# 行政院國家科學委員會專題研究計畫 期中進度報告

## 行為研究中的複決定係數(1/2)

<u>計畫類別</u>: 個別型計畫 <u>計畫編號</u>: NSC92-2118-M-009-009-<u>執行期間</u>: 92 年 08 月 01 日至 93 年 07 月 31 日 執行單位: 國立交通大學管理科學學系

計畫主持人: 謝國文

### 報告類型: 精簡報告

<u>處理方式:</u>本計畫可公開查詢

### 中 華 民 國 93年4月21日

#### SUPPRESSION SITUATIONS IN MULTIPLE LINEAR REGRESSION

Gwowen Shieh Department of Management Science National Chiao Tung University Hsinchu, Taiwan 30050, R.O.C. Email: gwshieh@mail.nctu.edu.tw

#### Abstract

In both behavioral and statistical sciences, the concept of suppression within the context of multiple linear regression has been the subject of considerable discussion, with much of the controversy focusing on the advantages and disadvantages associated with the definitions for this counterintuitive condition. This paper proposes alternative expressions for the two most prevailing definitions of suppression without resorting to the standardized regression modeling. The formulation provides a simple basis for the examination of their relationship. For the two-predictor regression, we demonstrate that the previous results in the literature are incomplete and oversimplified. The proposed approach also allows a natural extension for multiple regression with more than two predictor variables. It is shown that the conditions under which both types of suppression can occur are not fully congruent with the significance of the partial *F* test. This implies that all the standard variable selection techniques: backward elimination, forward selection and stepwise regression procedures can fail to detect suppression situations. This also explains the controversial findings in the redundancy or importance of correlated variables in applied settings. Furthermore, informative visual representations of various aspects of these phenomena are provided.

#### **1. Introduction**

Multiple regression analysis is one of the most widely used of all statistical methods. One of the purposes of multiple regression is to investigate the relative importance of a number of predictor variables for their relationship with a response variable. The predictor variables are typically correlated among themselves and therefore there is no simple answer concerning how to assess their individual contribution. Several measures have been proposed such as t values, standardized regression coefficient, increment in  $R^2$ , and correlation coefficients. Related comments and discussions can be found in Bring (1995, 1996) and their references. In this article, we focus on the concept of suppression that occurred when comparing the contribution of individual predictor variable with and without the presence of other predictor variables. Since Horst (1941) first discussed that a predictor variable can be totally uncorrelated with the response variable and still improves prediction by virtue of being correlated with other predictors, much discussion has been made concerning the concept of suppression in behavioral sciences. For detailed reviews of different approaches to defining suppression, see Conger (1974), Velicer (1978), Tzelgov & Henik (1981, 1991), Holling (1983) and Smith, Ager & Williams (1992).

In this study, we are especially concerned with the definitions proposed by Conger (1974) and Velicer (1978) because they have drawn the most attention in both behavioral and statistical research. Essentially, Conger's definition is based on the standardized regression coefficient and simple correlation, whereas Velicer's definition is referred to the squared multiple and simple correlations or equivalently the increment in  $R^2$ . As Pedhazur (1997) pointed out, the definition and interpretation of suppression, however, remain controversial. This is partly because the definitions of Conger (1974) and Velicer (1978) are fundamentally

different with respect to model formulation. Specifically, the comparisons between these two definitions are restricted to the special case of standardized regression model with two predictors as shown in Tzelgov & Henik (1981). Their results suggest that the cases of Conger's suppression situations subsume those under Velicer's definition. However, it is not clear exactly how and when such phenomenon can happen with respect to the interrelation of the response and two predictor variables. Although the aforementioned articles intended to address different aspects of the two definitions, it seems that the arguments are not settled. The major problem is the lack of schematic approach to the examination and comparison of the two definitions. The needed approach should be general enough to lay the same basis for the comparability of the two definitions and at the same time, should be precise enough to provide both concrete demonstration and visual representation for their similarities and differences.

Interestingly, the type of suppression studied in statistical literature is in agreement with the definition of Velicer (1978). The geometric description, numerical example and algebraic argument for the two-predictor regression have been given in Schey (1993), Neter et al. (1996) and Sharpe & Roberts (1997), respectively. However, there is no extension beyond the two-predictor case. As indicated in Velicer (1978), the advantage of defining suppression situation in terms of the increment in  $R^2$  is that such formulation can be extended immediately from the special case of two predictors to the general *p*-predictor case (p > 2). In relation to the notion of increase in  $R^2$ , the partial *F* test is the standard procedure for selecting important predictors. It should be extremely informative to clarify the relationship of both definitions of suppression with the partial *F* test in a general framework of multiple regression.

