Architecture Design of Shape-Adaptive Discrete Cosine Transform and Its Inverse for MPEG-4 Video Coding

Hui-Cheng Hsu, Kun-Bin Lee*, Member, IEEE*, Nelson Yen-Chung Chang*, Student Member, IEEE*, and Tian-Sheuan Chang*, Senior Member, IEEE*

*Abstract—***This paper presents efficient VLSI architectures of the shape-adaptive discrete cosine transform (SA-DCT) and its inverse transform (SA-IDCT) for MPEG-4. Two of the challenges encountered during the exploitation of more efficient architectures for the SA-DCT and SA-IDCT are addressed. One challenge is to handle the architectural irregularity due to the shape-adaptive nature. The other one is to provide acceptable throughput using minimal hardware. In the algorithm-level optimization, this work exploits the numerical properties found in the transform matrices of various lengths, and derives a fine-grained zero-skipping scheme for the IDCT which can perform 22.6% more zero-skipping than the common vector-based coarse-grained zero-skipping scheme does. In the architecture-level design, the 1-D variable-length DCT/IDCT architectures designed on the basis of the numerical properties are proposed. An auto-aligned transpose memory that aligns the data of different lengths is also incorporated. In addition, a zero-index table is also included in the transpose memory to support the fine-grained zero-skipping in the SA-IDCT. The synthesized designs of the SA-DCT and SA-IDCT** are implemented using UMC $0.18 - \mu m$ technology. The SA-DCT **architecture has 26 635 gates, and its average cycle-throughput is 0.66 pixels/cycle, which is comparable to other proposed architectures. On the other hand, the SA-IDCT architecture has 29 960 gates, and its cycle-throughput is 6.42 pixels/cycle. While decoding for CIF@30FPS, the SA-IDCT is clocked at 0.7 MHz, and the power consumption is 0.14 mW. Both the throughput and power consumption of the proposed SA-IDCT architecture are an order better than those of the existing SA-IDCT architectures.**

*Index Terms—***Discrete cosine transform (DCT), MPEG-4, video coding, VLSI.**

I. INTRODUCTION

MPEG-4 object-based video coding can achieve higher subjective picture quality, increased coding efficiency, as well as better user interactions. Many techniques for coding arbitrarily shaped image segments have been proposed [1]–[3]. Among these techniques, the shape-adaptive discrete cosine transform (SA-DCT) and its inverse transform (SA-IDCT) proposed by Sikora *et al.* [2] have been adopted in MPEG-4

Fig. 1. Relation among (a) shape, (b) texture, and (c) boundary block in a video object.

standard [4]. The SA-DCT/SA-IDCT performs forward/inverse DCT for the pixels within a video object of arbitrary shape, as illustrated in Fig. 1. Instead of performing a full 8×8 DCT after filling zeros to the nonobject pixels, the SA-DCT adaptively performs N -point DCTs based on the shape, where N represents the length of rows/columns within the video object in a block. Comparing SA-DCT with the combination of filling and 8×8 DCT, the SA-DCT provides a significantly better rate-distortion tradeoff [5].

However, as the shape of a video object varies, the irregularity of variable-length DCT/IDCT gives challenges to efficient architecture design. These challenges have not been encountered in the architecture design of traditional 8×8 DCT/IDCT. One of the major challenges is how to efficiently allocate computing resources for the computation of variable-length DCT/IDCT so that the throughput can still be acceptable. Another challenge is to cope with the irregularity due to the consecutive variable-length rows or columns computation which would significantly affect the pipeline schedule and the hardware efficiency.

To conquer the aforementioned challenges, we propose a hardware-efficient SA-DCT/IDCT architecture based on algorithm-level and architecture-level optimizations. In the algorithm-level optimization, we first explore the numerical properties within the transform matrices to reduce the computational requirements. Our exploration goes beyond the traditional even/odd symmetry in the 8×8 DCT/IDCT and covers all possible numerical properties in different transform lengths. This enables the proposed architecture to provide throughput comparable to other SA-DCT/IDCT architectures with less computing resource. In addition, we adopt a fine-grained zero-skipping scheme instead of the traditional coarse-grained zero-skipping scheme for the proposed SA-IDCT architecture. The proposed fine-grained zero-skipping scheme reduces both the computation and memory access at the same time.

Manuscript received May 8, 2005; revised April 4, 2006 and February 1, 2007. This paper was recommended by Associate Editor S. Panchanathan.

H.-C. Hsu and K.-B. Lee are with MediaTek, Inc., Hsinchu 300, Taiwan, R.O.C.

N. Y.-C. Chang and T.-S. Chang are with National Chiao-Tung University, Hsinchu 300, Taiwan, R.O.C. (e-mail: ycchang@twins.ee.nctu.edu.tw).

Color versions of one or more of the figures in this paper are available online at http://ieeexplore.ieee.org.

Digital Object Identifier 10.1109/TCSVT.2008.918275

Fig. 2. Process of SA-DCT computation.

Moreover, the fine-grained zero-skipping explores all possible skipping of transform computation on zero-valued inputs.

On the other hand, the architecture-level optimizations include careful scheduling based on the proposed three-stage pipelined architecture, the introduction of an auto-aligned transpose memory, and the use of a zero-index table. The architecture-level scheduling is based on the numerical properties explored during algorithm-level optimization. To handle the irregularity due to the shape-adaptive nature, the auto-aligned transpose memory is introduced to align rows and columns automatically based on the video object's shape information. In addition, the zero-index table is incorporated to enable the fine-grained zero-skipping scheme for the proposed SA-IDCT architecture. With the above optimizations, the proposed SA-DCT/IDCT architecture represents an efficient solution to overcome the challenges mentioned earlier.

The remainder of this paper is organized as follows. Section II first presents a brief introduction to the operations of the SA-DCT and SA-IDCT. Section III presents the related works on the DCT/IDCT and the SA-DCT/SA-IDCT architectures. The numerical properties exploited in the transform matrices and the fine-grained zero-skipping schemes are explained in Section IV. Section V introduces the proposed architectures of the SA-DCT/SA-IDCT. Design considerations of the architectures are also explained in Section V. Section VI presents the implementation comparison of the SA-DCT/SA-IDCT architectures. Finally, Section VII concludes this work.

II. SA-DCT AND SA-IDCT

The definition of the forward SA-DCT illustrated in Fig. 2 is based on the four subsequent processing steps listed as follows.

