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計畫主持人：郭家豪

計畫參與人員：碩士班研究生-兼任助理人員：陸志瑋
博士班研究生-兼任助理人員：王鈺仁

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Introduction

The valuation of risky debt is central to theoretical and empirical work in corporate finance. There are many existing literatures such as Anderson and Sundaresan (1996) and Mella-Barral and Parraudin (1997) arguing that costless debt renegotiation never obtains inefficient liquidations at equilibrium for the financing of the firm. When a firm cannot pay off a loan, it is technically bankrupt¹. Both the creditor and the firm may experience a Pareto-improvement in their positions by renegotiating the loan. By renegotiating the terms of the debt, the financially distressed firm can pay less than the originally-contracted interest payment and avoid the stigmatization of bankruptcy and the creditor can avoid the costs of taking the firm. Hence, debt renegotiation can eliminate inefficient liquidations. However, inefficient liquidations really occur in many markets even after renegotiation. This research is motivated by the empirical observation that banks do not always renegotiate and that costly bankruptcies are observed in many markets or countries.

Hackbarth, Hennessy, and Leland (2007) first used the trade-off theory between tax-shield and bankruptcy cost to explain these inefficient liquidations for weak firms (small/young corporations) after introducing market debts. They also showed that banks always accept strong firms' renegotiation offers and never liquidate these firms

¹ In practice, there exist some different definitions of bankruptcy or default. For example, the definition of the default applicable to the credit index includes restructuring, whereas the definition for CDS contracts on the reference entity does not.

no matter how the information on the debt contract conditions evolves over time. Their results are consistent with the findings of Blackwell and Kidwell (1988) that small firms issue privately placed debt almost exclusively and larger firms are more likely to issue market debt. Nevertheless, Bourgeon and Dionne (2007) argued that this scenario does not necessarily correspond to the reality. They introduced asymmetric information on the LGD (loss given default) value at the renegotiation date to explain why banks do not renegotiate with strong firms under certain circumstances. They found that the presence of asymmetric information between banks and firms induces that banks will not always renegotiate with strong firms with a high LGD or a low liquidation value. Their model contributes to explain some empirical findings of Carey and Gordy (2009).

Nevertheless, much recent research has focused on perfect information models on the firm's value for creditors. For examples, see Mella-Barral and Parraudin (1997), Bourgeon and Dionne (2007), and Hackbarth, Hennessy, and Leland (2007). However, indeed, there is asymmetric information between the firm and the creditor because it is typically difficult for the creditor to observe the firm's value directly. Hence, the creditor must instead draw inference about the state variable from publicly available information. The state variable may be the firm's value, the EBIT, the output price, or other specifications. As claimed in Duffie and Lando (2001), the creditor's imperfect

information on the firm's value makes default intensity is strictly positive at zero maturity because the creditor is uncertain about the nearness of current state variable to the trigger level at which the firm would declare default. The existence of the default intensity makes it reasonable that observed bond prices often drop abruptly at or around the time of default. Bond prices with perfect information instead converge continuously to its default-contingent value as default approaches. Moreover, yield spreads for risky firms' debts with complete information climbs rapidly with maturity, but bond-market participants' imperfect information on the firm causes a more moderate variation in yield spreads with maturity. And lots of empirical studies such as Fons (1994), Helwege and Turner (1999), and Sarig and Warga (1989) showed that severe variation in the shape of the term structure of yield spreads is seldom observed in bond markets.

In this research, we focus on the problem of the implications of strategic debt service with incomplete information. Under informational assumptions, we derive the creditor's conditional distribution of the firm's value, conditional default probability, and default intensity, explicitly accounting for the implications of imperfect information and renegotiation mechanism. Then, we show how the renegotiation bargaining power affects the debt value. In addition, we review related efficiency problem of debt issuing with imperfect information. To the best of our knowledge, the

proposed model here is the first structural model considering renegotiation with imperfect information and is consistent with a reduced-form representation.

Model

Throughout our analysis, we suppose that capital markets are frictionless and agents are risk neutral and can borrow and lend freely at a constant interest rate, r , but the bond-market information on the credit quality of the firm's debt is incomplete. We consider a firm that produces a unit of output for sale with an incurring cost of $w > 0$.

As well as Mella-Barral and Parraudin (1997), the stochastic process p describing the output price of our given firm is modeled as a geometric Brownian motion, which is defined, along with all other random variables, on a fixed probability space (Ω, F, P) . In particular, $p_t = e^{X_t}$, where

$$X_t = X_0 + mt + \sigma B_t \quad (1)$$

for B is a standard Brownian motion, a volatility parameter $\sigma > 0$, and a parameter $m \in (-\infty, \infty)$ that determines the expected price growth rate $t^{-1} \log[E(V_t/V_0)] = m + \sigma^2/2$. While in production at time t , the firm generates its net earnings flow

$$EBIT_t = p_t - w. \quad (2)$$

We also suppose that the bankruptcy may impair the firm's efficiency. After

bankruptcy, new owners of the firm can only generate earnings of

$$\xi_1 p_t - \xi_0 w, \quad (3)$$

where $\xi_1 \leq 1$ and $\xi_0 \geq 1$. The reason may be that the operation know-how of the firm is not well-known to the new owner. Alternatively, one may regard the expected, discounted value of the reduction in net earnings as the direct cost of bankruptcy.

Because creditors or bondholders are not responsible for the operation of the firm, they are not kept fully informed of the status of the firm. However, they do understand that optimizing equity owners will force liquidation when the firm's value falls to some critical threshold, γ , or, equivalently, the output price falls to the corresponding critical level, p_c . γ is the scrapping value of the firm at liquidation if the firm owner opts for liquidation. Because of the existence of a noisy accounting report of net earnings flow, creditors or bondholders may choose to estimate the true net earnings flow from the output price. However, it is not so easy to observe the output price process p directly because not only the incurring cost but also the output price belongs to the so-called "business secrets". It is important to recognize that the interpretation of p and w in this research is made simply to aid exposition. Hence, it is not really appropriate to select p and w by examining data on the output price and cost.

