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圓柱形洩漏波天線與寬頻 平面式洩漏波天線

Leaky-Wave Antennas on Cylinder Substrates and Broadband Planar Leaky-Wave Antennas

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本論文研究兩種形式的洩漏波天線:圓柱形介質上的洩漏波天線與平面介質 上的洩漏波天線。在理論上採用全波分析法-頻域法(Spectral domain approach) 來研究這兩種構造中洩漏波的傳播特性。

首先文中第一部分提出圓柱形微帶洩漏波天線。從數值計算得到的傳播常數 可得知圓柱形微帶洩漏波天線與平面式微帶洩漏波天線有著相同的特性。利用孔 徑耦合饋入結構,我們成功的激發了圓柱形微帶線的第一高階洩漏模,並實作出 高增益與寬頻的洩漏波天線。

同時本文也探討另外兩種圓柱形結構:挖槽同軸電纜與圓柱形共平面波導。 由理論計算得到不同電路尺寸參數下對此類圓柱形洩漏波天線傳播特性的影響, 進一步決定操作頻率。接著也設計了兩種對應結構的天線並加以量測。

本文第二部份則是主要著重在平面式洩漏波天線的設計上。我們研究槽線第一高階洩漏模與接地介質板的表面波之間的關係。在電路製作上用微帶線至共平

面波導的轉換電路,來激發槽線的第一高階洩漏模,設計出一支非常寬頻的天線。

最後本文提出一種新穎的倒T形洩漏波天線。它與單導體洩漏波天線有著相 同的特性,例如超寬頻與固定的主波束角度。和單導體洩漏波天線相比,倒T形 天線不需要寬頻的反相器,而且天線寬度也只有原來的一半,所以倒T形天線在 實作上具有更大的方便性。



# Leaky-Wave Antennas on Cylinder Substrates and Broadband Planar Leaky-Wave Antennas

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This thesis proposes two types of leaky-wave antennas. One type is on a cylindrical substrates and the other type is on a planar substrate. The well-known full-wave method, spectral domain approach, is applied to investigate the propagation characteristics of leaky modes on both configurations.

First, a cylindrical microstrip leaky-wave antenna is analyzed and designed. From the numerical results of computed propagation constants, it has the same characteristics as those of the planar ones. With the similar aperture-couple feeding structures used in planar microstrip leaky-wave antennas, the first higher order leaky mode is successfully excited. In addition, a high gain and wideband leaky-wave antenna is implemented.

Moreover, the first higher leaky modes on two cylindrical structures, slotted coaxial lines and cylindrical coplanar waveguides, are also studied. The effects of different parameters are shown and can be used to decide the operating frequency band of leaky-wave antennas. Two design examples are presented to show the performance of these types of leaky-wave antennas.

Second, the relationship between the first higher order leaky mode of a slotline and surface wave mode on a grounded dielectric slab is presented. A slotline leaky-wave antenna fed by a wideband microstrip-to-CPW transition is demonstrated.

Finally, an inverted-T leaky-wave antenna is introduced. It has the same properties as the single-conductor strip leaky-wave antennas, such as wide bandwidth and fixed mainbeams. Compared to the single-conductor strip antennas, the broadband phase inverter is not needed and the antenna width is halved. Therefore, the realization of inverted-T antennas is easier than that of single-conductor strip ones.



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## **Chapter 1**

#### Introduction

#### **1.1 Motivation**

The leakage phenomenon on planar printed transmission lines has been researched over the years [1]-[6]. The leaky-wave antennas of planar structures are mainly used as high-efficiency and broadband antennas []-[]. There are numerous issues about leaky-wave antennas are investigated, such as integrated leaky-wave antennas [1], feeding structures [2][3], full-wave analysis of leaky modes [4], mode couplings [5], and wideband antennas [6].

On the other hand, cylindrical structures also have been researched and developed for decades [7]-[15]. Several topics of cylindrical structures are studied, like array design [7], full-wave analysis [8]-[14], and different types of waves [15]. Although bound mode propagations on cylindrical transmission lines have been fully understood in these papers [7]-[15], leaky modes on cylindrical substrates have yet to be studied thoroughly in the literatures [16]-[17]. Such antennas may find applications in wireless communications or military systems that require antennas in cylindrical shapes.

Besides, planar leaky-wave antennas are usually wideband with a 20% bandwidth. However, in modern wireless systems like Ultra-wideband (UWB) systems, a 110% bandwidth (3.1-10.6 GHz) is needed. So how to increase the bandwidth of high-gain leaky-wave antennas is an important issue in antenna design. For example, a long tapered multi-section microstrip leaky-wave antenna [6] has successfully obtained a 157% bandwidth. In this thesis, other types of broadband leaky-wave antennas will be discussed.

#### **1.2 Organization of This Thesis**

Leaky modes on two types of substrates are investigated: cylindrical and planar types. The full-wave method, spectral domain approach (SDA) [18], is used to analyze the propagation characteristics of leaky modes on these structures. Odd-symmetry and even-symmetry current and electric-field basis functions combined with the edge conditions [18] are chosen in the longitudinal and transverse directions according to the symmetry represented by a virtual perfect electric conductor (PEC) or a perfect magnetic conductor (PMC). Leaky modes on both cylindrical and planar structures have wide radiation regions and can be implemented as high-gain antennas.

In Chapter 2, cylindrical microstrip leaky-wave antennas are thoroughly studied. Propagation constants of different structure parameters are calculated to decide the operating frequency band of cylindrical microstrip leaky-wave antennas. From the numerical results and measurement results, the cylindrical leaky-wave antennas have the similar propagation characteristics and antenna performance like those of planar microstrip leaky-wave antennas [1]-[6].

Most papers discussed the bound mode of coaxial lines [19]-[21] and cylindrical coplanar waveguides (CPW) [22], but few papers mentioned about leaky modes on such structures. In this thesis, the first higher order leaky modes on these two structures are studied in Chapter 3. For the first higher order leaky modes, the longitudinal currents of slotted coaxial lines are even-symmetric while the currents are odd-symmetric of CPWs. Two design examples are also presented to demonstrate the performance of slotted coaxial and CPW leaky-wave antennas.

Chapter 4 includes two broadband planar antennas: slotline leaky-wave antennas and inverted-T leaky-wave antennas. Slotlines and single-conductor strips are complementary structures indeed. From the calculated propagation constants, the first higher order leaky mode on slotlines can be viewed as guided surface wave modes of grounded dielectric slabs. With the broadband microstrip-to-CPW transition [24], a wideband slotline leaky-wave antenna is designed. The slotline leaky-wave antennas are dual-beam antennas with the frequency-scanning feature.