- **S1**) Vertically shift all object pixels in $f(i, j)$ to the upper most position to construct $shift\text{ }texture(i, j)$. Also construct the auxiliary $shift_shape(i, j)$ in the same way.
- **S2)** Apply 1-D variable-length DCT to the first $pels_height(j)$ pels in all columns of $shift_text{ter}(\mathbf{i}, \mathbf{j})$ with $pels_height(\mathbf{j})! = 0$.
- **S3)** Horizontally shift all intermediate coefficients in $F\text{-}intermediate(v, j)$ to the left most position to construct shift intermediate(v, u).
- **S4)** Apply 1-D variable-length DCT to the first $coeff_width(v)$ intermediate coefficients in all rows of $shift_intermediate(v, u)$ with $coeff_width(v)! = 0.$

The alignment in the SA-DCT is illustrated in Fig. 2, where the indexes denote the object pixels. The k th DCT coefficient $y_N(k)$ of a 1-D N-point $(1 \leq N \leq 8)$ DCT on data $x(n)$ is calculated as

$$
y_N(k) = C(k) \sum_{n=0}^{N-1} x(n) \cdot \cos \frac{(2n+1)k\pi}{2N}
$$
 (1)

where $C(0) = 1/\sqrt{N}$ and $C(k) = \sqrt{2/N}$ for $k =$ $\{1, 2, \ldots, N-1\}$. For the considered shape-adaptive transform, N varies for each row and column, which is controlled by a binary array $f_shape(i, j)$ that describes the shape of the input data $f(i, j)$. This binary array element is collocated with the pixel of the corresponding 8×8 block. An auxiliary binary array $shift_shape(i, j)$ and two 1-D counter arrays pels_height(j) and coeff_width(v) are computed from $f_shape(i, j)$ during the internal shift operations of the

Fig. 3. Process of SA-IDCT computation.

forward SA-DCT to generate the data position and the length of 1-D DCT.

At the inverse side, the process is reversed to recover an image, as shown in Fig. 3. The definition of the SA-IDCT is based on the five subsequent processing steps I-S1)–I-S5).

- **I-S1)** Compute the required shape parameters $coeff_width(v)$, $shift_shape(i, j)$ and $pels_height(j)$ from the decoded binary shape array $f_shape(i, j)$.
- **I-S2)** Apply 1-D variable-length IDCT to the first $coeff_width(v)$ decoded coefficients in all rows of $F(v, u)$ with $\text{coeff}_width(v)! = 0$. Store the reconstructed intermediate coefficients in $shift_intermediate(v, j).$
- **I-S3)** Horizontally shift all reconstructed intermediate coefficients in *shift-intermediate* (v, j) from the left most position to their original column position defined by $shift_shape(i, j)$. Store the horizontally shifted intermediate coefficients in $F\text{-}intermediate(v, j).$
- **I-S4)** Apply 1-D variable-length IDCT to the first $pel_height(j)$ intermediate coefficients in all columns of $F\text{-}intermediate(v, j)$ with $pels_height(j)! = 0.$
- **I-S5)** Vertically shift all reconstructed pixels in $shift\text{ }texture(i, j)$ from the upper most position to their original row position defined by $f_shape(i, j)$.

The shift operations of I-S3) and I-S5) are shown in Fig. 3, where the indexes denote the object coefficients. The *th data* $x_N(n)$ of an N-point $(1 \le N \le 8)$ 1-D IDCT for coefficient $y(k)$ is calculated as

$$
x_N(n) = C(n) \sum_{k=0}^{N-1} y(k) \cdot \cos \frac{(2n+1)k\pi}{2N}
$$
 (2)

where $C(0) = 1/\sqrt{N}$ and $C(n) = \sqrt{2/N}$ for $n =$ $\{1, 2, \ldots, N - 1\}$. As in the SA-DCT, N varies for each row and column in the SA-IDCT.

III. RELATED WORK

Previous designs on variable-length DCT and IDCT can be classified into two approaches: variable length in nature design [6], [7] and extension of 8×8 DCT and IDCT [8], [9]. Variable length in nature design adopts the recursive algorithm and architecture [6]. Although recursive designs have several advantages including modularity and scalability, they have a computational complexity which equals to the worst case of the direct implementation scheme. To tackle the problems of numerical instability found in the time-recursive design, Le and Glesner [7] proposed the feedforward architecture. However, they did not address the issues of transposing and shifting the variable-length DCT coefficients during the computation process, which are vital for both the SA-DCT and SA-IDCT.

The extension approaches extend the architectures of fixed 8-point DCT and IDCT to support variable-length DCT/IDCT. Tseng [8] proposed a reconfigurable architecture that can perform standard $2-D 8 \times 8$ DCT/IDCT and $2-D$ SA-DCT/IDCT. Tseng's variable-length 1-D DCT/IDCT is based on Madisetti's design [10] which performs eight regular multiplications, but Tseng's design performs seven constant multiplications instead. In addition, the shape formation, texture alignment, texture, and shape transpose memories are incorporated into Tseng's design to complete the 2-D SA-DCT/IDCT. Owzar *et al.* [9] extends a

standard 8×8 IDCT hardware architecture with the shape parameter extraction by using counting and comparing operations on row indexes and length registers.

As to the low-power DCT/IDCT design, most of the previous approaches explore the property of zero-valued inputs to save power [11]–[16]. Xanthopolous [11] exploits the relative occurrence of zero-valued DCT coefficients coupled with clock gating, which can reduce the power but cannot reduce the required computation time. Pai's [12] design uses Loeffler's [17] fast algorithm to reduce the multiplications and uses zero bypassing, data segmentation, input truncation, and hardwired canonical sign-digit (CSD) multipliers to reduce the run-time computation requirement. However, Pai's zero bypassing is performed mainly by data gating and did not reduce the computation cycles.

Being aware of the need to further reduce the computation cycles, Bae and Min [13] uses the sparsity of the IDCT input coefficients to compute only non-zero valued coefficients, which is different from Pai's approach. According to the simulation results, their algorithm is faster than the conventional algorithms by a factor of 2 to 10. Although Bae's algorithm speeds up the computation efficiently, their architecture can not reduce the memory access. Besides, they did not describe how the non-zero input is fed into the IDCT.

