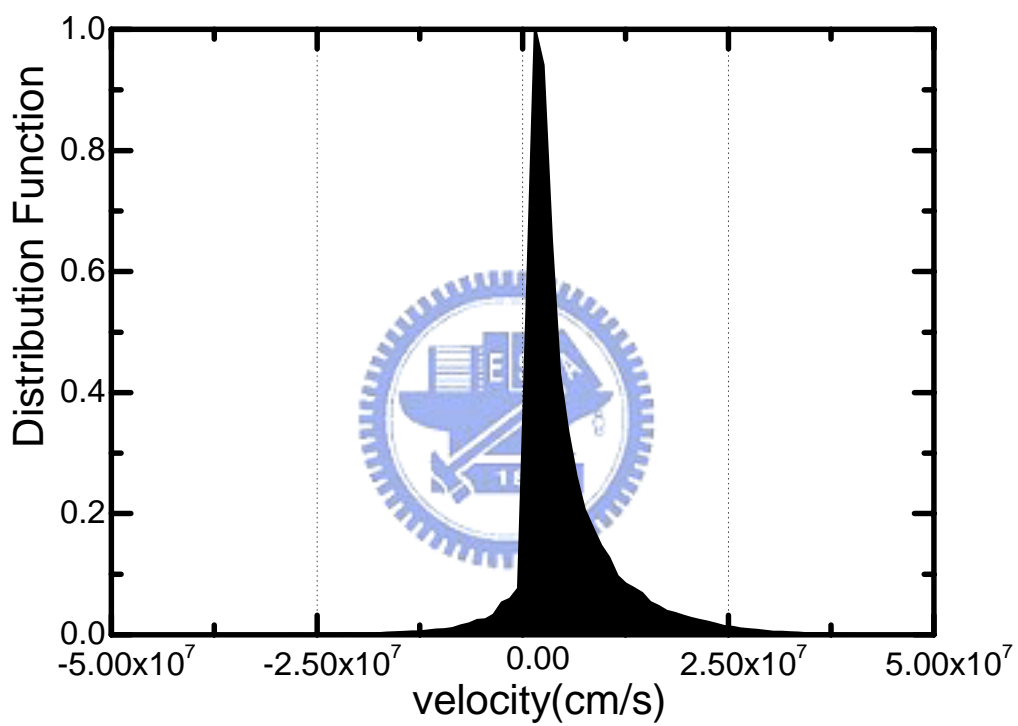


Fig. 3-2 An example case of the schematic velocity distribution. The backscattering coefficient  $r_C$  is just equal to the area ratio of negative to positive

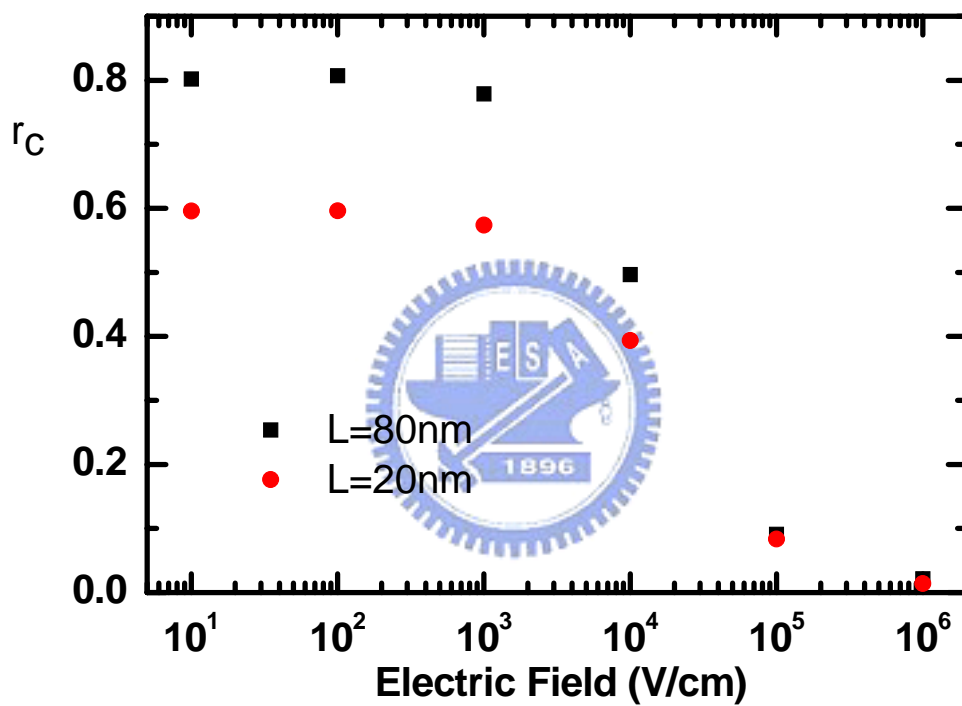


Fig. 3-3 The simulated backscattering coefficient of Monte Carlo evaluation under electric field from 10 V/cm to  $10^6$  V/cm for  $L = 80$  nm and  $L = 20$  nm.