In addition, many leaky-wave antennas require complicated feeding structures and large circuit size. Due to the current symmetry of the first higher order leaky modes, we only need a half of an antenna for space-wave leakage. Half-width leaky-wave antennas have several advantages such as suppression of bound mode [25], smaller size, and simpler feeding structure than full-width leaky-wave antennas. In the section 4.2, we design a novel broadband inverted-T leaky-wave antenna, which is derived from the single-conductor strip leaky-wave antenna.



## Chapter 2

#### **Cylindrical Microstrip Leaky-Wave Antennas**

This Chapter presents the first higher order leaky mode of cylindrical microstrip lines. The full-wave method is applied to calculate propagation constants under different structural parameters. From the numerical results, we observe the phenomena caused by various parameters and can select the suitable operating frequency band of the antenna. With the aperture-couple feeding structure, a high-gain and wideband cylindrical microstrip leaky-wave antenna is designed and measured. In conclusion, the first higher order leaky modes can exist on cylindrical microstrip lines as those leaky modes exist on planar microstrip lines.

#### 2.1 Spectral Domain Analysis

In this thesis, we use the spectral domain approach (SDA) to analyze the first higher leaky mode of cylindrical microstrip leaky-wave antennas. Fig. 2.1 shows the cross section of the cylindrical microstrip line. Region I is the cylindrical substrate with a permittivity of  $\varepsilon_1 = \varepsilon_r \varepsilon_0$  and a thickness of *h*. Region II is free space. The strip with a circumferential width *w* is placed on top of the substrate. The permeabilities of all materials are  $\mu_0$ . The thickness of the top strip and the ground conductor are assumed to be zeros. All the conductors and substrates are assumed to be lossless for simplification. First we expand the *z*-components of fields ( $E_z$ ,  $H_z$ ) in cylindrical coordinates by inverse Fourier series (suppressing the time-harmonic expression  $e^{j\omega t}$  and *z*-dependence  $e^{-jk_z z}$ ) [12] as:

$$E_{z1}(\rho,\phi) = \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \left[ A_{1n} H_n^{(1)}(k_{1\rho}\rho) + B_{1n} J_n(k_{1\rho}\rho) \right]$$
(2.1)

$$H_{z1}(\rho,\phi) = \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \bigg[ C_{1n} H_n^{(1)} \big( k_{1\rho} \rho \big) + D_{1n} J_n \big( k_{1\rho} \rho \big) \bigg]$$
(2.2)

$$E_{z2}(\rho,\phi) = \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \left[ A_{2n} H_n^{(2)}(k_{2\rho}\rho) \right]$$
(2.3)

$$H_{z2}(\rho,\phi) = \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \bigg[ C_{2n} H_n^{(2)} \big( k_{2\rho} \rho \big) \bigg]$$
(2.4)

where  $k_z^2 = k_i^2 - k_{i\rho}^2$ ,  $k_i = \omega \sqrt{\mu_0 \varepsilon_i}$ , i = 1, 2.

and define the z-direction propagation constant  $k_z$  such that  $-jk_z = -\alpha - j\beta$ , where  $\alpha$  and  $\beta$  are the attenuation constant and the phase constant, respectively.  $k_{i\rho}$  is the  $\rho$ -directed propagation constant of each region. The other components of fields  $(E_{\rho}, H_{\rho}, E_{\phi}, H_{\phi})$  can be expressed in terms of  $(E_z, H_z)$  from Maxwell's equations in cylindrical coordinates easily.

For the first higher order leaky mode with an odd symmetry, a virtual PEC boundary can be placed at the bottom ( $\phi = \pi$ ) in Fig. 2.2. The longitudinal fields  $(E_z, H_z)$  between the PEC sidewalls are considered as the standing waves. The creeping waves and surface waves [15] are ignored in this analysis.

The cross-section on the  $\rho\phi$ -plane can be transformed into that of the planar microstrip line with the PEC sidewalls, like shielded microstrip lines. This direct mapping is similar to that used in [26].



Fig. 2.1 The cross-sectional view of the cylindrical microstrip line.



Fig. 2.2 The PEC boundary representation and transformation.

The variables *n* of the inverse Fourier series (2.1)-(2.4) are integers on the real axis (*x*-axis) of the *n*-plane. In solving planar microstrip leaky-wave structures [27]-[30], the variables used in integrations over the real axis are continuous; however, variables are discrete in solving cylindrical structures. Since the surface-wave leakage phenomenon in planar transmission lines will not occur in cylindrical substrates, no consideration of the surface wave leakage is needed in this analysis. The branch points in solving planar microstrip leaky-wave structures are not needed in solving cylindrical structures because the variables *n* are irrelevant to  $k_{iq}$ .

The sign of  $\rho$ -direction wavenumber in free space  $k_{2\rho} = \sqrt{k_2^2 - k_z^2}$  in the series (2.1)-(2.4) should be chosen properly to satisfy the exponential growth condition of the space-wave leakage in the positive  $\rho$ -direction, and this square root is at the improper Riemann sheet. The similar choice of branch is defined in [31].

From (2.1)-(2.4) and boundary conditions between Region I and II with some algebraic operations, the unknowns  $(A_{1n}, B_{1n}, C_{1n}, D_{1n}, A_{2n}, C_{2n})$  are solved and we obtain the relationships between Fourier transforms of currents and electric fields,  $\tilde{J}$  and  $\tilde{E}$ :

$$\tilde{E}_{z2}(n) = \tilde{G}_{zz}(n)\tilde{J}_{z}(n) + \tilde{G}_{z\phi}(n)\tilde{J}_{\phi}(n)$$
(2.5)

$$\tilde{E}_{\phi 2}(n) = \tilde{G}_{\phi z}(n)\tilde{J}_{z}(n) + \tilde{G}_{\phi \phi}(n)\tilde{J}_{\phi}(n)$$
(2.6)

where  $(\tilde{J}_z, \tilde{J}_{\phi})$  are the Fourier transforms of the current density  $J_z(\phi), J_{\phi}(\phi)$  on the strip. The current densities  $J_z(\phi), J_{\phi}(\phi)$  are expanded in terms of basis functions  $J_{zp}(\phi), J_{\phi q}(\phi)$  as:

$$J_{z}(\phi) = \sum_{p=1}^{p_{\text{max}}} u_{p} J_{zp}(\phi), \ J_{\phi}(\phi) = \sum_{q=1}^{q_{\text{max}}} v_{q} J_{\phi q}(\phi),$$
(2.7)

