# 行政院國家科學委員會專題研究計畫成果報告

計畫名稱:自行車傳動系統測試軟體之類神經網路結構最佳化設計

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### 摘要

#### **ABSTRACT**

The integration of neural networks and optimization provides a tool for designing the network parameters and improving the network performance. In this study, the Taguchi method and Design of Experiment (DOE) methodology are used to optimize the network parameters. The users have to recognize the application problems and choose a suitable Artificial Neural Network (ANN) model. Then, the optimization problems can be defined according to the model. The Taguchi method is first applied to the problem for finding the more important factors. Then DOE methodology is performed for further analysis and forecast. An LVQ example is demonstrated for the application to bicycle derailleur systems.

Keywords: Neural networks; optimization; Taguchi method; design of experiments; bicycle derailleur systems.

## INTRODUCTION

Artificial Neural Networks (ANNs) are

receiving much attention currently because of their wide applicability in research, medicine, business, and engineering. ANNs offer improved performance in areas such as pattern recognition, signal processing, control, forecasting, etc.

In this study, a systematic process is introduced to obtain an optimum design of a neural network. The Taguchi method and the Design of Experiments technique (DOE) (Montgomery, 1991) are the main techniques used. Unlike previous studies, the Taguchi method is used here to simplify the optimization problems. Then, DOE is more easily performed. Because of the stronger statistical basis of **DOE** methodologies, many analyses can executed. Finally, a Learning Vector Quantization (LVQ) network is demonstrated as an example. The method proposed in this paper can also be applied to any ANN model. The integration of optimization and ANNs in this paper was simulated by a computer program which can be executed automatically and easily.

#### THE EXAMPLE

In order to demonstrate the optimum design processes, an application with a Learning Vector Quantization (LVQ) model is shown. In this example, the purpose is to distinguish the type of chain engagement to be used in the rear derailleur system of a bicycle.

#### 1. Problem description

The derailleur system in a bicycle is similar to the gear box in a motor vehicle. A complete derailleur system, as shown in In derailleur system designs, two types of chain engagement, Type I and Type II, have to be considered (Wang *et* al., 1996). The chainwheel and freewheel sprocket design of

the two types are different; therefore, it is very important for the designers to know which type occurs during each gear shift. So, the different design defects for the two types can be found and improved.

In a real riding or testing environment, it is very difficult to distinguish which type of chain engagement occurs. There must be a camera for monitoring purposes. This costs a lot of money and it is not very easy to install. The purpose of this example is to establish a better and easier method to distinguish the chain engagement type during gear shifts, using a neural- network model.

The data fed to the network are transferred from the time domain to the frequency domain by the FFT technique (John and Dimitris, 1996). In gathering training data, if the tooth numbers of two adjacent sprockets are both even and the tooth number of the chainwheel sprocket is also even, only one type of chain engagement will occur. If only one chain link is shifted from the previous situation, another type will occur.

#### 2. Choosing an ANN model

In supervised learning models, an LVQ example like that shown in Fig. 7 is selected because of this fast training speed, no local minimum traps and better performance in classification (Patterson, 1996). The LVQ is the transformation from the input vector  $\underline{x}$  of dimension n to known target output classifications  $t(\underline{x})=t$ , where each class is represented by a codeword or prototype vector  $\underline{w}_i$  (i=1, 2, ..., m). The index i is the class label for  $\underline{x}$ . Let  $C(\underline{x})$  denote the class of  $\underline{x}$  computed by the network;  $\underline{w}_c$  is the weight vector of the winning unit c. Then, C(x) is found using

$$\|\underline{w}_c - \underline{x}\| = \min_i \|\underline{w}_i - \underline{x}\|.$$

When the class is correct, i.e.  $C(\underline{x})=t$ , the weight vector of the winning unit c is shifted toward the input vector. When an incorrect classification is selected, i.e.  $C(\underline{x})Ot$ , the weight vector is shifted away from the

input vector. The update rule for the LVQ can be summarized as follows:

- 1) Initialize the weights w to small random numbers.
- 2) Find the prototype unit to represent  $\underline{x}$  by computing

$$\|\underline{w}_c - \underline{x}\| = \min_i \|\underline{w}_i - \underline{x}\|$$
.

