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A Study of Statistically Significant Difference Pattern Detection

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#### A Study of Statistically Significant Difference Pattern Detection

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## **A Study of Statistically Significant Difference Pattern Detection**

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#### **Abstract**

In the traditional Questionnaire Analysis, there exists a problem that researchers may miss or ignore some causes because the traditional analysis usually is performed in an experiential try-and-error manner. For example, the digital divide researchers may focus on the difference in the grade between different genders. But they may miss other causes of the difference in the grade (e.g., parents' education, living locations, parents' vocations). These causes may also lead to the difference in grade. We name it "Significant Difference Unawareness Problem".

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In order to solve the Significant Difference Unawareness Problem, we propose a semi-automatic discovery-based analysis method instead of the traditional hypothesis-based analysis manner. Since a more flexible analysis on richer data is required in our method. Hence, we apply the data warehousing technique is applied. We discuss how to detect the entire interesting pattern that implies the causes of the difference on the multi-dimensional data structure, and define this problem as Significant Difference Pattern Detection (SDPD). After applying the data warehousing, some problems must be solved: the data size is huge and the combination of dimensions is very complex. So we propose a greedy algorithm, WISDOM (Wisely Imaginable Significant Difference Observation Mechanism), to solve the SDPD problem. The WISDOM includes two major processes: (1) Data Reduction Process. The Data Reduction Process has a sensitive-less data filtering heuristic that is useful to reduce the data size. (2) SD Pattern Mining Processes. The SD Pattern Mining has a significant difference pattern determination heuristic that is effective to determinate if there exists a significant difference in a single dimension versus a single measure.

**Keyword**:**Data Mining, Significant Difference, Data Warehousing, On-Line Analytic Processing (OLAP), Digital Divide** 





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## **Chapter 1. Introduction**

Social science research is the use of scientific methods to investigate human behavior and social phenomenon [3]. However, the population of human society is generally very huge. Since it is impossible for social science researchers to thoroughly observe the huge population for a behavior or a phenomenon, they usually use questionnaire survey instead of investigating the whole population.

Questionnaire survey is usually done by selecting some representative samples from population according to the sampling methods. For analyzing the questionnaire data, researchers can use not only descriptive statistics methods, but also inferential statistics methods to infer the real human behavior and social phenomenon.  $n_{\rm H\,m\,s}$ 

In the questionnaire analysis, finding whether there is significant difference between two or more groups in one measure is one of the major problems in researches. For example, in a survey of junior high school students' current status, "Is there significant difference between different genders' IQ?" and "Is there significant difference between the mathematics grades of different areas in Taiwan?" are two interesting phenomenon that researchers want to know. [3] categorized the research questions into degree of relationship among variables, significance of group differences, prediction of group membership, and structure, which significance of group differences is used to find the significant difference. Therefore, finding possible significant difference between different groups is a very important research issue.

However, finding possible significant difference namely is difficult for social science researchers. In our observation, there are two main causes may lead to this issue.

The first cause is that researchers find the significant difference by their intuition and experience. For example, a junior researcher might consider that there is significant difference between different genders' IQ. She/He could make a hypothesis, "There will be difference between different genders' IQ," and then use inferential statistics method to test this hypothesis. This is basically a hypothesis-based search method. Once the hypotheses are not made the significant difference can not be found even if it really exists. However, senior researchers might find it easier because of **MATTERS** their rich experiences.

The second cause is that the original questionnaire data may be not good enough to find the significant differences. For example, in the survey of junior high school students' current status, the student's resident dimension doesn't have granularity, and just contains the region attribute. If there is no significant difference between the mathematics grades of different regions, the researcher can just say there is no significant difference between the mathematics grades of different regions. However, if the researchers combine their collected data with secondary data which are collected by other researches [23] like the government official statistical data, geographic information, or other researches data, and assume the student's resident dimension has granularity, they would drill down the dimension to find whether there is significant difference between the mathematics grades of different cities.

In order to overcome the Significant Difference Unawareness issue, we apply data warehousing technology to integrate and maintain the questionnaire data and secondary data, and use a discovery-based search method to find the possible significant differences from the data warehouse semi-automatically. Data warehouse, which has subject-oriented, integrated, time-variant, and nonvolatile features, is a repository of integrated information, available for queries and analysis [23]. It also supports OLAP systems which can be used to query and explore the data at different granularities. Furthermore, a discovery-based search method is used to find the possible significant differences from data warehouse before analyzing the questionnaire data. According to these results, researchers can briefly understand where the possible significant differences are, and they can easily explore the data  $n_{\rm H\,m\,N}$ using OLAP systems.

In this thesis, the Significant Difference Pattern is formally defined first. Next, a *Significant Difference Pattern Detection problem* (*SDPD problem*), which is the problem of finding all the possible significant difference from the data warehouse, is proposed. According to our observation of Significant Difference Pattern, a heuristic about the property of Significant Difference Pattern is proposed; besides, a greedy algorithm based on this heuristic is proposed to solve the Significant Difference Pattern Detection problem.

The rest of this thesis is organized as follows. Chapter 2 briefly introduces the related researches about fining significant difference. In Chapter 3, the clear definitions of Significant Difference Pattern and Significant Difference Pattern Detection problem are given. A greedy algorithm, WISDOM, is proposed in Chapter 4 to solve the Significant Difference Pattern Detection problem based on the heuristics. Moreover, some experiment results of the WISDOM algorithm are shown in Chapter 5 .Finally, we make conclusions and describe the future works in Chapter 6.



## **Chapter 2. Related Work**

According to our survey, there are no related researches on this significant difference pattern detection problem. In this chapter, we introduce some related work: The problem of the traditional quantitative research, the indicator of data warehouse to indicator the difference, the deviation detection to detect the pattern that differ from trend and the feature selection is also not a solution for this problem.

# **2.1.Quantitative research**

Quantitative research techniques [11] [23] are part of primary research and the data which are reported numerically can be collected through structured interviews, experiments, or surveys.