with unknown coefficients  $(u_p, v_q)$ . The basis functions used in the computations are:

$$J_{zp} = \frac{\sin\{(2p-1)\pi\phi/2\phi_w\}}{\sqrt{1-(\phi/\phi_w)^2}} \qquad J_{\phi q} = \frac{\cos\{(2q-1)\pi\phi/2\phi_w\}}{\sqrt{1-(\phi/\phi_w)^2}},$$
(2.8)

considering that z-component and  $\phi$ -component currents are odd and even and functions of  $\phi$ , respectively. The numbers of basis functions  $J_{zp}$  and  $J_{\phi q}$ , are  $p_{\max}$ and  $q_{\max}$ , respectively. Taking the inverse Fourier transform of (2.5)-(2.6), we can obtain the tangential *E* field in Region II. Then we apply the remaining boundary conditions that the tangential *E* fields vanish on the strip  $(-\phi_w \le \phi \le \phi_w)$ :

$$E_{z2}(\rho,\phi) = \sum_{p=1}^{p_{\text{max}}} u_p \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \tilde{G}_{zz}(n) \tilde{J}_{zp}(n) + \sum_{q=1}^{q_{\text{max}}} v_q \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \tilde{G}_{z\phi}(n) \tilde{J}_{\phi q}(n) = 0$$
(2.9)

$$E_{\phi 2}(\rho,\phi) = \sum_{p=1}^{p_{\text{max}}} u_p \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \tilde{G}_{\phi z}(n) \tilde{J}_{zp}(n) + \sum_{q=1}^{q_{\text{max}}} v_q \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} \tilde{G}_{\phi\phi}(n) \tilde{J}_{\phi q}(n) = 0 \quad (2.10)$$

For numerical computation, we take the inner products of the above two equations with the other sets of basis functions  $J_{zd}(\phi)$  and  $J_{\phi g}(\phi)$  as testing functions (Galerkin's method) over the top strip. The numbers of testing functions  $J_{zp}$  and  $J_{\phi q}$ , are  $p_{max}$  and  $q_{max}$ , respectively. After the inner product operations, we can obtain a matrix form:

$$\begin{bmatrix} \mathbf{Q}^{zz} & \mathbf{Q}^{z\phi} \\ \mathbf{Q}^{\phi z} & \mathbf{Q}^{\phi\phi} \end{bmatrix} \begin{bmatrix} \mathbf{u} \\ \mathbf{v} \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}$$
(2.11)

with  $N = p_{\max} + q_{\max}$ , where **u** and **v** are the column vectors of the unknown coefficients. The nontrivial solution of the complex propagation constant  $k_z$  exists only if

$$\det \begin{bmatrix} \mathbf{Q}^{zz} & \mathbf{Q}^{z\phi} \\ \mathbf{Q}^{\phi z} & \mathbf{Q}^{\phi\phi} \end{bmatrix} = 0.$$
 (2.12)

#### **2.2 Numerical Results**

#### 2.2.1 Convergence Test

Each element of the Q-matrix is an infinite series, e.g.

$$(\tilde{J}_{z}\tilde{G}_{zz}\tilde{J}_{zz}) = \sum_{n=-\infty}^{\infty} f_{zz}(n).$$
(2.13)

Convergence of the infinite series is investigated to clarify the truncation error. We show the relative deviation (from n=120 case) of real and imaginary parts in Fig. 2.3 to check the convergence of the series. Smaller outer radius causes the series to converge a little bit faster. Good convergences are obtained with the number of the summation terms n > 100 and with more than six basis functions used. The relative deviation of propagation constants for the number of basis functions is displayed in Fig. 2.4.





Fig. 2.3 Convergence of series  $\tilde{J}_z \tilde{G}_{zz} \tilde{J}_{zz}$ . w = 10 mm, h = 0.508 mm,  $\varepsilon_r = 2.2$ , and b = 10 and 20 mm at 9.5GHz



Fig. 2.4 Convergence of normalized phase constant and normalized attenuation constant of cylindrical microstrip leaky-wave antenna.  $w = 10 \text{ mm}, h = 0.508 \text{ mm}, \varepsilon_r = 2.2, b = 10 \text{ and } 20 \text{ mm}$  at 9.5GHz.

# 2.2.2 Comparison of the Results from the SDA to the Result from the Leaky-Mode Scattering Parameter Extraction

To check the validity of the numerical results, we introduce the leaky-mode scattering parameter extraction technique [32] to extract the propagation constants from scattering parameters.

We choose two sections of leaky-wave microstrip lines, with the same design except their longitudinal lengths. Then we place two identical leaky-mode excitation circuits at the both ports of each of the two leaky-wave microstrip lines. After we obtain the two sets of scattering parameters of these leaky-wave microstrip lines from the full-wave simulation software, we can extract the propagation constants with some simple calculations based on the transmission line theory [33]. Numerical results obtained by this method are checked with those obtained by SDA. They show a good agreement. An example is presented in Fig. 2.5.



Fig. 2.5 Comparisons of propagation constants of the first higher order mode  $(w = 10 \text{ mm}, h = 0.508 \text{ mm}, \varepsilon_r = 2.2, b = 30 \text{ mm}).$ 

#### 2.2.3 Effect of Different Outer Radii

First we use angular width R of the line width w to the outer radius b of the substrate,

$$R = w/b. \tag{2.14}$$

This definition represents the curvature of the cylindrical structure. If the radius becomes larger with a fixed line width, the angular width *R* decreases, which indicates that the structure is flatter. For example, the substrate thickness *h* is 0.508 mm and the antenna width is 10 mm. We choose three different outer radii, b = 10, 20, and 30 mm with three angular widths: 1, 0.5, and 1/3. It is reasonable that when the radius increases, the propagation constants gradually approach those of the planar microstrip leaky-wave modes.

Fig. 2.6 shows the computed normalized phase constant  $\beta/k_0$  and Fig. 2.7 shows the computed normalized attenuation constants  $\alpha/k_0$ , where  $k_z = \beta - j\alpha$ . We find that as the outer radius *b* or the angular width *R* becomes larger, the radiation region  $(\alpha \le \beta \le k_0)$  moves to a lower frequency band, with the point  $\alpha = \beta = 0.19$ , which can be used as the lower frequency limit of effective space-wave leakage [3]. The lower frequency limit occur at about 9.65, 9.45, and 9.25GHz, for b= 10, 20, and 30 mm, respectively.