This article aims to provide alternative expressions of Conger's and Velicer's definitions of suppression that not only take into account the problem of comparability, but also accommodate the extension to general multiple regression and permit thorough investigation of their relationship algebraically and graphically. In Section 2, we provide the revised constructions of the two criteria of suppression and present the important details of the conditions under which different types of suppression can occur. In Section 3, the concept of suppression is contrasted with the detection of important predictors in terms of the partial F test in variable selection. Finally, Section 4 contains some final remarks.

#### 2. Two definitions of suppression

Consider the general linear regression model with response variable *Y* and *p* ( $\geq 2$ ) predictor variables *X*<sub>1</sub>, ..., *X<sub>p</sub>*:

$$Y_{i} = \beta_{0} + \sum_{j=1}^{p} X_{ij} \beta_{j} + \varepsilon_{i}, i = 1, ..., n,$$
(1)

where  $Y_i$  is the value of the response variable;  $\beta_0$ ,  $\beta_1$ , ...,  $\beta_p$  are parameters;  $X_{i1}$ , ...,  $X_{ip}$  are the known constants of predictors  $X_1$ , ...,  $X_p$ , and  $\varepsilon_i$  are *iid*  $N(0, \sigma^2)$  random variables. We are interested in the occurrence of suppression in the general linear regression model (1). First, consider the definition of suppression defined by Conger (1974) as follows. A suppression situation exists whenever

$$|\hat{\beta}_b^*| > |r_{Yb}|,\tag{2}$$

for some b, b = 1, ..., p, where  $\hat{\beta}_b^*$  is the least squares estimator of the standardized regression coefficient (beta weight, beta coefficient) and  $r_{Yb}$  is the coefficient of correlation between *Y* and *X*<sub>b</sub>.

Next, Velicer (1978) defined a suppression situation in terms of the squared multiple and simple correlations:

$$R^2 > R_{Ya}^2 + r_{Yb}^2, (3)$$

for some b, b = 1, ..., p, where  $R^2$  is the squared multiple correlation coefficient of Y with  $(X_1, ..., X_p)$ , and  $R^2_{Ya}$  is the squared multiple correlation coefficient of Y with  $(X_1, ..., X_{b-1}, X_{b+1}, ..., X_p)$ ; that is,  $X_b$  is omitted from  $(X_1, ..., X_p)$ .

At first sight, the two definitions given in (2) and (3) may be fundamentally different. However, they are intertwined and are closely related. For the purpose of demonstrating their similarities and differences, we propose to consider two alternative formulations of suppression for providing important connection between Conger's and Velicer's definitions.

Definition 1. For regression model (1), a C-suppression situation exists if

$$|\hat{\beta}_b| > |\hat{\beta}_b^s| \tag{4}$$

for some b, b = 1, ..., p, where  $\hat{\beta}_b$  is the usual least squares estimator of the regression coefficient  $\beta_b$  in (1), and  $\hat{\beta}_b^S$  is the least squares estimator of the slope coefficient for the simple regression model of response *Y* and predictor  $X_b$ . It is important to note that throughout this article, we assume the regression model (1) is applicable.

It is well-known that the least squares estimators of the standardized regression coefficients associated with model (1) can be written as  $\hat{\beta}_b^* = \hat{\beta}_b(s_b/s_Y)$  with  $s_Y$  and  $s_b$  being the respective square root of  $s_Y^2$  and  $s_b^2$ , where

$$s_Y^2 = \sum_{i=1}^n (Y_i - \bar{Y})^2, s_b^2 = \sum_{i=1}^n (X_{ib} - \bar{X}_b)^2,$$

and,  $\overline{Y}$  and  $\overline{X}_b$  are the respective sample means of the Y and the  $X_b$  observations. Moreover,

the coefficient of correlation between Y and  $X_b$  can be expressed as  $r_{Yb} = \hat{\beta}_b^s(s_b/s_Y)$  with respect to the simple linear regression for Y with  $X_b$ . Hence, the condition (2) of suppression proposed in Conger (1974) is equivalent to  $|\hat{\beta}_b| > |\hat{\beta}_b^s|$ , which is exactly the condition of C-suppression defined in (4). Note that our formulation in Definition 1 is not limited to the case of standardized regression and consequently Definition 1 subsumes Conger's (1974) definition as a special case. Essentially, the proposed definition of C-suppression in (4) solves the comparability problem for the differences in the range of  $\hat{\beta}_b^*$  and  $r_{Yb}$  raised by Velicer (1978) that  $|r_{Yb}|$  is bounded by unity and  $|\hat{\beta}_b^*|$  is not. Furthermore, it provides useful connection with Velicer's definition of suppression shown next.