Lin [14] proposes an alternative high-performance Inverse-Scan DCT (ISDCT) architecture, which not only skips the computation of zero-value coefficients, but also merges the functions of inverse scan and IDCT without an additional inverse scan buffer. However, since Lin's ISDCT processes the data in the zigzag scan order instead of the common raster scan order, every intermediate partial product has to be stored in the memory and retrieved again for accumulation, which will increase the power consumption.

Chen *et al.* [18]–[20] propose an adder-based DCT/IDCT design which can adjust the coefficient's precision adaptively to achieve power reduction. Their IDCT engine is later adopted in [15]. In addition to adaptive precision adjustment, [15] also adopted the zero-vector detection technique to skip the transform computations for zero-vector inputs. Though the computation for the zero-vector is reduced in [15], the memory access is not reduced. In [16], both the computation and memory access are reduced at the same time by turning off the transform engine for skipping all-zero IDCT inputs. However, such coarse-grained zero-skipping is only limited to the computation and memory access reduction of macroblocks with all-zero IDCT inputs only. Hence, the computation and memory access reduction for the fine-grained scalar zero input should be further explored as well.

IV. ALGORITHM-LEVEL OPTIMIZATIONS

The algorithm-level optimization shares the multiplication by exploiting the numerical properties of transform matrices and fine-grained zero-skipping. Unlike Le's feedforward architecture [7], which only exploits the even/odd symmetry for the even/odd decomposition, the specific numerical properties for different transform lengths are also identified and applied for the multiplication sharing. In addition, the proposed fine-grained

Fig. 4. Average distribution of transform lengths over the 16 test sequences which are listed in Table III.

zero-skipping is derived to increase the opportunity for the computation and memory access reduction compared with the traditional zero-skipping schemes. These two features are explained in detail in the following two subsections.

A. Multiplication Sharing by Transform Matrices' Numerical Properties

The numerical properties exploited in this work are different from the traditional ones. The traditional numerical properties have been explored in many fast algorithms designed for the 1-D DCT or IDCT [21]. However, most of these researches focus on $N = 2^m$ with $m \geq 2$ and only consider the optimizations for a particular fixed-length 1-D DCT/IDCT. For the 1-D variable-length DCT/IDCT, optimizing the design for different lengths results in more complex resource allocation and scheduling. Neglecting the numerical properties of lengths other than 8-point avoids making a more complex design; however, it also reduces the opportunity for further resource sharing. According to the statistics on average distributions of different transform lengths shown in Fig. 4, the 8-point transform only accounts for 30% of all transforms, whereas other lengths account for 70% of all transforms. Hence, it is worth improving the resource sharing for transform lengths other than 8-point. Based on this statistic result, the numerical properties beyond the traditional ones for the fixed 8-point transform should thus be exploited.

To exploit the numerical properties, we have investigated N -point 1-D DCT/IDCT transformation matrices for $2 \leq N \leq 8$. The properties are listed below.

- a) Even columns are even-symmetric and odd columns are odd-symmetric in N -point 1-D IDCT transformation matrices.
- b) The values of column 0 of N -point 1-D IDCT transformation matrices are always $1/\sqrt{N}$.
- c) In even-point matrices, the values of the upper or lower half part of all columns except column 0 are odd-symmetric.
- d) The values of column 3 of a 6-point matrix are $\pm(1/\sqrt{3})\cos(\pi/4)$.
- e) The values of column 4 in an 8-point matrix are $\pm(1/2)\cos(\pi/4)$.
- f) The values of column 0 and column 2 in a 4-point matrix are ± 0.5 .
- g) The values of column 2 in a 6-point matrix are ± 0.5 .

These properties are demonstrated by taking the 4-point, 6-point, and 8-point transform matrices as examples, as shown in Fig. 5. The coefficients which satisfy the properties are

Fig. 5. Variable-length 1-D DCT transform matrices demonstrating different numerical properties. (a) 4-point DCT/IDCT transform matrix. (b) 6-point DCT/ IDCT transform matrix. (c) 8-point DCT/IDCT transform matrix.

marked with their corresponding properties in parentheses. We chose these three lengths as examples because they exhibit all of the properties listed above. Other lengths of transform matrices also exhibit some of the numerical properties. Take $N = 7$, for instance. Numerical properties 1) and 2) can also be found in its transform matrices.

The numbers of multiplications for N -point DCT/IDCT matrices are listed in Table I. The parentheses in this table mean the properties applied to obtain the number of multiplications. For instance, row 0 in an 8-point DCT/IDCT transform matrix has only one constant because of the property 2). As a result, $y_8(0) = C(0) \times [x(0) + x(1) + x(2) + x(3) + x(4) + x(5) + x(6) +$ $x(7)$; only one multiplication is required as indicated in Table I. Note that, based on properties 6) and 7), the multiplication of 0.5 is replaced by using right shift. Based on these numerical properties, the common subexpressions sharing, scaling, and inversion are performed to reduce the number of multiplication. After applying these reductions, at most four multiplications are necessary at the same time, as indicated in Table I.

In addition to resource sharing, careful scheduling is done to minimize the clock cycle counts required to finish the 1-D DCT/ IDCT. Table II lists the processing schedule of input $y_N(k)$,

TABLE I NUMBER OF MULTIPLICATIONS IN EACH ROW OF THE TRANSFORM MATRICES

'.ength Row	2	3		5	6		8
0	1(b)	1(b)	0(f)	1(b)	1(b)	1(b)	1(b)
\mathcal{I}	(a) 1	l(a)	2(a)	2(a)	3(a)	3(a)	4(a)
2		2(a)	0(f)	3(a)	θ (g)	4(a)	2(c)
\mathfrak{Z}			2(a)	2(a)	1(d)	3(a)	4(a)
4				3(a)	2(c)	4(a)	1(e)
5					3(a)	3(a)	4(a)
6						4(a)	2(c)
7							4(a)

TABLE II PROCESSING SCHEDULE OF N-POINT 1-D DCT/IDCT

where the subscript N is the length of the DCT/IDCT, and k indicates the k th input. The number in Table II represents k . For example, when $N = 5$, $y_5(1)$ and $y_5(3)$ are processed in the first cycle, $y_5(0)$ and $y_5(2)$ are processed in the second cycle, and $y_5(4)$ in the third. Similarly, an 8-point 1-D DCT can be completed in six clock cycles using four multipliers. To compute a full 8×8 DCT, the proposed architecture requires 100 cycles to be complete. Since both the forward and inverse 1-D variable-length transforms use the same numerical properties found in the transform matrices, the schedules of input for both transforms are arranged to be the same. By sharing the same input schedule, the design of the SA-DCT/SA-IDCT's multiplexers and demultiplexers can be shared.