Fig. 2.6 Normalized phase constants of the first higher order mode (w = 10 mm, h = 0.508 mm,  $\varepsilon_r = 2.2$ , b = 10, 20, 30 mm and planar ).





Fig. 2.7 Normalized attenuation constants of the first higher order mode (w = 10 mm, h = 0.508 mm,  $\varepsilon_r = 2.2$ , b = 10, 20, 30 mm and planar ).

#### 2.2.4 Effect of Different Substrate Thicknesses

Fig. 2.8 plots the computed normalized attenuation constants  $\alpha / k_0$  and the normalized phase constants  $\beta / k_0$  for two different substrate thicknesses h = 0.508 and 1.570 mm, with the same outer radius b = 10 mm. The antenna width w is 10 mm. When the substrate is thicker, the radiation region moves to a lower frequency band. In planar microstrip leaky-wave antennas, similar effects can be observed [5]. The attenuation constant  $\alpha / k_0$  also becomes smaller, which means less attenuation. The lower frequency limit of effective space-wave leakage ( $\alpha = \beta$ ) is 8.75 and 9.65GHz for h = 1.570 and 0.508 mm, respectively.



Fig. 2.8 Propagation constants of the first higher order mode (w = 10 mm, h = 0.508 and 1.570 mm,  $\varepsilon_r = 2.2$ , b = 10 mm).

#### 2.2.5 Effect of Different Line Widths

Fig. 2.9 shows the effects of the line width on the propagation constants of the cylindrical microstrip leaky-wave antennas. From Fig. 2.9, a smaller microstrip line width results in a higher frequency band for space-wave leakage. In planar microstrip leaky-wave antennas, similar effects can be observed [1]. The lower frequency limits of effective space-wave leakage appear at about 8.55, 9.30, and 10.15GHz, corresponding to widths w = 11, 10, and 9 mm, with almost the same values  $\alpha = \beta = 0.2$ . As the line width reduces, the lower frequency limit of the effective space-wave leakage increases.



Fig. 2.9. Propagation constants of the first higher order mode (w = 11, 10, and 9mm h = 0.508 mm c = -2.2 h = 30 mm)

#### 2.3 Design Example and Measurement

Since the first higher leaky mode of cylindrical microstrip lines has a wide radiation region, a broadband cylindrical type leaky-wave antenna can be implemented. We design aperture-coupling feeding structures with enough bandwidth to excite the first higher leaky mode and deliver power into antennas. The antenna system configuration in Fig. 2.10 consists of two layers of substrates. The upper substrate is utilized for the antenna, and lower substrate is applied for the feeding microstrip line, respectively. Both substrates share the same ground with the coupling slot. The top view of the antenna system in Fig. 2.11 shows the positions of the coupling slot and the feeding microstrip line.

Both of these substrates have a dielectric constant of  $\varepsilon_r = 2.2$  and a thickness of h = 0.508 mm. On the other hand, substrates thicker than 0.508 mm are too firm to bend into the cylindrical shape. The energy goes through the coupling slot to the leaky-wave microstrip and excites the first higher leaky mode [4].



Fig. 2.10 The feeding and the antenna structure.

The dimensions used are the following: the feeding line width  $w_f = 1.88$  mm, the distance from the feed line end to the antenna center  $l_m = 3.9$  mm, the slot width  $w_s = 0.5$  mm, the distance from the slot end toward the antenna to the antenna starting point  $l_c = 3$  mm, the slot length  $(l_c + l_o)$  with  $l_o = 9$  mm, the antenna width w = 10 mm, and the antenna length L = 150 mm. All of these structural parameters are selected to obtain a good impedance matching with enough bandwidth.

Two sets of antennas with two different outer radii b = 20 and 30 mm are designed, which are specified as Antenna I and Antenna II, respectively. From the measured scattering parameters shown in Fig. 2.12, the bandwidth (with S<sub>11</sub> < -10dB) of Antenna I is 9.59~12.71 GHz; and those for Antenna II is 9.77~12.89GHz. They both have 3.12GHz bandwidth. It is noted that this kind of antenna has the potential to be a good wideband antenna.

From the results in Fig. 2.12, we can find that a larger radius (b=30 mm) causes a lower operating frequency. There are two dips near 11GHz and 12.5GHz for each cases (b=30 for the solid line and b=20 mm for the dashed line). The dips are mainly due to the original resonant modes of the feeding microsotrip lines, the feeding substrates, and the ground plane.



Fig. 2.11 The top view of feeding and the antenna structure.



Fig. 2.12 Measured return loss of the cylindrical microstrip antenna with two angular widths (w = 10 mm, h = 0.508 mm,  $\epsilon_r$  = 2.2, b = 20 and 30 mm).

Copolarization radiation patterns of Antenna I and Antenna II in *xz*-plane are plotted in Fig. 2.13 and Fig. 2.14. Antenna I have the peak gains 11.79, 14.86, and 11.76 dBi for 10, 11, and 12GHz, respectively, in Fig. 2.13. The corresponding mainbeam directions starting from the z-direction (endfire direction) are  $67^{\circ}$ ,  $46^{\circ}$ , and  $33^{\circ}$ . This is the well-known frequency-scanning feature of leaky-wave antennas.

With the same three frequencies selected above, Antenna II has 12.76, 14.82, and 11.96 dBi peak gains, as shown in Fig. 2.14. Compared to the Antenna I, larger outer radius of the antenna causes smaller mainbeam directions from the endfire, due to its larger phase constants. This phenomenon can be deduced from the data in Fig. 2.6.



Fig. 2.13 Measured copolarization radiation patterns of the cylindrical microstrip antenna with an outer radius b = 20 mm.



Fig. 2.14 Measured copolarization radiation patterns of the cylindrical microstrip antenna with an outer radius b = 30 mm.



#### 2.4 Summary

This Chapter proposes a cylindrical microstrip antenna structure with a full-wave analysis and its implementation. We investigate how the angular widths and the substrate thicknesses affect the propagation constants and radiation patterns of this cylindrical structure. Measured scattering parameters and radiation patterns of these realized antennas circuits are presented. Finally, we conclude that cylindrical leaky-wave antennas have the high-gain and wideband features, similar to those of the planar leaky-wave antennas.