Quantitative research is all about quantifying relationships between variables. Variables are things like weight, performance, time, and treatment. You measure variables on a sample of subjects, which can be tissues, cells, animals, or humans. You express the relationship between variable using effect statistics, such as correlations, relative frequencies, or differences between means.

"Hypothesis Testing" is the most popular statistics method [11] to analyze the relationship between variables. And the researchers are most concerned about the differences between means, because the difference can immediately and effectively indicate the causality of the subject. If some variable like the gender of students versus the grades of students has a difference which is a statistical significant at a given *1-* confident level, then we said that there is a significant difference between the gender of students versus the grades.

In the traditional quantitative research, the researchers will firstly propose several hypotheses of the subject according to their experiences, and then test the hypotheses one by one to check if there exists a statistic significant in some hypotheses. Hence, it calls a try-and-error manner. The quality of the result using the manner, of course, is in accordance with the hypotheses made by the researchers.



Furthermore, the quantitative research researcher's aim is to determine the relationship between one thing and another in a population. Quantitative research designs are either descriptive (subjects usually measured once) or experimental (subjects measured before and after a treatment). An experiment establishes causality. For an accurate estimate of the relationship between variables, a descriptive study usually needs a sample of hundreds or even thousands of subjects; an experiment, especially a crossover, may need only tens of subjects. The estimate of the relationship is unlikely to be biased if researchers have a high participation rate in a sample selected randomly from a population. In several statistical experiments, bias is also unlikely if subjects are randomly assigned to treatments, and if subjects and researchers are blind to the identity of the treatments. In all studies, subject characteristics can affect the relationship you are investigating and limit their effect either by using a less heterogeneous sample of subjects or preferably by measuring the characteristics and including them in the analysis. In an experiment, they try to measure variables that might explain the mechanism of the treatment. In an unblended experiment, such variables can help define the magnitude of any placebo effect.

#### **2.2.Indicator**

Indicator [17] [18] is not used in a discovery-based analysis but is a useful tool to assist exploring the data cube of the data warehouse by OLAP. In order to implement indicators, a complete datacube should be constructed. In real case, building datacubes is very time consuming [1] [2] [4] [5]. Hence, using indicators is a computational expensive task.

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The data warehouse could consist with several datacubes or single datacube. For each datacube, it has several records and a star schema to describe the schema of the datacube's structure. In other word, the star schema can describe the dimensions with concept hierarchy and some measures of the datacube. And, the data warehouse supports an analysis tool: On-Line Analytic Processing (OLAP) [2] [19] [22]. It is a useful tool assistant to user exploring the datacube. OLAP can organize and present data in various formats in order to accommodate the diverse needs of the different analysis approaches. OLAP server provides server operations for analyzing multidimensional data cube:

**Roll-up**: the roll-up operation collapses the dimension hierarchy along a particular dimension(s) so as to present the remaining dimensions at a coarser level of granularity.

**Drill-down**: in contrast, the drill-down function allows users to obtain a more detailed view of a given dimension.

#### **AMMA**

**Slice**: Here, the objective is to extract a slice of the original cube corresponding to a single value of a given dimension. No aggregation is required with option. Instead, server allows the user to focus on desired values.

**Dice**: A related operation is the dice. In this case, users can define a sub cube of the original space. In other words, by specifying value ranger on one or more dimensions, the user can highlight meaningful blocks of aggregated data.

**Pivot**: the pivot is a simple but effective operation that allows OLAP users to visualize cube values in more natural and intuitive ways

The data warehouse also supports another analysis tool: On-Line Analytical Mining (OLAM) [2] [6] [12]. It integrates OLAP, data mining and knowledge discovering on multi-dimensional database structure into OLAM. Hence, OLAM is also called OLAP Data Mining. The OLAM supports several data mining tasks such as the concept description, mining association rules, classification & prediction, and time sequential analysis.

Typically, the data mining algorithm is performed on a single "data mining" table. This table is produced by using the transformations and aggregations on the base data. Often, we need to generate the single table. This transformation is a key part of the data mining process. Often, it is a manual process and the physically elapsed time for locating, migrating, and transforming data is the orders of magnitude greater than the involved computing time. It is important that effective tools are used to support this process.



However, neither the OLAP nor the OLAM is a discovery-based analysis tool, and it can not detect the significant difference pattern automatically or semi-automatically.

#### **2.3.Deviation Detection**

Deviation detection [13] is a research which aims to detect the pattern differed from the predict pattern. They use a mathematic mode to predict the trend of the measures. Then using the difference of the predict trend and measure to determinate

the deviation. For example, if we predict that the height of a man is taller than a woman. Then deviation detection will detect the pattern, there exists a woman is taller than the man. Similarly, if we predict the profit of products at may be \$10,000. Then deviation detection will detect the pattern that there exists a product, cell phone, has a large deviation on the profit. It may be \$15,000 or \$5,000.

#### **2.4.Feature Selection**

Feature selection [6] [14] [15], also known as subset selection or variable selection, is a process commonly used in machine learning, wherein a subset of the features available from the data is selected for application of a learning algorithm. Feature selection is necessary either because it is computationally infeasible to use all available features, or because of problems of estimation when limited data samples (but a large number of features) are present. The latter problem is related to the so-called curse of dimensionality.

Simple feature selection algorithms are ad hoc, but there are also more methodical approaches. From a theoretical perspective, it can be shown that optimal feature selection for supervised learning problems requires an exhaustive search of all possible subsets of features of the chosen cardinality. If large numbers of features are available, this is impractical. For practical supervised learning algorithms, the search is for a satisfactory set of features instead of an optimal set. Many popular approaches are greedy hill climbing approaches. Such an approach evaluates a possible subset of features and then modifies that subset to see if an improved subset can be found. Evaluation of subsets can be done many ways - some metric is used to score the features, and possibly the combination of features. Since exhaustive search is generally impractical, at some stopping point, the subset of features with the highest scores by the metric will be selected. The stopping point varies by algorithm.

Two popular metrics for classification problems are correlation and mutual information. These metrics are computed between a candidate feature (or set of features) and the desired output category.