B. Fine-Grained Zero-Skipping Scheme

Fine-grained zero-skipping offers more computation skipping than the traditional coarse-grained zero-skipping. In addition to computation reduction, the proposed fine-grained zero-skipping scheme also reduces the memory access at the same time. The traditional zero-skipping in [11], [15], and [16] is limited to row- or column-level granularity. When scalar zero coefficients are present, no computation or memory access can be skipped in a traditional vector-based coarse-grained zero-skipping scheme. In contrast, the fine-grained zero-skipping scheme proposed in this work decreases the level of granularity to a single coefficient instead of several coefficients in a row or column. This means that, whenever a coefficient is zero, we can skip its memory accesses and the computation for this zero-valued coefficient.

Table III shows the statistics of zero coefficients and zero rows/columns. These data are gathered from running the reference software of MPEG-4 decoder [22] over 16 test sequences listed in Table III. Moreover, the percentage of zero coefficients for the regular 8×8 IDCT is also investigated and listed in Table IV for reference. During the simulation, the quantization parameter (QP) is set to 10, which is relatively low compared with practical QP values. This implies that the percentage

TABLE III PERCENTAGE OF ZERO COEFFICIENTS FOR SA-IDCT

$QP=10$	Zero coefficient		Zero column/row		
	Zero cnt	٩,	zero cnt	ዱ	
brea_cif	145022 97.76		25449	92.93	
coastguard0 cif	6763777	94.42	1067524	81.88	
coastguard1 cif	3696252	87.55	526461	69.54	
coastquard2 cif	3042943	90.58	417608	73.32	
coastguard3 cif	2017455	95.59	340556	86.65	
dancer1 cif	3173476	81.89	415047	58.58	
foreman cif	2683770	95.65	442677	85.96	
singer1 cif	2428905	93.03	385910	80.49	
singer2 cif	2096560	77.44	298061	50.42	
stefan cif	1957706	81.84	265972	59.24	
brea qcif	67715	96.26	11611	89.25	
coastguard0 qcif	2843760	97.15	525357	89.63	
coastguard1_qcif	1412983	90.45	227161	75.18	
coastguard2 qcif	1252018	92.49	179932	76.42	
coastguard3_qcif	1167978	96.68	178627	87.83	
stefan qcif	731901	77.70	102074	54.53	
Total	35482221	89.92	5410027	73.89	

TABLE IV PERCENTAGE OF ZERO COEFFICIENTS FOR 8×8 IDCT

of zero coefficients is likely to be higher in practical QP settings. The simulation setting described here is also used in other statistic result in the rest of this paper.

According to Tables III and IV, the average percentage of zero coefficients for the SA-IDCT and regular 8×8 IDCT when $QP = 10$ are 89.9% and 90.7% respectively. Among the 16 test sequences, $brea_ci f$ has the highest zero-coefficient percentage while $singer2_{ci}f$ has the lowest zero-coefficient percentage. Therefore, we further investigate the impact of different QP values based on these two extreme test sequences. Fig. 6 shows the percentage of the SA-IDCT zero coefficients and zero rows/columns with respect to different QP values for these two sequences. It can be seen clearly that, for lower QP values, both sequences exhibit a higher percentage of zero coefficient than the percentage of zero rows/columns. This finding can also be found in Fig. 7, which is the plot for the regular 8×8 IDCT on the percentage of zero coefficients and zero rows/columns. The extra percentage of zero coefficients offers the extra opportunity to perform zero-skipping. Together with the aforementioned comparison on the percentage of zero coefficients and

Fig. 6. Plot of zero coefficients and zero row/column vectors for the SA-IDCT.

Fig. 7. Plot of zero coefficients and zero row/column vectors for the IDCT.

Fig. 8. 2-D SA-DCT/SA-IDCT architecture.

zero rows/columns, the proposed zero-skipping scheme can exploit 22.6% of extra zero-valued coefficients for skipping compared with the coarse-grained zero-skipping. The irregularity impact due to the fine-grained zero-skipping is solved by a lowcost zero-index table, which is part of the proposed architecture-level optimization. This will be explained in the next section.

V. ARCHITECTURE DESIGN

Fig. 8 shows the overall architectures of the proposed SA-DCT/SA-IDCT. Both of them are composed of a 1-D variable-length DCT or IDCT kernel, a transpose memory, an address generator, a multiplexer, and a demultiplexer. The main differences between the SA-DCT and SA-IDCT are the detailed architectures of the 1-D variable-length transform kernel and the transpose memory. For the SA-IDCT, the inverse transform and the extra support for the proposed fine-grained zero-skipping, such as the 64-bit zero-index table,

Fig. 9. Architecture of the 1-D variable-length DCT kernel.

Fig. 10. Reordering for the input of 8-point transform.

cause different architecture designs for the datapath of the 1-D variable-length transform kernel and transpose memory.

A. One-Dimensional Variable-Length DCT/IDCT Kernel

The architecture of the 1-D variable length DCT kernel is illustrated in Fig. 9. It is divided into three pipelined stages: data preparation unit (DPU), multiplication processing unit (MPU), and post-processing unit (PPU). Each stage is operated as follows.

• *Data Preparation Unit (DPU)*

The DPU stage performs two major tasks. The first task reorders the input samples by using two two-word LIFOs. The second task generates common subexpressions as inputs for the next stage, the MPU stage. For example, take the worst case 8-point DCT operations. The reordering process is illustrated in Fig. 10. First, $x_8(0)$ and $x_8(1)$ are stored into the LIFOs, then $x_8(2)$ and $x_8(3)$ are stored; when $x_8(4)$ and $x_8(5)$ are input, $x_8(2)$ and $x_8(3)$ are read from the LIFOs to compute the common subexpressions $x_8(2) + / -x_8(5)$ and $x_8(3) + / -x_8(4)$, and then the common subexpressions $x_8(0) + / -x_8(7)$ and $x_8(1) +$ $\gamma - x_8(6)$ are processed in the same way. At the end, the common subexpressions are stored into the registers named add $0 \sim$ add3 and sub $0 \sim$ sub3.

• *Multiplication Processing Unit (MPU)*

The intermediate products of the common subexpressions and the transform coefficients are computed in the MPU. In addition to the multipliers, four adders are included to add the common subexpressions before multiplication. The reason for adding the common subexpressions is to group the subexpressions with the same multiplicand based on the numerical properties found in the transform matrices.

