## Polarizing terahertz waves with nematic liquid crystals

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A Feussner-type terahertz polarizer with a nematic liquid crystal (NLC) layer between two fused-silica prisms is demonstrated. The polarization factor and extinction ratio of the NLC-based terahertz polarizer can exceed 0.99 and  $10^{-5}$ , respectively. © 2008 Optical Society of America *OCIS codes:* 230.1360, 230.3720, 260.1440, 260.3090, 260.5430, 300.6495.

With dramatic advances of terahertz (THz) technology [1], high-quality quasi-optic [2] components such as phase shifters, filters, and polarizers for THz are in great demand recently. For polarizing THz waves, wire-grid-type elements are widely used and commercially available [3]. Nonetheless, the manufacturing of high-quality THz wire-grid polarizers is a difficult process, and the finite conductivity of wires and the irregularities of grids cause loss in such polarizers, especially at the higher THz frequencies. Another promising THz polarizer employing a multigrid structure has been proposed [4]. A method for manufacturing wire-grid-type polarizers by using an inkjet printer was proposed and demonstrated by Kondo et al. [5]. They reported a degree of polarization or polarization factor greater than 0.90 for this device.

Birefringent crystals have been used to construct Nicol, Wollaston, and various Glan-type polarizers for lightwave applications. The Feussner-type design of birefringent polarizers [6] consists of an anisotropic layer inserted between a pair of isotropic prisms. In this device, the two polarization modes encounter different refractive indices at the prism-film interface. By judiciously choosing the angle of incidence and the refractive indices of the coupled prisms, one of the polarization components undergoes total internal reflection (TIR), while the other component propagates out of the device unimpeded. Different materials used with this design, e.g., sodium nitrate [7], and polymer films [8] have been proposed and demonstrated at optical wavelengths. In this work, we demonstrate a novel design of Feussner-type THz polarizers by exploiting the birefringence and transparency of nematic liquid crystals (NLCs) in the far infrared [9–13].

A schematic drawing of the proposed polarizer is shown in Fig. 1. From the top (x-z plane) of a rectangular parallelepiped made of fused silica (GE124, General Electric), we cut a diagonal groove for filling NLC (E7, Merck). Afterwards, the groove was sealed with a piece of Teflon. Three polarizers with different groove widths, d=0.75, 1.25, and 1.95 mm, respectively, were fabricated to study the thickness dependence of the LC layer on polarizing properties of the

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device. In the assembled polarizer, there was also a pair of permanent magnets (sintered Nd-Fe-B) that provided a magnetic field (>0.2 Tesla) to be sufficiently strong to fully align LC molecules along the direction of the field. The rectangular parallelepiped with the NLC layer and magnets can be rotated together about the propagation direction of the THz wave (*x* axis). The rotation angle,  $\psi$ , is defined as the angle between the direction of magnetic field and the *y* axis.

In the frequency ranging from 0.2 to 1.0 THz, the refractive index of fused silica, ordinary and extraordinary refractive indices of E7 are  $n_q = 1.95$ ,  $n_o = 1.58$ , and  $n_{\rho} = 1.71$ , respectively [11]. At the fused-silica–LC interface, the corresponding critical angle for total internal refraction (TIR),  $\theta_{co}$  and  $\theta_{ce}$  are 54.12° and 61.27°, respectively. Thus we designed the groove angle (incident angle) in the polarizer,  $\varphi = 56 \pm 0.5^{\circ}$  (as shown in Fig. 1). At  $\psi = 90^{\circ}$ , the director is perpendicular to the polarization direction of the THz wave (o-ray), satisfying the requirement for TIR. At  $\psi = 0^{\circ}$ , the director is parallel to the electric field direction of the THz wave (e-ray), allowing the electromagnetic wave to pass through. The device can thus be operated as a polarizer, as long as  $n_{\rm e} > 1.62$  and  $n_{\rm o}$ < 1.61. Based on the temperature-dependent indices of refraction of E7 measured in our lab (unpub-



Fig. 1. (Color online) Schematic drawing of the THz Feussner polarizer with a LC layer. The dimensions of the device,  $l \times w \times h$ , are 22.3 mm  $\times$  15 mm  $\times$  15 mm. The polarization direction of the THz wave incident on the polarizer is along the *y* axis.

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lished), we conclude that the polarizer will work reliably below 57°C, although the nematic range of E7 is from -10°C to 61°C. To guard against temperature fluctuations due to environmental perturbations, one can adopt typical measures for temperature control. The devices were characterized by using a photoconductive-antenna-based THz time-domain spectrometer (THz-TDS) described previously [14]. A pair of parallel wire-grid polarizers (Specac, GS57204) was placed before and after the device to ensure the polarization state of the THz beam transmitting through the device. The experiments were conducted at room temperature ( $23\pm0.5$ °C).

For e-ray, the THz wave incident on the polarizer experienced partial reflection and refraction at the LC-fused-silica interface and attenuation by the LC layer as well as fused-silica prisms. In the experiments, we take a rectangular solid fused silica identical to the proposed polarizer, except for the groove as the reference. The transmittance of the polarizer is normalized with respect to that of the reference. The transmitted power spectrum for the e-ray of the THz signal of our polarizer is thus given by [15]

$$T_e(f) = T'_e e^{-4\pi\kappa_e f d'/c},$$
 (1)

where

 $T'_e = (4n_q n_e \cos \varphi \cos \theta_{re})^2 / (n_q \cos \varphi + n_e \cos \theta_{re})^4$ = 0.801

is the power transmittance for the e-ray due to the two fused-silica–LC interfaces,  $\kappa_e = 0.007$  is the extraordinary extinction coefficient of E7 [11], f is the frequency of the THz wave, c is the speed of light in vacuum,  $d' = d/\cos \theta_{re}$  is the propagation distance of the refracted THz wave in the LC layer, and  $\theta_{re}$  is the refraction angle for the e-ray.