## *<u>ALLENY</u>*

In statistics the most popular form of feature selection is called stepwise regression. It is a greedy algorithm that adds the best feature (or deletes the worst feature) at each round. The main control issue is deciding when to stop the algorithm. In machine learning, this would typically be done by cross validation. In statistics, some criteria would be optimized.

## **Chapter 3. Problem Definition**

In order to avoid the Significant Difference Unawareness issue, we first build a data warehouse by integrating the questionnaire data and secondary data, and then use a discovery-based search method to find the possible significant differences from the data warehouse semi-automatically. Next, the desired significant difference is defined as Significant Difference Pattern. Finally, a new discovery-based problem, Significant Difference Pattern Detection problem, is proposed.



The data structure of *Data Warehouse*, containing dimensions, measures, and records, generally represents in a form of star schema, snowflake schema, or fact constellation schema, where the star schema is the most basic one and the other two can be derived by star schema [2][4][10]. To simplify our discussion, in this thesis, *Data Warehouse* based on the star schema is used to represent the data.

#### **DEFINITION 1:** *Data Warehouse*

A *Data Warehouse* contains *p* dimensions, *Dimension = {Di| i = 1…p}*, *q* measures, *Measure = {M<sub>i</sub>| i = 1...q}*, and *n* records, *Record = {R<sub>i</sub>| i = 1...n}*. Each dimension  $D_i$  contains  $f(i)$  levels of granularity, called attribute,  $D_i = \langle A_{i1}, A_{i2}, \ldots, A_{iM}\rangle$  *A<sub>if(i)</sub>*>. Each attribute *A<sub>ij</sub>* contains *g(i, j)* attribute values,  $A_{ij} = \{V_{ijk} | k = 1...g(i, j)\}$ . Each measure  $M_i$  is a continuous value. Each record  $R_i$  is the tuple of  $(A_{11}, ..., A_{1f(1)})$ *A21, …, A2f(2), …, Apf(p), M1, …, Mq)*.

The *Data Warehouse* of EXAMPLE 1 is built based upon a questionnaire survey data for all the elementary school students in Taiwan. In the rest of this thesis, all the examples are based on this *Data Warehouse*.

#### **EXAMPLE 1:**

The *Data Warehouse* contains 3 dimensions, i.e. *gender*, *resident\_area*, and *father\_education*, 2 measures, i.e. *IQ* and *math\_grade*, and 9 records. The detailed structure of dimensions and measures are listed as follows, and the 9 records are listed in Table 3.1.

- z *Dimension = {gender, resident\_area, father\_education}* 
	- *gender = <gender>* 
		- *gender = {male, female}*
	- *resident\_area = <region, city>* 
		- *region = {north, central, south, east}*
		- *city = {Taipei, Hsinchu, Taichung, Tainan, Hualien}*
	- *father\_education = <father\_education>* 
		- *father\_education = {elementary, junior\_high, senior\_high,*

*university, graduate}* 

- z *Measure = {IQ, math\_grade}*
- $Record = {R_1, R_2, R_3, ..., R_9}$

| Record | gender | region  | city            | father_education | IQ         | math_grade |
|--------|--------|---------|-----------------|------------------|------------|------------|
| $R_I$  | male   | east    | Hualien         | elementary       | 104        | 25         |
| $R_2$  | male   | north   | Hsinchu         | senior_high      | 116        | 66         |
| $R_3$  | female | central | <b>Taichung</b> | senior_high      | 124        | 45         |
| $R_4$  | female | north   | <i>Taipei</i>   | university       | 133        | 89         |
| $R_5$  | male   | central | <b>Taichung</b> | junior_high      | <i>110</i> | 34         |
| $R_6$  | male   | south   | <b>Tainan</b>   | junior_high      | 98         | 22         |
| $R_7$  | female | east    | Hualien         | university       | 116        | 64         |
| $R_8$  | male   | south   | <b>Tainan</b>   | elementary       | 124        | 38         |
| $R_9$  | female | north   | Taipei          | graduate         | 126        | 83         |

Table 3.1: The 9 records of EXAMPLE 1



#### **3.2.Significant Difference Pattern**

Significant difference, a specific term in statistics, represents two or more groups exist obviously different on a continuous variable. For representing clearly, a significant difference is defined as a *Significant Difference Pattern*.

#### **DEFINITION 2:** *Significant Difference Pattern*

The *Significant Difference Pattern* (*SDP*) is the pattern with a statistically

significant difference at the given *1*- confidence level, where  $\alpha$  is significance level in statistics. An *SDP* is composed by three parts: attribute part, condition part, and measure part. The attribute part contains one attribute, the condition part contains several "attribute equal to attribute value" pairs, and the measure part contains one measure. To simplify our discussion, assume there is only one "attribute equal to attribute value" pair in the condition part. The *SDP* is denoted as

$$
(A_{ij}/A_{xy}=V_{xyz}):M_k \qquad (3.1)
$$

It means that there is significant difference between different attribute values of  $A_{ij}$  on measure  $M_k$  for all the records satisfying  $A_{xy} = V_{xyz}$ . Generally speaking, the significance level  $\alpha$  is set as 5% or 1%.

#### **EXAMPLE 2:**

Given the *SDP*:

*(region | gender = male) : math\_grade* 

This *SDP* means that, for all *male*, there is significant difference between different resident regions on *math\_grade*.

#### **3.3.Significant Difference Pattern Detection**

The *Data Warehouse* and *Significant Difference Pattern* have been formally defined in the previous sections. In this section, we propose the problem of finding the possible *SDPs* from a given *Data Warehouse* as a new discovery-based problem, i.e. *Significant Difference Pattern Detection problem*.

## **DEFINITION 3:** *Significant Difference Pattern Detection problem*

Given a *Data Warehouse*, <sup>α</sup> , β , <sup>γ</sup> , and *Depth*, finding the possible *SDPs* from the *Data Warehouse*, where  $\alpha$  is significance level,  $\beta$  is sensitivity ratio threshold, γ is significance determination threshold, and *Depth* is search depth threshold. In the following, the *Significant Difference Pattern Detection problem* is denoted as *SDPD problem*.