As a result, the multiplications can be shared, and thus reduces the number of multiplier to four, which is one less than that of Le's feedforward architecture. Take the computation of $y_2(0)$ in a 2-point DCT as an example of multiplication sharing. Since both the common subexpressions $x_2(0) + x_2(2)$ and $x_2(1) + x_2(3)$ have to be multiplied with 0.5, they are grouped by adding both subexpressions together before multiplying, therefore only one multiplication is required instead of two in $y_2(0) = 0.5 \times$ ${x_2(0) + x_2(2)} + [x_2(1) + x_2(3)]$. Furthermore, two one-bit shifters are used instead of multipliers when the transform coefficients are 0.5. The hardware cost of two one-bit shifters is much less than that of one full multiplier. Note that there are four registers (reg $0 \sim$ reg3) in the MPU stage, which are illustrated in the lower part of the MPU in Fig. 9. These registers buffer the common subexpressions from the DPU stage which are not consumed by the adders and multipliers in the MPU. This allows the generation of the common subexpressions of the next row or column to continue in the DPU stage. As a result, the DCT operations of different rows or columns can be overlapped and thus improves the throughput.

• *Post-Processing Unit (PPU)*

In the PPU stage, the final transformed results are obtained by adding the intermediate products from the MPU stage. The additions are carried out by using three adders. To keep the output of the DCT in order, i.e., the output order shown in Fig. 11, four extra registers are used before the final output multiplexer in the PPU stage to reorder the results.

The architecture of the 1-D variable-length IDCT is illustrated in Fig. 12. It is also divided into three pipelined stages: multiplication processing unit (MPU), addition unit (ADU) and

Fig. 11. Input and output order of the 1-D DCT kernel.

Fig. 12. 1-D variable-length IDCT architecture.

accumulation unit (ACU). Each stage is described and explained as follows:

• *Multiplication Processing Unit (MPU)*

Unlike the architecture of the 1-D variable-length DCT, the inputs are multiplied by the corresponding inverse transform coefficients to generate the common products in the first stage. For example, the first input $z_8(0)$ of an 8-point

inverse transform coefficient is multiplied by $C_8(0)$ in the MPU. This common product $C_8(0) \times z_8(0)$ is required for the computation of all the eight inverse transform results $x_8(0) \sim x_8(7)$. The numerical properties of the transform matrices mentioned earlier are also facilitated in the IDCT's MPU stage. Therefore, only four multipliers and two one-bit shifters are used, which is the same as the number of multipliers and shifters of the MPU in the DCT. In addition, when the input is a zero coefficient, the multiplication for this zero coefficient will be skipped, and a zero value would be generated in the next stage.

• *Addition Unit (ADU)*

The common products from the MPU are added to each other in the ADU stage. This stage includes four adders and five registers. The registers store the sums of the common products. Take the same 8-point case used previously for example. The common products $C_8(0) \times z_8(0)$ and $C_8(2) \times z_8(2)$ are added together for further computation of $x_8(0)$ and $x_8(1)$. If the multiplication in the MPU is skipped due to the zero input, the corresponding input in this stage will be zero.

• *Accumulation Unit (ACU)*

The sums of the common products in the ADU stage are accumulated to obtain the final inverse transform results in the ACU stage. Eight accumulators, each corresponds to an output, are incorporated to compute the inverse-transformed values. Take the example of the 8-point IDCT, $x_8(0) = [C8(0) \times z_8(0) + C_8(2) \times z_8(2)] + \text{acc}$ $[C_8(4) \times z_8(4) + C_8(6) \times z_8(6)] +_{\text{acc}} [C_8(1) \times z_8(1)] +_{\text{acc}}$ $[C_8(3)\times z_8(3)] +_{\text{acc}} [C_8(5)\times z_8(5)] +_{\text{acc}} [C_8(7)\times z_8(7)],$ where $+_{\text{acc}}$ stands for the accumulation operation. Hence, only five accumulations are required to compute $x_8(0)$. If the sum of the common products is determined to be zero, the computation of this sum of common product is skipped in the MPU and the ADU stages. Then the input of the corresponding accumulator is multiplexed to zero instead of the original input.

B. Auto-Aligned Transpose Memory and Zero Index Table

In the conventional row-column decomposition of a 2-D DCT/IDCT, a transpose memory is required to store the intermediate results of the first 1-D DCT/IDCT. As for the SA-DCT/SA-IDCT, an additional horizontal shift or vertical shift is also required to perform on these intermediate results. To ease the transpose and the alignment tasks, we propose the auto-aligned transpose memory architecture.

The auto-aligned transpose memory architecture combines the transpose memory and address pointer together to automatically align the data during the transform computation. Thus, no data shift is required. For the SA-DCT, we first logically partition the transpose memory into eight rows and use eight address pointers (row_ptr(k), $0 = k = 7$) to denote the addressing of each rows. Then, when the first 1-D column DCT is computed, the result is directly written into the transpose memory addressed by the pointers. Each pointer is also increased by one when new data is written. After the whole 1-D transform is done, the data in these eight address pointers directly stand for the lengths of rows, and thus is ready for the second 1-D row DCT computation without explicit alignment. Take the DCT result

Fig. 13. Auto-alignment of the transpose memory using the addressing mode.

of column 2 in Fig. 13 for example. Before processing column 2, the results of column 0 and column 1 are already transposed and written into the buffer, the value of row $ptr(0)$ is also updated. After the transform for column 2, the first DCT result $y_2(0)$ is written to the offset pointed by row ptr(0) in row 0, and the second DCT result $y_2(1)$ is written to the offset pointed by row ptr(1) in row 1. The row pointers of rows 0 and 1 are also incremented after writing the results. By using the pointers, all information required for the second 1-D variable-length DCT is generated and all intermediate coefficients are auto-aligned to the correct positions. For the alignment in the SA-IDCT, the whole operation is similar to that in the SA-DCT, except that column pointers are updated instead of row pointers.

Although the proposed transpose memory supports the autoalignment for DCT/IDCT computation, the shifting of the input pixels to align to the top in the SA-DCT (S1 in Fig. 2) or the shifting of the reconstructed pixels to their original locations (IS-5 in Fig. 3) are assumed to be handled externally.