Along the same line of comparability issue, a little reflection should make one wary of the comparison of  $\hat{\beta}_b$  and  $\hat{\beta}_b^s$  because of the differences in the units involved. In order to permit comparison of the estimated regression coefficients  $\hat{\beta}_b$  and  $\hat{\beta}_b^s$  in the same units, the adjustment with respect to the estimated variance is employed in the following formulation.

Definition 2. For regression model (1), a V-suppression situation exists if

$$|t_b| > |t_b^S| \tag{5}$$

for some b, b = 1, ..., p, where

$$t_b = \frac{\hat{\beta}_b}{\{\hat{\sigma}^2(\hat{\beta}_b)\}^{1/2}} \text{ and } t_b^S = \frac{\hat{\beta}_b^S}{\{\hat{\sigma}^2(\hat{\beta}_b^S)\}^{1/2}},$$

and  $\hat{\sigma}^2(\hat{\beta}_b)$  and  $\hat{\sigma}^2(\hat{\beta}_b)$  are the estimated variance of  $\hat{\beta}_b$  and  $\hat{\beta}_b^s$ , respectively.

Under the model assumption (1), it can be shown that

$$\hat{\sigma}^2(\hat{\beta}_b) = \frac{\hat{\sigma}^2}{s_b^2(1 - R_{ba}^2)} \text{ and } \hat{\sigma}^2(\hat{\beta}_b^S) = \frac{\hat{\sigma}^2}{s_b^2}, \tag{6}$$

where  $\hat{\sigma}^2 = SSE/(n - p - 1)$  is the estimator of  $\sigma^2$ , *SSE* is the usual error sums of squares, and  $R_{ba}^2$  is the squared multiple correlation coefficient of  $X_b$  with  $(X_1, ..., X_{b-1}, X_{b+1}, ..., X_p)$ . Note that both  $t_b$  and  $t_b^S$  have a noncentral *t* distribution with n - p - 1 degrees of freedom. Also the estimators  $\hat{\beta}_b$  and  $\hat{\beta}_b^S$  can be expressed as follows

$$\hat{\beta}_b = \frac{r_{Y(b,a)}}{\left(1 - R_{ba}^2\right)^{1/2}} \cdot \left(\frac{s_Y}{s_b}\right) \text{ and } \hat{\beta}_b^s = r_{Yb}\left(\frac{s_Y}{s_b}\right), \tag{7}$$

where  $r_{Y(b,a)}$  is the semipartial correlation coefficient of *Y* with  $X_b$  and with  $X_b$  adjusted for  $(X_1, ..., X_{b-1}, X_{b+1}, ..., X_p)$ . Utilizing the results in (6) and (7), the condition (5) of V-suppression could be formulated as

$$|\boldsymbol{r}_{\boldsymbol{Y}(b,a)}| > |\boldsymbol{r}_{\boldsymbol{Y}b}|,\tag{8}$$

and equivalently,  $r_{Y(b,a)}^2 > r_{Yb}^2$  or  $R^2 - R_{Ya}^2 > r_{Yb}^2$  for  $r_{Y(b,a)}^2 = R^2 - R_{Ya}^2$ . For more detailed discussions of partial and semipartial correlations, see Pedhazur (1997, Chapter 7). Consequently, we can see that Definition 2 of V-suppression defined in (5) is the same as Velicer's (1978) definition of suppression given in (3). However, we believe that the revised expressions for C-suppression in (4) and V-suppression in (5) are more appealing than other approaches of conceiving the conceptual relationship of Conger's and Velicer's definitions of suppression. Furthermore, the mathematical relationship between Conger's and Velicer's definitions of conceiving the considering the alternative form of (4) for C-suppression. Equation (7) enables us to rewrite (4) as follows:

$$\frac{|r_{Y(b,a)}|}{(1-R_{ba}^2)^{1/2}} > |r_{Yb}|$$
(9)

or  $r_{Y(b,a)}^2/(1 - R_{b,a}^2) > r_{Yb}^2$ . Since  $r_{Y(b,a)}^2 > r_{Yb}^2$  implies  $r_{Y(b,a)}^2/(1 - R_{b,a}^2) > r_{Yb}^2$  for  $R_{b,a}^2 \in [0, 1)$ , we conclude from (8) and (9) that the occurrences of C-suppression subsume those of V-suppression as special cases.