#### **3.3.1 Difficulty of SDPD problem**

The *SDPD problem* has already been well defined, but there still exists a big

question: What's the complexity of the *SDPD problem*? In order to answer this question, let's consider the following special case.

The special case has a well defined Multidimensional Database Structure. The Multidimensional Database Structure contains n dimensions and only 1 measure. Each dimension contains only 1 attribute. Each attribute has k values. If someone wants to find all the Significant Difference Pattern in this Multidimensional Database Structure, she/he must take  $(k + 1)^n$  times statistic testing even in this special case. Thus, solving the *SDPD problem* is a very time consuming work.



## **Chapter 4. WISDOM: Wisely Imaginable Significant Difference Observation Mechanism**

In the last chapter, the *SDPD problem* has been proposed, and the fact that it is NP-hard has also been proven. Due to the complexity, it's hard to solve the problem directly without using any heuristics. Hence, two kinds of heuristics, reducing data size and reducing the complexity of the problem, are proposed to reduce the complexity of the problem based on our experiences and discussing with senior researchers. By using these heuristics, a *Wisely Imaginable Significant Difference Observation Mechanism* (*WISDOM*) algorithm is also proposed to solve the *SDPD*   $400011$ *problem*.

The *WISDOM* algorithm, as shown in Figure 4.1, is designed for discovering the possible *SDPs* in a given *Data Warehouse* efficiently. The *WISDOM* algorithm processes one measure at a time, and includes three steps: Data Reduction step, SDP Mining step, and SDP Ranking step. First, Data Reduction step reduces the data size by filtering the sensitive-less and categorizing the continuous data into discrete data. Next, SDP Mining step finds the possible *SDPs* from the reduced *Data Warehouse* by a tree-like greedy algorithm. Finally, SDP Ranking step sorts the found *SDPs* from more important to less important.



*Figure 4.1: The flowchart of WISDOM algorithm* 

The pseudo code of *WISDOM* algorithm is listed in Table 4.1.

Table 4.1: The *WISDOM* algorithm



```
Depth: A search depth threshold; 
Output: 
    SDPs: The SDPs; 
Begin 
    Set SDPs ; 
    For each Mi of Measure, Do
         DW' DataReduction(DW, Mi, ); 
         Set SDPs' ; 
         SDPMining(DW', Mi, Dim, , , , , Depth, SDPs'); 
         SDPs SDPs SDPRanking(SDPs'); 
    Return SDPs; 
End
```


Without loss of generality, the values of measure  $M_i$  are distributed in normal distribution as shown in Figure 4.2. Lots of records are distributed nearly the mean,  $\overline{X}_{M}$ , but these records are sensitive-less about measure  $M_i$ . When the size of records is huge, processing these sensitive-less records will become very inefficient. Therefore, the *Sensitive-less Data Filtering* heuristic is proposed to filter these sensitive-less records. In addition, computing the continuous measure also consumes a lot of computational power; thus, *Sensitive Data Categorizing* heuristic is proposed to categorize the continuous measure into discrete measure further.



*Figure 4.2: The normal distribution* 

## **HEURISTIC 1:** *Sensitive-less Data Filtering*

The *Sensitive-less Data Filtering* heuristic filters the sensitive-less records about measure  $M_i$  between  $\overline{X}_{M_i} + \beta S_{M_i}$  and  $\overline{X}_{M_i} - \beta S_{M_i}$ , where  $\overline{X}_{M_i}$  and  $S_{M_i}$  are the mean and standard deviation of measure  $M_i$ , and  $\beta$  is sensitivity ratio threshold. The value of  $\beta$  can be greater than or equal to 0 to infinity. The smaller  $\beta$  will filter fewer records and own better accuracy and, on the other hand, the bigger  $\beta$  will filter more records and own worse accuracy.

#### **EXAMPLE 3:**

Based on EXAMPLE 1, Table 4.2 shows the records with one attribute, *region*, and one measure, *math\_grade*.

| Record         | region  | math_grade |
|----------------|---------|------------|
| $R_I$          | east    | 25         |
| $R_2$          | north   | 66         |
| $R_3$          | central | 45         |
| $R_4$          | north   | 89         |
| $R_5$          | central | 34         |
| $R_6$          | south   | 22         |
| R <sub>7</sub> | east    | 64         |
| $R_8$          | south   | 38         |
| $R_9$          | north   | 83         |

Table 4.2: The records with attribute *region* and measure *math\_grade*

In Table 4.2,  $\overline{X}_{\text{math\_grade}}$  is 51.78, and  $S_{\text{math\_grade}}$  is 24.67. Given = 1,  $\overline{X}_{math_{math\_grade}} + \beta S_{math_{math\_grade}}$  is 76.45, and  $\overline{X}_{math\_grade} - \beta S_{math_{math\_grade}}$  is 27.11. After applying *Sensitive-less Data Filtering* heuristic, *R2*, *R3*, *R5*, *R7*, and *R8* are filtered due to their *math\_grade* is between  $\overline{X}_{math>{math>path\_grade}} - \beta S_{math>{math>path\_grade}}$  and  $\overline{X}_{math>{math>path\_grade}} + \beta S_{math>{math>path\_grade}}$ and the result is shown in Table 4.3.

Table 4.3: The records after applying *Sensitive-less Data Filtering* heuristic

| Record             | region           | math_grade    |
|--------------------|------------------|---------------|
| $R_I$              | east             | 25            |
| $R_{\rm Z}$        | <del>north</del> | 66            |
| $R_{\overline{3}}$ | <del>centr</del> | 45            |
| $R_4$              | north            | 89            |
| $R_{5}$            | لصيدمه<br>courai | 24            |
| $R_6$              | south            | 22            |
| $R_7\,$            | <del>east</del>  | 64            |
| $R_\delta$         | ovun             | <del>38</del> |
| $R_{9}$            | north            | 83            |

#### **HEURISTIC 2:** *Sensitive Data Categorizing*

The *Sensitive Data Categorizing* heuristic categorizes the origin continuous measure  $M_i$  into a new discrete measure  $M_i' = \{good, bad\}$ . The records whose measure  $M_i$  is greater than  $\overline{X}_{M_i} + \beta S_{M_i}$  are labeled as *good*. On the contrary, the records whose measure  $M_i$  is less than  $\overline{X}_{M_i} - \beta S_{M_i}$  are labeled as *bad*.