For the o-ray, the transmitted intensity of THz signal can be written as [15]

$$T_o(f) = e^{-4\pi\kappa_0 f d/c} e^{-2\alpha d}, \qquad (2)$$

where  $\kappa_o = 0.020$  is the ordinary extinction coefficient of E7 [11] and  $\alpha = 2\pi f / c [(n_q \sin \varphi/n_o)^2 - 1]^{1/2}$  is the decay factor in amplitude of the THz wave in the LC medium.

In this work, the polarizers are characterized by their degree of polarization or polarization factors and extinction ratios. The former, P, is defined by [16]

$$P = \frac{T_e(f) - T_o(f)}{T_e(f) + T_o(f)},$$
(3)

where  $T_e(f)$  and  $T_o(f)$  are spectral transmittance for e-ray and o-ray, respectively. For an ideal polarizer, P=1, according to Eq. (3). The extinction ratio is defined by

$$E = \frac{T_o(f)}{T_e(f)}.$$
(4)

For an ideal polarizer, E = 0.

The normalized spectral transmittances of e-ray and o-ray for the three polarizers we fabricated are shown in Fig. 2. The theoretical predicted transmittance according to Eqs. (1) and (2) are also plotted in Fig. 2. The experimental results are in good agreement with theory. The transmittances of the THz wave for o-ray declines significantly with increasing LC layer thickness. This is a manifestation of the higher extinction coefficients of E7 for o-ray.

The peak values of the THz field transmitted through the polarizer rotated at different angles  $\psi$ with respect to the incident polarization, normalized to the peak value of THz field at  $\psi=0^{\circ}$ , are plotted in the inset of Fig. 3. The agreement with the theoretical curve according to Malus' law is excellent.

In Fig. 3, we show the experimental data and theoretical predictions of polarization factors of the three LC THz polarizers. For the polarizer with a 0.75-mm-thick LC layer, P > 0.95 when f > 0.44 THz. It is, however, not an effective one in the lower sub-THz frequency ranges, as the LC layer thickness is comparable or shorter than that of the wavelengths. The polarizer with a 1.95-mm-thick LC layer, on the other hand, exhibits the best P value, which is greater than 0.99 for f > 0.20 THz. For the polarizer with a 1.25-mm-thick LC layer,  $P \sim 0.99$  for f > 0.32 THz. These results are better than those of the printed wire-grid-type polarizers (0.90 at 0.5 THz) [5] and wire-grid polarizers reported in [17] (0.93 at 2.3 THz). Commercially available far-infrared polarizers typically are specified with degrees of polarization ranging from 95% to better than 99.99%. The P values of our polarizers rise and approach unity with increasing thickness of the LC layer, because of the higher extinction coefficient of LC for o-rays.

Theoretical and experimental extinction ratios of the three polarizers studied are illustrated in Fig. 4. The best *E* values of the polarizers with 1.95-, 1.25-, and 0.75-mm-thick LC layers are  $10^{-5}$ ,  $10^{-5}$ , and  $10^{-3}$ 



Fig. 2. (Color online) Normalized transmittance of three polarizers studied. The solid and open marks represent experimental data for e-ray and o-ray, respectively. The black circles, red squares, and blue triangles represent data for polarizers with 1.95-, 1.25-, and 0.75-mm-thick LC layers. The solid and dashed curves are the theoretical curves for e-ray and o-ray, respectively.



Fig. 3. (Color online) Polarization factors of THz LC polarizers. The black circles, red squares, and blue triangles represent the polarizer with 1.95-, 1.25-, and 0.75-mm-thick LC layers, respectively. The marks and curves are the experimental data and theoretically predicted polarization factors. The inset shows the normalized peak transmission of the THz wave propagated through the THz LC polarizer as a function of the rotation angle,  $\psi$ . The solid curve is the theoretical curve according to Malus' law.

at 0.50, 0.70, and 0.75 THz, respectively. Theoretically, the E values of polarizers with 1.95-mm-thick and 1.25-mm-thick LC layers could be as high as  $10^{-11}$  and  $10^{-7}$ , respectively. The discrepancy with the experimental data can be explained as due to the reduced transmittance of the polarizers at high fre-



Fig. 4. (Color online) Calculated and measured extinction ratios of three THz LC polarizers. Black (solid), red (dashed), and blue (dotted) lines represent theoretical extinction ratios of the THz polarizer with 1.95-, 1.25-, and 0.75-mm-thick LC layers. Black circles, red squares, and blue triangles represent experimentally determined extinction ratio of THz polarizer with 1.95-, 1.25-, and 0.75-mm-thick LC layers.

quencies and the limit of the signal-to-noise ratio of our THz-TDS ( $\sim 10^{-5}$ ). From Eqs. (3) and (4), we know that the *P* and *E* values can be improved by increasing the thickness of LC layer, with the penalty of greatly reduced  $T_e$  values. The three polarizers with 0.75-, 1.25-, and 1.95-mm-thick LC layers are thus suitable for f>0.7, 0.7>f>0.45, and 0.45>f>0.3 THz, respectively.

In summary, a Feussner-type THz prism polarizer using a NLC layer is demonstrated. For the polarizer with a 1.95-mm-thick LC layer, the polarization factor is better than 0.99 from 0.20 to 1.00 THz, and the extinction ratio reaches  $10^{-5}$ . This is comparable with that of the common wire-grid polarizers. By choosing different thicknesses of the LC, one can achieve a similar level of performance for THz polarizers in different frequency ranges.

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