In addition to the auto-alignment, to support zero-skipping in the proposed SA-IDCT architecture, the address generator in the transpose memory must be able to calculate the number of zerovalued intermediate coefficients for the second 1-D SA-IDCT. Hence, the transpose memory has a *zero-index table* with 64 bits to record whether each intermediate coefficient in a block is zero or not. The zero-index table is reset to zero each time a new block is to be processed. The proposed SA-IDCT architecture only writes the nonzero term into the transpose memory, then it changes the value of the bit at the corresponding position in the zero-index table from zero to one. As a result, using the proposed zero-index table to calculate zero information not

only reduces the computation complexity from 16 bits to 1 bit, but also can decrease the routing complexity, the number of multiplexers, and the power consumption.

VI. IMPLEMENTATION RESULTS

The proposed SA-DCT and SA-IDCT architectures are both synthesized from Verilog RTL design using UMC 0.18 μ m 1P6M CMOS technology [23]. The SA-DCT synthesized design has a gate count of 26 657 (including the transpose memory). When the SA-DCT synthesized design is clocked at 100 MHz, the maximum average throughput is 65.75 Mpixels/s. As for the synthesized design of the proposed SA-IDCT architecture, the synthesized gate count of the synthesized design is 31 473 (including transpose memory). When the SA-IDCT synthesized design is clocked at 62.5 MHz, the average throughput with the fine-grained zero-skipping enabled can reach up to 401.41 Mpixels/s. If the fine-grained zero-skipping is disabled, the design's average throughput is 47.69 Mpixels/s. Note that the transpose memory is implemented with registers. Using registers instead of memories only increases the total area by 3%, which is only a small area overhead.

The core characteristics of the SA-DCT and SA-IDCT are compared with other architectures in Table V. The power consumptions of the proposed SA-DCT and SA-IDCT architectures are evaluated using Synopsys Prime Power. The power consumptions are reported from the gate-level simulation upon three frames of $ste fan_qcif$ sequence. Since the percentage of zero coefficients in $ste fan_qci f$ is the second lowest among the sequences, this power consumption can be regarded as a higher bound. The power consumptions are compared using the scaled power in Table V, which is scaled to match 0.18 μ m process, 1.8 V, and the required clock rate for CIF@30fps. It is believed that comparing with the scaled power should be more adequate than comparing the original power consumption directly.

To scale the power, the scaling process first calculates the required clock rate to achieve the decoding of CIF@30fps based on the original throughput; the clock scaling equation is shown as

CIF@30fps clock_rate =
$$
\frac{\text{Pixels.in.30CIF frames}}{\text{cycle} - \text{throughput}} \text{ Hz. (3)}
$$

Then, the power scaling is performed by the voltage scaling, process scaling, and frequency scaling shown as

scaled-power = orig-power
$$
\frac{(1.8)^2}{(\text{orig_voltage})^2}
$$

$$
\times \frac{(0.18 \,\mu\text{m})^2}{(\text{orig_vposes_parameter})^2}
$$

$$
\times \frac{\text{CIF@30fps-clock_rate}}{\text{orig_clock_rate}} \text{mW} \quad (4)
$$

This scaling equation is derived from the dynamic power equation $P = V^2CF$, where V is the supply voltage, C is the capacitance, and F is the working frequency. By assuming that the capacitance is linear with the square of the process parameter, the power equation becomes $P = V^2k\lambda^2F$, where λ is the process parameter and k is a constant. By using this equation, the ratio of

	Madisetti's	Xanthopolous's	Le's	Chen's	Tseng's	Proposed	
	[10]	$[11]$	7	[18]	[8]		
Function	$2-D$ 8×8 DCT/IDCT	2-D 8×8 IDCT	1-D variable length DCT	SA-DCT/IDCT	SA-DCT/IDCT	SA-DCT	SA-IDCT
Technology (µm)	0.8	0.5	0.7	0.35	0.35	0.18	0.18
Logic gate count	N.A. (67K transistors)	N.A.	N.A.	1 ALU $(3,100)$	40.518	26,657 (100MHz)	31,473 (62.5MHz) 29,960 (2.14MHz)
Multipliers #	$\overline{7}$	8	5	Ω	8	$\overline{4}$	4
Adders#	8	16	11	$\mathbf{1}$	10 ¹⁰	11	12
Memory	64-word DRAM	Dual port 64- word SRAM×2	N.A.	32-word RAM	64×16 , 64×2 two port RAM		
Original power	N.A.	4.65 mW @1.32V,14MHz	N.A.	23.6mW @1.6V, 83MHz	240mW (a)3.3V, 62.5MHz	18.24 mW @1.8V, 100MHz	0.433 mW @ 1.8V, 2.14MHz
Scaled power Scaled to 0.18um, 1.8V CIF@30fps	N.A.	0.37mW (4.6MHz)	N.A.	7.92mW (83MHz)	2.04mW (6.8MHz)	1.26 mW (6.9MHz)	0.14mW (0.7MHz)
Average cycle- throughput (pels/cycle)	$\mathbf{1}$	$\mathbf{1}$	0.36	0.04	0.67	0.66	6.42 (no skip: 0.77)
Hardware efficiency per cycle (pels $\times 10^{-5}$ /cycle-gate)	N.A.	N.A.	N.A.	1.29	1.65	2.48	20.40 (no skip: 2.45)

TABLE V COMPARISON OF SA-DCT/IDCT CORE CHARACTERISTICS

the power in 0.18 μ m process and in the original process represents the scaling factor. The scaled power can then be estimated by multiplying the power scaling factor with the original power.

We take the power scaling of Xanthopolous's design as an example. There are 30 frames of 22×18 YUV 8×8 blocks that have to be processed within one second, where each block has 64 pixels. The cycle-throughput of Xanthopolous's design is one pixel per cycle. Hence, the required clock rate of Xanthopolous's design to decode CIF@30fps would be

$$
\frac{64 \times 6 \times 22 \times 18 \times 30 \text{ (pixels/s)}}{1 \text{ (pixel/cycle)}} = 4.6 \text{ MHz}
$$

and the scaled power is

$$
4.65 \times \frac{(1.8)^2}{(1.32)^2} \times \frac{(0.18)^2}{(0.5)^2} \times \frac{4.6}{14} = 0.37 \text{ mW}
$$

The comparison of the core characteristics of the SA-DCT and SA-IDCT are explained in the following two subsections.