#### **EXAMPLE 4:**



Following the EXAMPLE 3, a new Measure *math\_grade'* is added, as shown in Table 4.4. *R4* and *R9* are labeled as *good* due to their *math\_grade* is greater than  $\overline{X}_{M_i}$  +  $\beta S_{M_i}$ , and  $R_1$  and  $R_6$  are labeled as *bad* due to their *math\_grade* is less than  $\overline{X}_{M_i} - \beta S_{M_i}$ .

| Record      | region | math_grade | math_grade' |
|-------------|--------|------------|-------------|
| $R_I$       | east   | 25         | bad         |
| $R_4$       | north  | 89         | good        |
| $R_6$       | south  | 22         | bad         |
| $R_{\rm 9}$ | north  | 83         | good        |

Table 4.4. The records after applying *Sensitive Data Categorizing* heuristic

Although the *Sensitive-less Data Filtering* and *Sensitive Data Categorizing* heuristics can reduce the data size to decrease the process time, it will loss some accuracy contrarily. These heuristics are proposed based on our experiences and discussing with senior researchers, so they are just one of the reducing data size methods.

Data Reduction step uses the *Sensitive-less Data Filtering* and *Sensitive Data Categorizing* heuristics to reduce the data size. The pseudo code of *DataReduction* algorithm is listed in Table 4.5.



#### **4.2.SDP Mining step**

Data Reduction step filters the sensitive-less records and categorizes the continuous measure  $M_i$  to a new discrete measure  $M_i$ <sup>'</sup>. For the original continuous measure  $M_i$ , researches find significant differences by using statistical testing; however, how can we find the *SDPs* from the new discrete measure *Mi'*? Therefore, a definition, *Score and Range*, and *Significant Difference Determination* heuristic are proposed as follows. The *Score and Range* definition is used to calculate the متقلقته difference among different attribute values of an attribute, and the *Significant Difference Determination* heuristic is used to determine whether the difference is 15 1896 significant or not.

#### **DEFINITION 4:** *Score and Range*

Given an attribute  $A_{ij} = \{V_{ijk} | k = 1...g(i, j)\}\$  and a discrete measure  $M_i$ <sup>'</sup>.  $G_{A_{ij} = V_{ijk}}$ is the number of records whose attribute  $A_{ij} = V_{ijk}$  and measure  $M_i' = good$ , and  $B_{A_{ij}=V_{ijk}}$  is the number of records whose attribute  $A_{ij}=V_{ijk}$  and measure  $M_i' = bad$ . *Score*( $A_{ij} = V_{ijk}$ ) can be used to represent the relation between the total mean  $\overline{X}_{M_i}$ and the mean  $\overline{X}_{A_{ij}=V_{ijk}}$ . *Score*( $A_{ij} = V_{ijk}$ ) is defined as:

$$
Score(A_{ij} = V_{ijk}) = \begin{cases} \frac{G_{A_{ij} = V_{ijk}} - B_{A_{ij} = V_{ijk}}}{G_{A_{ij} = V_{ijk}}} & , \quad \text{if } G_{A_{ij} = V_{ijk}} + B_{A_{ij} = V_{ijk}} \neq 0\\ 0, & \quad \text{otherwise} \end{cases} \tag{4.1}
$$

The value of  $Score(A_{ij} = V_{ijk})$  is between 1, representing all the values of measure *Mi'* are *good*, and -1, representing all the values of measure *Mi'* are *bad*.

*Range*( $A_{ij}$ ) is the maximum difference of *{Score*( $A_{ij} = V_{ijk}$ )/ $k = 1, 2, ..., g(i, j)$ }, and it can be used to represent the difference in the attribute  $A_{ij}$ .  $Range(A_{ij})$  is defined as:

*Range*(*Aij*) = max{*Score*(*Aij* = *Vijk* )| *k* = 1,2,K, *g*(*i*, *j*)}− min{*Score*(*Aij* = *Vijk* )| *k* = 1,2,K, *g*(*i*, *j*)} *(4.2)*

Due to the value of  $Score(A_{ij} = V_{ijk})$  is between 1 and -1, the value of  $Range(A_{ij})$ is between 2 and 0.

The idea of *Score*( $A_{ij} = V_{ijk}$ ) is from the z-score of the mean  $\overline{X}_{A_{ij}=V_{ijk}}$ . The value *good* means this record's measure  $M_i$  is greater than  $\overline{X}_{M_i} + \beta S_{M_i}$ , and the value *bad* means this record's measure  $M_i$  is less than  $\overline{X}_{M_i} - \beta S_{M_i}$ . Hence,  $\overline{X}_{A_{ij}=V_{ijk}}$  can be calculated as:

$$
\overline{X}_{_{A_{ij}=V_{ijk}}}=\frac{\left(\overline{X}_{_{M_{i}}+{\beta}S_{_{M_{i}}}}\right)\!{G}_{_{A_{ij}=V_{ijk}}+\left(\overline{X}_{_{M_{i}}}-{\beta}S_{_{M_{i}}}\right)\!{B}_{_{A_{ij}=V_{ijk}}}}{G_{_{A_{ij}=V_{ijk}}+B_{_{A_{ij}=V_{ijk}}}}=\overline{X}_{_{M_{i}}}+\frac{G_{_{A_{ij}=V_{ijk}}}-B_{_{A_{ij}=V_{ijk}}}}{G_{_{A_{ij}=V_{ijk}}+B_{_{A_{ij}=V_{ijk}}}}}\beta S_{_{M_{i}}}
$$

The z-score of  $\overline{X}_{A_{ij}=V_{ijk}}$ ,  $Score(A_{ij}=V_{ijk})$ , can be calculated as:



#### **EXAMPLE 5:**

Given the attribute *region* and measure *math\_grade'* shown in Table 4.4, the *Scores* and *Range* are calculated as:

$$
Score(region = north) = \frac{2 - 0}{2 + 0} = 1
$$

$$
Score(region = central) = 0
$$

$$
Score(region = south) = \frac{0-1}{0+1} = -1
$$

$$
Score(region = east) = \frac{0-1}{0+1} = -1
$$

 $Range-region) = Score(region = north) - Score(region = south) = 1 - (-1) = 2$ 

The *Score* and *Range* can be represented as Figure 4.3.