Without loss of generality, we assume that creditors or bondholders cannot

observe the output price process p directly. Instead, they receive imperfect information on the output price. We assume that, at each observation time t , there is an observed noisy output price, given by \hat{p}_t , where $\log \hat{p}_t$ and $\log p_t$ are joint normal. The observed noisy output price may come from the public information on the industrial average whole sale price. If creditors or bondholders want to calculate the firm's value, the first thing that all they can do is to infer the true output price from the imperfect information which is publicly available. Specifically, we suppose that $\hat{p}_t = p_t e^{U_t} = e^{X_t + U_t} = e^{Y_t}$, where U_t is normal distributed and independent of X_t . The expectation of U_t is u and the variance of U_t is a^2 . Conditional on X starting at some level x_0 , we know

$$Y_t \sim Normal(x_0 + mt + u, a^2 + \sigma^2 t). \quad (4)$$

Let $W(p_t)$ denote the total value of the pure equity firm in the hands of its initial equityholders, and $X(p_t)$ denote the total value of the pure equity firm in the hands of the other owners after bankruptcy. Mella-Barral and Parraudin (1997) derived the following equations:

$$W(p_t) = \begin{cases} \frac{p_t}{r - \mu} - \frac{w}{r} + \left[\gamma - \frac{p_c}{r - \mu} + \frac{w}{r} \right] \left(\frac{p_t}{p_c} \right)^\lambda & \text{for } p_t \geq p_c \\ \gamma & \text{for } p_t < p_c \end{cases} \quad (5)$$

$$X(p_t) = \begin{cases} \frac{\xi_1 p_t}{r - \mu} - \frac{\xi_0 w}{r} + \left[\gamma - \frac{\xi_1 p_x}{r - \mu} + \frac{\xi_0 w}{r} \right] \left(\frac{p_t}{p_x} \right)^\lambda & \text{for } p_t \geq p_x \\ \gamma & \text{for } p_t < p_x \end{cases} \quad (6)$$

where $\mu = m + \sigma^2/2$, $p_c = -\frac{\lambda}{1-\lambda} \frac{w+r\gamma}{r} (r-\mu)$, $p_x = -\frac{\lambda}{1-\lambda} \frac{\xi_0 w+r\gamma}{\xi_1 r} (r-\mu)$, and

λ is the negative root of the quadratic equation $\lambda(\lambda-1)\sigma^2/2 + \lambda\mu = r$.

Results

Proposition 1. *Under imperfect market, we assume the noisy accounting report of assets is given by $\hat{p}_t = p_t e^{U_t} = e^{Y_t}$, conditional on $\tau > t$ and the starting level x_0 .*

The total value of the pure equity firm in the hands (i) of its initial equityholders,

$W_{ulnr}(\hat{p})$ (unleveraged and no renegotiation), and (ii) of other owners after

bankruptcy, $X_{ulnr}(\hat{p})$, under imperfect market are equal to

$$W_{ulnr}(\hat{p}) = \frac{p_c}{r-\mu} A_{1c} - \frac{w}{r} + \left[\gamma - \frac{p_c}{r-\mu} + \frac{w}{r} \right] A_{\lambda c} \quad (7)$$

$$X_{ulnr}(\hat{p}) = \frac{\xi_1 p_x}{r-\mu} A_{1x} - \frac{\xi_0 w}{r} + \left[\gamma - \frac{\xi_1 p_x}{r-\mu} + \frac{\xi_0 w}{r} \right] A_{\lambda x} \quad (8)$$

where $p_c = -\frac{\lambda}{1-\lambda} \frac{w+r\gamma}{r} (r-\mu)$, $p_x = -\frac{\lambda}{1-\lambda} \frac{\xi_0 w+r\gamma}{\xi_1 r} (r-\mu)$, and $A_y(\hat{p}_t)$ refer

to the Appendix, and λ is the negative root of the quadratic equation

$$\lambda(\lambda-1)\sigma^2/2 + \lambda\mu = r.$$

Proposition 2. *Under incomplete market, we assume the noisy accounting report of*

assets is given by $\hat{p}_t = p_t e^{U_t} = e^{X_t+U_t} = e^{Y_t}$, conditional on $\tau > t$ and the starting

level x_0 . If $L_{wlnr}(\hat{p})$ (with leverage and no renegotiation) and $V_{wlnr}(\hat{p})$ respectively

denote the values of the firm's debt and equity under these assumptions, then, if

$\gamma \geq b/r$, the debt is riskless, and

$$L_{wlnr}(\hat{p}) = \frac{b}{r} \quad (9)$$

$$V_{wlnr}(\hat{p}) = W_{ulnr}(\hat{p}) - \frac{b}{r}. \quad (10)$$

If $\gamma < b/r$, the debt is risky and the expected values of the $\hat{V}(p_t)$ and $\hat{L}(p_t)$ are given by

$$V_{wlnr}(\hat{p}) = \begin{cases} \frac{p_b}{r-\mu} A_{1b} - \frac{w+b}{r} - \left[\frac{p_b}{r-\mu} - \frac{w+b}{r} \right] A_{\lambda b} & \text{for } p_b < p_x \\ \frac{p_x}{r-\mu} B_{1xb} - \frac{w+b}{r} B_{0xb} - \left[\frac{p_b}{r-\mu} - \frac{w+b}{r} \right] \left(\frac{p_x}{p_b} \right)^\lambda B_{\lambda xb} & \text{for } p_b \geq p_x \end{cases} \quad (11)$$