Update the weight vectors according to

$$\underline{w}_{c}^{new} = \underline{w}_{c}^{old} + r^{+}(\underline{x} - \underline{w}_{c}) \qquad \text{if } C(\underline{x}) = t \\
\underline{w}_{c}^{new} = \underline{w}_{c}^{old} - r^{-}(\underline{x} - \underline{w}_{c}) \qquad \text{if } C(\underline{x}) \neq t \\
\underline{w}_{i}^{new} = \underline{w}_{i}^{old} \qquad \text{for all } i \neq c$$

where

coefficients of two different cases.

3) Repeat steps 2 and 3 until the weights stabilize.

#### 3. Define the optimization problem

The optimal physical problem can be covered by a mathematical model of design optimization involving the procedures below.

- Choose design variables. In this example, the chosen design variables from the LVQ network parameters are the number of input units,  $\Gamma^+$  and  $\Gamma^-$ , and the weight initialization range. The number of input units is a discrete design parameter, and continuous design parameters, and the weight initialization range is a qualitative design parameter.
- 2) Define an objective function: The objective function in this example is defined as the grouping error of the network,

cost function = 
$$\sum_{i} f_{diff}(C_{i}(\underline{x}), t_{i})$$
,

where

$$\begin{cases} f_{diff} = 0 & \text{if } C_i(\underline{x}) = t_i \\ f_{diff} = 1 & \text{if } C_i(\underline{x}) \neq t_i \end{cases}$$

and i=1 to the size of the training

- data. The output of interest of this example is a "smaller-the-better" quality characteristic.
- 3) Identify constraints. A suggested range of design variables from the solver SNNS (Zell, 1995) will be described in next section

## 4. The Taguchi Method

The theories and principles used in the Taguchi Method (Taguchi, 1986; Peace, 1993) will not be described in detail; only the key points and analyzed results are shown below.

- 1) For the number of input units; the vibration signals during gear-shifting are transformed into the frequency domain by the FFT to 256 data points. Therefore, in this factor (the number of input units), three levels (256, 128 and 32 points) are selected.
- 2)  $0.05 \le r^+, r^- \le 0.3$  is assumed, and three levels (0.05, 0.1 and 0.3) are selected.
- 3) For the weight initialization range, a small range is suggested from the software (Zell, 1995). Therefore,  $\pm 0.1$ ,  $\pm 0.3$  and  $\pm 0.5$  are selected.

After the factors and levels are determined, a suitable orthogonal array can be selected for the training process. Table is the  $L_0(3^4)$  orthogonal array for the factors and levels in this example. For instance, in the first training experiment, there are 256 input units,  $V^+$  and  $V^-$  are set to 0.05, and the weight initialization range is between +0.1 and -0.1. After nine training experiments have been made, the grouping errors of the 80 training data are summarized in Table 1. Because there are no local minimum traps in this model, replicate training is not needed for the same For some other models, the parameters. final results may be affected by different Therefore, replicated initial designs. training is necessary for the following S/N analysis.

The last column in Table 1 is the signal-to-noise ratio (S/N). The equation for calculating the S/N for the smaller-the-better quality characteristic is Equation A.1. In this example, there is only one replicate, therefore, the physical meaning of S/N is similar to the grouping errors in Table 1. The grouping errors are used here instead of S/N for easier understanding.

The next step in the Taguchi method is Level Average Analysis. The goal is to identify the strongest effects, and to determine the combination of factors and levels that can produce the most desired results. Table 2 is the response table, which shows the average experiment at result for each factor level. The total effect of the 256 input units is 16. This is the average grouping error of the first three rows in Table 2((1+14+80)/3=16). Other response values can be calculated by using a similar method. For the number of input units, 256 units can get a smaller grouping error than other levels. The same principle can be used to make  $V^{+}$ and  $\sqrt{\phantom{a}}$  equal to 0.05, and the weight initialization range to be between +0.3 and Therefore, the recommended factor levels are: 256 input units,  $V^+ = 0.05$ , V = 0.05 and a weight initialization range of  $\pm 0.3$ .

## **CONCLUSIONS**

Optimization techniques have been widely used in many applications. In this paper, two major categories, the Taguchi method and the DOE methodology, are applied to improve one the original designs of ANNs. The users have to recognize the design problem and choose a suitable ANN model. Then, the optimization problems can be defined according to the model. The Taguchi method is first applied to find the more important factors, and to simplify the design problems. DOE methodologies are then used to find the sensitivity and a more precise combination of design parameters. The final results of the examples introduced

in this study indeed improve the initial designs and get a better performance.