*Figure 4.3: The Score and Range of attribute region*

*Range*( $A_{ii}$ ) can be used to represent the difference of means of different attribute values in an attribute  $A_{ij}$ . Obviously, the bigger  $Range(A_{ij})$  represents there is more significant difference in different attribute values in attribute *Aij*. Hence, the *Significant Difference Determination* heuristic is proposed to determine whether there exists the *SDP* in an attribute *Aij* or not.

#### **HEURISTIC 3:** *Significant Difference Determination*

Given an attribute  $A_{ij} = \{V_{ijk} | k = 1, 2, ..., g(i, j)\}\$ , and a measure  $M_k$ <sup>'</sup>, if  $Range(A_{ij})$ is greater than or equal to  $\gamma$ , there exist a *SDP*,  $(A_{ii})$ :  $M_k$ , where  $\gamma$  is significance determination threshold.

#### **EXAMPLE 6:**

Given the attribute *region* and measure *math\_grade'* shown in Table 4.4, the *Range(region)* = 2 has been calculated in EXAMPLE 5. Given  $= 0.4$ ,



Hence, there exists the *SDP*

*(region) : math\_grade (4.3)* 

In general, researchers are interested in investigating the more general human behavior and social phenomenon. If there is a significant difference on the more general phenomenon, they won't usually be interested in the more specific one. Hence, *The Most General SDP First* heuristic is proposed.

#### **HEURISTIC 4:** *The Most General SDP First*

*The Most General SDP First* heuristic is that the general *SDP* is more interesting than the specific *SDP*. The "general" means the higher level *SDP* and fewer dimensions *SDP* is better. Hence,

- Higher-level *SDP* is more interesting than lower-level *SDP*.
- Fewer-dimension *SDP* is more interesting than more-dimension *SDP*.







```
(city): math grade (4.5)
```
If there is a significant difference between different resident regions on measure *math\_grade*, researchers won't usually be interested in whether there is a significant difference between different resident cities on measure *math\_grade* or not.

#### **EXAMPLE 8:**

Given two *SDPs*:

$$
(gender): math\_grade
$$
\n
$$
(4.6)
$$

(gender | city = Taipei) : math\_grade *(4.7)*

If there is a significant difference between different gender on measure *math\_grade*, researchers won't usually be interested in whether there is a significant difference between different gender in measure *math\_grade* for the records only living in Taipei or not.



*The Most General SDP First* heuristic is proposed based on our experiments and discussing with senior researchers. It's just a general phenomenon when researchers find the significant difference. In other words, it will not always be correct at different situations. For example, researchers might also be interested in whether there is a significant difference between different gender on measure *math\_grade* for the records only living in Taipei in EXAMPLE 8. However, the complexity of the *SDPD problem* can be decreased effectively by using *The Most General SDP First* heuristic.

Based on the *Significant Difference Determination* and *The Most General SDP First* heuristics, *SDPMining* algorithm is a greedy algorithm, and it searches the *Data Warehouse* to find the *SDPs* like a BFS search tree. The pseudo code of *SDPMining* algorithm is listed in Table 4.6.



At the beginning, it computes the  $Range(A_{i1})$  of for the first attribute  $A_{i1}$  of each dimension  $D_i$ . If  $Range(A_{i,j})$  is greater than threshold , which means  $A_{i,j}$  is

significant, the rest attributes of dimension  $D_i$  will not be searched due to the heuristic. All the non-significant dimensions will be expanded to the next level and search go on. The following two examples explain *SDPMining* algorithm more clearly.

#### **EXAMPLE 9:**

At the beginning, *SDPMining* algorithm computes the *Range(Ai1)* of for the first attribute, *gender*, *region*, and *father\_education*, of each dimension. Due to the attribute *region* is significant, the attribute *city* will not be searched. The attribute *region* is significant and the attribute *gender* and *father\_education* are not significant. The result is shown in Figure 4.4.



*Figure 4.4: The result after searching the first level in* 

After expanding the non-significant attribute, the result is shown in Figure 4.5.

|                       |                    | Attribute        | Range |
|-----------------------|--------------------|------------------|-------|
|                       |                    | father_education | 1.3   |
|                       |                    |                  |       |
|                       |                    | Attribute        | Range |
|                       | 1723 A             | father_education | 0.7   |
|                       | teplate            |                  |       |
| Attribute<br>Range    |                    | Attribute        | Range |
| 0<br>gender           |                    | gender           | 0.2   |
| 2<br>region           | eleozenfary        |                  |       |
| $420 -$               | <u>iunior_bieb</u> | Attribute        | Range |
| 0<br>father education |                    | gender           | 0.3   |
|                       | sentor_high        |                  |       |
|                       |                    | Attribute        | Range |
|                       | umixersit          | gender           | 0.7   |
|                       |                    |                  |       |
|                       |                    | Attribute        | Range |
|                       | gradbate           | gender           | 0,9   |
|                       |                    |                  |       |
|                       |                    | Attribute        | Range |
|                       |                    | gender           | 0.8   |

*Figure 4.5: The result after searching the second level in* 



*(region) : math\_grade* 

*(father\_education| gender = male) : math\_grade (father\_education| gender = female) : math\_grade (gender| father\_education = senior\_high) : math\_grade (gender| father\_education = university) : math\_grade (gender| father\_education = graduate) : math\_grade* 

#### **EXAMPLE 10:**

At the beginning, *SDPMining* algorithm computes the *Range(Ai1)* of for the first

attribute, *gender*, *region*, and *father\_education*, of each dimension. Due to the attribute *region* is not significant, the attribute *city* is also processed. The attribute *region* is significant and the attribute *region*, *gender* and *father\_education* are not significant. The result is shown in Figure 4.6.

| Attribute        | Range |
|------------------|-------|
| gender           | U. 3  |
| region           | 0. I  |
| city             | 1.2   |
| father education |       |

*Figure 4.6: The result after searching the first level in* 

**MAREA** 

After expanding the non-significant attribute *region*, the result is shown in Figure



4.7.