$$L_{wlnr}(\hat{p}) = \begin{cases} \frac{b}{r} + \left[X(p_b) - \frac{b}{r} \right] A_{\lambda b} & \text{for } p_b < p_x \\ \frac{\xi_1 p_x}{r-\mu} (A_{1x} - B_{1xb}) - \frac{\xi_0 w+b}{r} (1 - B_{0xb}) \\ \quad + \left[\gamma - \frac{\xi_1 p_x}{r-\mu} + \frac{\xi_0 w}{r} \right] (A_{\lambda x} - B_{\lambda xb}) \\ \quad + \frac{b}{r} B_{0xb} \left[X(p_b) - \frac{b}{r} \right] \left(\frac{p_x}{p_b} \right)^\lambda B_{\lambda xb} & \text{for } p_b \geq p_x \end{cases} \quad (12)$$

where $p_x = -\frac{\lambda}{1-\lambda} \frac{\xi_0 w + r\gamma}{\xi_1 r} (r-\mu)$, $p_b = -\frac{\lambda}{1-\lambda} \frac{w+b}{r} (r-\mu)$, $A_{ij}(\hat{p}_t)$ and

$B_{ijk}(\hat{p}_t)$ refer to the Appendix, and λ is the negative root of the quadratic equation

$$\lambda(1-\lambda)\sigma^2 / 2 + \lambda\mu = r.$$

The prediction value, $W_{ulnr}(\hat{p}_t)$, $V_{wlnr}(\hat{p}_t)$, and $L_{wlnr}(\hat{p}_t)$ from Proposition 1 and 2 are illustrated in Figure 1. Even if outer investors know that the observed price is unbiased, they still feel frightened when the observed price decreases to p_c . As long as the firm does not declare bankruptcy, outer investors will overestimate the

firm value because debtholders seem optimistic about the firm under this situation. It is familiar to the expected value of the debt and the equity value. However, inferior information will eventually decrease the debt value as the observed output price increases rapidly.

When the debt principal, b/r , is greater than the scrapping value, bondholders are the residual claimants, and the debt is risky. Because of the direct bankruptcy costs, the total firm value, $W_{wlnr}(\hat{p}_t)$, which is defined by $V_{wlnr}(\hat{p}_t) + L_{wlnr}(\hat{p}_t)$, will decrease as b increases. Leverage generates losses from an ex ante point of view because of the direct bankruptcy costs it entails under complete market. From Figure 2, it is easy to see the difference between complete information market and noisy information market. When b is small, such that b/r is smaller than γ , the debt is riskless, and the payment of the coupon does not affect debtholders' estimation of the firm value under the unbiased observation price ($W_{wlnr}(\hat{p}_t) = W_{ulnr}(\hat{p}_t)$). When b increases and b/r becomes larger than γ , leverage becomes costly because it may result in early liquidation at p_b but not at p_c . If $p_b \leq p_x$, the firm may go to "liquidation bankruptcy," which means debtholders will prefer to liquidate the firm than take over at bankruptcy. If $p_b > p_x$, there is some difference in estimating the value of the debt because the bankruptcy occurs at p_x . When $p_b > p_x$, the firm is asserted to be "an operating concern bankruptcy". When the output price hits p_b ,

bondholders tend to take over the firm but not to liquidate the firm instantly. Note that there still is a debt capacity under noisy information since the total firm value eventually converges to X_{ulnr} as b increases.

We also want to consider how the value of the firm's security is affected if debtholders and equityholders can renegotiate coupon payments. As the claim in Mella-Barral and Perraudin (1997), the firm will not liquidate at p_x or p_b but at p_c when coupon payments can be renegotiated and equityholders can make take-it-or-leave-it offers to debtholders. Hence, we define $X_{wltwr}(\hat{p}_t) \equiv \int_{\log(p_c)}^{\infty} X(e^x) g_{p_c}(x|\hat{p}_t, x_0, t) dx$ be the estimated total value of the firm in the hands of other owners but liquidated at p_c . Let us denote α as the equityholders' bargaining power and $1-\alpha$ as the debtholders' bargaining power. When $\alpha = 1$, it indicates that equityholders can make take-it-or-leave-it offers to debtholders. We shall assume that possible strategies for equityholders consist of piecewise right-continuous service flow functions of \hat{p}_t , the observation price. Under this situation, equityholders will pay the full coupon, b , as the observation price larger than a trigger price, $\hat{p}_{\alpha=1}$, and when the observation price is less than $\hat{p}_{\alpha=1}$, equityholders can extract a surplus by offering debtholders a service flow less than b as long as the debt value exceeds $X_{wltwr}(\hat{p}_t)$. When $\alpha = 0$, debtholders will try to increase the value of their claims compared to the situation without renegotiation

because debtholders can make take-it-or-leave-it offers. Under this situation, debtholders will act as residual claimants who maximize the firm value subject to the constraints placed upon them by the "outside option" of equityholders. Therefore, the debt value will equal to the firm value when the observed output price is less than $\hat{p}_{\alpha=0}$, and the equityholders will take these concessions as long as the equity value does not become negative. Nevertheless, debtholders do not obtain all information on the firm, so they will ask debt value equal to $W_{wlr}(\hat{p}_t) = W_{ulr}(\hat{p}_t)$ instead of $W(p_t)$ when the observed output price is less than $\hat{p}_{\alpha=0}$. Hence, as $0 < \alpha < 1$ and $\hat{p} < \hat{p}_{\alpha}$, the debt value will equal $\alpha X_{wlr}(\hat{p}_t) + (1 - \alpha)W_{wlr}(\hat{p}_t)$.