In order to understand the features of both types of suppression defined above, we begin by focusing on the case of two-predictor regression and then extend the discussion to the general multiple regression situations.

#### 2.1 Two-Predictor Regression

For p = 2, model (1) reduces to

$$Y_i = \beta_0 + X_{i1}\beta_1 + X_{i2}\beta_2 + \varepsilon_i, i = 1, ..., n.$$

In this case, it follows from (4) that a C-suppression situation exists if

$$\frac{|r_{Y_j} - r_{12}r_{Y_k}|}{1 - r_{12}^2} > |r_{Y_j}|, \tag{10}$$

where  $j \neq k$  with j, k = 1 and 2, and  $r_{12}$  is the coefficient of correlation between  $X_1$  and  $X_2$ . To lay the basis for developing a simplified view and providing a concise visualization of the suppression situations, we define

$$\gamma = r_{Y2}/r_{Y1}.$$

Since the designation of  $X_1$  and  $X_2$  is arbitrary, as long as only one of  $r_{Y_1}$  and  $r_{Y_2}$  is zero,  $\gamma$  can be set as zero. The case that both  $r_{Y_1}$  and  $r_{Y_2}$  are zero will be excluded because all the least squares estimators  $\hat{\beta}_1$ ,  $\hat{\beta}_2$ ,  $\hat{\beta}_1^s$ , and  $\hat{\beta}_2^s$  are obviously zero without practical meaning. We are especially concerned with the cases that  $X_1$  alone,  $X_2$  alone or both are suppressors. By definition, predictor  $X_k$  is a suppressor with respect to C-suppression if condition (10) holds. In terms of the definition of  $\gamma$ , it can be shown that both predictors  $X_1$  and  $X_2$  are suppressors simultaneously or there is mutual or reciprocal C-suppression if

$$\gamma < r_{12}/(2 - r_{12}^2)$$
 or  $\gamma > (2 - r_{12}^2)/r_{12}$  for  $0 < r_{12} < 1$ ;  
 $\gamma < (2 - r_{12}^2)/r_{12}$  or  $\gamma > r_{12}/(2 - r_{12}^2)$  for  $-1 < r_{12} < 0$ 

Predictor  $X_1$  is the only suppressor if

$$1/r_{12} < \gamma < (2 - r_{12}^2)/r_{12}$$
 for  $0 < r_{12} < 1$ ;  
 $(2 - r_{12}^2)/r_{12} < \gamma < 1/r_{12}$  for  $-1 < r_{12} < 0$ .

On the other hand, predictor  $X_2$  is the only suppressor if

$$r_{12}/(2 - r_{12}^2) < \gamma < r_{12}$$
 for  $0 < r_{12} < 1$ ;  
 $r_{12} < \gamma < r_{12}/(2 - r_{12}^2)$  for  $-1 < r_{12} < 0$ .

Figure 1 presents the occurrence of C-suppression for combinations of  $r_{12}$  and  $\gamma$ . The dotted areas stand for the occurrence regions of C-suppression. The areas marked with "C" represent the occurrence of mutual C-suppression. Those areas marked with "C1" or "C2" represent the occurrences of single C-suppression with  $X_1$  or  $X_2$  as the only suppressor, respectively. We believe that Figure 1 can communicate the results of C-suppression more effectively than the respective Figure 1 in Conger (1974) or Tzelgov & Henik (1991), where the identification of suppression was not directly related to correlations or was indirectly presented with selected values of  $\gamma$ .