#### Chapter 3

#### Leaky Modes on Cylindrical Substrates

In this Chapter, the first higher order leaky modes on the other two types of cylindrical structures are demonstrated: slotted coaxial lines and cylindrical coplanar waveguides. They have different field symmetries which are represented with virtual PMC or PEC about the center. With the same method used in Chapter 2, spectral domain approach, propagation characteristics of the first higher order leaky modes on both structures are investigated. From the measurement results of two design examples, these two types of antennas can also be high-gain and wideband. Briefly, we have shown that such two structures can support space-wave leaky modes.

#### 3.1 Leaky Modes of Slotted Coaxial Lines

#### 3.1.1 Spectral Domain Analysis of Slotted Coaxial Lines

This section discusses the propagation characteristics of slotted coaxial lines. Fig. 3.1(a) shows the cross section of slotted coaxial lines. The slot with width *w* is on top of the substrate. The inner ground conductor and the outer conductor shell are located at circumferences of radii *a* and *b*, respectively. The permeabilities of all materials are  $\mu_0$ . The thickness of the outer shell and the ground conductor are assumed to be zero. In the analysis of the first high order leaky mode of slotted coaxial lines, we place a PMC boundary at the bottom ( $\phi = \pi$ ) in Fig. 3.1(b) to represent the appropriate field symmetry about the center.

The z-direction fields represented as inverse Fourier series are the same as in (2.1)-(2.4). Similarly, the time-harmonic expression  $e^{j\omega t}$  and z-dependence  $e^{-jk_z z}$  are assumed. The longitudinal (z-direction) electric field on the slot is

even-symmetric about  $\phi = 0$ , whereas the transverse electric field ( $\phi$ -direction) is odd-symmetric about  $\phi = 0$ . For slotted coaxial lines, the longitudinal electric field distributions are like the transverse current distributions of cylindrical microstrip lines, and the transverse electric field distributions are like the longitudinal current distributions of cylindrical microstrip lines. If the electric fields of the first higher leaky mode in slotted coaxial lines are equivalent to magnetic currents  $(M_z = E_\phi \times \hat{\rho}, M_\phi = E_z \times \hat{\rho})$ , these magnetic currents will be similar to electric currents of the first higher leaky mode in cylindrical microstrip lines.



Fig. 3.1 (a) The cross-sectional view of the slotted coaxial line. (b) The PMC boundary representation the slotted coaxial line.

We solve the coefficients by applying boundary conditions. Therefore we obtain Green's functions:

$$\tilde{J}_{z}(n) = \tilde{G}_{zz}(n)\tilde{E}_{z2} + \tilde{G}_{z\phi}(n)\tilde{E}_{\phi 2}(n)$$
(3.1)

$$\tilde{J}_{\phi}(n) = \tilde{G}_{\phi z}(n)\tilde{E}_{z2} + \tilde{G}_{\phi \phi}(n)\tilde{E}_{\phi 2}(n)$$
(3.2)

The *E*-fields and electric currents *J* are equivalent to magnetic currents and *H*-fields, respectively. Appropriate basis functions for  $(E_{z2}, E_{\phi 2})$  should be chosen. After the similar procedures in (2.9)-(2.11), a matrix *T* is obtained and can be rewritten in a product of two matrices:

$$\begin{bmatrix} \mathbf{T}'(k_z) \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} 0 \end{bmatrix} .$$
(3.3)

(u, v) are the unknown coefficients for the basis functions. Finally we solve for  $k_z$ 

from det[  $T'(k_z)$  ]=0.



#### **3.1.2 Numerical Results**

The effects of three parameters: the slot width w, the outer radius b, and the substrate thickness h, are investigated. The dielectric constant of the substrate  $\varepsilon_r$  is 2.2. In Fig. 3.2, the radius b is 100 mm, the thickness h is 10 mm, and the widths w are 10, 15 and 20 mm. As the slot width w increases, the curve of the propagation constant moves to a lower frequency region. Fig. 3.3 shows how the radius b affects the curves. The slot width w is 10 mm, the thickness h is 10 mm, and the outer radii b are 20, 40, and 80mm. The larger radius also changes the propagation constant to a lower frequency band.

Fig. 3.4 plots the curves for three different substrate thicknesses h, which are 6, 8, and 10mm. The slot width w is 10 mm and the outer radius b is 50 mm. The lower

bounds  $(\alpha = \beta)$  of the radiation regions  $(\alpha \le \beta \le k_0)$  occur at 9.675, 8.750, and 6.125GHz, corresponding to h = 6, 8, and 10 mm. It is notably that these frequencies are approximately proportional to the reciprocal of substrate thicknesses. We conclude that the outer radius and slot widths do not affect propagation constants very much, whereas the substrate thickness may dominate the operating frequency.



Fig. 3.2 The normalized propagation constants of different slot widths (b = 100 mm, h = 10 mm,  $\varepsilon_r = 2.2$ , and w = 10, 15 and 20 mm).



Fig. 3.3 The normalized propagation constants of different slot widths (b = 100 mm, h = 10 mm,  $\varepsilon_r = 2.2$ , and w = 10, 15 and 20 mm).



Fig. 3.4 The normalized propagation constants of different substrate thicknesses (b = 50 mm, h = 6, 8, and 10 mm,  $\varepsilon_r = 2.2$ , and w = 10 mm).

#### 3.1.3 Design Example: A Conductor-backed Slotline Leaky-Wave Antenna

From the numerical results in Section 3.1.2, the radius of the coaxial line is too large (6 mm or more) in fabrication for operating frequencies less than 14 GHz. Therefore we design a planar type of slotted coaxial lines, which are equivalent to the conductor-backed slotlines to demonstrate that such a leaky mode can propagate in this structure. Fig. 3.5 illustrates the proposed conductor-backed slotline leaky-wave antenna, with a simple microstrip line and a gap resonator feeding. The substrate is chosen as air to reduce the electrical length of the substrate thickness, and the operating frequency is lowered. The substrate thickness *h* is 10 mm, the slot width  $w_1$  is 10 mm, the width of two side top conductors  $w_2$  is 20mm, and the length of top conductors is 150 mm.





Fig. 3.5 The proposed conductor-backed slotline leaky-wave antenna.

Fig. 3.6 displays the normalized phase constants and attenuation constants. The radiation region starts at 12 GHz. As shown Fig. 3.7, the bandwidth of this antenna is about 2.95 GHz, which begins from 15.95 to 18.90 GHz. At 13, 14, 15 GHz, the antenna gains plotted in Fig. 3.8 are 9.75, 12.16, 14.01 dBi, respectively. At 16, 17, 18 GHz, the antenna gains plotted in Fig. 3.9 are 15.02, 14.95, 16.52 dBi, respectively. This conductor-backed slotline leaky-wave antenna has the similar frequency-scanning property as a microstrip leaky-wave antenna does.