Let $\tilde{s}(\hat{p})$ be the optimal debt service flow function under noisy information market. The intuitive explanation of the service flow function is that debtholders require a service flow from equityholders whose capitalized value is sufficient to dissuade them from bankruptcy in order to keep operating. Therefore, equityholders must provide enough income flow worth of $XW_{wlr}(\hat{p}; \alpha) = \alpha X_{wlr}(\hat{p}) + (1 - \alpha)W_{wlr}(\hat{p})$ when $\hat{p} < \hat{p}_{\alpha}$. From the above, we assume that

$L_{wlr}(\hat{p}; \alpha)$ satisfies the following PDE when $\hat{p} \geq \hat{p}_{\alpha}$,

$$rL_{wlr}(\hat{p}; \alpha) = \tilde{s}(\hat{p}) + \hat{\mu}\hat{p}L'_{wlr}(\hat{p}; \alpha) + \frac{\hat{\sigma}^2}{2}\hat{p}^2L''_{wlr}(\hat{p}; \alpha) \quad (13)$$

with the service flow function $\tilde{s}(\hat{p})$ where $\hat{\mu}$ and $\hat{\sigma}^2$ are the estimated mean and variance of the logarithm of the observed output price under noisy information market.

Our assumption implies that $L_{wlr}(\hat{p}; \alpha) = XW_{wlr}(\hat{p}; \alpha)$ (with leverage and with renegotiation) for all $\hat{p} < \hat{p}_\alpha$. No bubble condition includes $\lim_{\hat{p} \rightarrow \infty} L_{wlr}(\hat{p}; \alpha) = \frac{b}{r}$.

Under this situation, equityholders know the real price of the output, so the value of equityholders is the real firm value minus the estimated value of debtholders, i.e.

$$V_{wlr}(p, \hat{p}; \alpha) = W(p) - L_{wlr}(\hat{p}; \alpha).$$

Proposition 3. Under incomplete market, we assume the noisy accounting report of assets is given by $\hat{p} = pe^U = e^{X+U} = e^Y$, and equityholders adopt the service flow function, $\tilde{s}(\hat{p})$. The values of equity, $V_{wlr}(p, \hat{p}; \alpha)$, and debt, $L_{wlr}(\hat{p}; \alpha)$, are as follows:

$$V_{wlr}(p, \hat{p}; \alpha) = W(p) - L_{wlr}(\hat{p}; \alpha) \quad (14)$$

where, if $\gamma \geq b/r$, then debt is riskless, and $L_{wlr}(\hat{p}; \alpha) = b/r$. If $\gamma < b/r$, then the debt is risky, and

$$L_{wlr}(\hat{p}; \alpha) = \begin{cases} \frac{b}{r} + \left[XW_{wlr}(\hat{p}_s; \alpha) - \frac{b}{r} \right] \left(\frac{\hat{p}}{\hat{p}_\alpha} \right)^{\hat{\lambda}} & \text{for } \hat{p} > \hat{p}_\alpha \\ XW_{wlr}(\hat{p}_s; \alpha) & \text{for } \hat{p} \leq \hat{p}_\alpha \end{cases} \quad (15)$$

where \hat{p}_α is solved by $L'_{wlr}(\hat{p}_\alpha; \alpha) = XW'_{wlr}(\hat{p}_\alpha; \alpha)$, and $\hat{\lambda}$ is the negative root of the quadratic equation $\hat{\lambda}(\hat{\lambda} - 1)\hat{\sigma}^2 / 2 + \hat{\lambda}\hat{\mu} = r$.

Proposition 4. Under incomplete market, we assume the noisy accounting report of

assets is given by $\hat{p}_t = p_t e^{U_t} = e^{X_t + U_t} = e^{Y_t}$. If debtholders can make take-it-or-leave-it offers, then renegotiation will not occur, and the firm will declare bankruptcy at p_b , i.e. the issuance of debt cannot generate an efficient outcome when the observation price is unbiased.

Conclusions

Our study shows that, if equityholders can make take-it-or-leave-it offers, then equityholders have to give up some equity value in order to convince the debtholders to lower the bond coupon, and debt values will approximate the firm's taken-over value when the firm is in financial distress. Clearly, when the information on the product price is more transparent, there is less information asymmetry, and debtholders will require a lower information premium when equityholders want to renegotiate the debt service.

When debtholders can make take-it-or-leave-it offers, no matter how low the observation price is under the unbiased assumption, they will never renegotiate actively with the unbiased observation price. The observation price is the only source for debtholders to decide the renegotiation timing. Hence, they really care about the price being underestimated or overestimated, and these two situations will lead to opposite decisions. In order to avoid taking more risk, they are more passive, which

results in inefficient bankruptcy.

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Table 1: \hat{p}_α for different α with different a .

$b = 4$, $w = 1$, $\sigma = 0.1$, $r = 0.05$, $\mu = 0$, $\gamma = 60$, $\xi_1 = 0.9$, $\xi_0 = 1.1$, $t = 1$.