For the occurrence of V-suppression situation, it can be shown that the condition (5) reduces to

$$\frac{|r_{Y_j} - r_{12}r_{Y_k}|}{\sqrt{1 - r_{12}^2}} > |r_{Y_j}|, \tag{11}$$

where  $j \neq k$  with j, k = 1 and 2. Alternatively, the condition (11) of V-suppression in terms of  $r_{12}$  and  $\gamma$  is

$$\gamma < \left(1 - \sqrt{1 - r_{12}^2}\right)/r_{12} \text{ or } \gamma > \left(1 + \sqrt{1 - r_{12}^2}\right)/r_{12} \quad \text{for } 0 < r_{12} < 1;$$
  
$$\gamma < \left(1 + \sqrt{1 - r_{12}^2}\right)/r_{12} \text{ or } \gamma > \left(1 - \sqrt{1 - r_{12}^2}\right)/r_{12} \quad \text{for } -1 < r_{12} < 0.$$

With two predictors (p = 2), it is easy to see that (3) corresponds to the inequality between the coefficient of determination and the sum of two squared simple correlation coefficients:  $R^2 > r_{Y1}^2 + r_{Y2}^2$  or the inequality between the extra sum of squares and the sum of squares for simple regression. Related comments and discussions can be found in Currie & Korabinski (1984), Hamilton (1987), Bertrand & Holder (1988), Schey (1993), Sharpe & Roberts (1997), and Shieh (2001). However, these articles do not cover the relationship between different definitions of suppression.

Unlike that C-suppression may be single or mutual, it is important to note that V-suppression is always mutual, see Velicer (1978). As visual supplement, Figure 1 also presents the occurrence of V-suppression by areas covered in horizontal lines and marked with "V". It can be seen from the plot that V-suppression is a subset of C-suppression, as pointed out in Tzelgov & Henik (1981). Nevertheless, it can be more precise that V-suppression is encompassed by mutual C-suppression as a special case, although their differences are marginal. This reveals that the figure in Tzelgov & Henik (1981) is oversimplified and questionable. Furthermore, it should be clear that our Figure 1 conceives the occurrences of different suppressions more effectively than Figure 2 of Tzelgov & Henik (1991).

#### 2.2 Multiple Regression

We consider the general setup of multiple regression with at least three predictors in the

model. For the purpose of permitting clear and informative visual representation, we define  $\Gamma = r_{Y(b,a)}/r_{Yb}$ . It follows from (9) that the condition of C-suppression is  $|\Gamma| > (1 - R_{ba}^2)^{1/2}$ , whereas the condition of V-suppression in (8) is  $|\Gamma| > 1$  with proper  $r_{Yb}$  and  $R_{ba}^2$ . The relation between both types of suppression is presented in Figure 2 for combinations of  $R_{ba}^2$  and  $\Gamma$  where "C" and "V" denote the C- and V-suppression situations, respectively. Similar results for Velicer's suppression situations have been shown in Smith et al. (1992) and they also extended the discussion to relations between two sets of predictors. However, the emphasis here is on the relation between different types of suppression. In addition, it should be noted that both definitions (4) and (5) treat the p - 1 predictors ( $X_1, ..., X_{b-1}, X_{b+1}, ..., X_p$ ) as a whole that lead to suppression.

#### 3. Suppression and variable selection

In multiple regression, variable selection procedures are commonly used to identify the legitimate variables and discard those that are not useful. All the backward elimination, forward selection and stepwise regression procedures are the typical algorithms for selecting the best subset of predictor variables. These procedures determine whether a predictor should be added to or deleted from the candidate set of predictor variables according to the significance or non-significance of the partial F test at each step. As shown in the previous section, the contribution of a predictor can be enhanced in the presence of other predictors for the intercorrelation or multicollinearity among them. Hamilton (1987) pointed out the inability of the forward selection technique to detect important predictors and recommended backward elimination as a more robust alternative for such seemingly paradoxical situations.

At each stage of the variable selection procedures with predictors  $(X_1, ..., X_p)$ , the partial

*F* test statistic can be written as  $F_b = t_b^2$ , where  $F_b$  follows the *F* distribution with (1, n - p - 1)degrees of freedom or  $F_{n-p-1}^1$ , and  $t_b$  is defined in (5) which follows a *t* distribution with n - p - 11 degrees of freedom under the hypothesis  $\beta_b = 0$ . The predictor  $X_b$  is retained with the subset of predictors  $(X_1, ..., X_{b-1}, X_{b+1}, ..., X_p)$  if  $F_b > F(1, n - p - 1, \alpha)$  where  $F(1, n - p - 1, \alpha)$  is the  $(1 - \alpha)$  percentile of  $F_{n-p-1}^1$ . From the previous results, the respective condition of C- and V-suppression can be expressed as

$$|t_b/t_b^S| \ge (1 - R_{ba}^2)^{1/2}$$
 and  $|t_b/t_b^S| \ge 1$ .