Fig. 3.6 The normalized phase constants and attenuation constants.



Fig. 3.7 The return loss of the conductor-backed slotline antenna.



Fig. 3.8 The copolarization radiation patterns at 13, 14 15 GHz in the xz-plane.



Fig. 3.9 The copolarization radiation patterns at 16, 17, 18 GHz in the xz-plane.



#### **3.2 Leaky Modes of Coplanar Waveguides on Cylindrical Substrates**

## 3.2.1 Spectral Domain Analysis of Coplanar Waveguides on Cylindrical Substrates

The proposed leaky CPW on cylindrical substrate is plotted in Fig. 3.10(a). Region I and III are both free space. Region II is the cylindrical substrate with a permittivity of  $\varepsilon_{2=\varepsilon_r}\varepsilon_o$  and a thickness of *h*. The center strip (with the width *w*) and the slots (with the widths *s*) are on the top of the substrate. The center strip, slots, and ground conductor are all located at circumferences of radius *b*. As the same symmetry shown in Chapter 1, a PEC boundary is placed at the top and the bottom ( $\phi = 0, \pi$ ) in Fig. 3.10(b). The longitudinal currents (z-direction) on the center strip and the ground conductor are odd-symmetric about  $\phi = 0, \pi$ . The transverse currents ( $\phi$ -direction) are even-symmetric about  $\phi = 0, \pi$ . This CPW leaky mode is similar to the coupled slotline mode [34]-[35], and the main difference is that the currents of CPW leaky mode are attenuating.



Fig. 3.10 (a) The cross-sectional view of the CPW on the cylindrical substrate. (b) The PEC boundary representation.

The three sets of longitudinal (z-direction) fields  $(E_{zi}, H_{zi})$  are represented as inverse Fourier series:

$$E_{zi}(\rho,\phi,z) = \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} P_{in}(k_{i\rho}\rho) \qquad H_{zi}(\rho,\phi,z) = \sum_{n=-\infty}^{\infty} \frac{e^{-jn\phi}}{2\pi} Q_{in}(k_{i\rho}\rho) \qquad (3.4)$$
  
where  $k_z^2 = k_i^2 - k_{i\rho}^2$ ,  $k_i = \omega \sqrt{\mu_0 \varepsilon_i}$ ,  $i = 1, 2, 3$ .

and  $(P_{in}, Q_{in})$  are the linear combinations of appropriate kinds of Bessel functions with unknown coefficients. The E-fields  $(E_{z2}, E_{\phi 2})$  are expanded with appropriate basis functions. The remaining procedures are identical to those in Section 3.1 except the different Green's functions, which are obtained after applying boundary conditions.

# TIES A

**3.2.2 Numerical Results** 

Three parameters, outer radius *b*, center strip width *w*, and slot widths *s* have been changed to check how they influence the propagation constants of the first higher order leaky mode. The two unchanged parameters: dielectric constant of the substrate  $\varepsilon_r$  is 2.2, and the thickness of the substrate *h* is 0.508 mm. Fig. 3.11, 3.12, and 3.13 plotted the calculated normalized attenuation constants and phase constants ( $\alpha/k_0$ ,  $\beta/k_0$ ). In Fig. 3.11, the outer radii *b* are 10, 12, and 14mm, the center strip width *w* is 10 mm, and the slot width is 5mm. When the outer radius *b* increases, the curve of the propagation constants moves to a lower frequency region.

Fig. 3.12 shows the effect of the center strip width w. The slot width s is 5mm, while the center strip widths w are 10, 8, and 6mm. Narrower w causes the propagation constants shift to a higher frequency band.

Fig. 3.13 plots the curves for three different slot widths s, which are 10, 5, and 1 mm. The center stripe width w is 10 mm and the outer radius b is 20 mm. It is

interesting that Fig. 3.13 is very analogous to Fig. 3.12. This implies that both of center strip width and slot width may have the equivalent effect for leaky modes of CPW on cylindrical substrates. The normalized phase constants  $\beta/k_0$  in all figures are less than unity, and this implies that this structure has a wide radiation region ( $\alpha \le \beta \le k_0$ ).



Fig. 3.11 The normalized propagation constants of different outer radii ( b = 10, 12 and 14 mm, h = 0.508 mm,  $\epsilon r = -2.2$ , s = 5 mm, and w = 10 mm).



Fig. 3.12 The normalized propagation constants of different center strip widths
(b = 20 mm, h =0.508 mm, ar = 2.2, s = 5 mm, and w = 10, 8, and 6 mm).

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Fig. 3.13 The normalized propagation constants of different slot widths (b = 20 mm, h =0.508 mm, εr = 2.2, s = 10, 5, and 1 mm, and w = 10 mm).

#### 3.2.3 Design Example: A Cylindrical Coplanar Waveguide Leaky-Wave Antenna

In this section, we design a cylindrical coplanar waveguide leaky-wave antenna. The dielectric constant of the substrate  $\varepsilon_r$  is 2.2, and the thickness *h* is 0.508mm. The outer radius *b* is 80 mm, the center strip width *w* is 10 mm, and the slot width is 5mm. Due to the odd-symmetry of longitudinal currents, two sets of inverted balanced lines [23] are fed into the CPW, as shown in Fig. 3.14. The length of the CPW antenna is 150 mm.

Fig. 3.15 plots the normalized propagation constants. Its radiation region starts at 9.5 GHz and extend to 16.0 GHz. The measured return loss is shown in Fig. 3.16. At 6, 7, and 8 GHz, the measured antenna gains are 6.8, 9.2, and 7.3 dBi, respectively. In addition, the measured antenna gains are 9.1, 9.4, and 8.5 dBi at 9, 10, and 11 GHz, respectively. In Fig. 3.17 and 3.18, the antenna mainbeams are fixed at the endfire direction. Both of CPW leaky-wave antennas and single-conductor leaky-wave antennas [23] have fixed mainbeams because their similar structures and current symmetries.



Fig. 3.14 The proposed cylindrical coplanar waveguide leaky-wave antenna.



Fig. 3.15 The normalized phase constants and attenuation constants.



Fig. 3.16 The measured return loss of the proposed cylindrical coplanar waveguide leaky-wave antenna.



Fig. 3.17 The measured copolarization radiation patterns at 6, 7, and 8 GHz in the xz-plane.



Fig. 3.18 The measured copolarization radiation patterns at 9, 10, and 11 GHz in the xz-plane.