A. Comparison of SA-DCT

The often-cited design for the fixed-size DCT/IDCT proposed by Madisetti [10] is also listed for reference. We will use the cycle-throughput to compare the computation speed among the architectures. This *cycle-throughput* is defined as the number of pixels processed within one clock cycle; hence, the cycle-throughput is independent of the clock rate

used. Madisetti's architecture achieves the highest average cycle-throughput among the compared architectures. This is because Madisetti's design only supports the fixed 8-point DCT/IDCT, and therefore the multipliers can be hardwired to carry out constant multiplications. In contrast, using full multipliers constrains the maximum clock frequency of all of the other designs except for Chen's ALU-based design. However, Chen's approach focuses on a very low-cost architecture. Consequently, its cycle-throughput is very low due to the use of only one single adder. Therefore, the comparison is focused on comparing the proposed SA-DCT architecture with Le's feedforward and Tseng's SA-DCT architectures. The cycle-throughput of the proposed architecture is very close to Tseng's, which outperforms the rest of the SA-DCT architectures listed in Table V. Nevertheless, the proposed SA-DCT architecture requires the fewest number of multipliers compared with Le's and Tseng's architectures, whereas the number of adders for the proposed architecture is the same as Le's. The reduced number of multipliers also reduces the power consumption of the proposed SA-DCT when it is compared with Tseng's design.

Two factors enable the cycle-throughput of the proposed SA-DCT architecture to outperform Le's design. One factor is that our design can support more than one pixel per clock cycle for input and output. This is reasonable when a wider system bus is employed. The other factor is that the DCT operations on consecutive rows or columns can be overlapped because of the four extra registers in the MPU stage. As for Le's design, the

DCT operation of the next row or column can only start when the DCT operation of the current row or column is finished.

In summary, the proposed SA-DCT architecture achieves a comparable cycle-throughput using fewer multipliers and fewer total gate count. This indicates that the proposed SA-DCT architecture is a more cost-effective architecture compared with Le's and Tseng's.

B. Comparison of SA-IDCT

The comparison for the SA-IDCT architectures shows that both the cycle-throughput and the power consumption of the proposed SA-IDCT architecture outperform other architectures listed in Table V. Due to the benefits of the fine-grained zero-skipping scheme and efficient resource sharing, the average cycle-throughput of the proposed SA-IDCT architecture is much higher than that of other architectures. However, to support zero-skipping, extra cost overhead for the zero-index table is incurred. Therefore, the proposed SA-IDCT architecture has more gate count than the proposed SA-DCT architecture. Nevertheless, the *hardware efficiency per cycle*, which is defined as the ratio between the average cycle-throughput and the logic gate count, is one order higher than other SA-IDCT architectures. If the proposed zero-skipping is disabled, the worst case cycle-throughput is 0.77 pels/cycle; the hardware efficiency per cycle without zero-skipping is still higher than those of Le's and Tseng's architectures.

The greatly increased average cycle-throughput and the zeroskipping scheme also benefit the power consumption of the proposed SA-IDCT architecture. On one hand, the increased cyclethroughput enables the opportunity of using a lower clock rate to achieve the same throughput requirements for different profiles and levels and thus lowers the power consumption. On the other hand, zero-skipping skips the memory accesses and computations for zero-valued coefficients and thus saves power. Therefore, the proposed SA-IDCT is capable of achieving the least power consumption using the least clock rate among the compared architectures while decoding CIF@30fps.

With the efficient resource sharing and zero-skipping schemes, the proposed SA-IDCT architecture outperforms other architectures in terms of both cycle-throughput and power while its cost remains comparable to other similar architectures. In summary, the proposed SA-IDCT architecture is more energy-efficient and cost-effective than other compared architectures.

VII. CONCLUSION

This paper presents the SA-DCT and SA-IDCT architectures that can efficiently cope with the complexity that arises due to the variable-length nature. The approach includes algorithm-level optimizations and architecture design. In the algorithm-level optimizations, the numerical properties of the transform matrices beyond the traditional 8-point transform are explored. Moreover, a fine-grained zero-skipping scheme is proposed for SA-IDCT. Based on the analysis of zero coefficients, the fine-grained zero-skipping scheme can skip more memory accesses and computations of zero coefficients than the vector-based coarse-grained zero-skipping can. In the

architecture-level design, the proposed 1-D variable-length DCT/IDCT kernel architectures are designed based on the numerical properties of various lengths, resource sharing, and careful scheduling to improve the cycle-throughput and the hardware efficiency per cycle. In addition, an auto-aligned transpose memory using row and column pointers instead of shifting is designed to deal with the transpose operation for the data of different lengths.

The implementation result shows that the proposed architectures have fewer gate counts than other existing architectures while having comparable or higher cycle-throughputs. Hence, we believe that the proposed SA-DCT and SA-IDCT architectures have better hardware efficiency per cycle when compared with others. The proposed fine-grained zero-skipping scheme can also greatly improve the cycle-throughput of the SA-IDCT while effectively reducing the memory accesses in the SA-IDCT. The power consumption of the proposed SA-IDCT using UMC 0.18 μ m technology is 0.14 mW when it is decoding for CIF@30FPS. Therefore, the proposed SA-IDCT can be considered as an energy efficient architecture. However, the proposed dedicated variable-length DCT/IDCT architecture may not be suitable for fixed-length integer transforms which are regular and require no multiplication.