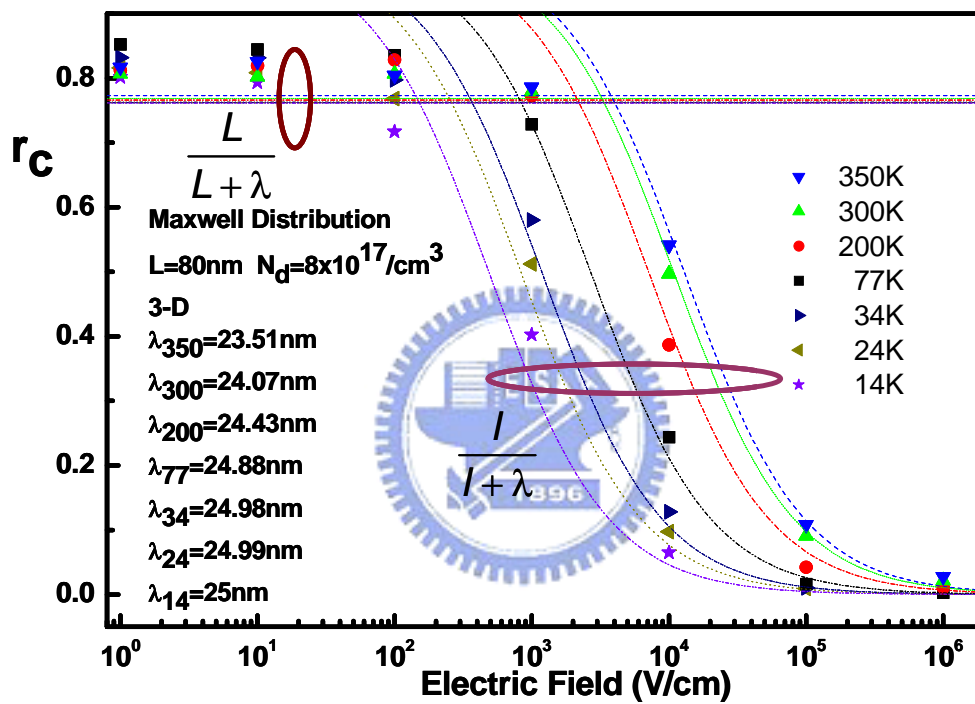


Fig. 3-4 The mean-free-path  $\lambda$  extracted from the  $r_C$ -E relation.