# **Chapter 4**

#### **Broadband Leaky-Wave Antennas**

This chapter mainly discusses planar broadband leaky-wave antennas. The slotline antenna is a complementary structure of the single-conductor strip antenna, whereas the inverted-T antenna is derived from the single-conductor strip antenna. All of these three types of structures can be very wideband antennas, due to their surface-wave-like leaky modes. A wideband slotline leaky-wave antenna with a microstrip-to-CPW feeding structure and an inverted-T leaky-wave antenna with simple ground plate are presented.

#### 4.1 Slotline Leaky-Wave Antennas

The cross-sectional views of single-conductor strip leaky-wave antennas [23] and slotline leaky-wave antennas [36] and are plotted in Fig. 4.1. It is obvious that they are complementary structures. The center PEC and PMC represent odd-symmetry and even-symmetry for longitudinal currents, respectively. In this section, we focus on the slotline leaky mode and its corresponding feeding structure.





By using the spectral domain approach, we calculate the normalized phase constants and attenuation constants of the first higher leaky-mode of slotlines. Moreover, slotlines belong to the structure plotted in Fig. 3(f) in Oliner's paper [37], which indicates the existence of leaky modes. The propagation constants of  $TM_1$  surface wave of grounded dielectric slabs [33] are also computed. When we compare these two different propagation constants in Fig. 4.2, it can be found that as the slot width decreases, the propagation constants of slotlines are approaching those of grounded dielectric slabs. Therefore, the first higher order leaky mode of slotlines may be treated as a guided surface wave propagating along the longitudinal direction of the slot. Since single-conductor strips are complementary structures of slotlines, the surface wave mode and the first higher leaky mode should have the similar relationship

in single-conductor strips.





Fig. 4.2 The normalized phase constants and attenuation constants of slotlines and  $TM_1$  surface wave mode of grounded dielectric slab (w=0 case).

Since the radiation region of the slotline leaky mode is very wide, a broadband feeding circuit should be utilized to provide the required bandwidth. The broadband microstrip-to-CPW transition [24] is adopted to excite the first higher leaky mode of slotlines. Besiders, a section of tapered line is also combined with the microstrip-to-CPW transition.



Fig. 4.3 The proposed slotline leaky-wave antenna. (a) The top view . (b) The bottom view.

The proposed slotline leaky-wave antenna shown in Fig. 4.3 has the following structural parameters: slot width is 10 mm, antenna length is 90 mm, the dielectric constant is 2.2, and the substrate thickness is 0.508 mm. Fig. 4.4 plots the measured return loss, and this antenna has a bandwidth about 14.7 GHz, starting from 11.8 to 26.5 GHz. The measured copolarization radiation patterns at 14 and 16 GHz are illustrated in Fig. 4.5, with antenna gains 8.9 and 10.1 dBi, respectively. In Fig. 4.6, the measured radiation patterns at 18 and 20 GHz are, with antenna gains 11.5 and 12.3 dBi, respectively. In Fig. 4.7, antenna gains at 22 and 24 GHz are 13.3 and 12.3 dBi. The two mainbeams of upper and lower half-space are closer to each other as the frequency increases.





Fig. 4.4 The measured return loss of the slotline leaky-wave antenna.



Fig. 4.5 The measured copolariztion radiation patterns at 14 and 16 GHz.



Fig. 4.6 The measured copolariztion radiation patterns at 18 and 20 GHz.



Fig. 4.7 The measured copolariztion radiation patterns at 22 and 24 GHz.



#### 4.2 Broadband Inverted-T Leaky-Wave Antenna

For the first higher order leaky mode in single-conductor strip leaky-wave antenna plotted in Fig 4.8(a), an infinite virtual PEC boundary is assumed at the center of the strip, in which the longitudinal currents are odd-symmetric and transverse currents are even-symmetric with respect to the center. From the image theory, the inverted-T leaky-wave antenna with infinite PEC boundary in Fig. 4.8(b) will have the same radiation characteristics for the y > 0 plane with that of the single-conductor strip leaky-wave antenna shown in Fig. 4.8 (a).



Fig. 4.8 (a) The single-conductor strip leaky-wave antenna. (b) The inverted-T leaky-wave antenna.

Since the inverted-T and the single-conductor strip leaky-wave antenna are equivalent in the half space, we first calculate the normalized propagation constants of the single-conductor strip leaky-wave antenna with the spectral domain approach. Shown in Fig. 4.9 are the normalized phase constants and attenuation constants for the single-conductor strip leaky-wave antenna with the following structural parameters: antenna width  $w_s$ =14 mm, the dielectric constant of the substrate  $\varepsilon_r$ =2.2 and the substrate thickness *h*=0.508 mm. The radiation region is from 6.6 GHz to 18.0 GHz, with the normalized phase constant remains almost a constant, which implies that the mainbeam will be fixed around the endfire direction.

To excite the first higher order leaky mode of single-conductor strip antenna in Fig. 4.8(a), a broadband feeding structure consists of two out-of-phase balanced microstrip lines that utilizes a broadband phase inverter [23]. However, only a finite conductor plate is needed for the inverted-T leaky-wave antenna, and the difficulty in design of the broadband phase inverter is removed.

We implement an inverted-T antenna shown in Fig. 4.10 with the antenna width  $w_a=7$  mm, the antenna length  $L_a=100$  mm, a substrate of dielectric constant  $\varepsilon_r=2.2$  and the substrate thickness h = 0.508 mm. The half-width strip is mounted vertically over the conductor plate. A signal line is fed at the edge opposite to the plate, and the conductor plate is the ground. The measured return loss is plotted in Fig. 4.11. The bandwidth extends from 10.9 to 18.0 GHz, for a bandwidth ratio about 1.65:1.

The measured co-polarization radiation patterns in the *xz*-plane at 13, 14, and 15 GHz are shown in Fig. 4.12, with the measured gains 7.44, 9.48, and 10.58dBi, respectively. The mainbeam directions at these three frequencies are all around  $66^{\circ}$  from the broadside direction. Fig. 4.13 plots the measured co-polarization radiation patterns in the *xz*-plane at 16, 17, and 18GHz, while the measured gains are 10.94,

11.71, and 10.94 dBi, respectively. The mainbeam directions at these three frequencies are close to 68° from the broadside direction.

The patterns of this antenna vary slightly from 13 to 18 GHz, and the shapes of the mainbeams are almost the same. For a single-conductor strip leaky-wave antenna, its mainbeam always keeps at the endfire direction. But the mainbeam of an inverted-T leaky-wave antenna is tilted from the endfire direction since the ground plate is not infinite.