REFERENCES

- [1] M. Gilge, T. Engelhardt, and R. Mehlan, "Coding of arbitrarily shaped image segments based on a generalized orthogonal transform," *Signal Process. Image Commun.*, vol. 1, pp. 153–180, Oct. 1989.
- [2] T. Sikora, "Low complexity shape-adaptive DCT for coding of arbitrarily shaped image segments," *Signal Process. Image Commun.*, vol. 7, pp. 381–395, Nov. 1995.
- [3] R. Stasinski and J. Konrad, "A new class of fast shape-adaptive orthogonal transforms and their application to region-based image compression," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 9, no. 1, pp. 16–34, Feb. 1999.
- [4] Information Technology–Coding of Audio-Visual Objects , Dec. 2001.
- [5] P. Kauff, K. Schuur, and M. Zhou, Experimental Results on a Fast SA-DCT Implementation ISO/IEC JTC1/SC29/ WG11 MPEG98/M3640, Jul. 1998.
- [6] K. J. R. Liu, C. T. Chiu, R. K. Kolagotla, and J. F. Jala, "Optimal unified architectures for the real-time computation of time-recursive discrete sinusoidal transforms," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 4, no. 2, pp. 168–180, Apr. 1994.
- [7] T. Le and M. Glesner, "Flexible architectures for DCT of variablelength targeting shape-adaptive transform," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 10, no. 12, pp. 1489–1495, Dec. 2000.
- [8] P. C. Tseng, "Design and implementation of reconfigurable discrete cosine transform processor with shape-adaptive capability," Master's thesis, Dept. Electron. Eng., National Taiwan Univ., Taipei, Taiwan, R.O.C., Jun. 2001.
- [9] M. Owzar, M. Talmi, G. Heising, and P. Kauff, Evaluation of SA-DCT Hardware Complexity ISO/IEC JTC1/SC29/ WG11 MPEG99/M4407, Mar. 1999.
- [10] A. Madisetti and A. N. Willson, Jr., "A 100 MHz 2-D 8×8 DCT/IDCT processor for HDTV applications," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 5, no. 2, pp. 158–165, Apr. 1995.
- [11] T. Xanthopolous and A. Chandrakasan, "A low-power IDCT macrocell for MPEG-2 MP@ML exploiting data distribution properties for minimal activity," *IEEE J. Solid-State Circuits*, vol. 34, no. 5, pp. 693–703, May 1999.
- [12] C.-Y. Pai, W. E. Lynch, and A. J. Al-Khalili, "Low-power data-dependent 8 \times 8 DCT/IDCT for video compression," *Proc. IEE Vision*, *Image and Signal Process.*, vol. 150, no. 4, Aug. 22, 2003.
- [13] S.-O. Bae and S.-J. Min, "A computationally efficient IDCT algorithm," in *Proc. Midwest Symp. Circuits Syst.*, 1997, vol. 2, pp. 973–976.
- [14] S.-T. Lin, "Analysis and design of a high-throughput two dimension inverse scan discrete cosine transform processor," M.S. thesis, Dept. Electron. Eng., National Chiao Tung Univ., Hsinchu, Taiwan, R.O.C., Jun. 2000.
- [15] C.-C Lin, H.-C. Chang, K.-H. Chen, and J.-I. Guo, "Reconfigurable low power MPEG-4 texture decoder IP design," in *Proc. IEEE Asia-Pacific Conf. Circuits Syst.*, Dec. 2004, pp. 153–156.
- [16] N. August and D. S. Ha, "On the low-power design of DCT and IDCT for low bit-rate video codecs," in *Proc. IEEE Int. Conf. ASIC/SOC*, Sep. 2001, pp. 203–207.
- [17] C. Loeffler, A. Lifhtenberg, and G. S. Moschytz, "Practical fast 1-D DCT algorithm with 11-multiplications," in *Proc. ICASSP*, May 1989, vol. 2, pp. 988–991.
- [18] K.-H. Chen, J.-I. Gua, J.-S. Wang, C.-W. Yeh, and T.-F. Chen, "A power-aware IP core design for the variable-length DCT/IDCT targeting at MPEG4 shape-adaptive transforms," in *Proc. IEEE ISCAS*, May 2004, vol. 2, pp. 141–144.
- [19] R.-C. Ju, J.-W. Chen, J.-I. Guo, and T.-F. Chen, "A parameterized power-aware IP core generator for the 2-D 8×8 DCT/IDCT," in *Proc. IEEE ISCAS*, May 2004, vol. 2, pp. 769–772.
- [20] K.-H. Chen, J.-I. Guo, J.-S. Wang, C.-W. Yeh, and J.-W. Chen, "An energy-aware IP core design for the variable-length DCT/IDCT targeting at MPEG4 shape-adaptive transforms," *IEEE Trans. Circuits Syst. Video Technol.*, vol. 15, no. 5, pp. 704–715, May 2005.
- [21] K. Rao and P. Yip*, Discrete Cosine Transform: Algorithms, Advantages and Applications*. London, U.K.: Academic, 1990.
- [22] MPEG-4 Video Verification Model Version 18.0 ISO/IEC JTC1/SC29/ WG11 N3908, Jan. 2001.
- [23] UMC Free-of-Charge Libraries [Online]. Available: http://www.umc. com/english/design/b_3.asp

Kun-Bin Lee (M'05) received the B.S. degree in electrical engineering from National Sun Yat-Sen University, Taiwan, R.O.C., in 1996, and the M.S. and Ph.D. degrees in electronics engineering from National Chiao-Tung University, Hsinchu, Taiwan, R.O.C., in 1998 and 2003, respectively.

He is currently with MediaTek, Inc., Hsinchu. His current research interests include processor architecture, digital signal processing, video coding systems, and system-level exploration with a focus on data transfer optimization and memory management for

image and video applications.

Dr. Lee is a member of Phi Tan Phi. In 2004, he was the recipient of the Long-Term Paper Award from Acer, the Professor Wen-Zen Shen Thesis Award from Taiwan IC Design Society, and the Outstanding Design Award of University LSI Design Contest from ASP-DAC. In 2005 and 2006, he received the Outstanding Paper Award from MediaTek.

Nelson Yen-Chung Chang (S'06) received the B.S. degree in electrical engineering from National Tsing-Hua University, Hsinchu, Taiwan, R.O.C., in 2000, and the M.S. degree in electronic engineering from National Chiao-Tung University, Hsinchu, in 2002. He is currently working toward the Ph.D. degree at National Chiao-Tung University.

His research interests include VLSI signal processing, video codec VLSI design, and system-level design. Currently, he is engaged in real-time advanced stereo vision system research.

Hui-Cheng Hsu received the B.S. and M.S. degrees in electrical engineering from National Chiao-Tung University, Hsinchu, Taiwan, R.O.C., in 2002 and 2004, respectively.

She is currently with MediaTek, Inc., Hsinchu. Her research interests include processor architecture, digital signal processing, and video display systems.

Tian-Sheuan Chang (S'93–M'06–SM'07) received the B.S., M.S., and Ph.D. degrees in electronics engineering from National Chiao-Tung University, Hsinchu, Taiwan, R.O.C., in 1993, 1995, and 1999, respectively.

He is currently with the Department of Electronics Engineering, National Chiao-Tung University, as an Assistant Professor. From 2000 to 2004, he was with Global Unichip Corporation, Hsinchu. His research interests include IP and SOC design, VLSI signal processing, and computer architecture.