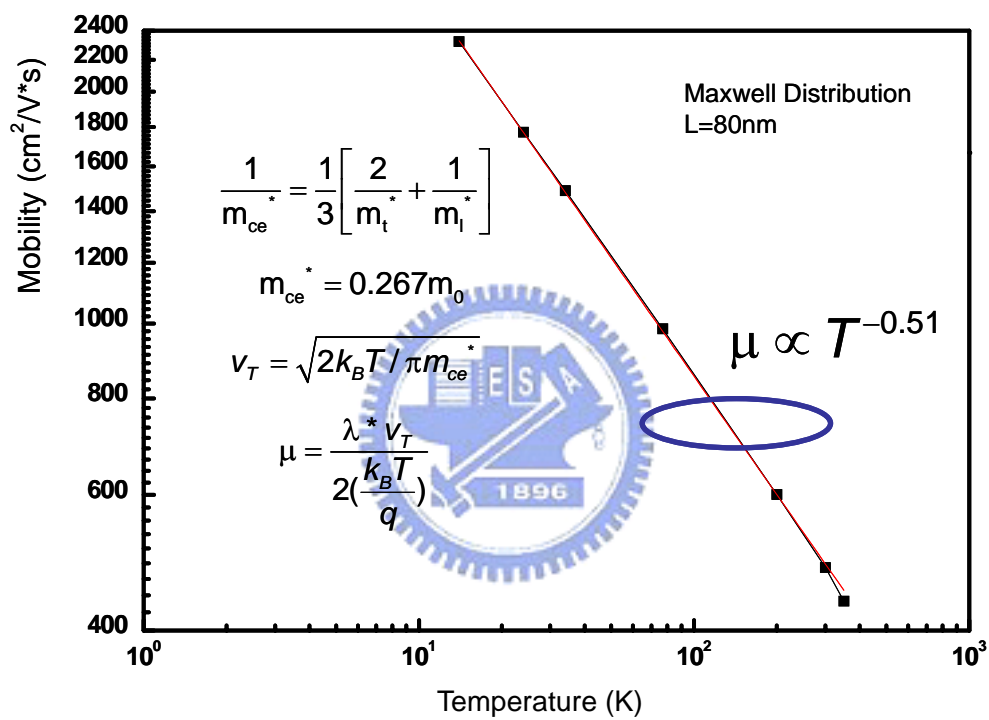
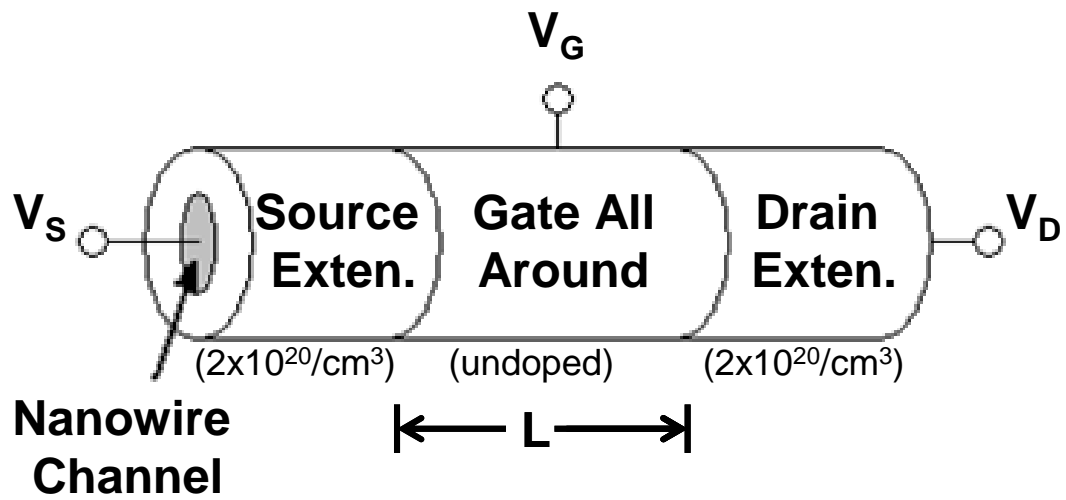


Fig. 3-5 The low-field mobility of electrons

(a)



(b)

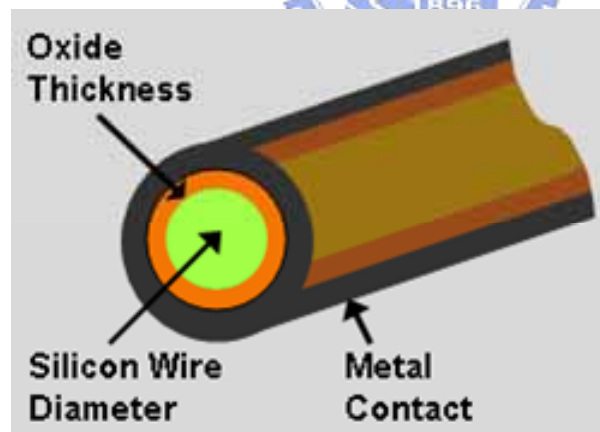


Fig. 4-1 (a) A schematic diagram of the simulated nanowire FETs.  
(b) Schematic cross section of the Si nanowire under study.