(%) denotes the percentage of \hat{p}_α .

a	α				
	0	0.25	0.5	0.75	1
0.1	3.3928 (92.97%)	3.4733 (92.34%)	3.5701 (92.02%)	3.6776 (91.84%)	3.7929 (91.71%)
0.2	3.2023 (87.75%)	3.2655 (86.81%)	3.3443 (86.20%)	3.4391 (85.88%)	3.5466 (85.75%)
0.5	2.9873 (81.86%)	3.0093 (80.02%)	3.0441 (78.46%)	3.1047 (77.54%)	3.2097 (77.61%)
p_α	3.6492	3.7615	3.8797	4.0043	4.1358

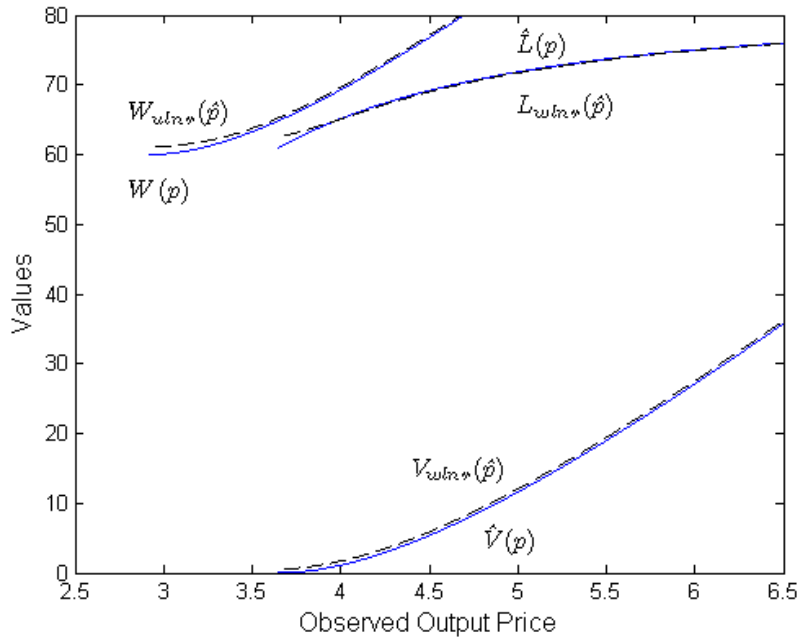


Figure 1: Security valuation with no renegotiation

$b = 4$, $w = 1$, $\sigma = 0.1$, $r = 0.05$, $\mu = 0$, $\gamma = 60$, $\xi_1 = 0.9$, $\xi_0 = 1.1$, $t = 1$,
 $p_c = 2.9194$, $p_b = 3.6492$.

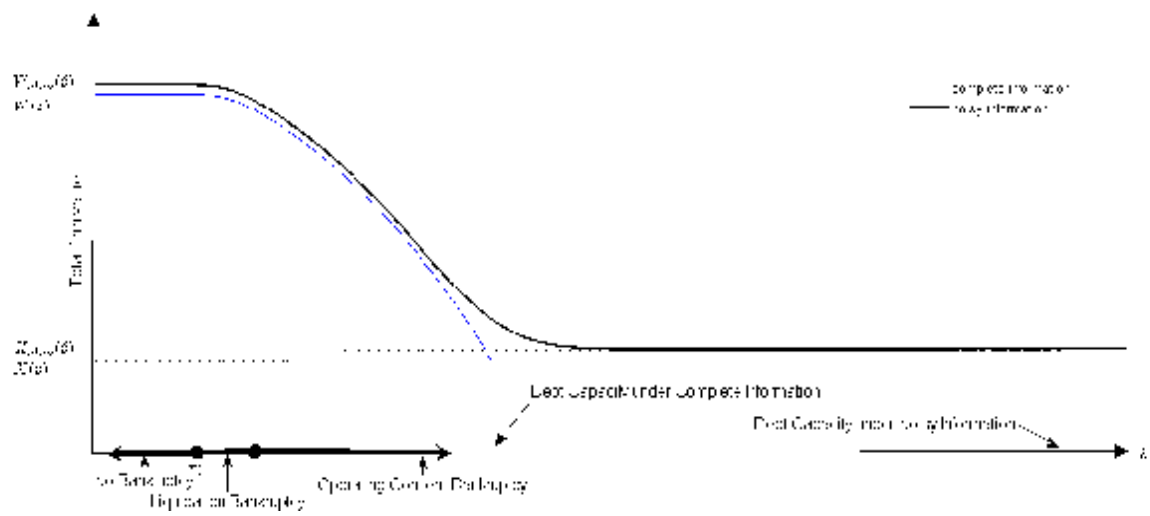


Figure 2: Total firm value and leverage

$w=1$, $\sigma=0.1$, $r=0.05$, $\mu=0$, $\gamma=60$, $\xi_1=0.9$, $\xi_0=1.1$, $a=0.1$, $t=1$, and the observed output price is 5.

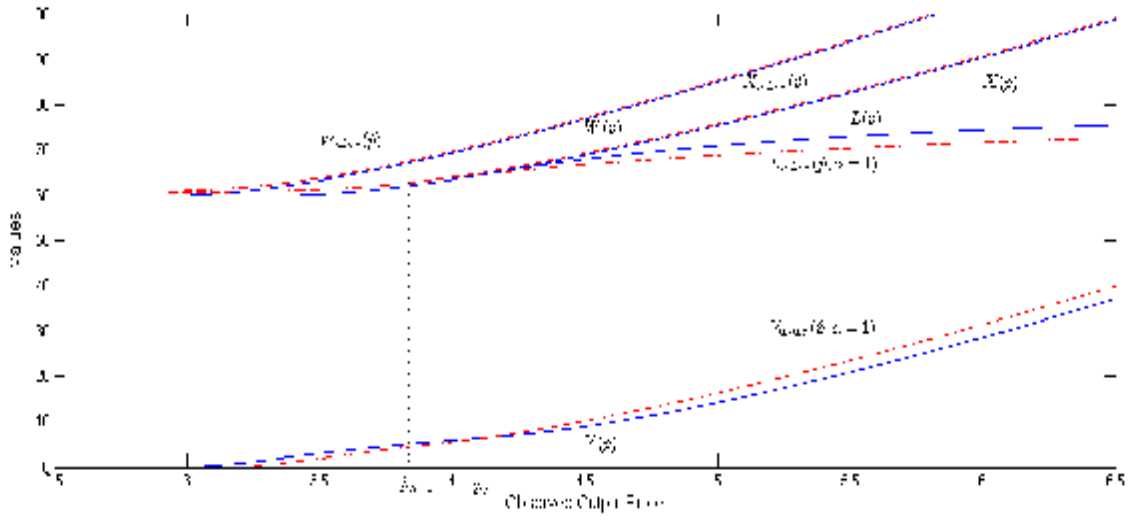


Figure 3: Security valuation with equityholder offer

$b = 4$, $w = 1$, $\sigma = 0.1$, $r = 0.05$, $\mu = 0$, $\gamma = 60$, $\xi_1 = 0.9$, $\xi_0 = 1.1$, $a = 0.1$,
 $t = 1$, $p_c = 2.9194$, $p_s = 4.1358$, $\hat{p}_{\alpha=1} = 3.7929$ (91.71%).