Obviously, the detection of an important predictor with the partial F test in all variable selection procedures is not completely compatible to the occurrences of both definitions of suppression. These phenomena are presented in Figure 3 for  $R_{ba}^2 = 0.5$  and  $F(1, n - p - 1, \alpha) =$  $t_b^2 = 4$ . As in Figure 2, "C" and "V" denote the C- and V-suppression situations, respectively. The area below the dashed horizontal line represents the nonsignificant cases of the partial Ftest. Therefore, any of the variable selection procedures can fail to uncover the C- or V-suppression when there is a significant partial F test. On the other hand, it is possible to have either types of suppression even the partial F test is nonsignificant. This observation is generally true for all  $R_{ba}^2 \in [0, 1)$  and  $F(1, n - p - 1, \alpha) > 0$ . Hence, the inclination in Hamilton (1987) that backward elimination is satisfactory for those not wanting to miss enhancement or synergism is open to question. Note that his illustrations of  $R^2 > r_{Y1}^2 + r_{Y2}^2$  is equivalent to the notion of V-suppression for p = 2 as shown in Section 2.1. Furthermore, Velicer's (1978) claim that his definition of suppression is consistent with stepwise regression procedures is doubtful. To exemplify these findings, we consider the problem given in Kleinbaum et al. (1998, pp. 126-127) that a sociologist used data from 20 cities to investigate the relationship between the homicide rate per 100,000 city population (Y) and the following three independent variables: the city's population size ( $X_1$ ), the percentage of families with yearly income less than \$5,000 ( $X_2$ ), and the rate of unemployment ( $X_3$ ). The numerical results are summarized below for each variable.

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In conclusion, the partial F test of single parameter with respect to the increase in  $R^2$  is not a profound indicator of the suppression situations in multiple regression.

#### 4. Conclusions

In social studies, it is often the case that many of the variables are highly correlated. According to previous results, we wish to stress to users of multiple linear regression that the contribution of a variable can be enhanced by the presence of other variables. In general, it is not recommended to discard variables that are highly correlated with the variables to be retained in the best subset.

In view of the discrepancy between different suppression definitions in behavioral

literature, the proposed C- and V-suppression are more appealing for several reasons. They simplify, clarify and expand the existing formulations. More importantly, it leads to results that are not well known. With the added information of distinguishing between mutual and single suppressions algebraically and graphically, we are able to discern the complexities of the definitions of Conger (1974) and Velicer (1978). This study permits new insights into their definitions of suppression as to how they occur and when they differ. Although our presentation is concerned exclusively with the suppression situations in multiple regression, it can be applied easily to other designs (ANOVA and ANCOVA) and multivariate models.

We also present new characteristics about the contribution of each variable in multiple regression. Recognition of the relationship between suppression situations and partial F test helps clarify the issue of variable selection. This information should be useful in screening existing measurements and designing new ones. In fact, the occurrence of suppression and the significance of a partial F test can be employed simultaneously in the stepwise technique of variable selection. Further investigation and verification of this combined approach under a variety of different applications would be useful.

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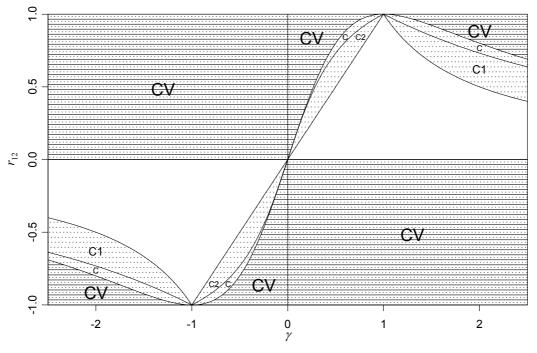


Figure 1. The regions of different types of suppression.

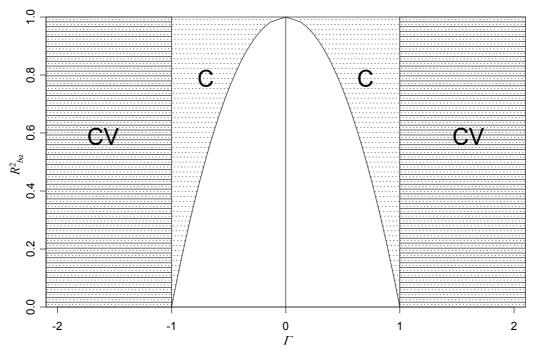


Figure 2. The regions of C- and V-suppression.