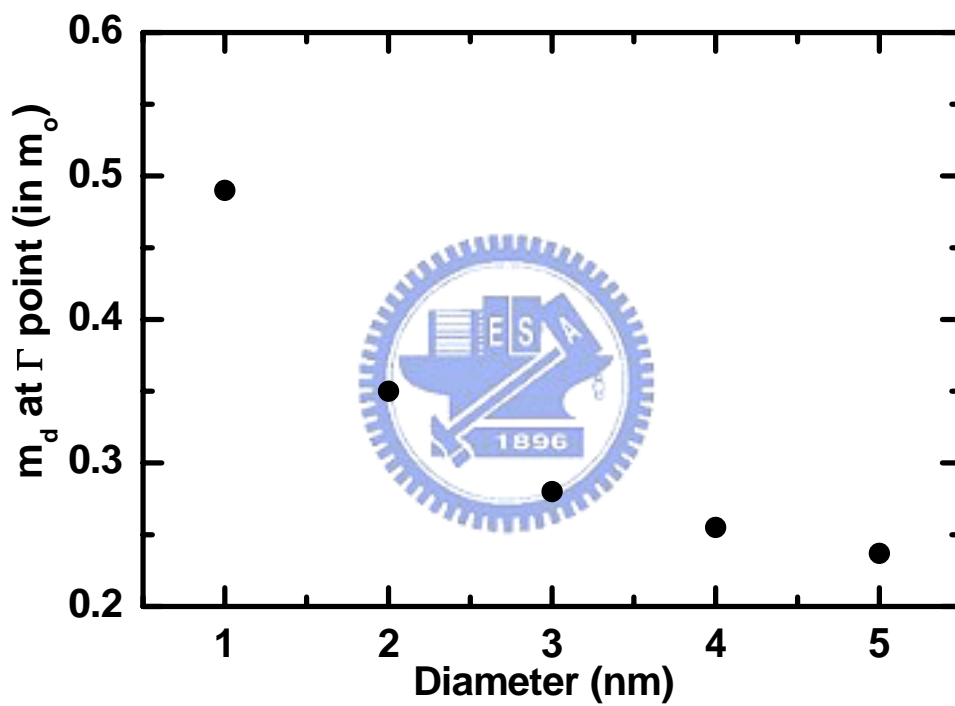
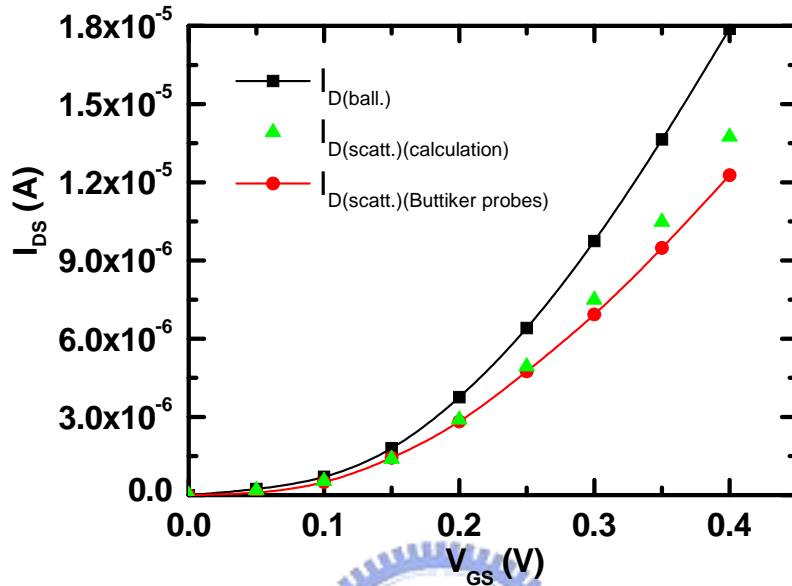


Fig. 4-2 The density-of-states effective mass at  $\Gamma$  point in the wire conduction band versus wire diameter  $D$  for a  $[100]$  oriented Si nanowire.

(a)



(b)

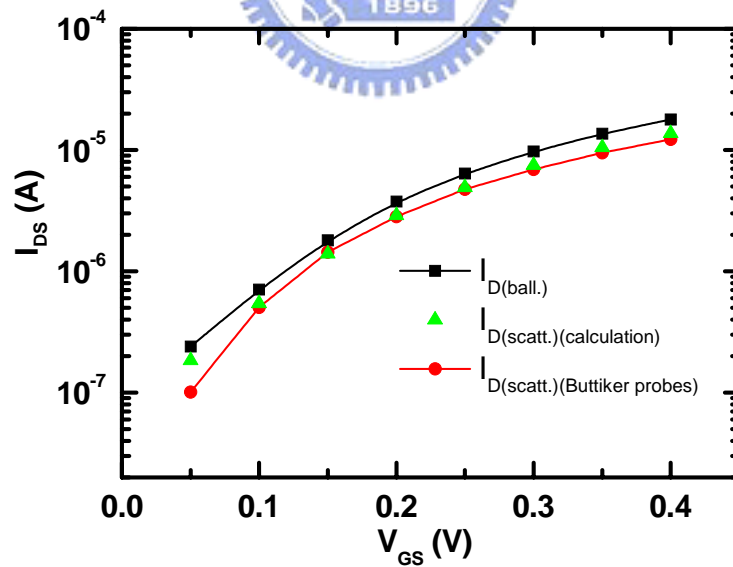


Fig. 4-3 Comparison of calculated drain current by (a) linear and (b) logarithmic scale versus  $V_{GS}$  with that from Buttiker probes model. Here we assumed that  $r_C$  is consistent in a whole range of  $V_{GS}$ .