Fig. 4.9 The computed normalized phase constants and attenuation constants



Fig. 4.10 The proposed inverted-T leaky-wave antenna.





Fig. 4.11 The measured return loss.



Fig. 4.12 Measured co-polarization radiation patterns at 13, 14 and 15 GHz in the xz-plane.



Fig. 4.13 Measured co-polarization radiation patterns at 16, 17 and 18 GHz in the xz-plane.

#### **Chapter 5**

#### **Conclusion and Future Work**

This thesis studies the propagation characteristics of leaky modes on cylindrical substrates and broadband planar leaky-wave antennas. Two kinds of leaky-mode symmetries represented with PEC and PMC on both structures are analyzed by the full-wave method.

Three cylindrical types of transmission lines: microstrip lines, slotted coaxial lines, and coplanar waveguides are investigated. The effects on propagation constants under different structural parameters are presented. All of these leaky modes on cylindrical substrates have wide radiation regions. Feeding structures used in planar leaky-wave antennas, such as aperture-coupling and inverted balanced microstrip lines, are applied to excite the first higher leaky mode on cylindrical leaky-wave antennas successfully.

A broadband feeding structure, microstrip-to-CPW transition, is utilized for slotline leaky-wave antennas. From the measured radiation patterns, slotline leaky-wave antennas can have high gains in a wide bandwidth. Besides, a novel inverted-T leaky-wave antenna, which is modified from a single-conductor strip leaky-wave antenna, is developed and implemented. The feeding circuits are simplified by replacing the phase inverter by a finite ground plate.

However, there are still many issues that need to be further investigated in this thesis. These topics are listed in the following:

- 1. The creeping waves, the second or higher leaky modes on cylindrical substrates.
- 2. Mode-coupling between transmission lines on cylindrical substrates.
- 3. Implementation of slotted leaky-wave antenna on standard coaxial lines like RG-58, including the feeding structures of the first higher leaky-mode.

- 4. Better impedance matching circuits for planar and cylindrical CPW leaky-wave antennas.
- 5. More relationships between surface waves and leaky modes on slotlines and single-conductor strip lines.
- 6. Design of feeding structure of slotline leaky-wave antennas to obtain a leaky mode purity and reduce the sidelobes.



# Appendix

The Green's functions used in cylindrical microstrip lines are listed as following:

$$\begin{bmatrix} \tilde{G}_{zz} & \tilde{G}_{z\phi} \\ \tilde{G}_{\phi z} & \tilde{G}_{\phi \phi} \end{bmatrix} = \begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} \begin{bmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{bmatrix}^{-1}$$
(A-1)

where

$$\begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} = \begin{bmatrix} H_n^{(2)}(k_{2\rho}b) & 0 \\ -\frac{nk_z H_n^{(2)}(k_{2\rho}b)}{k_{2\rho}^2 b^2} & \overline{Z} H_n^{(2)}(k_{2\rho}b) \\ -\frac{k_z H_n^{(2)}(k_{2\rho}b)}{k_{2\rho}^2 b^2} & \overline{Z} H_n^{(2)}(k_{2\rho}b) \end{bmatrix}$$
(A-2)

$$T_{11} = (q_1 + T_{21}q_2) \tag{A-3}$$

$$T_{12} = (q_3 + T_{22}q_2) \tag{A-4}$$

$$T_{21} = q_4 q_5 \frac{\left(k_{1\rho}^2 - k_{2\rho}^2\right) n k_z}{k_{2\rho}^2 k_{1\rho} \overline{Z} b} H_n^{(2)} \left(k_{2\rho} b\right)$$
(A-5)

$$T_{22} = q_4 q_5 \frac{k_{1\rho}}{k_{2\rho}} H_n^{(2)} \left( k_{2\rho} b \right) - H_n^{(2)} \left( k_{2\rho} b \right)$$
(A-6)

$$q_{1} = \frac{q_{6}\overline{Y}_{1}}{k_{1\rho}} \times \frac{H_{n}^{(2)}(k_{2\rho}b)H_{n}^{(1)}(k_{1\rho}a)}{\left(-J_{n}(k_{1\rho}a)H_{n}^{(2)}(k_{1\rho}b)+J_{n}(k_{1\rho}b)H_{n}^{(1)}(k_{1\rho}a)\right)} - \frac{H_{n}^{(2)}(k_{2\rho}b)\overline{Y}_{2}}{k_{2\rho}} \quad (A-7)$$

$$q_2 = -\frac{nk_z}{k_{1\rho}^2 b} \tag{A-8}$$

$$q_{3} = \left(\frac{1}{k_{1\rho}^{2}} - \frac{1}{k_{2\rho}^{2}}\right) \frac{nk_{z}}{b} H_{n}^{(2)}\left(k_{2\rho}b\right)$$
(A-9)

$$q_{4} = -\frac{J_{n}'(k_{1\rho}a)}{H_{n}^{(1)'}(k_{1\rho}a)}H_{n}^{(1)}(k_{1\rho}b) + J_{n}(k_{1\rho}b)$$
(A-10)

$$q_{5} = \frac{H_{n}^{(1)}(k_{1\rho}a)}{-J_{n}(k_{1\rho}a)H_{n}^{(1)}(k_{1\rho}b) + J_{n}(k_{1\rho}b)H_{n}^{(1)}(k_{1\rho}a)}$$
(A-11)

$$q_{6} = -\frac{J_{n}\left(k_{1\rho}a\right)}{H_{n}^{(1)}\left(k_{1\rho}a\right)}H_{n}^{(1)'}\left(k_{1\rho}b\right) + J_{n}'\left(k_{1\rho}b\right)$$
(A-12)

$$\overline{Z} = j\omega\mu, \,\overline{Y_1} = j\omega\varepsilon_1, \,\overline{Y_2} = j\omega\varepsilon_2.$$
(A-13)

The Green's functions used in slotted coaxial lines are listed as following:

$$\begin{bmatrix} \tilde{G}_{zz} & \tilde{G}_{z\phi} \\ \tilde{G}_{\phi z} & \tilde{G}_{\phi \phi} \end{bmatrix} = \begin{bmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{bmatrix} \begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix}^{-1}$$
(A-14)

The elements  $\begin{bmatrix} T_{11} & T_{12} \\ T_{21} & T_{22} \end{bmatrix}$  and  $\begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix}$  are from (A-2)-(A-13).



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