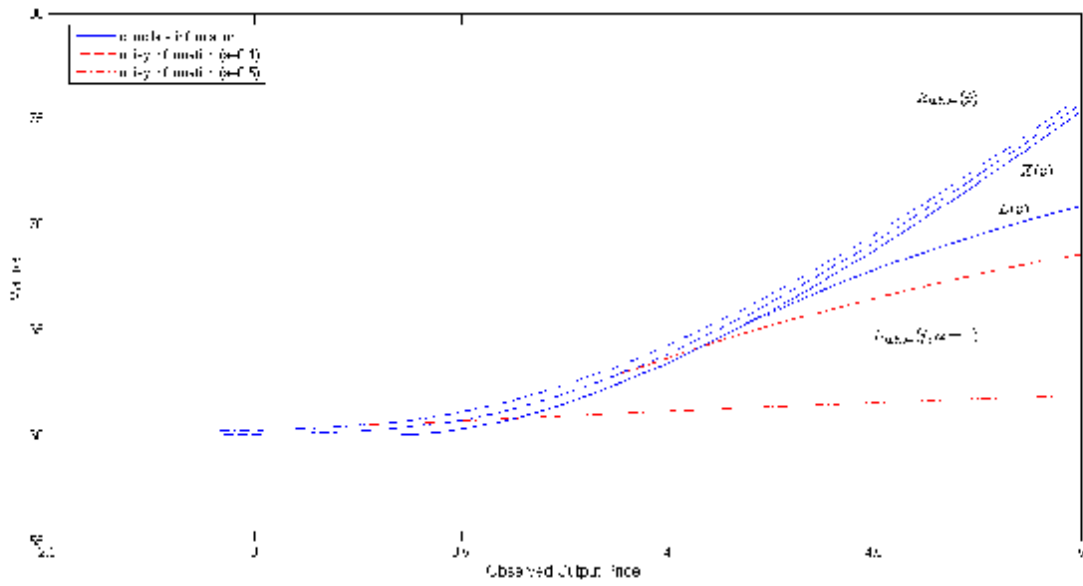


Figure 4: Security valuation with equityholder offers and different a
 $b = 4$, $w = 1$, $\sigma = 0.1$, $r = 0.05$, $\mu = 0$, $\gamma = 60$, $\xi_1 = 0.9$, $\xi_0 = 1.1$, $t = 1$,
 $p_c = 2.9194$, $p_s = 4.1385$, $\hat{p}_{\alpha=1}(a = 0.1) = 3.7929$ (91.71%) ,
 $\hat{p}_{\alpha=1}(a = 0.5) = 3.2097$ (77.61%).

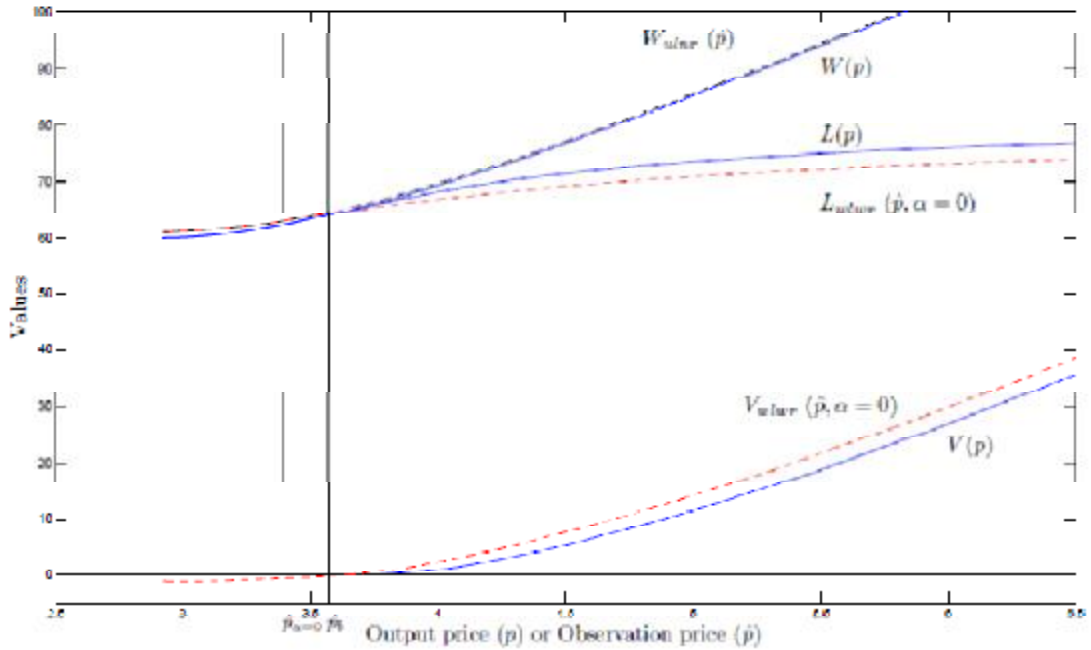


Figure 5: Security valuation with debtholder offers

$b = 4$, $w = 1$, $\sigma = 0.1$, $r = 0.05$, $\mu = 0$, $\gamma = 60$, $\xi_1 = 0.9$, $\xi_0 = 1.1$, $a = 0.1$,
 $t = 1$, $p_c = 2.9194$, $p_b = 3.6492$, $\hat{p}_{a=0}(a = 0.1) = 3.3928$ (92.97%) .