Although only one ANN model, LVQ, is demonstrated in this paper, other models, such as ADALINE, MADALINE, Hopfield Networks, MLFF, Boltzmann Machines, Recurrent Neural Networks, Neocognitrons, etc., are also suitable. Many benefits can be mentioned. First, this is a systematic method to use for a neural-network design. It means that the engineer, whether or not he or she is experienced in ANN, the Taguchi method and DOE, can follow this process Many commercial software easily. packages can be applied, such as SNNS in ANN and SAS in the DOE. Second, it will not take too much computational effort and The results of the demonstrated time. examples can be obtained within 5 minutes with a Pentium-150 PC. This detail was not emphasized in this paper because it is not the major concern here. Finally, in engineering applications, it is not necessary to get a global optimization of the problems, because that takes too much time or the algorithms complicated. may be verv improvement of the original designs in an acceptable region is helpful for engineers.

## REFERENCES

Arora, J. S. (1989). Introduction to Optimum Design. McGRAW-HILL Book Company. Gill, P. E., Murray, W., and Margaret, H. W. (1981). Practical Optimization. Academic Press.

John, G. P. and Dimitris, G. M. (1996). Digital Signal Processing. Prentice-Hall, Inc. Khaw, B. S. L., John, F. C., and Lennie, E. N. L. (1995). Optimum design of neural networks using the Taguchi method. Neurocomputing, **7**, pp. 225-245.

Lin, T.Y., and Tseng, C.H. (1998). Using fuzzy logic and neural network in bicycle derailleur system tests", Proceeding of the International Conference on Advances in Vehicle Control and Safety (AVCS'98), Amiens, France, pp. 338-343.

Miller, G. F., Todd, P. M. and Hedge, S. U. (1989). Designing neural networks using genetic algorithms. Proc. 3<sup>rd</sup> Int. Conf. On Genetic Algorithms, pp. 379-384.

Montgomery, D. C., 1991. Design and Analysis of Experiments. John Wiley & Sons, Inc.

Patterson, D. W. (1996). Artificial Neural Networks, Theory and Applications, Prentice Hall.

Peace, G. S. (1993). Taguchi Methods, A Hands-On Approach. Addison-Wesley Publishing Company.

Taguchi, G. (1986). Introduction to Quality Engineering, Asian Productivity Organization, Tokyo.

Teo, M. Y. and Sim, S. K. (1995). Training the neocognitron network using design of experiments. Artificial Intelligence in Engineering, 9, pp. 85-94.

Wang, C. C., Tseng, C. H. and Fong, Z. H. (1996). A method for improving shifting performance. International Journal of Vehicle Design, 18(1), pp. 100-117.

Zell, A. (1995). SNNS, Stuttgart Neural Network Simulator User Manual, Version 4.1, University of Stuttgart, IPVR, Report No. 6/95.

	Input Units	$\mathcal{Y}^{^{+}}$	У	Weight Initial Range	Grouping Error	S/N
1	256	0.05	0.05	± 0.1	1/80	19.03 dB
2	256	0.1	0.1	±0.3	14/80	7.56 dB
3	256	0.3	0.3	± 0.5	34/80	3.72 dB

4	128	0.05	0.1	$\pm 0.5$	18/80	6.48 dB
5	128	0.1	0.3	± 0.1	34/80	3.72 dB
6	128	0.3	0.05	±0.3	5/80	12.04 dB
7	32	0.05	0.3	±0.3	35/80	3.59 dB
8	32	0.1	0.05	$\pm 0.5$	43/80	2.70 dB
9	32	0.3	0.1	± 0.1	33/80	3.85 dB

Table 1 Training results.

Factor	Level	Error	Factor	Level	Error
	256	16	У	0.05	16
Input units	128	19		0.1	22
	32	37		0.3	34
	0.05	18	Weight initial range	± 0.1	23
$\mathcal{Y}^{^{\!\scriptscriptstyle{+}}}$	0.1	30		± 0.3	18
	0.3	34		$\pm 0.5$	32

Table 2 Response table.

Source	Sum Square	Degree of Freedom	Mean Square	$F_0$	<i>Pr&gt;</i> F
$\mathcal{Y}^{^{+}}$	141.56	2	70.78	0.42	0.6827
$y^{}$	205.56	2	102.78	0.61	0.5868
Error	673.11	4	168.27		
Total	1020.23	8			

Table 3 The ANOVA table.