The following *SDPs* can be found in Figure 4.7:

*(city) : math\_grade (gender| region = north) : math\_grade (father\_education| region = north) : math\_grade (father\_education | region = central) : math\_grade (gender | region = east) : math\_grade* 

#### **4.3.SDP Ranking step**

SDP Ranking step sorts the SDPs in the order of importance by the Range(Aij), and the Standard Deviation of Score. Range(Aij) represents the degree of difference; hence, Range(Aij) can be used to sort the SDPs found in SDP Mining step. In addition, the Standard Deviation of Score can also be used to sort the SDPs because the bigger standard deviation expresses the wider distribution. The pseudo code of SDPRanking algorithm is listed in Table 4.7. For example, there are three patterns of Figure 4.7 as follows:



Since the range of Pattern 1 is greater than Pattern 2 and range of Pattern 2 is equal to Pattern 3, Pattern 1 is more interesting than Pattern 2 and we need observe the standard deviations. Here, the Scores distribution of Pattern 2 and Pattern 3 are denoted as Scores 2 and Scores 3, respectively.

*Scores2: { Score(elementary), Score(junior\_high), Score(senior\_high), Score(*university*), Score(*graduate*) } = { -0.3, 0, 0, 0, 0.2 }* 

```
Scores3: { Score(elementary), Score(junior_high), Score(senior_high), 
Score(university), Score(graduate) } = { -0.3, -0.2, 0.1, 0.2, 0.2 }
```
Since standard deviations of Scores 2 and Scores 3 are 0.2 and 0.23, respectively,

the Pattern 3 is more interesting than Pattern 2.





## **Chapter 5. Experiment**

In this chapter, we design the experiments to evaluate the accuracy and the execution time of the WISDOM. Firstly, we simply explain our design of the experiments. Secondly, we experiment on the accuracy of the WISDOM with parameter and in Section 5.1. Finally, we discuss the issue of the execution time about parameter , dimensions and concept hierarchy in Section 0.

As shown in Figure 5.1, a digital divide data warehouse  $($ having six questionnaire datacube, executive (having six questionnaire datacube, executive (https://

 $\alpha$ , vocational school (a), elementary school ( $\alpha$ ), elementary school ( $\alpha$ ),

 $j$ unior high school ( $j$ and teacher ( $k$ ) is used in this thesis, and its data source is a survey of *the Assessment and Analysis of Establishing the Digital Divide Criteria Indexes and Evaluation for Current K-12 Digital Divide Status in School* (A project of the Ministry of Education, ROC) [24] [25]. In our experiments, the elementary school questionnaire datacube using the star schema is chosen as shown in Figure 5.2.

The elementary school datacube has lots of measures and several dimensions with concept hierarchical structure. For example, the datacube has dimensions like gender (the gender of the students), location (the location which the student lived, and the location has dimension area, city), father education (the education level of the student's father), mother education (the education level of the student's mother), etc., and measure like Q11 ( $\qquad \qquad$ ), Q12 (

$$
), Q13 (
$$

the measure SUM11 16 is the sum of the measures Q11, Q12, Q13…and Q16. SUM11\_16 implies *the quota of well-fine using the computer resource*. In order to

simplify our discussion, we select 3,504 records from the elementary school datacube and call it DB3504. The elementary school datacube has 67,463 records. The following experiments are done on the DB3504.



*Figure 5.1The digital divide data warehouse* (  $($ 



#### **5.1. Accuracy and Recall of the WISDOM**

In this section, we explain experiments briefly and show the results of the accuracy and recall of parameter and . Without loss of the generality, we assume the value of confident level 1- is 95%, and the value of is 0.05.

The accuracy means the probability of the SD pattern found by WISDOM is real significant in the statistic test, and the recall means the percentage of the total SD patterns which WISDOM found. For example, there are 10 SD patterns found by WISDOM and only 7 SD patterns are real significant in the statistical test, and the number of real SD pattern is 14. Hence, the accuracy and recall are 70 % and 50%, respectively.

In order to evaluate the accuracy, we use the statistic tool – SPSS to test and find the entire significant difference pattern amount these dimensions versus the measure SUM11\_16 followed the heuristics of the WISDOM. The chosen dimensions and results of SPSS are shown in Figure 5.3. Hence, we can evaluate the accuracy of the WISDOM by this pattern found manually in the SPSS process.

#### **Dimension**

**Is significant difference**

buddy level3 computer\_stuent\_level3 buddy ie level3 internetTime computer teacher level3 motherEdu fatherEdu citytype teacher\_communication buddy level2 parents buddy ie level2 computer\_stuent\_level2 L region motherIE  $fatherIE$ computer\_teacher\_level2 gender seed XXX and X  *Figure 5.3 The results of the nineteen dimensions versus measure SUM11\_16 using SPSS.* 

#### **5.1.1 Parameter** γ **versus Accuracy and Recall**

In previous section, we have found several significant difference pattern using a manually method. In this section, we evaluate the accuracy and recall of WISDOM by comparing the results of WISDOM and the results of SPSS. Firstly, we assume the value of the parameter is zero. We will discuss the value of in next section. Secondly, in order to simplify the discussion of the SPSS process, we assume the value of the parameter depth is 1. Then several experiments are done with accuracy and recall to evaluate the parameter . The value of parameter ranges from 0.1 to 2 increasing by 0.1. The results of accuracy and recall are shown in Figure 5.4.