Self-Examination

When firms experience financial distress, equityholders may act strategically, forcing concessions from debtholders and paying less than the originally-contracted interest payment. This article incorporates a strategic debt service under imperfect information, which enables debtholders to receive the observation price instead of the real price, and develops simple closed-form expression for debt and equity values. We analyze the efficient implications of renegotiation, showing that debtholders will ask for information premium when equityholders can make take-it-or-leave-it offers, and debtholders will never renegotiate actively when they can make take-it-or-leave-it

offers. These findings inspire our further empirical studies. We plan to write in more formal form and submit the paper to financial journals.

國科會補助專題研究計畫項下出席國際學術會議心得報告

日期：100年7月15日

計畫編號	NSC99-2410-H-009-043		
計畫名稱	不完全資訊下之策略性債務協商：理論與實證研究		
出國人員姓名	郭家豪	服務機構及職稱	國立交通大學財務金融研究所 助理教授
會議時間	100年6月26日 至 100年6月29日	會議地點	Rome, Italy
會議名稱	(中文) (英文)18th Annual Conference of the Multinational Finance Society		
發表論文題目	(中文) (英文)A Closed-form Solution for Options with Daily Price Limits		

一、參加會議經過

此次 Multinational Finance Society 於義大利羅馬所舉辦之第十八屆學術研討會，由 6/26 日開始至 6/29 日止共計四天，第一天 10:00 a.m. ~12:30 p.m. 於 Hotel FENIX 接受參加研討會現場註冊並於 7 p.m. ~10 p.m. 舉辦接待歡迎會，可以與世界各國參與研討會學者或專業人士交流討論。第二天 8:30 a.m. 開始各場次之學術論文發表討論，一天分四個時段，分別是 8:30 a.m. ~10:15 a.m.、10:30 a.m. ~12:15 a.m.、2:15 p.m. ~4:00 p.m.、4:15 p.m. ~6:00 p.m.，每個時段有八至十個論文研討議題場次同時進行，如 Asset Pricing、Banks、Financial Crisis、Microstructure、Econometrics、Derivative Markets、

Monetary Policy、Cross Listing、IPOs、Funds、Liquidity、Insider Trading、Payout Policy、Corporate Finance、Ownership Structure、International Finance、Exchange Rates、Portfolio Management、Valuation、Bonds、Executive Compensation、Corporate Restructuring、Interest Rates、Real Options & Real Estate、Analysts、Corporate Governance、Capital Structure、Earnings Quality、Credit Risk、Emerging Markets、Commodities、Option Markets、Volatility、M&As、Behavioral Finance、Venture Capital、Hedging、Bankruptcy/Financial Distress、Cost of Equity Capital、Derivative Markets、Hedge Funds、Option Models、Pension Funds、Market Efficiency 等，幾乎包含財務各個子領域研究範疇，研討會參與者可以自由選擇有興趣的議題場次參加，除聆聽先端研究論文發表，也可以參與國際學者討論並互相交換意見。第三天也是 8:30 a.m. 開始各場次之學術論文發表討論，同樣一天分四個時段，也是自由選擇有興趣的議題場次參加。在第二天的議程安排上，除了各場次學術論文發表討論外，大會還安排重要學者 Prof. Subrahmanyam 演講，精彩演說令人眼界一開，收獲甚豐；第三天的議程安排也有 Prof. Constantinides 及 Prof. Shefrin 兩位重要學者發表 Keynote Speech，一樣令人印象深刻。研討會於第四天正式結束，與會者紛紛互相留下各自連絡方式，以便日後就有興趣之議題可以繼續討論或共同合作，在互道珍重後正式結束為期四天之國際學術研討會。

二、與會心得

此次參加國際學術研討會，個人發表之論文為“A Closed-form Solution for Options

with Daily Price Limits”，本篇論文主旨在討論價格限制市場下的選擇權評價公式，目前已推導得到在 Black-Scholes 模型下其封閉解，相較於文獻中已知的 finite difference method 或 Monte Carlo simulation 等數值方法，此封閉解顯著具有計算速度上明顯優勢，論文於研討會發表後引起與會者熱烈討論，與會者對此論文有諸多建議，如建議可以將公式解與 finite difference method 之解，兩者列表比較其結果之一致性；也可以於論文一開始先加入一敘述統計，如一年內個股觸及漲跌停次數，說明發展此一選擇權評價模型與推導公式解之重要性；也有與會者建議可以增加避險相關議題討論，相信在實務上應該可以作出許多貢獻，如避險策略的擬定或計算避險部位的建立及調整上應有相當助益。個人覺得此次參加國際學術研討會收穫甚豐，除開闊個人眼界外，透過與國際學者專家的交流討論，對改善個人論文品質與可讀性，都有很大的助益，有利於日後論文修改後投稿頂尖國際學術期刊，相信不管對學術研究或實務應用都可以再作出更大的貢獻。另外，透過參與此次研討會，得以瞭解最新國際學術研究議題趨勢與發展，也有益於日後個人研究議題的孕育成形，更是無形的重要收穫，如有與會學者發表將景氣循環納入利率模型中，惟並未考量景氣循環預測之不確定性，個人認為如能改善此一限制，則該議題未來應該可以有很多繼續發展的空間。再者，由此次參加研討會中，也見識許多國際學者發表論文或演說的技巧，對改善個人教學或演說的技巧甚有助益，從如何生動吸引觀眾注意的口述方式及肢體語言，至充分說明研究議題之動機與重要性，都是值得好好學習效法之處。