*Figure 5.4 The accuracy and recall of WISDOM.*  $=0.1 \times 2$  *increasing by 0.1*  $=0$ , *depth*=1

In Figure 5.4, we can find that the accuracy intersect recall in the section  $(0.1~0.3)$  of . Hence, some experiments are done with accuracy and recall to evaluate the parameter . The value of parameter ranges from 0.1 to 0.3

increasing by 0.01. The results of accuracy and recall are shown in Figure 5.5

In Figure 5.5, we can find that the recall will almost be 100% when the is small than 0.16. When the is 0.16, the accuracy of WISDOM is 87.5%. In addition, if the gamma is greater than 0.25 the accuracy will almost be 100% but the recall will decrease seriously. Hence the value of the parameter which we suggested is 0.16 because it has the higher accuracy 87.5% and the ideal recall 100.



*Figure 5.5 The accuracy and recall of WISDOM.* = 0.1~0.32 increasing by 0.01 = 0, depth=1

#### **5.1.2 Parameter •• versus Accuracy and Recall**

We have got the best value of parameter in Section  $5.1.1$ . In this section, we will discuss the relationship of the parameter versus accuracy.

Firstly, we assume the value of parameter is 0.16, and then some experiments are done with the accuracy and recall to evaluate the parameter . The value of is from 0 to 2 increasing by 0.1. The results are show in Figure 5.6. we can find the recall is decreasing seriously when the value of is greater than 1.9. Hence the value of the parameter which we suggested is not greater than 1.9 and we will discuss the relationship between parameter and execution time in next section.



*Figure 5.6 The accuracy and recall of WISDOM =0.16, depth=1, =0~2 increasing by 0.1* 

#### **5.2.Performance of the WISDOM**

We have already known relationship between accuracy and recall versus the value of parameter and . In this section, we show the results of the performance, execution time, of WISDOM in different value of parameter and depth, number of dimensions and number of concept hierarchies.

#### **5.2.1 Parameter •• versus Execution Time**

Firstly, we evaluate the execution time of the WISDOM. The value of is from 0 to 2 increasing by 0.1. The results are shown in Figure 5.7. After observing もも見見され Figure 5.7, we can find the trend of the execution time of WISDOM is decreasing when the beta is growing up.



*Figure 5.7 The execution time of WISDOM =0.16,depth=1, =0~2 increasing by 0.1* 

Secondly, we compare the accuracy which mentioned in the Figure 5.6 of the front section and the execution time of the WISDOM mentioned in Figure 5.7. In Figure 5.8, the results show that the execution time decreases about 10% when the is greater than 1.4 and the accuracy keeps at least 80%. Hence we suggest the value of parameter is 1.4.



In this section, several experiments are done with the execution time to evaluate the parameter depth. We assume the value of parameter is 3 and fix is 0. The results are shown in Figure 5.9.

In this experiment, we prefer to discuss the relationship without some heuristics of WISDOM. Since the maximum range is 2 and we assume the value of parameter

 is 3, we can guarantee the case is the worst case of execution time without performing some heuristics. For example, the heuristic 4, "*The Most General SDP First*", will prune lots of search space and save much execution time. We can compare the execution time in Figure 5.7 and Figure 5.10 mentioned in the next section. The execution time using heuristic 4 is 2,922ms (The DB3504 has more than 12 dimensions), and the execution without heuristic1 is longer than 250,000ms. And in Figure 5.8, we can find that the value of parameter also affects the execution time deeply.

In Figure 5.9, the execution time is growing up in an exponential trend. Hence, we suggest the value of the parameter depth is smaller than 3.



*Figure 5.9 The execution time of WISDOM. =3, depth=1~5 increasing by 1, =0.*

#### **5.2.3 Dimensions versus Execution Time**

Several experiments are done with the execution time to evaluate the number of dimensions. The number of dimensions ranges form 3 to 12, the value of parameter

 is 0 and the value of parameter is 3 as described in section 5.2.2. In Figure 5.10, we can observe that the execution time of WIDSOM almost linearly growing with number of dimensions.



*Figure 5.10 The relationship between number of dimensions and execution time. =3, depth=3, =0.*

#### **5.2.4 Concept Hierarchy versus Execution Time**

We have known the relationship of dimensions and execution time which is almost growing linearly. In this section, some experiments are done with the execution time to evaluate the number of level per dimension. We done the experiments as follows.

Firstly, we also assume the value of parameter is  $3$ , is 0 and the depth is 3 as described in section 5.2.2. And the number of dimension ranges from 3 to 7 and increasing by 1.. We discussion the WISDOM on three cases, each case has k-levels per dimension. The value of k ranges from 1 to 3 and increasing by 1. In Figure 5.11, we can observe that the execution time of WISDOM increases rapidly when the concept hierarchy gets more complex.



*Figure 5.11 The relationship between concept hierarchy and execution time. =3, depth=3, =0.* 

## **5.3. Experiments Summ**

We applied the WISDOM to the digital divide data warehouse and we found 896 some interesting patterns. For example, the pattern, "(computer\_teacher\_level2|seed='''):SUM11\_16", implies these is a significant difference between different groups of computer teacher level 2 in the computer seed school, and the researchers are unaware this pattern.

## **Chapter 6. Conclusion**

In the questionnaire analysis, finding whether there is a significant difference between two or more groups in one measure is one of the major problems which social science researchers are concerned about. However, finding possible significant differences is difficult for social science researchers. We call it Significant Difference Unawareness issue. In order to overcome the Significant Difference Unawareness issue, in this thesis, we firstly build a data warehouse by integrating the questionnaire data and secondary data. Secondly, the WISDOM algorithm is proposed to find the possible significant differences from the data warehouse semi-automatically.



The results of experiments show that the suggested value of the parameter is 0.16 because there is a higher accuracy 87.5% and an ideal recall 100%. The execution time decreases about 10% when the is greater than 1.4 and the accuracy keeps at least 80%. Hence, we suggest the value of parameter is between  $0 \sim 1.4$ . Furthermore, several experiments are done with the execution time to evaluate dimensions and levels of concept hierarchy. The execution time is rapidly growing up when the number of dimensions or the number of levels of concept hierarchy is increasing.

In the near future, we will aim to apply the WISDOM in several domains like digital divide, statistic for business and economics. Besides, we will discuss the relationship between the value of parameter and the amount of records.

Furthermore, the parameter implies the degree of the difference. Hence, we will also discuss the relationship between degree of difference and the parameter in the future.



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