三、考察參觀活動(無是項活動者略)：無。

四、建議

個人認為如要邁向國際頂尖學術研究，除了以發表論文於國際頂尖期刊之獎勵誘因以外，應該搭配鼓勵國內學者專家參加國際學術研討會，或廣邀世界各國學者參與於國內舉辦之學術研討會等配套措施，由於頂尖學術研究的產生往往是經過許多學者腦力激盪互相討論後的結果，如能透過學術研討會，增加國際學者專家與國內學者專家互相交流討論的機會，相信應該更有機會激盪出具頂尖學術研究價值的議題，也更能明瞭國際學術研究趨勢與發展，進而促成國際研究團隊的組成，增加國內學術研究於國際間的能見度與影響力。

五、攜回資料名稱及內容

MFC-18-Brochure 學術會議資料，內含本次學術會議議程及所有發表論文簡要內容等。

六、其他：無。

國科會補助計畫衍生研發成果推廣資料表

日期:2011/09/17

國科會補助計畫	計畫名稱: 不完全資訊下之策略性債務協商: 理論與實證研究
	計畫主持人: 郭家豪
	計畫編號: 99-2410-H-009-043- 學門領域: 財務
無研發成果推廣資料	

99 年度專題研究計畫研究成果彙整表

計畫主持人：郭家豪		計畫編號：99-2410-H-009-043-				計畫名稱：不完全資訊下之策略性債務協商：理論與實證研究	
成果項目		量化			單位	備註（質化說明：如數個計畫共同成果、成果列為該期刊之封面故事...等）	
		實際已達成數（被接受或已發表）	預期總達成數（含實際已達成數）	本計畫實際貢獻百分比			
國內	論文著作	期刊論文	0	1	40%	篇	數個計畫共同成果
		研究報告/技術報告	0	0	100%		
		研討會論文	3	4	40%		數個計畫共同成果
		專書	0	0	100%		
	專利	申請中件數	0	0	100%	件	
		已獲得件數	0	0	100%		
	技術移轉	件數	0	0	100%	件	
		權利金	0	0	100%	千元	
	參與計畫人力（本國籍）	碩士生	1	0	100%	人次	
		博士生	1	0	100%		
		博士後研究員	0	0	100%		
		專任助理	0	0	100%		
國外	論文著作	期刊論文	5	7	40%	篇	數個計畫共同成果
		研究報告/技術報告	0	0	100%		
		研討會論文	2	4	40%		數個計畫共同成果
		專書	1	0	10%		章/本
	專利	申請中件數	0	0	100%	件	
		已獲得件數	0	0	100%		
	技術移轉	件數	0	0	100%	件	
		權利金	0	0	100%	千元	
	參與計畫人力（外國籍）	碩士生	0	0	100%	人次	
		博士生	0	0	100%		
		博士後研究員	0	0	100%		
		專任助理	0	0	100%		

<p>其他成果 (無法以量化表達之成果如辦理學術活動、獲得獎項、重要國際合作、研究成果國際影響力及其他協助產業技術發展之具體效益事項等，請以文字敘述填列。)</p>	<p>無</p>
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	成果項目	量化	名稱或內容性質簡述
科 教 處 計 畫 加 填 項 目	測驗工具(含質性與量性)	0	
	課程/模組	0	
	電腦及網路系統或工具	0	
	教材	0	
	舉辦之活動/競賽	0	
	研討會/工作坊	0	
	電子報、網站	0	
	計畫成果推廣之參與(閱聽)人數	0	

國科會補助專題研究計畫成果報告自評表

請就研究內容與原計畫相符程度、達成預期目標情況、研究成果之學術或應用價值（簡要敘述成果所代表之意義、價值、影響或進一步發展之可能性）、是否適合在學術期刊發表或申請專利、主要發現或其他有關價值等，作一綜合評估。

1. 請就研究內容與原計畫相符程度、達成預期目標情況作一綜合評估

達成目標

未達成目標（請說明，以 100 字為限）

實驗失敗

因故實驗中斷

其他原因

說明：

2. 研究成果在學術期刊發表或申請專利等情形：

論文： 已發表 未發表之文稿 撰寫中 無

專利： 已獲得 申請中 無

技轉： 已技轉 洽談中 無

其他：（以 100 字為限）

3. 請依學術成就、技術創新、社會影響等方面，評估研究成果之學術或應用價值（簡要敘述成果所代表之意義、價值、影響或進一步發展之可能性）（以 500 字為限）

The valuation of risky debt is always central to theoretical and empirical work in corporate finance because debt financing plays an essential role in firm financing. In this research, we focus on the problem of the implications of strategic debt service with incomplete information. We reexamine related efficiency problems via renegotiation with imperfect information. Our study shows that, if equityholders can make take-it-or-leave-it offers, then equityholders have to give up some equity value in order to convince the debtholders to lower the bond coupon, and debt values will approximate the firm's taken-over value when the firm is in financial distress. Clearly, when the information on the product price is more transparent, there is less information asymmetry, and debtholders will require a lower information premium when equityholders want to renegotiate the debt service.

When debtholders can make take-it-or-leave-it offers, no matter how low the observation price is under the unbiased assumption, they will never renegotiate actively with the unbiased observation price. The observation price is the only source for debtholders to decide the renegotiation timing. Hence, they really care about the price being underestimated or overestimated, and these two situations will lead to opposite decisions. In order to avoid taking more risk, they are more

passive, which results in inefficient bankruptcy. To the best of our knowledge, the proposed model here is the first structural model considering renegotiation with imperfect information. We believe that this research will contribute to the literature of related studies of debt service.